

**Supplementary Information**

# **Co-carbonized Waste Polythene/Sugarcane Bagasse Nanocomposite for Aqueous Environmental Remediation Applications**

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**Text S1.**

Non-linear forms of Langmuir [63] (Equation (S1)) and Freundlich [64] (Equation (S2)), and Dubinin–Radushkevich (D-R) (Equations (S3) – (S5)) [65] isotherm models were applied to analyze the experimental data.

$$q_e = \frac{q_m K_L C_e}{1 + K_L C_e} \quad (S1)$$

$$q_e = K_F C_e^{1/n} \quad (S2)$$

$$q_e = q_s e^{-K_{DR} \varepsilon^2} \quad (S3)$$

$$\varepsilon = RT \ln \left( 1 + \frac{1}{C_e} \right) \quad (S4)$$

$$E = \frac{1}{\sqrt{2K_{DR}}} \quad (S5)$$

where,  $K_L$  (L/mg),  $K_F$  (mg/g)(L/mg)<sup>1/n</sup>, and  $n$  are Langmuir constant, Freundlich constant, and degree of the adsorption process, respectively.  $C_e$  (mg/L) is the MG concentration at equilibrium,  $q_e$  (mg/g) is the amount of MG adsorbed onto SBPE and SBPEAC composites at equilibrium;  $Q_m$  (mg/g) is the maximum adsorption capacity;  $q_s$  (mg/g) is the adsorption capacity;  $K_{DR}$  (mol<sup>2</sup>/kJ<sup>2</sup>) is the constant related to the sorption energy;  $\varepsilon$  is the Polanyi potential; and  $E$  (kJ/mol) is the mean adsorption energy.

**Text S2.**

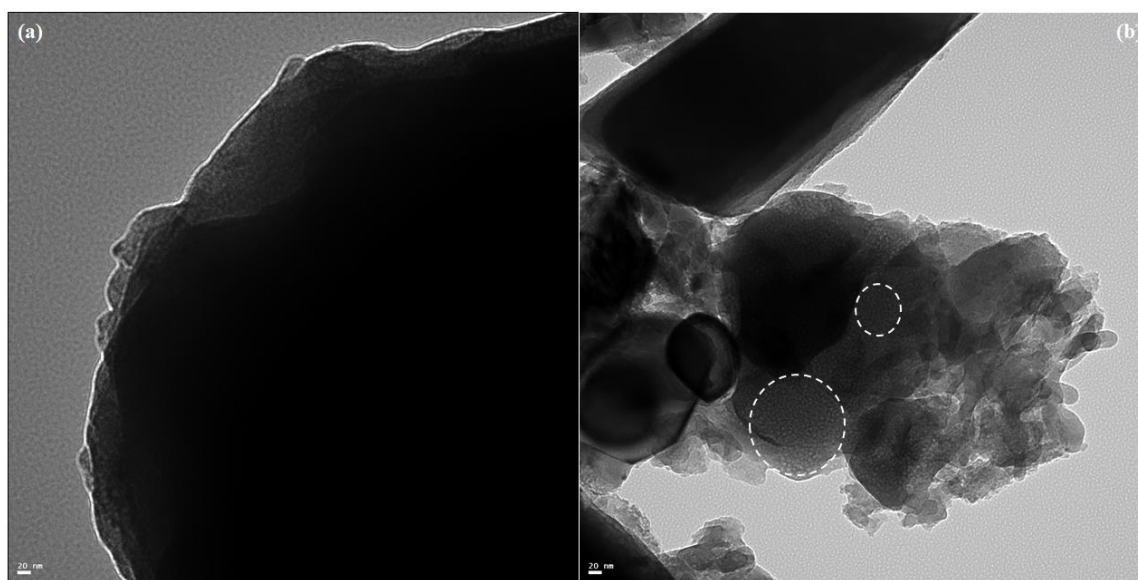
Non-linear pseudo-first order [69] (Equation (S6)), pseudo-second-order (Equation (S7)) [69], and Elovich models (Equation (S8)) [70] were used to investigate the reaction mechanism and rate of MG adsorption on SBPE and SBPEAC composites.

