

Supplemental Materials

1 CODES TO PERFORM BMA TO EXPLORE RACIAL DISPARITY IN BREAST CANCER DIAGNOSTIC AGE

```
M1=cbind(M1$Isolation,M1$poverty,M1$under18,M1$intden,
M1$StrDen,M1$cnr,M1$comorb1,M1$comorb2,M1$insurance1,
M1$insurance2,M1$marry1,M1$marry2,M1$marry3,M1$stage1,
M1$stage2,M1$stage3,M1$stage4,M1$BMI_c1,M1$BMI_c2,M1$BMI_c3)
#####
contm=c(1,2,3,4,5,6)
p1=length(contm)
deltam=rep(0.01,p1)
contm1=matrix(data=c(1,2,3,4,5,6,1,2,3,4,5,6),6,2)
binm=NULL
p2=length(binm)
catm1=matrix(data=c(7,10,13,17,22,9,12,16,21,25),5,2)
catm=c(7,8,9,10,11)
p3=length(catm)
cat2=c(3,3,4,5,4)
cat1=max(cat2)-1
P=ncol(M1)
mu=rep(0,P)
Omega=diag(0.000001,P)
mu0.1=rep(0,P)
Omega0.1=diag(0.000001,P)
mu1.1=rep(0,P)
Omega1.1=diag(0.000001,P)
mu0.a=rep(0,p1)
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Omega0.a=diag(0.000001,p1)
mu1.a=rep(0,p1)
Omega1.a=diag(0.000001,p1)
mu0.b=rep(0,p2)
Omega0.b=diag(0.000001,p2)
mu1.b=rep(0,p2)
Omega1.b=diag(0.000001,p2)
mu0.c=rep(0,cat1)
Omega0.c=diag(0.000001,cat1)
mu1.c=rep(0,cat1)
Omega1.c=diag(0.000001,cat1)
nrow(datanew0)
M22=M2[,c(3:8,15,10,11,12,14)]
nrow(M2)
data0<- list (N=2275,x=datanew0$race,y=datanew0$age_at_diagnosis,
M1=M1,M2=M22,contm=contm,contm1=contm1,p1=p1,
cat1=cat1,cat2=cat2,catm=catm,p3=p3,P=P,
mu=mu,Omega=Omega,mu0.1=mu0.1,mu1.1=mu1.1,Omega0.1=Omega0.1,
Omega1.1=Omega1.1,mu0.a=mu0.a,mu1.a=mu1.a,Omega0.a=Omega0.a,
Omega1.a=Omega1.a,mu0.c=mu0.c,mu1.c=mu1.c,Omega0.c=Omega0.c,
Omega1.c=Omega1.c)
inits<- function(){list()}
med0<- jags(data0, inits,
model.file = "C:/Users/wcao/Desktop/test1.txt",
parameters = c("beta0","c","beta","prec4","alpha0","alpha1","prec2",
"alpha0.a","alpha1.a","prec1","alpha0.c","alpha1.c"),
n.chains = 1, n.iter = 11000,n.burnin=1000,n.thin = 1)
#check the results
#calculate the mediation effects
N=2275
N1=10000
M3=M1
M3[,1:6]=M3[,1:6]+0.01
attach(med0$BUGSoutput$sims.list)
#method 1
aie1=matrix(0,N1,p1+p3)
for (j in 1: p1)
{aie1[,contm[j]]=alpha1.a[,j]*beta[,contm[j]]}

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}

for (j in 1:p3){
  mu_Mc1<-matrix(0,N1,cat2[j]-1)
  mu_Mc0<-matrix(0,N1,cat2[j]-1)
  for (k in 2:cat2[j]){
    mu_Mc1[,k-1] <- exp(alpha0.c[,j,k-1]+alpha1.c[,j,k-1])
