



Article Ionization Detail Parameters for DNA Damage Evaluation in Charged Particle Radiotherapy: Simulation Study Based on Cell Survival Database

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Abstract: Details of excitation and ionization acts hide a description of the biological effects of charged particle traversal through living tissue. Nanodosimetry enables the introduction of novel quantities that characterize and quantify the particle track structure while also serving as a foundation for assessing biological effects based on this quantification. This presents an opportunity to enhance the planning of charged particle radiotherapy by taking into account the ionization detail. This work uses Monte Carlo simulations with Geant4-DNA code for a wide variety of charged particles and their radiation qualities to analyze the distribution of ionization cluster sizes within nanometer-scale volumes, similar to DNA diameter. By correlating these results with biological parameters extracted from the PIDE database for the V79 cell line, a novel parameter R_2 based on ionization details is proposed for the evaluation of radiation quality in terms of biological consequences, i.e., radiobiological cross section for inactivation. By incorporating the probability *p* of sub-lethal damage caused by a single ionization, we address limitations associated with the usually proposed nanodosimetric parameter F_k for characterizing the biological effects of radiation. We show that the new parameter R_2 correlates well with radiobiological data and can be used to predict biological outcomes.

Keywords: nanodosimetry; track structure; Monte Carlo simulations; Geant4-DNA; radiation response; DSB; radiobiological cross sections

1. Introduction

Track structure analysis is gaining attention because it could examine the nature of radiation damage from a nanoscale perspective. However, a key challenge remains: bridging the gap between observed biological response and the underlying physical interactions at the nanometric scale. This motivates researchers in experimental nanodosimetry to develop new quantifiable measures that properly describe both aspects. Previous studies provide compelling evidence that differences in the effects of sparsely and densely ionizing radiation at the cellular and molecular levels can be explained by the complexity of local DNA lesions. Indeed, nearly three decades ago, it was postulated that the precise spatial arrangement of ionizing events along a particle's trajectory through DNA significantly influences the complexity and repairability of double-strand breaks (DSBs) in irradiated cells [1].



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Brenner and Ward [2] showed that the frequency of clusters of ionizations within a 2–3 nm target correlates well with the yield of DSB. A similar finding was soon reported by Michalik [3]. Also, the maximum relative biological effectiveness (RBE) for most biological endpoints occurs for 100 keV/µm of linear energy transfer (LET), which coincides with a \sim 2 nm mean free path length for ionizations [1]. There is growing evidence that these observations are not just a coincidence but reflect the importance of clustered ionizations occurring at the scale of DNA diameter [4]. Therefore, the ionization cluster size distribution (ICSD) evaluation in nanometric volumes and nanodosimetric quantities derived from this basic concept are promising candidates for describing radiation quality [5,6].

The use of nanodosimetric quantities is of great importance for understanding the response of cells exposed to radiation that differs in the ionization density. With the ongoing development of nanodosimetric techniques supported with Monte Carlo (MC) simulations, it presents a valuable opportunity to improve the future planning of charged particle radiotherapy by considering ionization details. The evolving understanding of proton and ion radiobiology requires a more nuanced approach compared to current clinical methods relying on LET and RBE for charged particle radiotherapy; therefore, a formalism based on ionization detail parameters and cluster dose instead of current LET- and RBE-based models has been proposed for use in particle radiotherapy treatment planning [7]. For several years, researchers have been focusing on the nanodosimetric quantity expressing the probability of formation of the ionization clusters and its parameters for DNA damage evaluation. Descending to the nanometric scale allows us to count ionization acts in volumes comparable to short segments of DNA and link the number with DNA damage. For example, DSBs appear when two ionizations break two strands of a DNA molecule in close proximity. Based on the ionization pattern, the probability of occurrence of a given number of ionizations (i.e., a given cluster size)—aforementioned ICSD—can be calculated. ICSD is also used to estimate the cumulative probability F_k of the formation of clusters of a given size (k) or larger. Representation of the ionization cluster size equal to or greater than two (described by cumulative probability F_2) as the yield of DSB of the DNA, at least, for electrons [8] is valid because of a similar dependence on energy.

In many studies, the potential use of F_k was evaluated [6,7,9,10]. F_2 was chosen as the first quantity to assess because of the requirement for at least two ionizations leading to DSB. However, it became obvious that not every two ionizations lead to a double-strand break and hence the subsequent hypotheses about the validity of using F_3 , F_4 , or F_5 . The index value selection in F_k is not straightforward, but the question remains: is this choice even necessary? With F_k , regardless of the chosen k value, we consistently overlook events smaller than k and treat all other events as equally probable in causing a biological effect. Additionally, discrete values of k cause a discontinuous transition between F_k and F_{k+1} , making it impossible to precisely fit biological outcomes. This effect has been noticed in studies where linear combinations of F_2 and F_3 were demonstrated, marking the first indication that perhaps clusters of sizes 2 and 3 should not be considered with the same probability [11]. The introduction of R_2 , a new nanodosimetric quantity proposed in this work, addresses all these issues due to the continuous range of parameter values p along a biologically interpretable line and the intuitiveness of selecting a value in the index to be two because of the requirement for at least two ionizations leading to DSB.