$$q_t = q_e(1 - e^{-K_1 t}) \quad (S6)$$

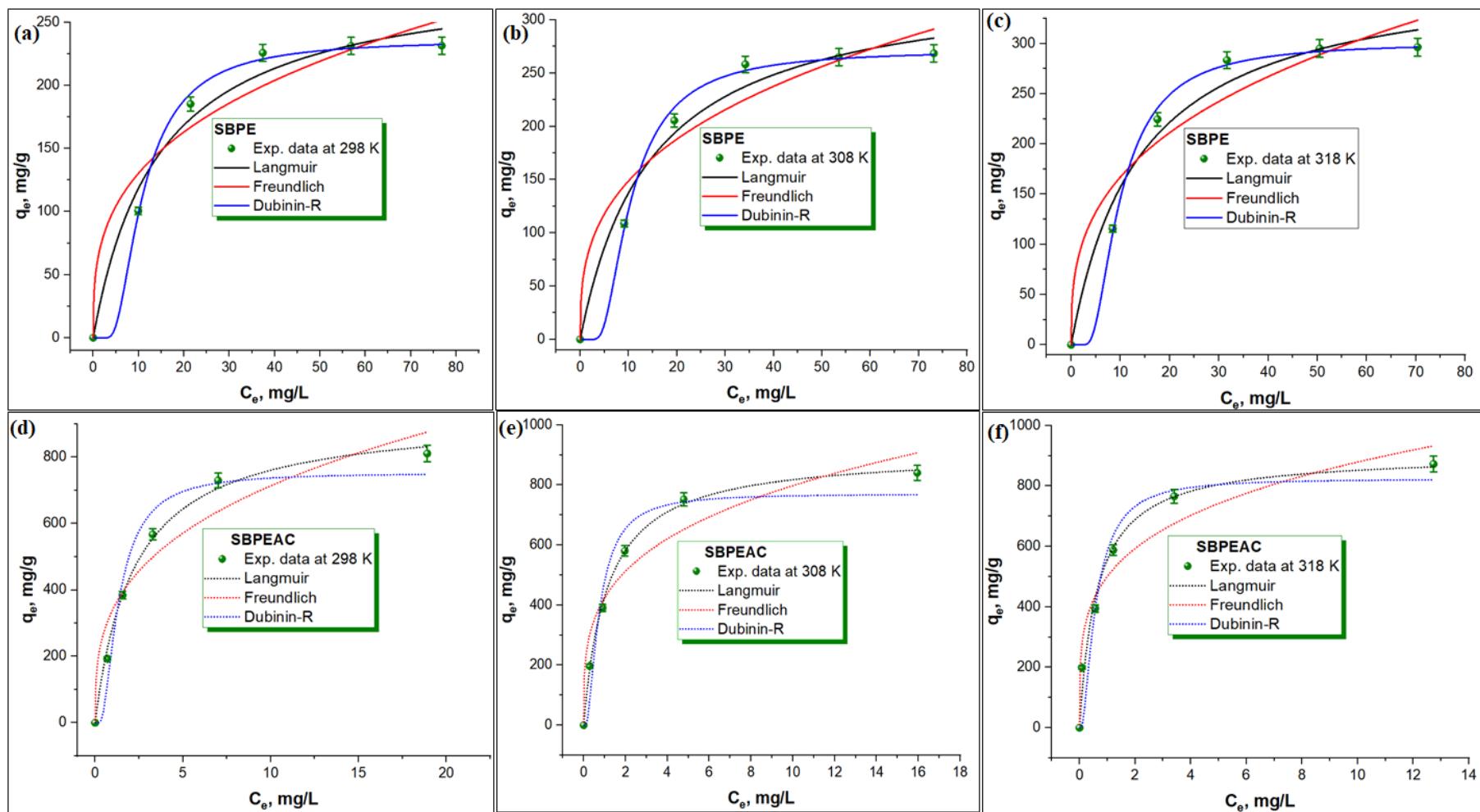
$$q_t = \frac{q_e^2 k_2 t}{1 + q_e k_2 t} \quad (S7)$$