    mu_Mc0[,k-1] <- exp(alpha0.c[,j,k-1])
  }
  sum_Mc1 <-apply(mu_Mc1,1,sum)+1
  sum_Mc0 <-apply(mu_Mc0,1,sum)+1
  aie1[,catm[j]]<-diag((diag(1/sum_Mc1)%*%mu_Mc1-diag(1/sum_Mc0)%*%
  mu_Mc0)%*%t(beta[, (catm1[j,1]-j+1):(catm1[j,2]-j)]))
}
de1=c
te1=apply(aie1,1,sum)+de1

#method2
aie2=matrix(0,N1,p1+p3)
ie2=array(0,dim=c(N1,N,p1))
for (j in 1:p1){
  ie2[, , j]=(alpha1.a[, j]/deltam[j])* 
  (beta[, contm1[j,1]:contm1[j,2]]%*%t(M3[, contm1[j,1]:contm1[j,2]] 
  -M1[, contm1[j,1]:contm1[j,2]]))
  aie2[, contm[j]]=apply(ie2[, , j], 1, mean)
}

for (j in 1:p3){
  mu_Mc1<-matrix(0,N1,cat2[j]-1)
  mu_Mc0<-matrix(0,N1,cat2[j]-1)
  for (k in 2:cat2[j]){
    mu_Mc1[,k-1] <- exp(alpha0.c[,j,k-1]+alpha1.c[,j,k-1])
    mu_Mc0[,k-1] <- exp(alpha0.c[,j,k-1])
  }
  sum_Mc1 <-apply(mu_Mc1,1,sum)+1
  sum_Mc0 <-apply(mu_Mc0,1,sum)+1
  aie2[,catm[j]]<-diag((diag(1/sum_Mc1)%*%mu_Mc1-diag(1/sum_Mc0)%*%
  mu_Mc0)%*%t(beta[, (catm1[j,1]-j+1):(catm1[j,2]-j)]))
}

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de2=c
te2=apply(aie2,1,sum)+de2

#method 3:parametric
ate3=NULL
aie3=NULL
for (m in 1:N1)
{mu_M2=M1
mu_M3=M1
for (j in 1:p1){
for (k in contm1[j,1]:contm1[j,2]){
mu_M2[,k] <- alpha0[m,k]+alpha1[m,k]
mu_M3[,k] <- alpha0[m,k]
}}}

for (j in 1:p3){
mu_Mc2=rep(0,cat2[j]-1)
mu_Mc2[1:(cat2[j]-1)]<-exp(alpha0.c[m,j,(2:cat2[j])-1] +
alpha1.c[m,j,(2:cat2[j])-1])
sum_Mc2 <-sum(mu_Mc2)+1
mu_M2[, (catm1[j,1]-j+1):(catm1[j,2]-j)] <-
matrix(rep(mu_Mc2/sum_Mc2,each=N),N)
mu_Mc3=rep(0,cat2[j]-1)
mu_Mc3[1:(cat2[j]-1)] <- exp(alpha0.c[m,j,(2:cat2[j])-1])
sum_Mc3 <-sum(mu_Mc3)+1
mu_M3[, (catm1[j,1]-j+1):(catm1[j,2]-j)] <-
matrix(rep(mu_Mc3/sum_Mc3,each=N),N)
}

mu_y1<- rep(beta0[m,],each=N) + rep(c[m],each=N) + mu_M2%*%beta[m,]
mu_y0<- rep(beta0[m,],each=N) + mu_M3%*%beta[m,]
te3<- mu_y1-mu_y0
ate3=c(ate3,mean(te3))
j1=sample(1:N,replace=T)
j2=sample(1:N,replace=T)
ie=matrix(0,N,p1+p3)
#1. p1 is the total number of continuous mediators
for (j in 1:p1){

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if(contm1[j,1]<contm1[j,2])
ie[,j]<-te3-(mu_y1-mu_M2[,contm1[j,1]:contm1[j,2]]%*%
beta[m,contm1[j,1]:contm1[j,2]]+
M1[j1,contm1[j,1]:contm1[j,2]]%*%beta[m,contm1[j,1]:contm1[j,2]]-
mu_y0+ mu_M3[,contm1[j,1]:contm1[j,2]]%*%
