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Evaluation of Ground-Based Models for Estimating Surface Albedo with In-Situ Radiometric Measurements across China

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Abstract: Surface albedo is an essential parameter in many solar radiation applications. Although several models are available, it remains debatable whether they are applicable to other locations. Using long-term daily measurements of radiation acquired by observational networks in China, this study examined the applicability of six existing albedo models: Ineichen model (IeM), Gueymard model (GM), Dong model (DeM), Iziomon-Mayer model (IMM), Morton model (MM), and Zhou model (ZeM). The evaluation results of model performance through statistical analysis showed that among the available ground albedo models, ZeM had the best overall performance at 12 selected stations, IeM was shown to provide acceptable estimations for locations where albedo records are readily available. The statistical results of individual station have shownthat the number of input parameters is not the only key factor for determining the predictive performance of ground albedo models. In other words, a simple model has potential for accurate estimation of ground albedo with appropriate model parameters. Therefore, the simple two-parameter DeM was selected to re-calibrate with in-situ radiometric measurements, which can be adopted as a surrogate for ZeM to predict surface albedo in China.

Keywords: surface albedo; model evaluation; solar height angle; solar radiation

1. Introduction

Increasing application of solar energy in various respects for environmental and economic proposes has highlighted the importance of reliable estimation of solar radiation incident on a target surface [1–3], which consists primarily of direct, diffuse, and reflected components [4]. The most direct method for achieving such estimations is to conduct in situ measurements, which entails implementation of a set of various instruments to sample the temporal variations of these components at the measured surface [5]. Of the three components of solar radiation, the reflected component is the most complex because it is strongly conditioned by surface properties and diverse external factors [6], making it inappropriate to apply site-specific measurements to other unmonitored locations [7]. Furthermore, the high costs of instrumentation and technical constraints have meant that reflected radiation was measured only at limited scientific stations in earlier studies [8,9]. Owing to a lack of observational data, pioneering researchers (e.g., Liu and Jordan [10]) usually quantified the reflected component of radiation in terms of surface albedo, defined as a fraction of the accessible global solar radiation [11]. This alternative has been used widely in subsequent radiation-related studies.

As an essential climate variable for controlling the surface energy budget, surface albedo has been measured routinely at an increasing number of meteorological stations around the world [12,13]. Meanwhile, certain databases such as the Global Energy Balance Archive have been developed through systematic extraction of solar radiation data



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). measured at globally distributed observing stations [14]. Continuous measurements of surface albedo with high temporal resolution have been achieved following the increase in coverage of regional and global radiometric networks, e.g., Fluxnet [15], the Greenland Climate Network [16], and the Baseline Surface Radiation Network [17]. Nevertheless, ground-based radiometric measurements have limited spatial resolution because it is not possible to install the expensive instrumentation required at all locations necessary [6,18]. Understanding the spatial heterogeneity of surface albedo at regional and global scales requires remotely sensed measurements, which could be acquired using airborne [19] and/or satellite instruments [12]. Recently, together with the increasing availability of multi-decadal satellite data, the derivation of albedo from satellite-based products has become the most practical method for estimation of regional and global surface albedo in climate and biogeochemical modelling [20,21]. The retrieval of surface albedo from remote sensing measurements entails the removal of the effects of coupled atmospheresurface scattering processes, which involves applying corrections for both atmospheric effects and anisotropic surface reflections [22]. The inherent complexity of land surface processes results in considerable uncertainty in the albedo retrieved using satellite products, which should be evaluated carefully prior to use [23]. It has become common to use radiometric measurements for validation of satellite-derived albedo via direct point-to-pixel comparisons [12,24–26] or upscaling methods [23]. In addition, radiometric measurements have been proven important in the following respects: (1) detection of decadal changes in surface radiative components [13,27]; (2) generation of spatiotemporally continuous albedo datasets for use in combination with regional and global satellite-based albedo products [28,29]; (3) validation of simulated results of surface albedo in physical models [6]; and (4) use in applications such as solar power generation and agricultural water management [1,30]. These applications highlight the importance of systematic and continuous radiometric measurements. However, most areas of the world remain unmonitored. The practical needs of solar radiation applications in unmonitored regions rely strongly on the development of predictive models for estimation of solar radiation components including surface albedo.