Our studies aim to introduce a new descriptor for DNA damage after charged particle irradiation calculated based on ICSD parameters simulated with Geant4-DNA [12–15] and using experimental cell survival data. Being aware that a simple sum of probabilities associated with clusters of very different sizes may overestimate the assessment of the late biological outcome, based on previous findings and as a step toward novel dosimetry, we propose the use of the R_2 quantity as a new approach in determining the biological effects of the exposure. In our approach, we decided not to assume that in each case, two

ionizations are a sufficient condition to cause a DSB when considering a biological target. That is why we propose quantity R_2 based on binomial distribution and defined as:

$$R_2(p) = \sum_{\nu=2}^{\infty} \sum_{k=2}^{\nu} P_{\nu} B_k(\nu, p),$$
(1)

where P_{ν} is a probability distribution of cluster size ν , $B_k(\nu, p)$ is the probability of k ionizations that have provided a sub-lethal lesion in a sequence of ν ionizations, and p is the probability of creating a sub-lethal lesion by a single ionization in this sequence. Here, a sub-lethal lesion is an elementary lesion that on its own is not harsh enough to drive apoptosis, but two or more of them within close range are enough to cause a DSB or severe lesion. The exact reasoning can be found in Section 4.1.2.

2. Results

2.1. Nanodosimetric Alternative Metric

We use nanoscale quantities that describe local energy deposits to calculate R_2/M_1 rather than using dose values to calculate RBE, which we know are not the best descriptors of cellular response. Figure 1 shows R_2/M_1 as a function of LET (Figure 1A) and mean cluster size M_1 (Figure 1B). This reveals a characteristic curve resembling relative biological effectiveness as a function of linear energy transfer.

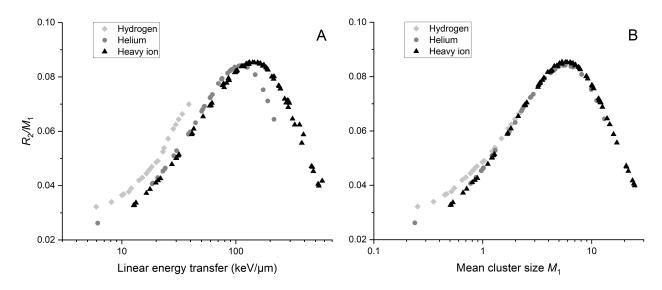


Figure 1. Ratio R_2 to mean cluster size M_1 as a function of linear energy transfer (**A**) and mean cluster size (**B**). M_1 values were simulated for a 2.3 × 3.4 nm² target size. Data points are indicated by shades of gray and shapes representing ion type. "Hydrogen" includes protons and deuterons, while "Helium" includes ³He²⁺ and ⁴He²⁺ ions, along with alpha particles. Other used ions (⁷Li, ¹¹B, ¹²C, ¹⁴N, ¹⁶O, ²⁰Ne) are classified as heavy ions.

When plotting R_2/M_1 against LET, there is a significant shift of the maximum ratio toward lower LET when considering lighter ions. This effect is not noticeable when plotted against mean cluster size M_1 . The maximum R_2/M_1 occurs at the LET and M_1 values for which we expect the maximum biological effectiveness (around 100 keV/µm of LET).

Consequently, we decided to calculate RBE for a 5% survival level using the α and β parameters of the linear-quadratic (LQ) model from the Particle Irradiation Data Ensemble (PIDE), which is presented in Figure 2. PIDE is a GSI biophysics project that compiles over 1200 pairs of in vitro cell survival experiment results after photon and ion irradiation from 131 publications. Data are stored in easily accessible file formats and include raw data, experiment specifications, linear-quadratic parameters and references. PIDE is continuously developed and it is freely available after registration. A disturbing observation in

Figure 2 may be the dispersion of points in the graph. The reason for this difference may be that the experiments whose results were used to calculate RBE may have included studies that examined cells with different proportions in each phase. This is important because cell survival depends on the phase of the cell cycle. Another detail worth mentioning, but in this case much more specifically, is the presence of two outlier points for protons for low LET, exhibiting an RBE almost twice as high as the general trend. In the original paper, the reported α/β ratios for these points were about five times higher than five, usually reported for V79 cells. Given that this ratio is cell line specific, we could exclude these points. As this example shows, analyzing the dispersion would demand significant effort since many issues should be considered. PIDE does not provide uncertainties of presented values and certain other details regarding survival experiments that may lead to the exclusion of data from the analysis due to differences in experimental conditions. That is why we suggest considering this figure as a general trend indicating the advantages of using mean cluster size M_1 , for which the RBE(M_1) peak occurs for the same value of M_1 regardless of the ion type (except for protons) used to irradiate cells. Maximum RBE values for helium and heavy ions are obtained for different values of LET, 123.58 keV/µm and 161.32 keV/µm, respectively, but for the same value of M_1 , approximately 6.6.

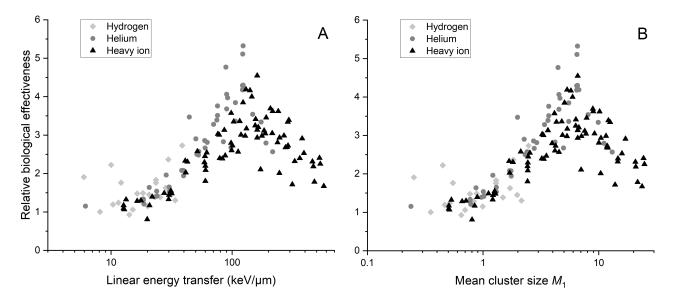


Figure 2. The RBE for a survival level of 5%, calculated as the ratio of dose from reference photon radiation to dose from ions, as a function of LET (**A**) and mean cluster size M_1 (**B**). The reference dose is computed using fitted survival parameters from the PIDE database for reference radiation, while the ion dose is determined using corrected survival parameters from PIDE for ion radiation. The simulation are performed for a 2.3×3.4 nm² target size. Data points are differentiated by shades of gray and shapes representing ion type. The category "Hydrogen" includes protons and deuterons, while "Helium" includes ³He²⁺ and ⁴He²⁺ ions, along with alpha particles. Results for 8 experiments were not included due to insufficient information regarding reference radiation.