beta[m,contm1[j,1]:contm1[j,2]]-
M1[j1,contm1[j,1]:contm1[j,2]]%*%beta[m,contm1[j,1]:contm1[j,2]]) 
else
ie[,j]<-te3-(mu_y1-mu_M2[,contm1[j,1]]*beta[m,contm1[j,1]]+
M1[j1,contm1[j,1]]*beta[m,contm1[j,1]]-
mu_y0+ mu_M3[,contm1[j,1]]*beta[m,contm1[j,1]]-
M1[j1,contm1[j,1]]*beta[m,contm1[j,1]])
}
for (l in 1:p3){
ie[,l+p1+p2]<-te3-(mu_y1-mu_M2[, (catm1[l,1]-l+1):(catm1[l,2]-l)]%*%
beta[m,(catm1[l,1]-l+1):(catm1[l,2]-l)]+
M1[j1,(catm1[l,1]-l+1):(catm1[l,2]-l)]%*%
beta[m,(catm1[l,1]-l+1):(catm1[l,2]-l)]-
mu_y0+ mu_M3[, (catm1[l,1]-l+1):(catm1[l,2]-l)]%*%
beta[m,(catm1[l,1]-l+1):(catm1[l,2]-l)]-
M1[j1,(catm1[l,1]-l+1):(catm1[l,2]-l)]%*%
beta[m,(catm1[l,1]-l+1):(catm1[l,2]-l)])
}
aie3=rbind(aie3,apply(ie,2,mean))
}
de3=c

```

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#method 3: nonparametric
M111=cbind(M1,datanew0[,1])
M.0=M111[M111[,21]==1,]
M.1=M111[M111[,21]==2,]
M.0=M.0[,-21]
M.1=M.1[,-21]
ate4=NULL
aie4=NULL

for(m in 1:N1){

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j1=sample(1:N,replace = T)
j2=sample(1:N,replace = T)
j3=sample(1:nrow(M.0),N,replace = T)
j4=sample(1:nrow(M.1),N,replace = T)
te<- c[m] + (M.1[j4,]-M.0[j3,])%*%beta[m,]
ate4=c(ate4,mean(te))
#ie for continuous mediators
ie=matrix(0,N,p1+p2+p3)
for (j in 1:p1){
M.1.0=M.1[j4,]
M.0.0=M.0[j3,]
M.1.0[,contm1[j,1]:contm1[j,2]]=M1[j1,contm1[j,1]:contm1[j,2]]
M.0.0[,contm1[j,1]:contm1[j,2]]=M1[j2,contm1[j,1]:contm1[j,2]]
ie[,contm[j]]<-te-c[m]-(M.1.0-M.0.0)%*%beta[m,]
}
#ie for categorical mediators
for (j in 1:p3){
M.1.0=M.1[j4,]
M.0.0=M.0[j3,]
M.1.0[,,(catm1[j,1]-j+1):(catm1[j,2]-j)]=
M1[j1,(catm1[j,1]-j+1):(catm1[j,2]-j)]
M.0.0[,,(catm1[j,1]-j+1):(catm1[j,2]-j)]=
M1[j1,(catm1[j,1]-j+1):(catm1[j,2]-j)]
ie[,catm[j]]<-te-c[m]-(M.1.0-M.0.0)%*%beta[m,]
}
aie4=rbind(aie4,apply(ie,2,mean))
}
de4<-c
summary.med<-function(vec,qua=c(0.025, 0.25, 0.5, 0.75,0.975), digit=4)
{round(c(mean=mean(vec),sd=sd(vec),quantile(vec,qua)),digit)}
summary.med.re<-function(vec,vec1,
qua=c(0.025, 0.25, 0.5, 0.75,0.975),digit=4)
{vec=vec/vec1
round(c(mean=mean(vec),sd=sd(vec),quantile(vec,qua)),digit)}
result1<-apply(cbind(te1,de1,aie1),2,summary.med)
result4<-apply(cbind(ate4,de4,aie4),2,summary.med)