Over previous decades, numerous studies have investigated parameterization of surface albedo using different model parameters at different timescales. Gueymard [31] presented a regression equation to estimate monthly average surface albedo as a function of latitude. Paltridge and Platt [32] proposed a general exponential equation to describe the dependence of surface albedo on solar height angle, which has been applied to estimation of surface albedo over certain land cover types, e.g., grassland [30,33], cropland [34], and bare soil [35]. Nkemdirim [8] proposed an exponential function to describe diurnal, latitudinal, and seasonal variations of surface albedo with the position of the Sun in terms of solar zenith angle (SZA). Alnaser [36] calculated monthly average albedo as a function of relative sunshine duration. Morton [37] determined daily average surface albedo by integrating the Nkemdirim equation over the range of SZAs, weighted with the diurnal course of extraterrestrial radiation, and by incorporating the relative sunshine duration to take the impact of cloud cover into account. Zhou et al. [7] modified the Morton model by adding a function of the leaf area index (LAI) to account for the effect of vegetation phenology on seasonal variation of surface albedo. They applied their proposed model to estimation of the zonal surface albedo of a hypothetical reference surface in different agricultural zones across China. In general, these ground-based models adopted surface albedo parameterized to certain accessible ground-based measurements, e.g., geographic information (i.e., latitude, longitude, and elevation), sunshine duration, and precipitation. In addition, other influential factors have increasingly been taken into consideration as a reflection of the progress in the understanding of surface-reflected processes. Recently, some physical models, which can simulate reflected processes precisely, have been developed for surface albedo estimation for any climate and receiver geometry without need of site-dependent measurements [6]. However, ground-based models remain the primary

tool in many respects owing to the simplicity in their application and the relatively less computational effort involved.

Evaluation of the performance of such ground-based surface albedo predictors against ground-based measurements has been undertaken in sporadic studies. For example, Ineichen et al. [38] used six databases of multi-year measurements from four countries to examine five surface albedo estimation models, obtaining the best results with a site-dependent constant mean value. Psiloglou and Kambezidis [4] evaluated eight models for surface albedo estimation against in-situ measurements that were obtained at the National Observatory of Athens. They found adaptation to the local conditions of models that were more complex was superior to models that used a constant albedo value. However, some critical issues remain: which is more appropriate among these existing models, is the model parameter more, the better the model performance?

In China, a network of 105 stations has been established to measure radiation components over all major climatic zones [7]. Multi-decadal data measured by this network are available online, providing the opportunity to address the outstanding issues highlighted above. Therefore, the main objective of this study was to assess existing models for surface albedo estimation with in-situ radiometric measurements across China during 1993–2015. The findings of this study could provide an important reference for future model development in large regions with different conditions.

2. Materials and Methods

2.1. Observational Sites and Data Processing

Among the present-day network of 105 radiation stations, only the 21 first-level stations have measured simultaneously the reflected and global radiation components required for surface albedo estimation since 1993 [7]. Excluding one pair of stations with close geographic location (i.e., Shanghai and Chengdu) and shorter records of observations, daily observations of radiation and meteorological parameters recorded at the remaining 19 stations were obtained for use in this study from the National Meteorological Information Centre (NMIC), a central depository of meteorological data sponsored by the China Meteorological Administration. Observed surface albedo can be computed directly using reflected and global radiation:

$$_{\rm Dm}^{k,i} = \frac{R_r^{k,i}}{R_g^{k,i}} \tag{1}$$

where α_{Dm} is the daily mean value of measured surface albedo, R_r and R_g are measured values of daily reflected and global radiation, respectively, and superscripts *k* and *i* are used to denote parameters on the *k*th day and in the *i*th year, respectively.

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Among the various influencing factors of surface albedo, snow cover has notable impact on the surface properties of the radiation layer by directly replacing its underlying surface [21,26]. It introduces considerable uncertainty for surface albedo estimation because the surface albedo of snow cover can fall from 0.90 to 0.50 or less, depending on snow condition [39]. Therefore, this study focused on snow-free surface albedo, referred to as ground albedo. All measured data required for surface albedo computation are examined by NMIC through standard processes for data quality control. However, when computing daily mean values of measured ground albedo using Equation (1) for model evaluation, the following six types of measured data were discarded:

- 1. Missing values of daily global radiation component;
- 2. Missing values of daily reflected radiation component;
- 3. Zero values of daily global solar radiation and/or daily reflected solar radiation
- 4. Measured values of daily reflected radiation near the minimum detection limits of the instrumentation;
- 5. Values observed during snow-covered seasons;
- 6. Values when corresponding meteorological variables as model inputs were unavailable.

After quality control processing, four stations located in cold regions (i.e., Urumchi Mohe, Shenyang, and Harbin stations) were identified as receiving rainfall and frequent snowfall with air temperatures below zero during winter-spring seasons. Consequently, daily measurements from these four stations acquired during the cold seasons were largely discarded. Therefore, daily measurements from 12 stations with valid data available for all days of the year during 1993–2015 were selected to evaluate the predictive performance of the studied models. Details of the geographic locations and solar radiation datasets of the 12 selected stations are listed in Table 1 and illustrated in Figure 1.