As can be seen in Figure 2A, the biological effectiveness may be higher for lighter than for heavier ions, even though they are described with the same LET value. As the ion's mass number decreases, there is a pronounced shift of the RBE spectra towards the low-LET region. This relationship is not noticeable at the RBE graph plotted against mean cluster size M_1 (Figure 2B). When considering two different particles with the same LET, their biological effectiveness differs. However, two particles with the same M_1 exhibit the same biological effectiveness. In this context, M_1 appears to be a more suitable metric than LET for characterizing the quality of ionizing radiation. So, the trend presented in Figure 1 is also noticeable in this case.

2.2. Cell Inactivation Cross Sections

In response to the recognized limitations of linear energy transfer in fully characterizing radiation quality and its biological effects, we wanted to further explore the potential of R_2 as an alternative metric. However, this approach requires the calculation of another biological quantity. For this reason, we determined inactivation cross sections $\sigma_{5\%}$ for a 5% survival level and illustrated their relationship with both LET and mean cluster size M_1 in Figure 3A and Figure 3B, respectively. A 5% survival level was chosen because Belloni et al. [16] demonstrated that in this case, fitting parameters of the sigma dependence on LET indicate the same relationship regardless of the type of particle applied to irradiate the V79 cells. The mean cluster size was simulated based on the energy associated with LET for a cylindrical target with dimensions of 2.3×3.4 nm² (diameter × height). Figure 3 visually demonstrates the obtained sigmoidal relationship. $\sigma_{5\%}$ increases until it shows a saturation effect for larger LET or M_1 values as a result of overkilling. We used various data point shapes to address data variance, especially regarding the ion used to irradiate the cells and study their survival. Despite noticeable fluctuations, we decided to use all data presented in Figure 3 for further analysis, acknowledging the particular biological variation. Additionally, we included all variants of the V79 cell line from the PIDE database. Notably, no significant differences were observed among the considered cell sub-types.

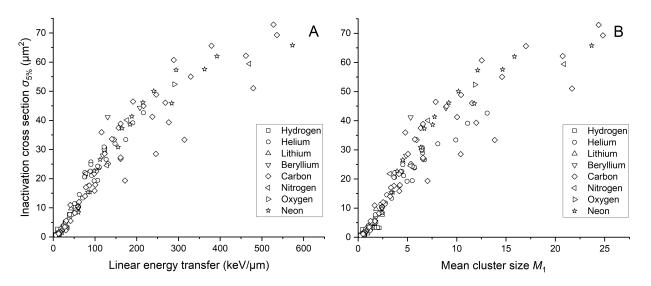


Figure 3. Inactivation cross section of the V79 cell line as a function of linear energy transfer (**A**) and simulated mean cluster size M_1 (**B**). LET was calculated using SRIM-2013 software based on energy from PIDE. Simulations are performed for a cylindrical target size of $2.3 \times 3.4 \text{ nm}^2$. The shape of each data point indicates the ion used for irradiating the cells. "Hydrogen" includes protons and deuterons, while "Helium" includes ³He²⁺ and ⁴He²⁺ ions, along with alpha particles. All other particles are considered heavy ions.

The mean cluster size M_1 use allows maintaining the sigmoidal shape of the dependency. The graph does not indicate deviations from the expected trend for any ion. Minor shifts in Figure 3B result from the fact that we used LET values to calculate $\sigma_{5\%}$.

2.3. Ionization Details Parameters

Based on the results of the nanodosimetric simulations, we analyzed the variation of R_2 as a function of mean cluster size M_1 for each tested target size d and the entire range of p. Observing that the curve shape corresponds to the previously identified pattern (see Figure 3) and using a direct proportionality between F_2 and $\sigma_{5\%}$ with the proportionality constant K established in prior studies [6], we aimed to identify the optimal

parameters (*d*, *p* and *K*) that yield the best fit. This corresponds to minimizing the modified χ^2 value as explained in Section 4.

The heatmap, shown in Figure 4, illustrates the relationship between probability p of creating a sub-lethal lesion by a single ionization and target size d, depicting the best fitting between $\sigma_{5\%}$ and R_2 for K equal to 57 µm². The variations observed are minimal, with the area of optimal fit (indicated by yellow) transitioning from small p and high d values to high p and low d values. While the heatmap provides valuable insights, it is important to note that identifying the best pair of p and d requires additional knowledge, such as the size of the DNA molecule.

We deduce that the consistency of R_2 with biological data for many p and d pairs is a result of the scaling procedure used to reach material equivalence [17]. Therefore, identifying the most accurate combination of p and d should involve focusing on the size of DNA fragments relevant from the ionizing radiation interactions perspective. This selection would lead to a p value, the assessment of which is more challenging. For this reason, these studies will focus on a target of 2.3×3.4 nm² for which we obtained the best fit for p = 0.35.