colnames(result1)=c("TE", "DE", "Isolation", "poverty", "under18",
"intden", "StrDen", "cnr", "comorb",

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"insurance", "marstat1","Satge","BMI")
colnames(result4)=c("TE", "DE", "Isolation", "poverty", "under18",
"intden", "StrDen", "cnr", "comorb",
"insurance", "marstat1","Satge","BMI")
result1
result4

```

2 JAGS MODEL FOR BMA TO EXPLORE RACIAL DISPARITY IN BREAST CANCER DIAGNOSTIC AGE

```

model {
for(i in 1:N){
mu_y[i]<- beta0 + c*x[i] + inprod(beta,M1[i,])
y[i] ~ dnorm(mu_y[i],prec4)
for (j in 1:p1){
mu_M1[i,j] <- alpha0.a[j]+alpha1.a[j]*x[i]
M2[i,contm[j]] ~ dnorm(mu_M1[i,j],prec1[j])
for (k in contm1[j,1]:contm1[j,2]){
mu_M1_c[i,k] <- alpha0[k]+alpha1[k]*x[i]
M1[i,k] ~ dnorm(mu_M1_c[i,k],prec2[k])
}
}

for (j in 1:p3){
mu_Mc[i,j,1] <- 1 #baseline is the 1st category
for (k in 2:cat2[j]){
mu_Mc[i,j,k] <- exp(alpha0.c[j,k-1]+alpha1.c[j,k-1]*x[i])
}
sum_Mc[i,j] <-sum(mu_Mc[i,j,1:cat2[j]])
for (l in 1:cat2[j])
{mu_Mc0[i,j,l] <- mu_Mc[i,j,l]/sum_Mc[i,j]}
M2[i,catm[j]]~dcat(mu_Mc0[i,j,1:cat2[j]])
}

}
}

```

```

#priors
beta[1:P] ~ dmnorm(mu[1:P], Omega[1:P, 1:P])
alpha0[1:P] ~ dmnorm(mu0.1[1:P], Omega0.1[1:P, 1:P])
alpha1[1:P] ~ dmnorm(mu1.1[1:P], Omega1.1[1:P, 1:P])
for (i in 1:p1){
  var2[i] ~ dgamma(1,0.1)
  prec2[i] <-1/var2[i]
}
#3. alpha0.a, alpha1.a, prec1
alpha0.a[1:p1] ~ dmnorm(mu0.a[1:p1], Omega0.a[1:p1, 1:p1])
alpha1.a[1:p1] ~ dmnorm(mu1.a[1:p1], Omega1.a[1:p1, 1:p1])
for (i in 1:p1){
  var1[i] ~ dgamma(1,0.1)
  prec1[i] <-1/var1[i]
}
#5. alpha0.c, alpha1.c
#cat1=max(cat2)-1
for (i in 1:p3){
  alpha0.c[i,1:cat1] ~ dmnorm(mu0.c[1:cat1], Omega0.c[1:cat1, 1:cat1])
  alpha1.c[i,1:cat1] ~ dmnorm(mu1.c[1:cat1], Omega1.c[1:cat1, 1:cat1])
}
beta0 ~ dnorm(0, 1.0E-6)
c ~ dnorm(0, 1.0E-6)
var4 ~ dgamma(1,0.1)
prec4 <-1/var4
}

```

3 Figures

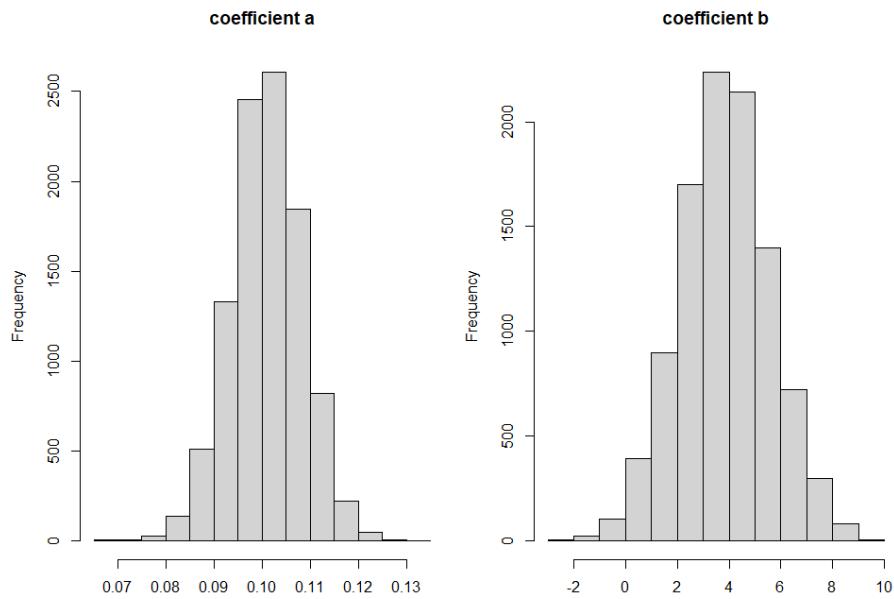


Figure 1: Posterior distribution for coefficients relating to language isolation. The posterior distribution of the coefficient a for race to predict language isolation (left panel), and the posterior distribution of the coefficient b for language isolation to predict the diagnostic age of breast cancer (right panel).

