



Figure S2. Structures of (a) rutile $3 \times 2 \times 4$ supercell, (b) substitution of one Ti for two Y and one oxygen vacancy, (c) rutile $2 \times 2 \times 6$ supercell, and (d) substitution of Ti for two Nb and one Y.