No.	Location	Latitude (deg., N)	Longitude (deg., E)	Altitude (m)	T _{mean} (°C)	P (mm)	<i>n</i> (h)	R_g (MJ m ⁻² day ⁻¹)	v 1	Measured Albedo	
									КD	Period	Mean ²
1	Ejin Banner	41.95	101.07	940.5	9.73	35	9.12	17.83	0.32	1993-2015	0.25
2	Beijing	39.80	116.47	31.3	13.28	588	6.76	13.51	0.48	1993-2015	0.17
3	Zhengzhou	34.72	113.65	110.4	15.35	639	5.15	12.92	0.60	1993-2015	0.17
4	Kashgar	39.48	75.75	754.5	12.74	66	7.98	15.56	0.44	1993-2015	0.22
5	Wuhan	30.60	114.05	23.6	17.47	1259	4.96	11.71	0.60	1993-2015	0.17
6	Shanghai	31.40	121.45	5.5	17.18	1164	4.77	12.51	0.56	1993-2015	0.17
7	Guangzhou	23.22	113.48	70.7	22.46	1737	4.24	11.68	0.63	1993-2015	0.18
8	Chengdu	30.75	103.87	547.7	21.17	905	4.33	9.88	0.73	2004-2015	0.16
9	Kunming	25.02	102.65	1888.1	16.02	989	6.02	15.44	0.46	1993-2015	0.17
10	Sanya	18.22	109.58	419.4	25.29	1340	6.10	16.52	0.46	1993-2015	0.19
11	Golmud	36.42	94.92	2807.6	6.37	40	8.32	18.77	0.35	1993-2015	0.22
12	Lhasa	29.67	91.13	3648.9	9.05	434	8.22	20.47	0.30	1993–2015	0.21

Table 1. Geographical locations and datasets of the 12 stations used in this study.

¹ T_{mean} represents mean air temperature, *P* mean annual precipitation, R_g mean global radiation, K_D mean ratio of diffuse radiation to global radiation; ² Measurements obtained on February 29 in each leap year have been discarded from analysis for convenience.



Figure 1. Geographical distribution of the solar radiation observation stations used in this study.

The predictive performance of ground-based models for surface albedo estimation is commonly evaluated through comparison of modelled results conducted for several specific sites against in situ measurements obtained at those sites [7,40]. However, it has been shown that almost everything forming the surroundings of a specific site affects the surface albedo of that site [6]. This dependence of ground albedo on multiple factors makes it impossible to develop a ground-based model that integrates all relevant influencing factors. Actually, for most proposed predictive models, the anisotropy of surface albedo is described by only one

or two model variables [7,41]. It is impracticable to use point-to-point comparison methods to assess the performance of ground-based models with consideration of only a limited number of influencing factors against in situ measurements that were obtained under the effect of all influencing factors. Moreover, in situ measurements used for computing surface albedo themselves have inherent uncertainties related to instrument precision and data processing [42]. In this context, multi-year mean values of daily ground albedo are recommended for use as true values in model evaluation, which can be determined as follows:

$$x_{\rm Ym}^{k} = \frac{1}{L^{k}} \sum_{i=1}^{L^{k}} \alpha_{\rm Dm}^{k,i}$$
(2)

where α_{Ym} is the multi-year mean value of daily ground albedo, and *L* is the number of years with valid data after data quality control.

2.2. Surface Albedo Prediction Models

2.2.1. Ineichen Model (IeM)

In pioneering studies of the solar energy balance over a large land area, it was customary to use a constant (i.e., 0.20) as an a priori value of zonal mean albedo because of the scarcity of ground albedo observations [1,4]. Following the development of advanced instrumentation for measuring radiation, Ineichen et al. [38] used site measurements of radiation components to examine the applicability of the default value. Their comparative results showed ground albedo is generally site-dependent and should be replaced by a value more representative of the measurement site. Following the suggestions of Psiloglou and Kambezidis [4], geometric mean value is used in the evaluation, i.e.,

$$\alpha_{\text{IeM}} = \left(\prod_{k=1}^{K} \alpha_{\text{Ym}}^{k}\right)^{1/K} \tag{3}$$

where α_{IeM} is IeM-estimated ground albedo, *K* is the number of days with valid measured data.

2.2.2. Gueymard Model (GM)

Gueymard [31] attributed the site variation of surface albedo to latitude dependence and parameterized the monthly regional albedo as a function of latitude through polynomial fitting of site measurements of surface albedo in North America as follows:

$$\boldsymbol{\kappa}_{\rm GM}(\boldsymbol{\varphi}) = \mathbf{C} \boldsymbol{\Phi}^{\rm T} \tag{4}$$

where α_{GM} is GM-estimated ground albedo, $\Phi = (1, \varphi, \varphi^2, \varphi^3)$ is the variable matrix, in which φ (deg.) is latitude, and $\mathbf{C} = (c_0, c_1, c_2, c_3)$ is the coefficient matrix. When latitude is < 30°, $\mathbf{C} = (-0.18, 0.024, -0.0004, 0)$; when 30° < $\varphi < 60°$, the coefficient matrix \mathbf{C} is specific for each month, as provided by Gueymard [31]. In addition, daily values can be obtained through interpolation. Although GM was proposed originally to estimate regional ground albedo, it has been extended to prediction of local ground albedo [4].