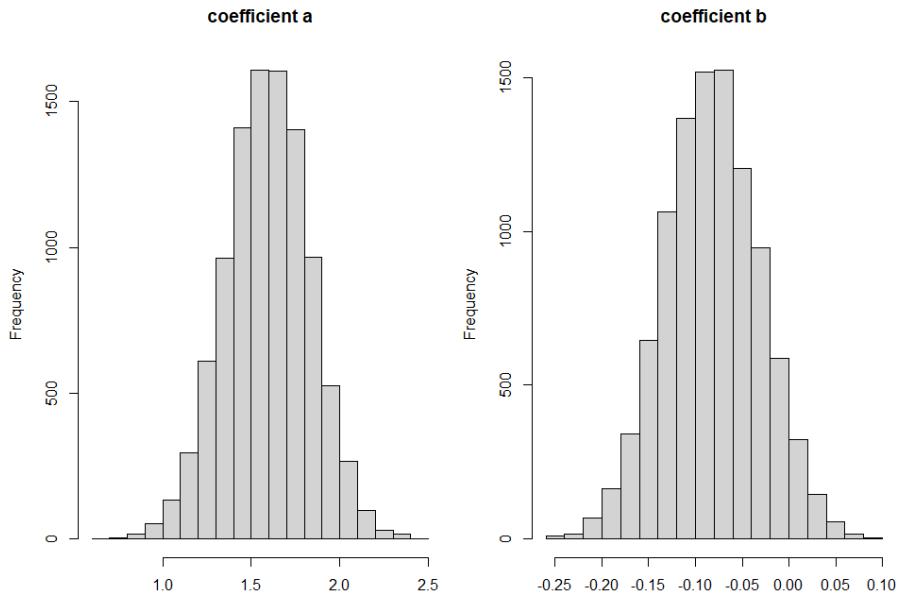


Figure 2: Posterior distribution for coefficients relating to percentage of persons under age 18. The posterior distribution of the coefficient a for race to predict percentage of persons under age 18 (left panel), and the posterior distribution of the coefficient b for percentage of persons under age 18 to predict the diagnostic age of breast cancer (right panel).

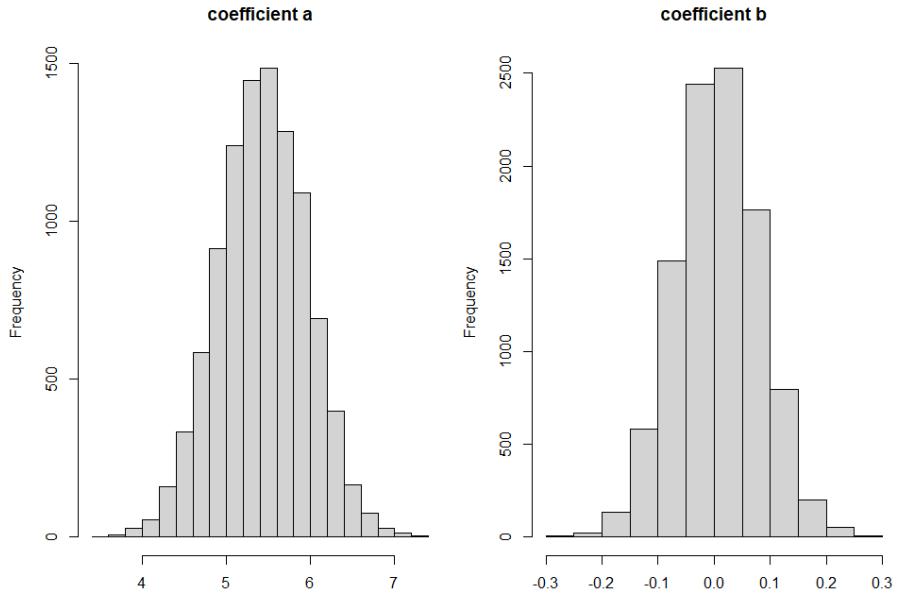


Figure 3: Posterior distribution for coefficients relating to street density. The posterior distribution of the coefficient a for race to predict street density (left panel), and the posterior distribution of the coefficient b for street density to predict the diagnostic age of breast cancer (right panel).