$$q_t = \frac{1}{\beta} \ln(1 + \alpha \beta t) \quad (S8)$$

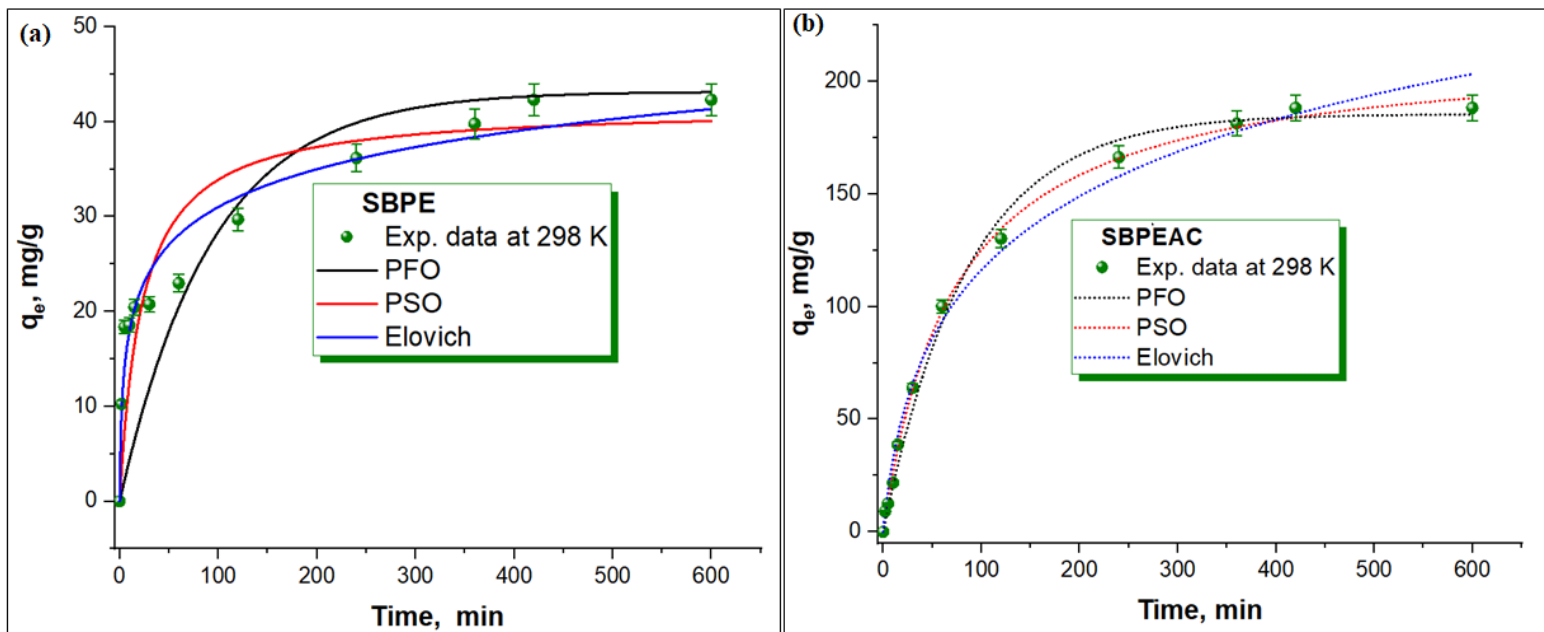
where,  $k_1$  (1/min), and  $k_2$  (g/mg min) are the rate constants for pseudo- first-order and pseudo-second-order models, respectively;  $q_t$  and  $q_e$  are the amounts of MG adsorbed at time  $t$  and equilibrium, respectively;  $\alpha$  (mg/g-min) is the initial adsorption rate;  $\beta$  (mg/g) is the desorption constant during any one experiment.