2.2.3. Dong Model (DeM)

Paltridge and Platt [32] examined the dependence of surface albedo on solar height angle and proposed an exponential equation for determining surface albedo; however, they did not provide values of the model parameters for detailed land types. Subsequently, Dong et al. [30] collected meteorological data from a network of 53 stations in California (USA) to examine the efficacy of the exponential equation through nonlinear regression analysis, and a modified exponential equation was proposed:

$$\alpha_{\rm DeM}^k = 0.0905h^k + 0.3860\exp\left(-1.0772h^k\right) \tag{5}$$

where α_{DeM} is DeM-estimated ground albedo, *h* (rad) is the solar height angle, which is determined as follows:

$$h^{k} = \frac{\pi}{2} - \left| \delta^{k} - \frac{\pi}{180} \varphi \right| \tag{6}$$

in which δ is solar declination

2.2.4. Iziomon-Mayer Model (IMM)

Iziomon and Mayer [33] recognized that the limitation of DeM in estimating surface albedo results from its ignorance of certain elevation-dependent factors, and they modified DeM by incorporating an elevation term:

$$\alpha_{\rm IMM}^k = 0.0905h^k + 0.3860 \exp\left(-1.0772h^k\right) + 0.00002H \tag{7}$$

where α_{IMM} is IMM-estimated ground albedo, *H* (m) is the altitude of the target location.

2.2.5. Morton Model (MM)

Nkemdirim [8], who found that surface albedo is largely dependent on SZA, expressed the instantaneous clear-sky ground albedo as an exponential function of SZA. By integrating the Nkemdirim equation over the range of SZA, Morton [37] developed an empirical model for determining daily average albedo:

$$\alpha_{\rm MM}^{k,i} = \alpha_{\rm 0MM}^k \left[S^{k,i} + \left(1 - S^{k,i} \right) \left(a_{\rm MM} + b_{\rm MM} Z^k \right) \right] \tag{8}$$

where α_{MM} is MM-estimated ground albedo, *S* is the relative sunshine duration, *Z* (=0.5 π – *h*) (rad) is the SZA at noon, a_{MM} and b_{MM} are constants, and α_{0MM}^k is the daily mean value of ground albedo under clear sky conditions determined as follows:

$$\alpha_{0\rm MM}^k = \alpha_z F\!\left(\omega_0, Z^k\right) \tag{9}$$

$$F\left(\omega_0, Z^k\right) = \frac{\exp(0.5\pi\omega_0) - \exp\left(\omega_0 Z^k\right) \left(\omega_0 \cos Z^k + \sin Z^k\right)}{\left(1 + \omega_0^k\right) \left(1 - \sin Z^k\right)}$$
(10)

where ω_0 is a constant associated with radiation layer characteristics. In the procedure of Morton [37], constant $\omega_0 = 0.6875$, $a_{\text{MM}} = 1$, $b_{\text{MM}} = -6/(11\pi)$, and α_z is determined as follows:

$$\alpha_{z} = \begin{cases} 0.11 & \text{for } \alpha_{zd} < 0.11 \\ \alpha_{zd} & \text{for } 0.11 \le \alpha_{zd} \le 0.17 \\ 0.17 & \text{for } \alpha_{zd} > 0.17 \end{cases}$$
(11)

where a_{zd} is the zenithal clear-sky ground albedo in the dry season given by:

$$a_{\rm zd} = 0.26 - 0.00012 p_s^{0.5} P \Big[1 + |\varphi/42| + (\varphi/42)^2 \Big]$$
(12)

in which *P* (mm) is the mean annual precipitation, and p_s is the relative atmospheric pressure.

2.2.6. Zhou Model (ZeM)

Zhou et al. [7] used the same form of equation as shown in Equation (8) to estimate ground albedo of a grassy surface but with the following three modifications:

- 1. ZeM uses different values of two coefficients from those used in the MM (i.e., $a_{ZeM} = 0.832$, $b_{ZeM} = 0.032$) to take the effect of cloud cover into consideration.
- 2. ZeM treats a vegetated surface as a mixture of vegetation and its underlying bare soil to incorporate the effect of vegetation phenology, weighted by the proportions

of bare soil and vegetation coverage. The daily mean ground albedo under clear sky conditions is thus determined as follows:

$$\alpha_{0\text{ZeM}}^{k} = \alpha_{s}^{k} (1 - f_{0}^{k}) + \alpha_{v}^{k} f_{0}^{k}$$
(13)

in which f_0 is the fraction of vegetation cover given by [7]:

$$f_0^k = 1 - \exp\left(-\zeta \cdot \psi^k\right) \tag{14}$$

where ψ is the daily LAI, ζ is the canopy extinction coefficient, α_s and α_v are the daily mean values of clear-sky ground albedo over the bare soil surface and over the vegetated surface, respectively.