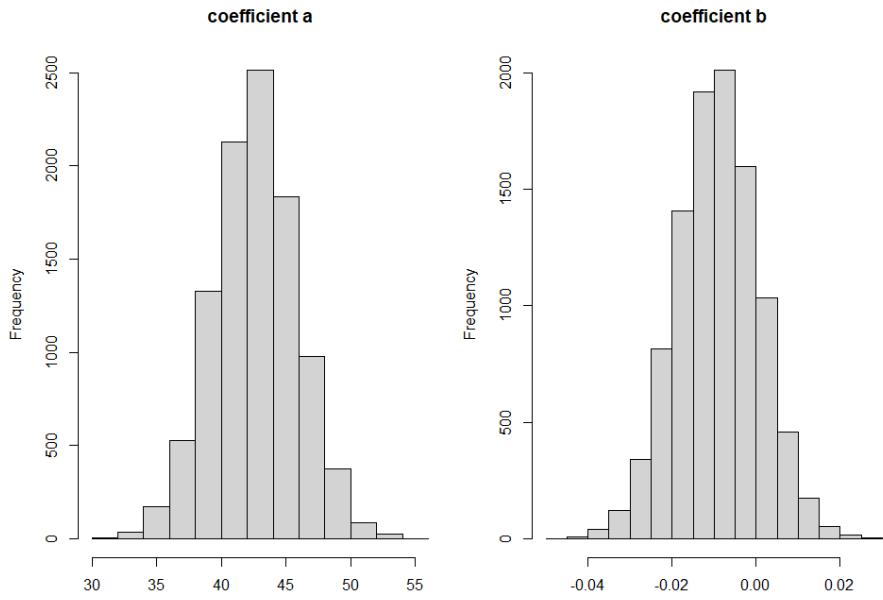


Figure 4: Posterior distribution for coefficients relating to intersection density. The posterior distribution of the coefficient a for race to predict intersection density (left panel), and the posterior distribution of the coefficient b for intersection density to predict the diagnostic age of breast cancer (right panel).

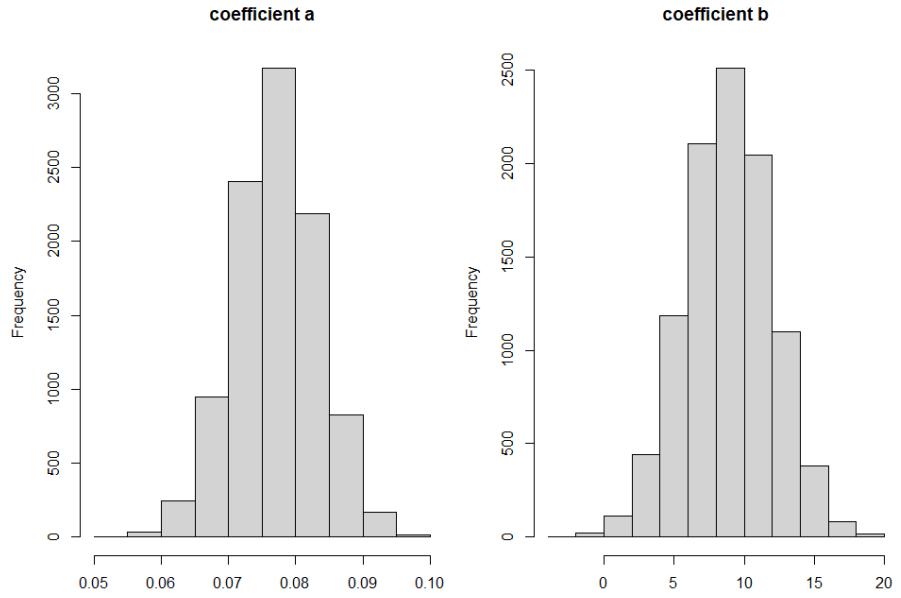


Figure 5: Posterior distribution for coefficients relating to street connected node ratio. The posterior distribution of the coefficient a for race to predict street connected node ratio (left panel), and the posterior distribution of the coefficient b for street connected node ratio to predict the diagnostic age of breast cancer (right panel).