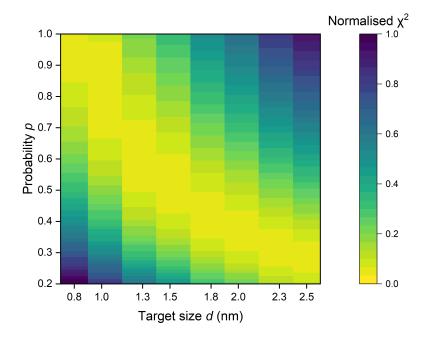


Figure 4. The heatmap, which displays the relationship between probability *p* and target size *d*, highlights the best fit between $\sigma_{5\%}$ and R_2 with *K* set to 57 µm². Yellow areas indicate the region of optimal fit *d* and *p* parameters. χ^2 is normalized to the highest χ^2 value obtained within the specified range of *p* and *d*.

Figure 5 shows R_2 and a few selected cumulative probabilities F_k as a function of mean cluster size for two different target sizes: $1 \times 1 \text{ nm}^2$ (Figure 5A) and $2.3 \times 3.4 \text{ nm}^2$ (Figure 5B). Cumulative probabilities F_k were selected within the range of three consecutive k values for which the behavior of F_k closely resembles that of R_2 as a function of mean cluster size M_1 . For a target size of $1 \times 1 \text{ nm}^2$, this includes F_2 , F_3 , and F_4 , while for $2.3 \times 3.4 \text{ nm}^2$, F_4 , F_5 , and F_6 are chosen.

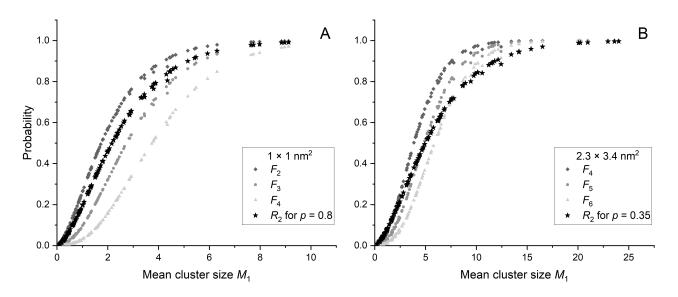


Figure 5. Probabilities R_2 and chosen F_k as a function of M_1 for a target size of $1 \times 1 \text{ nm}^2$ (**A**) and $2.3 \times 3.4 \text{ nm}^2$ (**B**). Black stars represent the R_2 for p value corresponding to the best agreement with $\sigma_{5\%}$.

The *p* parameter influences the R_2 curve slope as seen in Figure 5. The curve with *p* values closer to 1 (p = 0.8 in Figure 5A) may pass between the curves F_k and F_{k+1} . A significant decrease in *p* (p = 0.35 in Figure 5B) allows the R_2 curve to intersect the curves F_k and F_{k+1} . When using F_k , the discrete choice of curves makes fitting to biological data much more difficult.

2.4. Link between Radiobiology and Nanodosimetry

Given the significant variability observed in the results across various target sizes d and probabilities p, which align well with biological data, we have chosen to focus on the findings regarding the 2.3 × 3.4 nm² target size. This size represents short DNA segments, approximately one helical turn in length. We present R_2 values adjusted with the optimal K factor and compare them with $\sigma_{5\%}$ in Figure 6.

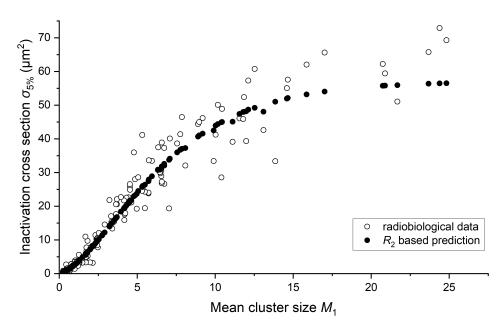


Figure 6. Inactivation cross section as a function of mean cluster size M_1 , representing considered biological data, alongside the R_2 based model results represented by R_2 obtained for p equal to 0.35 and multiplied by the optimal K factor for a target size of 2.3 × 3.4 nm².

This demonstrates the relationship between the proposed nanodosimetric parameter R_2 and the biological metric across different mean cluster size M_1 values, revealing a strong alignment that suggests a significant correspondence. More details of this fit, particularly the justification for adopting simple proportionality between $\sigma_{5\%}$ and R_2 as well as a comparison with F_k , are presented in Appendix A. Figure A1 shows $\sigma_{5\%}$ plotted against R_2 for a specified target size (Figure A1A), along with the residuals of $\sigma_{5\%}$ plotted against R_2 (Figure A1B). Considering the possibility that F_k might offer a better fit to radiobiological data compared to R_2 , we present F_k , which yielded the best fit with radiobiological data, alongside R_2 for the p value that resulted in the best fit, shown as functions of M_1 in Figure A2.

Additionally, to illustrate that R_2 correlates better with radiobiological data than with the discrete models provided by F_k , linear fit and regular residuals for F_5 and F_2 are calculated and presented in Appendix A as Figures A3 and A4. F_5 was chosen as a F_k providing best fit, while F_2 is a quantity including also events with two ionisations—the minimal number that can lead to DSB induction. The coefficient of determination calculated for all three models shows that the R_2 -based model correlates the best (0.971), while for F_5 and F_2 , it is equal to 0.955 and 0.839, respectively.

3. Discussion

The possibility of applying ionization detail parameters to describe the cellular response to ionizing radiation is supported by experimental cell survival data from the particle irradiation database [18]. The mean cluster size parameter, similar to LET, can be used to characterize particle track structure and its impact on the biological effect regardless of the ion type used for irradiation. The inactivation cross sections calculated using radiobiological data correlate well with the R_2 parameter based on the nanometric track structure. Both measured and simulated cross section are presented as a function of the mean cluster size instead of LET, which is the standard parameter for the interaction description at the macroscopic level. R_2 and M_1 are used, as they may be more suited to describe the stochastic nature of radiation and its effects, especially at the subcellular (nm) level and thus allow understanding of the cellular response to ionizing radiation in the context of DNA damage. The number of ionization acts in the volume of individual DNA nucleotides is the main factor determining the RBE of ionizing radiation.