1. ZeM notes the discrepancy in form between Nkemdirim's exponential function and the regression equations of numerous subsequent observations for describing the variation of instantaneous ground albedo with SZA, and it modifies the exponential function by adding a constant term. The computational formulae of α_v and α_s thus become

$$\alpha_v^k = A_v F\left(\omega_v, Z^k\right) + B_v\left(0.5\pi - Z^k\right) \tag{15}$$

$$\alpha_s^k = A_s F\left(\omega_s, Z^k\right) + B_s\left(0.5\pi - Z^k\right) \tag{16}$$

where ω_s and ω_v are statistically estimated coefficients, and A_v , A_s , B_v , and B_s are empirical constants. In the calculation procedure, $\omega_s = 0.4732$, $\omega_v = 0.6090$, and the empirical coefficients A_s and A_v can be determined as follows:

$$A_s = C_{1s} P_r^{-0.5} \xi_s + C_{2s} \tag{17}$$

$$A_v = C_{1v} P_r^{-0.5} \xi_v + C_{2v} \tag{18}$$

where ξ_s and ξ_v are constants, and C_{1s} , C_{2s} , C_{1v} , and C_{2v} are constants that need to be calibrated. The values of these constants have been calibrated against meteorological observations across China.

2.3. Statistical Evaluation

The performance of the studied models was evaluated using six dispersion indicators and one global performance indicator (GPI). The dispersion indicators included the mean absolute percentage error (MAPE), root mean square error (RMSE), relative root mean square error (RRMSE), t-statistics (TS), uncertainty at 95% (U_{95}), and coefficient of determination (R^2). Details of these dispersion indicators are listed in Table 2. The closer the R^2 value is to 1, and the smaller the values of all other indicators, the better the model performs.

The GPI, proposed by Despotovic et al. [2] to compare the performance of various different models, combines all the selected dispersion indicators into a single indicator, i.e.,

$$GPI_m = \sum_{j=1}^{6} \kappa_j (\hat{\eta}_j - \eta_{j,m})$$
(19)

where GPI *m* is the GPI value for model *m*, $\eta_{j,m}$ is the scaled value of indicator j for model *m*, 0 is scaled for the minimum value, and 1 for the maximum value; $\hat{\eta}_j$ is the median of the scaled value of indicator *j*, κ_j is equal to 1 for all indicators except it is equal to -1 for *j* = 6 (\mathbb{R}^2). A higher value of the GPI indicates greater model accuracy.

Indicator	Concept	Equation ¹	Function	Ideal Value	Author(s)
Mean bias error (MBE)	Arithmetic mean of the errors	$\text{MBE} = \frac{1}{K} \sum_{k=1}^{K} \left(\alpha_{\text{De}}^{k} - \alpha_{\text{Dm}}^{k} \right)$	A statistical indicator for testing the long-term tendency of the models	0	Behar et al. [3]
Mean absolute percentage error (MAPE)	Arithmetic mean of magnitude of relative errors	$\text{MAPE} = \frac{1}{K} \sum_{k=1}^{K} \left \frac{\alpha_{\text{De}}^{k} - \alpha_{\text{Dm}}^{k}}{\alpha_{\text{Dm}}^{k}} \right $	A statistical indicator for comparing predictive errors of different models	0	Gueymard [42] Fan et al. [43]
Root mean square error (RMSE)	Square root of the mean square errors	$\text{RMSE} = \sqrt{\frac{1}{K}\sum_{k=1}^{K} \left(\alpha_{\text{De}}^{k} - \alpha_{\text{Dm}}^{k}\right)^{2}}$	A measure of error-magnitude variance for examination of the short-term performance of the models	0	Willmott and Matsuura [44]
Relative root mean square error (RRMSE)	RMSE divided by the average value of measured data	$RRMSE = \frac{RMSE}{\alpha_m}$	A measure of the overall relative accuracy of the models	0	Jamieson et al. [45] Li et al. [46]
<i>t</i> -statistics (TS)	Statistical significance of model estimates at a particular confidence level	$TS = \sqrt{\frac{(K-1)MBE^2}{RMSE^2 - MBE^2}}$	A conjunction of the RMSE with MBE for more reliable assessment of model performance	0	Stone [47]
Uncertainty at the 95% level (U ₉₅)	Expanded uncertainty with 95% confidence	$U_{95} = 1.96 \left(\text{SD}^2 + \text{RMSE}^2 \right)^{1/2}$	An indicator representing information of model deviation	0	Gueymard [42]
Coefficient of determination(R^2)	Square of the correlation coefficient	$R^{2} = \frac{\left[\sum_{k=1}^{K} \left(\alpha_{De}^{k} - \alpha_{e}\right) \left(\alpha_{Dm}^{k} - \alpha_{m}\right)\right]^{2}}{\sum_{k=1}^{K} \left(\alpha_{De}^{k} - \alpha_{e}\right)^{2} \sum_{k=1}^{K} \left(\alpha_{Dm}^{k} - \alpha_{m}\right)^{2}}$	A measure of model linearity relative to measured data	1	Behar et al. [3] Gueymard [42]

Table 2. Statistical indicators for performance evaluation of ground albedo models.