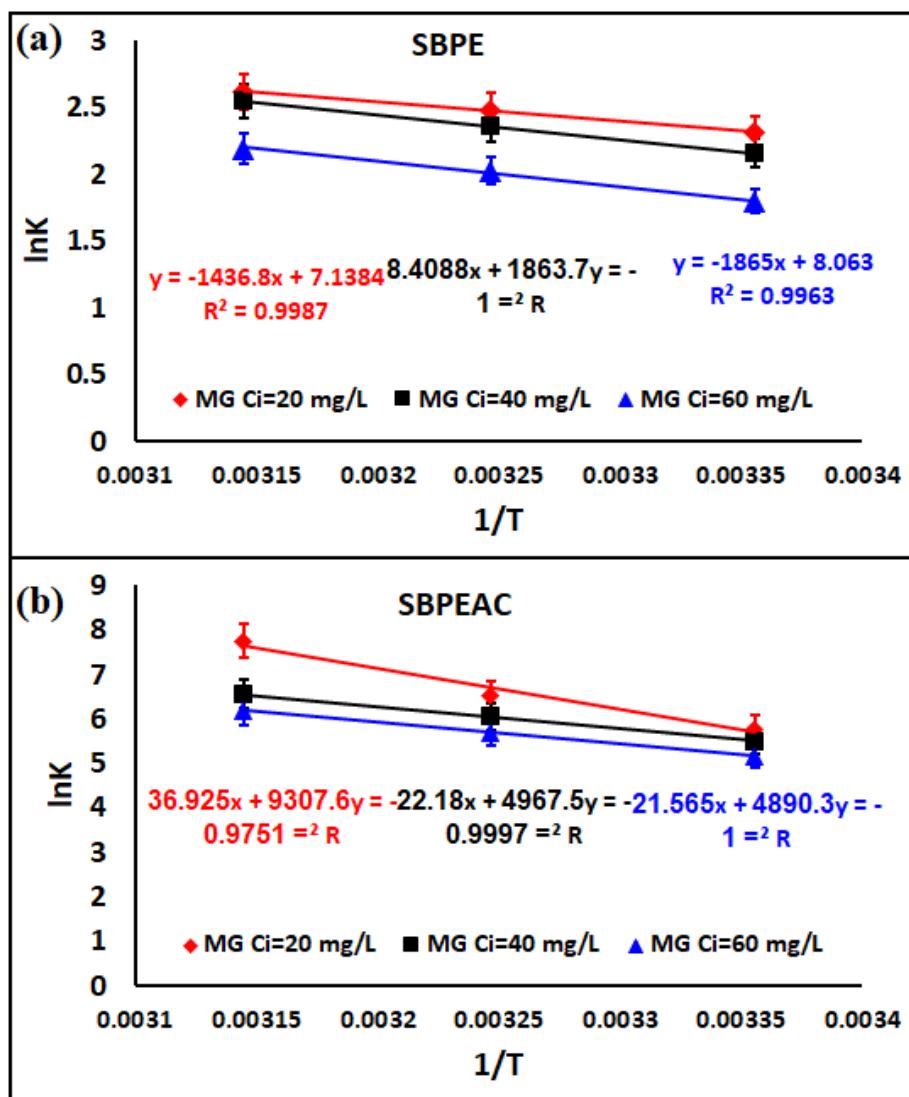
**Figure S1.** TEM images of SBPE (a), and SBPEAC (b) composites.



**Figure S2.** Non-linear isotherm models for MG adsorption on SBPE at 298 K (a), 308 K (b), 318 K (c), and on SBPEAC at (d) 298 K, (e) 308 K, (f) 318 K.



**Figure S3.** Non-linear kinetic models for MG adsorption on SBPE (a), and SBPEAC (b) composites.



**Figure S4.** Van't Hoff plots for MG adsorption on SBPE (a), and SBPEAC (b) composites.



## References

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