Calculations based on the spatial distribution of the ionization acts can recreate the relation between RBE and LET (or M_1). Namely, for both RBE and R_2/M_1 plotted as functions of LET (or M_1), one can see the same shape of the curve, with the characteristic peak at about 100 keV/µm (or corresponding M_1 value). Ionization detail parameterization is closer to the phenomena description at the nanoscale than the average LET parameter. Both nanodosimetric measurements and Monte Carlo simulations allow estimating ionization detail parameters.

Based on ICSD parameters, we introduce R_2 as a novel metric describing the probability associated with DNA damage derived from the binomial distribution of the P_{ν} . The subscript value of R_2 was selected based on the necessary condition for DSB (probability distributions of the induction of ionization clusters with a size equal to or greater than a fixed number). Unlike the discrete parameter k in F_k , R_2 uses the continuous parameter p, which may have a potential association with the chromatin arrangement within the nucleus of a given cell line. R_2 depends on the target size; however, due to biological variability, we could not determine significant differences among different target sizes. The chosen target size serves as a representative measure of biologically significant volume, equivalent to the short DNA segment, approximately one helical turn in length, or about 10 base pairs.

In previous studies [6,9], the best fit was achieved with *K* equal to 65 μ m², in contrary to presented here the value of 57 μ m², but it is important to note that the mentioned studies incorporated only selected biological data. Outliers below the $\sigma_{5\%}$ (LET) curve were not considered, particularly those that underestimate *K*. In our study, inactivation cross sections were also derived from published in vitro survival parameters for the V79 cell line but we

focus on a greater variety of ion types and radiation qualities. Additionally, we included all variants of the V79 cell line from the PIDE database. Notably, no significant differences were observed among the considered sub-types. In the cited publications, the quantity F_2 was used, and the best fit was obtained for 1×1 nm². In subsequent studies [11] that employed a linear combination of F_2 and F_3 for a spherical volume with a diameter of 1 nm, this K value was found to be equal to 50 μ m² for the V79 cell line. Still, only selected data points were used, but the comparison is challenging due to the different shapes of the considered target. For this reason, we will temporarily focus on analyzing the results that correlated with F_2 , which is a representation of R_2 with p = 1. We deduce that the consistency of F_2 for a 1 \times 1 nm² target size with biological data is a simple result of the scaling procedure shown by [17]. A broad spectrum of probability p and target size d pairs yields acceptably good fits between nanodosimetric cumulative probability and biological data. This range begins with p approximately equal to $1 (F_2)$ and a target size of 1×1 nm², extending as p decreases and d increases. Therefore, finding the most accurate p and d combination requires at least a general knowledge of the size of DNA fragments important in the context of interactions with ionizing radiation and a sensible approach to assessing the resulting p value based on the chosen d. For that reason, these studies focus on R_2 for a target of 2.3 \times 3.4 nm². Basing on R_2 is not contrary to the approach proposing ionization details [7]. It presents the opportunity to enhance this approach using the proposed universal descriptor R_2 .

Another interesting feature of R_2 is the fact that it can be directly measured, as the ion counting efficiency η of a nanodosimeter can be tuned to the same value as the probability p in $R_2(p)$. In measurement practice, calculating F_2 from the ion cluster size spectrum obtained with a device characterized by ion counting efficiency $\eta = p$ is equivalent to calculating $R_2(p)$ on the true spectrum of ionization clusters. This equivalence can be also interpreted by treating a DNA segment as a nanodosimeter with efficiency p being its ion detection efficiency. After all, a nanodosimeter is a physical model of the short DNA segment and its interaction with ionizing particles. In both systems (DNA and nanodosimeter), there is a certain number of ionizations and a detector that detects them either by being damaged (in the case of DNA) or by producing electric signals (in the case of nanodosimeter). If their detection efficiency is the same, the probability distribution of the number of DNA lesions in a DNA segment is the same as the measured ICSD. The possibility of the direct measurement of a biologically relevant nanodosimetric parameter is the key idea that drives the development of a small device that could be easily and routinely used in the clinical environment. The recent advancements in the thick-GEM technology [19,20] suggest that such a device can be proposed in a few years.

The concept of R_2 as a radiation quality factor that should replace F_k is similar to the earlier attempts to predict DNA strand break yield [21]. Authors of the mentioned work also consider simple binomial distribution to calculate probability per projectile of generating a specific complex lesion, e.g., DSB. However, their model accounts also for the fact that to produce a DSB, at least one break on each strand should be considered. This nuance is neglected in R_2 presented in this work. As a result, R_2 can be directly measured using a standard nanodosimeter setup with a single target. Modeling the actual twostrand DNA in a nanodosimeter would require two neighboring targets in a close vicinity. Such experimental setups are not unthinkable and were in fact proposed recently [22–24]. However, the level of complication of these experiments prevents the use of such methods in a clinical environment, especially given that miniaturized nanodosimeters still struggle to provide even a single target model [19,20]. In conclusion, since we cannot define any radiation quality factor in isolation from the properties of the biological system, we should take at least this minimal step and account for the finite probability p of converting an ionization into a lesion. Making this minimal necessary step leads to the concept of R_2 that happens to be a measurable quantity well correlated to biological parameters like a radiobiological cross section for cell inactivation.