¹ *K* is the number of days with valid measured data, SD represents the standard deviation of the difference between estimated results and observed data, α_m and α_e represent the annual mean values of measured and estimated ground albedo, respectively.

3. Results and Discussion

3.1. Model Evaluation

Figure 2 depicts graphically the MAPE values for the six models. It can be seen from the figure that the best MAPE was obtained with ZeM, which produced the smallest MAPE at 10 out of 12 selected stations with mean MAPE of 3.76% ranging from 2.00% (Golmud) to 6.10% (Chengdu). IeM also produced acceptable estimations of surface albedo at all selected stations with mean MAPE of 4.82% ranging from 3.02% (Sanya) to 9.28% (Lhasa). For the remaining models, i.e., GM, DeM, IMM, and MM, the MAPE values were in the range 3.35–34.58%, 6.55–43.03%, 6.11–52.55%, and 6.23–48.98%, respectively.



Figure 2. MAPE values for the six models at 12 selected stations.

The lowest values of RMSE were obtained for ZeM at 9 out of 12 selected stations with mean RMSE of 0.0087 varying from 0.0055 (Golmud) to 0.0152 (Kashgar). For IeM, GM, DeM, IMM, and MM, the RMSE values were in the range 0.0068–0.0225, 0.0070–0.0664, 0.0170–0.0702, 0.0188–0.0898, and 0.0134–0.1094, respectively. In terms of RRMSE, as presented in Figure 3, ZeM showed the lowest values at 11 out of 12 selected stations with mean RRMSE of 4.62% ranging from 2.54% (Golmud) to 7.62% (Chengdu). IeM also provided reasonably small values of RRMSE (mean: 5.99%). However, the mean RRMSE values of the remaining four models were dramatically higher than both ZeM and IeM, ranging from 18.34% (GM) to 32.03% (IMM). Jamieson et al. [44] used the criteria "excellent", "good", "fair", and "poor" to test the goodness-of-fit between estimated results and measured data. For solar radiation time series, a RRMSE values of <10%, 10–20%, 20–30%, and >30% are considered excellent, good, fair, and poor, respectively [45]. According to these criteria, the RRMSE indicator ranked ZeM excellent at all selected stations. Although the RRMSE ranked GM fair at high-latitude stations (e.g., Ejin Banner, Beijing, Kashgar, and Golmud stations), the model was ranked excellent or good at certain mid-latitude stations (e.g., Kunming, Wuhan, and Shanghai stations). Similar results were found based on the estimated results from the other five models.



Figure 3. RRMSE values for the six models at 12 selected stations.

The mean U_{95} values were 0.0312, 0.0869, 0.0903, 0.1196, 0.1065, and 0.0230 for IeM, GM, DeM, IMM, MM, and ZeM, respectively, i.e., IeM produced the lowest U_{95} value. In terms of individual stations, the estimated TS values for the GM, DeM, IMM, MM and ZeM models significantly greater than 1.96 (except ZeM that produced TS value of <1.96 at the Kashgar station, Figure 4), indicating statistically significant difference between the paired values of estimated and measured data at the 95% confidence level. However, for the IeM model, the calculated TS values for the 12 selected stations are generally less than 1.96.



Figure 4. TS values for the six models at 12 selected stations.

In terms of R^2 , ZeM showed the highest degree of agreement between the estimations and measurements with mean R^2 of 0.3942. Despite being the model with the best overall performance, the R^2 values of ZeM, which ranged from 0.0029 to 0.9459, reflected that the model produced an almost perfect linear relationship between the modelled results and measured data at certain studied stations (e.g., Ejin Banner, Guangzhou, Golmud, and Lhasa stations), while it performed poorly at other stations (e.g., Chengdu, Wuhan, and Kashgar stations). The R^2 value for IeM was zero at each selected station, and the remaining models (i.e., GM, DeM, IMM, and MM) had R^2 values of around zero at most selected stations, indicating absence of a linear relationship between the modelled results and measured data. Comparisons of the modelled results with measured data at 12 selected stations are shown in Figure 5.



Figure 5. Comparisons of estimated results with measured data at (a) Ejin Banner, (b) Beijing, (c) Kashgar, (d) Zhengzhou, (e) Wuhan, (f) Shanghai, (g) Chengdu, (h) Kunming, (i) Guangzhou, (j) Sanya, (k) Golmud, and (l) Lhasa stations.