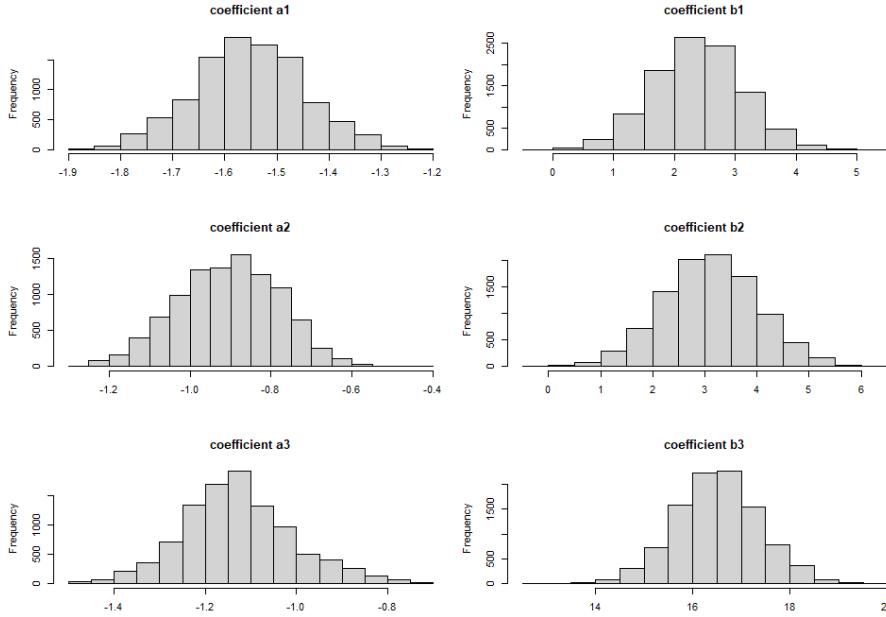


Figure 6: Posterior distribution for coefficients relating to the categorical variable-marital status. The posterior distribution of the coefficient a_1 , a_2 , a_3 for race to predict a log function of patients' marital status (left panel), the posterior distribution of the coefficient b_1 for patients' marital status (married vs single) to predict the diagnostic age of breast cancer (upper right panel), the posterior distribution of the coefficient b_2 for patients' marital status (separated/divorce vs single) to predict the diagnostic age of breast cancer (middle right panel), and the posterior distribution of the coefficient b_3 for patients' marital status (widowed vs single) to predict the diagnostic age of breast cancer (lower right panel).

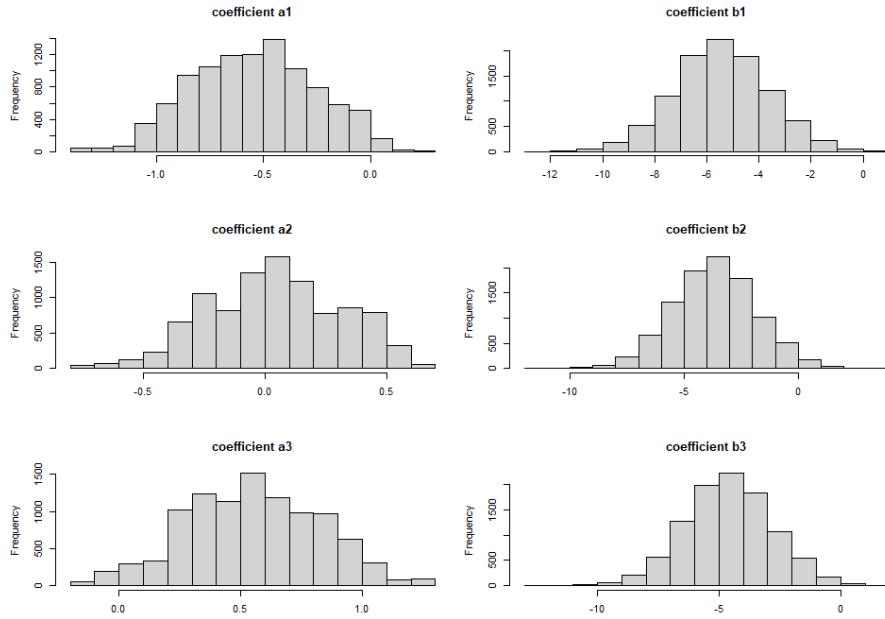


Figure 7: Posterior distribution for coefficients relating to the categorical variable-BMI. The posterior distribution of the coefficient a_1 , a_2 , a_3 for race to predict a log function of patients' BMI (left panel), the posterior distribution of the coefficient b_1 for patients' BMI (healthy weight vs underweight) to predict the diagnostic age of breast cancer (upper right panel), the posterior distribution of the coefficient b_2 for patients' BMI (overweight vs underweight) to predict the diagnostic age of breast cancer (middle right panel), and the posterior distribution of the coefficient b_3 for patients' BMI (obesity vs underweight) to predict the diagnostic age of breast cancer (lower right panel).