The beauty of the nanoscale approach to radiation therapy treatment planning is that the ionization detail parameter characterizes the radiation field regardless of the radiation type that created the cluster. In other words, the ID, frequency distribution of the ionization cluster size, or R_2 parameter are independent of the composition of primary particles in the radiation field. This paves the way for much easier and more precise radiation therapy treatment planning with various radiation quantities, for instance, multiple ions. The nanoscale approach based on ionization detail parameters is furthermore an opportunity for boron neutron capture radiation therapy [25], where low-energy lithium ions and alpha particles are the source of complex DNA lesion clusters that are lethal to cells. Further therapy enhancement methods, benefiting from boron [26–30] or gadolinium [31] radiation sensitizers exposed to a neutron radiation field produced by a proton beam in a patient, would greatly benefit from a unified nanoscale physics quantity that considers the radiation effectiveness of different particles in a stochastic way.

4. Materials and Methods

4.1. Nanodosimetric Data

4.1.1. Jet Counter Nanodosimeter

Jet Counter (JC) is a fully functioning low-pressure gas-based detection system designed and developed in the National Centre for Nuclear Research, Poland. It allows creating an equivalent nanometric volume by injecting the target gas (such as N₂ or C₃H₃) into one side of an open cylindrical space at a few millibars of pressure and registering ions being produced as a result of an incoming projectile. This cylindrical volume simulates short DNA segments of approximately one helical turn in length, equivalent to about 10 base pairs and 3.4 nanometers in length, adjustable by modifying gas pressure. Incoming ionizing particles directed through this gaseous nanometric target produce ions, which are then extracted, guided by electrodes, and quantified within a vacuum using an electron multiplier. The number of individual ionizations in a nanodosimetric target volume per energy deposition event is called the ionization cluster size ν . Using coincidence techniques such as counting ionizations alongside pulsed gases targeted simultaneously or by accumulating ionization counts over multiple coincidences, the system gathers the necessary data to prepare the ionization cluster size distribution spectra. The procedure of the density scaling application [17,32] is conducted to compare a measured number of ionizations produced in a gaseous sensitive volume with cluster sizes simulated with track structure simulations performed in water.

The work details of the JC device are extensively described in [33,34] for alpha particles, single electrons [34,35], and carbon ions [24,36,37]. In the middle of 2023, preliminary measurements were conducted with JC on a proton beam at the Institute of Nuclear Physics, Polish Academy of Sciences in Krakow, using the AIC-144 cyclotron. Experimental results obtained with Jet Counter were used as a validation of Monte Carlo codes as detailed in Appendix B.

4.1.2. ICSD and Other Nanodosimetric Quantities

Nanodosimeters, such as JC, make it possible to measure the size distributions of ionization clusters that are formed as a result of a particle passing through a gaseous medium (ICSD) and to determine the average size of such a cluster. This quantity (often denoted M_1) is calculated as the first moment of ICSD using the following formula:

$$M_1 = \sum_{\nu=0}^{\infty} \nu P_{\nu}.$$
 (2)

As the M_1 is the average number of ionizations produced in a nanometric volume (such as DNA), it is conceptually similar to restricted LET, as it takes into account ionizations caused primarily by low-energy electrons. However, as it is restricted geometrically and not energetically, it actually takes into account contributions from all secondary electrons but

with different weights determined by the spatial distribution of ionization events produced by these electrons.

 F_k is one of the most strongly suggested nanodosimetric radiation quality parameters, as it is found to be proportional to radiobiological cross sections σ [6,9,10,38]. It is defined as the simple sum of probabilities of creating clusters of size k:

$$F_k = \sum_{\nu=k}^{\infty} P_{\nu}.$$
(3)

This approach neglects all ionization clusters smaller than k. For example, F_3 takes into account events with 3 or more ionizations and does not include contributions of events with two ionizations. Taking into account only events strictly larger than 2 (k > 2) is contradictory to the fact that two ionizations can be enough to cause a severe lesion like DSB. The purpose of this is to reflect the fact that larger clusters are more probable to cause a DSB. What it truly does is that it weights the probability P_{ν} of creating a cluster of size ν by a factor 0 for $\nu < k$ and factor 1 for $\nu \ge k$. However, a more natural approach is to assign a weight to each cluster size that reflects its probability of causing severe damage. In such case, clusters of size $\nu < 2$ should have a weight equal to 0 as they can, at best, create a single strand break (SSB). Clusters of size $\nu = 2$ should have the smallest but non-zero weight, and the larger the cluster is, the larger the weight should be, peaking at value 1 for large clusters, which most certainly will cause severe, irreparable damage. To quantify this idea, we propose considering the probability p that a single ionization creates a sub-lethal lesion, defined as a lesion that alone cannot lead to apoptosis but two or more of them in close vicinity are enough to do that. In such a case, the probability that a cluster of a given size will produce a lethal lesion is given by simple binomial distribution $B_k(v, p)$. In conclusion, both F_k and R_2 can be seen as a weighted sum of ICSD. The difference is that the weighting function of R_2 is not an arbitrarily chosen step function (as in the case of F_k) but a product of the stochastic nature of the considered phenomena. The difference is visualized in Figure 7 for weights of F_5 as an example, which is the best fit in Figure 5B among different F_k . For the same reason (best fit in Figure 5B), the value of p, for which R_2 weights are shown, was chosen to be equal to 0.35.