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The calculated GPI values for the studied models are presented in Figure 6. Based on the composite indicator GPI, ZeM was found the best-performing model for ground albedo estimation in China with mean GPI of 1.58 varying from 0.95 (Ejin Banner) to 2.29 (Beijing). The second most accurate model was IeM with mean GPI of 0.68, followed by GM (-0.78), MM (-1.22), and DeM (-1.65); the model with the poorest performance was IMM (-2.64). It should be noted that the two most accurate models, i.e., ZeM and IeM (in essence), were developed using in situ measurements from meteorological stations in China, whereas the remaining four models (i.e., GM, DeM, IMM, and MM), which produced unsatisfactory predictions of ground albedo in China, were proposed based on measurements processed from sites outside China. It is emphasized that existing groundbased albedo models are generally site-specific and are thus inapplicable to other locations without model re-calibration. It is also important to note that some simple models with poor overall performance produced the best GPI value at certain individual stations. For instance, GM produced the best GPI value at Chengdu station. It reveals that for large-scale areas with different conditions, it is impossible for a fixed-parameter model, even a complex one, to perform well everywhere, whereas even a simple model has potential for accurate estimation of ground albedo with appropriate model parameters.



Figure 6. GPI values for the six models at 12 selected stations.

3.2. Re-Calibration with In-Situ Measurements

Previous studies have shown that ground albedo is largely dependent on solar height angle. In addition, the use of the solar height angle has the advantage that this single easily accessible variable can account for both the spatial and the temporal variations of surface albedo with latitude and solar seasonal variation, respectively. Therefore, DeM was selected to re-calibrate (referred to as rDeM) with in-situ measurements across China. The general equation of rDeM can be written as

$$\alpha_{\rm rDeM}^k = a_n^k H^k + b_n^k \exp\left(-1.0772H^k\right) \tag{20}$$

where α_{rDeM} is rDeM-estimated daily ground albedo, *a* and *b* are constants to be calibrated against measured data, and subscript *n* denotes parameters for the *n*th station.

The general equation for each delineated region was calibrated against the measured data from the 12 selected stations. The values of a_n and b_n were adjusted repeatedly until the calculated results of the selected statistical indictors were as close as possible to their ideal values. The calibrated values of a_n and b_n for all studied stations are listed in Table 3. Figure 7 depicts the comparisons between the estimated results and the measured data with acceptable values of MAPE in the range from 2.99% to 6.28%, RMSE from 0.0075 to 0.0168, RRMSE from 4.03% to 7.57%, U95 from 0.0116 to 0.0463, TS from 1.19 to 9.11, and R2 from 0.0078 to 0.7879, as listed in Table 3. With consideration of the indicator GPI illustrated



in Figure 8, rDeM has the potential to predict surface albedo as accurately as a complex model (ZeM). The results indicate that rDeM can be adopted as a surrogate for ZeM to predict surface albedo in China.

Figure 7. Comparisons of rDeM predictions with measured data at (a) Ejin Banner, (b) Beijing, (c) Kashgar, (d) Zhengzhou, (e) Wuhan, (f) Shanghai, (g) Chengdu, (h) Kunming, (i) Guangzhou, (j) Sanya, (k) Golmud, and (l) Lhasa stations.

Station	Model Pa	rameters	Statistical Indicators							
Station –	a _n	b_n	MAPE (%)	RMSE	RRMSE (%)	U_{95}	TS	<i>R</i> ²		
Ejin Banner	0.1140	0.354	3.55	0.0116	4.63	0.0310	7.36	0.6944		
Beijing	0.0779	0.250	4.75	0.0094	5.42	0.0251	8.14	0.1666		
Kashgar	0.1112	0.300	6.28	0.0168	7.57	0.0463	2.63	0.0128		
Zhengzhou	0.0722	0.250	5.06	0.0104	6.19	0.0116	1.19	0.1362		
Wuhan	0.0854	0.250	3.92	0.0086	4.94	0.0238	1.28	0.2201		
Shanghai	0.0831	0.250	4.44	0.0093	5.46	0.0248	7.71	0.0753		
Chengdu	0.0791	0.232	5.55	0.0109	6.86	0.0299	4.57	0.0078		
Kunming	0.0814	0.250	3.37	0.0075	4.42	0.0208	1.92	0.0002		
Guangzhou	0.0831	0.258	4.79	0.0103	5.81	0.0277	7.22	0.3848		
Sanya	0.0882	0.285	2.99	0.0077	4.03	0.0203	8.84	0.0073		
Golmud	0.0963	0.325	3.54	0.0091	4.23	0.0251	2.86	0.5104		
Lhasa	0.0756	0.386	5.83	0.0152	7.04	0.0402	9.11	0.7879		

Table 3. Calibrated values of rDeM parameters for selected stations.



Figure 8. GPI values for each station when DeM is replaced by rDeM for model comparison.