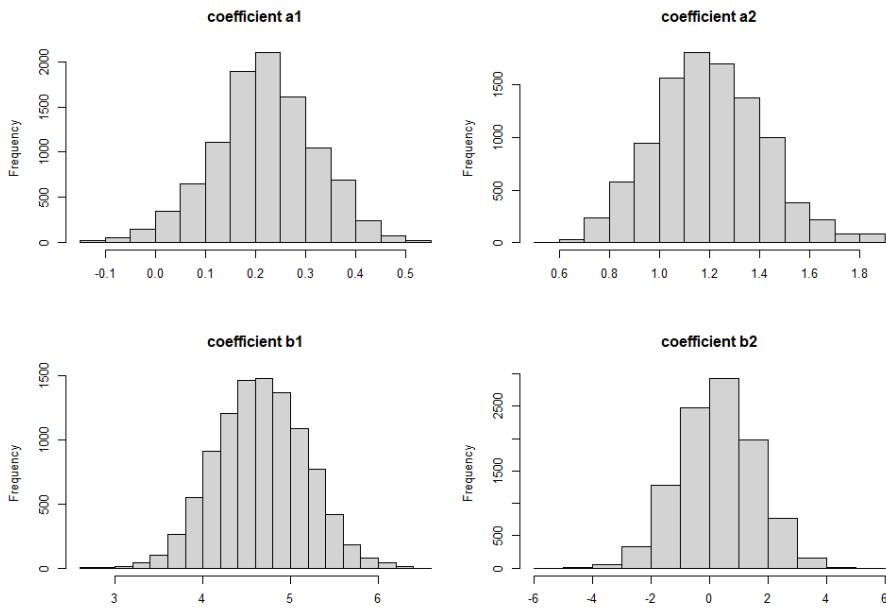


Figure 8: Posterior distribution for coefficients relating to the categorical variable-comorbidity. The posterior distribution of the coefficient a_1 , a_2 , a_3 for race to predict a log function of patients' comorbidity (left panel), the posterior distribution of the coefficient b_1 for patients' comorbidity (moderate vs no/mild) to predict the diagnostic age of breast cancer (upper right panel), and the posterior distribution of the coefficient b_2 for patients' comorbidity (severe vs no/mild) to predict the diagnostic age of breast cancer (lower right panel)

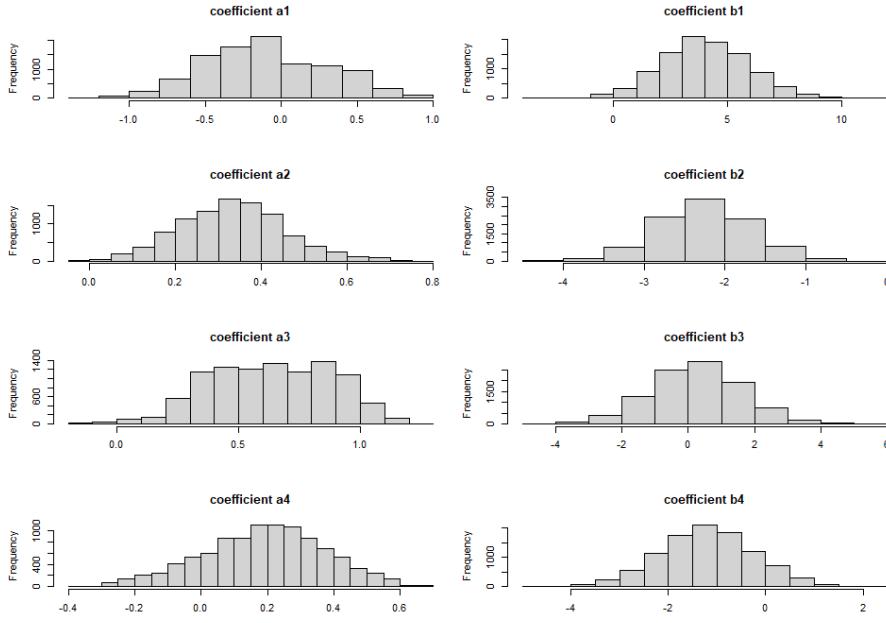


Figure 9: Posterior distribution for coefficients relating to the categorical variable-cancer stage. The posterior distribution of the coefficient a_1 , a_2 , a_3 , a_4 for race to predict a log function of patients' cancer stage (left panel), the posterior distribution of the coefficient b_1 for patients' cancer stage (regional by direct extension only vs localized) to predict the diagnostic age of breast cancer (upper right panel), the posterior distribution of the coefficient b_2 for patients' cancer stage (ipsilateral regional lymph nodes only vs localized) to predict the diagnostic age of breast cancer (middle right panel), the posterior distribution of the coefficient b_3 for patients' cancer stage (regional by 2 and 3 vs localized) to predict the diagnostic age of breast cancer (middle right panel), and the posterior distribution of the coefficient b_4 for patients' cancer stage (distant sites vs localized) to predict the diagnostic age of breast cancer (lower right panel).