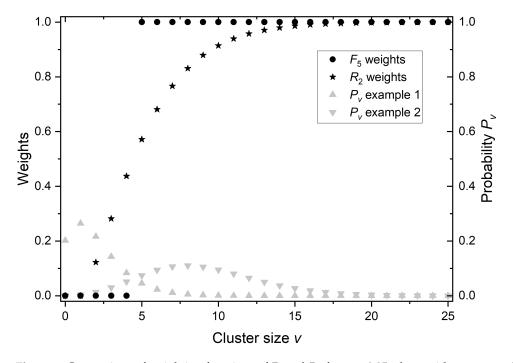


Figure 7. Comparison of weighting functions of F_5 and R_2 for p = 0.35, along with two examples of ICSD (P_{ν}).

In Figure 7, two examples of ICSD are presented to illustrate how R_2 and F_5 weights interact with different ICSDs. ICSD of example 1 is composed mainly of small ionization clusters (low-LET radiation), while example 2 is composed mainly of large ionization clusters (high-LET radiation). In the case of low LET (example 1), $R_2 = 0.16$ and $F_5 = 0.09$. Such a small value of F_5 results from the complete neglect of clusters 2, 3, and 4, thus leading to the possible underestimation of the probability of severe lesions that those clusters may sometimes cause. On the other hand, in the case of high LET (example 2), $R_2 = 0.8$ and $F_5 = 0.9$, so the relative difference is small, but this time, F_5 may overestimate the probability of severe lesions. By the nature of F_k , choosing smaller k to compensate for the underestimation in the low-LET case would increase the overestimation in the high-LET case. In practice, i.e., in proton therapy, any chosen F_k is going to underestimate the radiobiological effect in the healthy tissue and proximal part of a tumor (relatively low LET protons) and overestimate the effect in the distal part of the tumor and healthy tissue behind (relatively high LET protons).

4.1.3. Monte Carlo Simulations

The accuracy and robustness of the used Monte Carlo models were first estimated by the comparison with nanodosimetric experiments presented in Appendix B. These simulations are based on the Jet Counter Monte Carlo simulation presented earlier for *a* particles [39] and recently extended to carbon ions [24]. This simulation code was built using the Geant4 (ver. 4.11.0.0) general-purpose MC simulation toolkit [40,41] with Geant4-DNA extension [12–15]. The Geant4-DNA option 4 [13,42–44] was used to simulate particle tracks in the sensitive volume (SV) of the detector down to the ionization threshold of around 10 eV. It contains models for elastic scattering, excitations, and ionizations in liquid water for all simulated particles. The processes were modeled in the track-structure mode simulating interactions in a step-by-step manner as opposed to the condensed-history mode applied in G4EmLivermore physics list. To simulate interactions in SV walls, the less accurate but faster models from G4EmLivermore list were applied with a 100 eV cut-off for ionization by electrons.

For the retrospective simulation representing radiobiological experiments reported in the PIDE database, only the Geant4-DNA option 4 was used, as it presents a good agreement with the nanodosimetric experiments. In these simulations, SV was a cylindrical nanometric target representing the short segment of DNA, which was placed in the center of $10 \times 10 \times 10$ nm³ world filled with liquid water (G4_WATER material).

We completed simulations for target sizes of (1) diameters equal to height of 0.8, 1.0, 1.3, 1.5, 1.8, 2.0, 2.3 and 2.5 nm, (2) diameters of 1.0, 2.0, and 2.3 nm, and height/diameter ratio of 1.48. The source was a pencil beam of ¹H, ⁴He, ⁷Li, ¹¹B, ¹²C, ¹⁴N, ¹⁶O, ²⁸Si to provide various radiation qualities and consistency with radiobiological data. Since Geant4-DNA can only simulate ionization caused by incident ions predominant in the cosmic spectrum, direct results for ²⁰Ne were not available, leading to interpolation using ¹²C, ¹⁴N, ¹⁶O, and ²⁸S. The interpolation method was tested for ¹⁶O using ¹²C, ¹⁴N, and ²⁸S, yielding very good agreement with the result of the direct simulation for ¹⁶O. We used about 40 different energy points from 0.2 to 1000 MeV to evenly cover the whole energy range on a logarithmic scale. We obtained datasets with probabilities of creating a cluster size of different sizes for a given energy and LET calculated using SRIM software [45] for each tested particle type and target size. That allowed us to prepare ionization cluster size distributions (ICSDs) and calculate mean cluster size M_1 and cumulative probabilities F_k of the formation of clusters sized equal to or greater than *k* for a given energy. These data enabled interpolation using a second-order polynomial to obtain M_1 for a given energy and particle used in radiobiological studies. We also used these ICSDs to calculate R_2 for a given M_1 and wide range of p. To keep the results at a similar level of uncertainties as in the nanodosimetric experiments with the Jet Counter, we simulated 100,000 particle histories for each case (particle type, energy, and target size).

Our final datasets for each target size and particle include energy (as mentioned), LET, M_1 , R_2 for p from 0.2 to 1.0 (F_2) with a step of 0.01 and F_k for $k \in \langle 3, 4, 5, 6, 7 \rangle$. These datasets allowed us to interpolate all discussed quantities for energies and ions used in radiobiological experiments which we have chosen for further analysis.

4.2. Radiobiological Data

Radiobiological data were extracted from the particle irradiation data ensemble (PIDE) version 3.4 database [18,46]. Our focus lies on the linear (α) and quadratic (β) terms of the survival curves derived from graphs from many publications by the authors of PIDE. To obtain these parameters, they developed a computer program to digitize the data points in the figures. Subsequently, they determined α and β by fitting a second-order polynomial with an ordinary least squares fit to the negative logarithm of the survival.