3.3. Temporal Stability Analysis

Surface albedo varies with everything that forms the local surroundings. These are impossible to parameterize fully into a simple model, whilst in situ measurements used for model development would be conducted under the effect of all possible factors. Therefore, in this paper multi-year mean daily values of time series data were used to evaluate and calibrate the studied models. Given the vulnerability of time series dynamics to alterations in the mean and variance [48], particular care should be taken to check the temporal stability of the time series data obtained from all the selected stations. To eliminate the effect of short-term random fluctuations and daily data gaps arising from data quality control, monthly mean values of measured ground albedo were used for the analysis, which were derived as follows:

$$\alpha_{\rm Mm}^{r,k} = \frac{1}{N^r} \sum_{i=1}^{N^r} \alpha_{\rm Dm}^{k,i}$$
(21)

where α_{Mm} is the monthly mean value of daily ground albedo, N^r is the number of days in the *r*th month.

For the *r*th month, the Θ^r -year accumulated mean and corresponding variation coefficient were determined as follows:

$$\mu^{r,\Theta^r} = \frac{1}{\Theta_r} \sum_{i=1}^{\Theta^r} \alpha_{\mathrm{Mm}}^{r,i}, \ 1 < \Theta^r \le I$$
(22)

$$\sigma^{r,\Theta^r} = \frac{1}{\mu_{\rm Mm}^{r,\Theta^r}} \sqrt{\frac{1}{\Theta^r - 1} \sum_{i=1}^{\Theta^r} \left(\alpha_{\rm Mm}^{r,i} - \mu^{r,\Theta^r}\right)}$$
(23)

where *I* is the number of years in the period, μ^{r,Θ^r} and σ^{r,Θ^r} are the mean and the variance, respectively. If a value of Θ^r exists that is less than *I* and makes the following two formulae true, and where the formulae are also satisfied for an arbitrary value greater than Θ^r , the time series tested in the *r*th month can be considered temporally stable:

$$\Delta_{\mu}^{r,\Theta^{r}} = \left| \left(\mu^{r,\Theta^{r}} - \mu^{r,I} \right) / \mu^{r,I} \right| \le \varepsilon_{\mu}$$
(24)

$$\Delta_{\sigma}^{r,\Theta^{r}} = \left| \left(\sigma^{r,\Theta^{r}} - \sigma^{r,I} \right) / \sigma^{r,I} \right| \le \varepsilon_{\sigma}$$
(25)

where Δ_{μ} and Δ_{σ} are the relative differences for the mean and the variation coefficient in the *r*th month, and ε_{μ} and ε_{σ} are acceptable relative differences. Taking two stations as examples, the variations of $\mu^{r,\Theta^{r}}$ and $\sigma^{r,\Theta^{r}}$ with Θ^{r} are shown in Figure 9.



Figure 9. Temporal stability checks of accumulated mean surface albedo at (**a**) Kunming and (**b**) Guangzhou stations.

It can be seen that the values of $\Delta_{\mu}^{r,\Theta^{r}}$ and $\Delta_{\sigma}^{r,\Theta^{r}}$ in each month tend to be stable as *i* increases. The minimum Θ^{r} value was defined as the critical value of observation years for collecting time series data with temporal stability in the *r*th month, denoted as Θ_{*}^{r} . Hence, the maximum value of the critical values for all months throughout the year is the shortest year for observing data with temporal stability, that is,

$$\Theta_* = \max(\Theta_*^r) \tag{26}$$

where Θ_* represents the critical value of observation years for collecting stable time series data at selected stations. The mean and standard deviation of Θ_*^r for each station are shown in Figure 10. Most generally, if one station in China continuously observes albedo data for more than 10 years, the time series obtained is considered temporally stable.

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Figure 10. Mean and standard deviation of Θ_*^r for collecting temporally stable time series at 12 selected stations.

4. Conclusions

This study investigated the applicability of six available models for ground albedo estimation with long-term measurements of global and reflected radiation components acquired by the network for solar radiation observation across China. Comparative results indicated that model performance does not rely merely on the number of model parameters, that is, a simplemodel with appropriate model parameters has the potential to predict surface albedo as accurately as a complex model. Hence, the simple two-parameter DeM was re-calibrated for surface albedo estimation in China. The detailed conclusions derived from this study are summarized as follows.

- 1. The evaluation results of model performance through statistical analysis showed that among the available ground albedo models, ZeM had the best overall performance at 12 selected stations for model evaluation. IeM was shown to provide acceptable estimations for locations where albedo records are readily available, which limits its scope of application. However, the simple models with fixed parameters (i.e., GM, DeM, and IMM) are site-specific. Therefore, when applied to other locations, these models should be re-calibrated with measured data.
- 2. In the re-calibration procedure of DeM, multi-year mean daily values of time series data were used in this paper. Special care was taken to examine the temporal stability of these series. It was found that, in general, a time series of in situ measurements extending over a period greater than 10 years could be considered temporally stable.
- 3. The performance of re-calibrated DeM was as acceptable as that of the complex ZeM in China. This simple model offers an alternative for surface albedo estimation with easily accessible inputs and less computational effort.

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