We decided to focus our analysis on well-established asynchronous Chinese hamster lung fibroblast cells (V79), regardless of their sub-type, as we found no effect on the results obtained. Some points in the PIDE database are labeled as V79, while others are labeled as V79-4. We included all types since the category V79 includes both unspecified V79 cells and those with specific types (such as V79-379A, V79-754B, V79-S171, and even V79-4).

Survival parameters are driven from publications by many research groups around the world [47–76]. In these studies, we categorized experiments from PIDE using various criteria, such as ions used to irradiate cells. Under this classification, the "Hydrogen" category includes protons and deuterons, while "Helium" includes ${}^{3}\text{He}^{2+}$ and ${}^{4}\text{He}^{2+}$ ions, along with alpha particles from radiation sources. All remaining ions are classified as heavy ions. We narrowed studies to irradiation modalities labeled as monoenergetic and ions ranging from protons through neon (${}^{20}\text{Ne}$), covering the LET range up to 528 keV/µm, which includes 152 survival curves. We used the LQ coefficients fitted by the authors of the PIDE database. In certain instances, the β parameter was fitted by them with a negative value, likely due to statistical fluctuations or systematic deviations. In such cases, we adopted the formalism provided by the authors of the PIDE database, adjusting the α parameter downward to compensate for β , thus obtaining an estimator for the best purely linear fit with β equal to 0. We did not use numerical values for the LQ coefficients from original papers to maintain consistency in our methodology.

The RBE was calculated as the ratio of the reference photon radiation dose to the dose required from tested ion radiation to achieve the same effect, specifically 5% survival. Doses were calculated by solving the equation $\alpha D + \beta D^2 = -\ln(5\%)$ for *D*. The ion dose was determined using corrected survival parameters from PIDE for ion radiation, while the reference dose was computed using fitted survival parameters also from the PIDE database. The reference radiation included the following sources: ⁶⁰Co, ¹³⁷Cs, X-ray tube (100–300 kVp), or linear accelerator (6 MV).

Based on the α and β values from the PIDE database, we calculated the inactivation cross section σ_l for a survival level of 5% for a monoenergetic ion beam, using the following equation [16]:

$$\tau_{5\%} = \frac{k}{\rho} \text{LET} \sqrt{\alpha^2 - 4\beta \ln 5\%},\tag{4}$$

where $\sigma_{5\%}$ is given in μm^2 , *k* is 0.1602 when LET is expressed in the unit of keV/ μm , α in Gy⁻¹ and β in Gy⁻². We calculated LET based on energy from PIDE and using SRIM software. ρ is the density of the irradiated matter ($\approx 1 \text{ g/cm}^3$).

When R_2 values adjusted with the optimal K factor were compared with $\sigma_{5\%}$ to identify the optimal parameters yielding the best fit (d, p and K), we used the modified χ^2 , which is the sum of squares of differences between the value of σ for a given energy used in a given radiobiological experiment and $K \times R_2$ calculated for the respective energy corresponding to σ . This modified χ^2 was calculated for all selected K, p, and d. For R_2 , the optimal fit was achieved in all cases for $K = 57 \ \mu\text{m}^2$, regardless of varying the values or pairs of p and d. It can be assumed that the K factor represents a saturation threshold for a specific cell line and depends on its nucleus size.

5. Conclusions

Since the structure of the particle track is of great importance for the response of irradiated cells, our studies attempt to correlate the physical description of the radiation interaction with biological endpoints such as cell survival. In our work, we study nanodosimetric quantities in the context of their application to the interpretation of radiobiological data, as potential quantities that describe the complexity of biological damage. We conclude that the previously proposed cumulative probability overlooks a significant fraction of events in the target volume and treats other cluster sizes as evenly influencing the radiation response. This simplification contradicts the statistical character of ionizing radiation interactions with biological systems. Therefore, we propose considering a variable parameter pthat reflects this complexity. These studies do not resolve the issue of finding the ultimate values of the *p* and *d* pair for a given cell line but indicate a general direction that should be explored so as not to lose the opportunity to use nanodosimetric description in the future charged particle radiotherapy planning. While a general formalism bridging the gap between nanoscale parameters and macroscale voxels used in the clinical practice of radiation therapy has recently been proposed, there is still a lack of knowledge and experimental data justifying the selection of appropriate ionization detail parameters to be applied. Our work on the PIDE database and proposal of the R_2 parameter represent important steps towards reaching a consensus. However, further validation studies, including in vitro and in vivo experiments, are required to conclusively determine the applicability of the nanoscale approach to radiation therapy treatment planning and radiation protection.

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Conflicts of Interest: The authors declare no conflicts of interest.

Abbreviations

The following abbreviations are used in this manuscript:

- DNA Deoxyribonucleic Acid
- DSB Double Strand Break
- GEM Gas Electron Multiplier
- GSI GSI Helmholtz Centre for Heavy Ion Research, Darmstadt, Germany
- ICSD Ionization Cluster Size Distribution
- JC Jet Counter
- LET Linear energy transfer
- LQ Linear-Quadratic model
- MC Monte Carlo
- PIDE Particle Irradiation Data Ensemble
- RBE Relative Biological Effectiveness
- SRIM Stopping and Range of Ions in Matter
- SSB Single Strand Break

Appendix A

To provide justification for the choice of a linear dependence between $\sigma_{5\%}$ and R_2 , we illustrate in Figure A1 the relationship between $\sigma_{5\%}$ and R_2 with the best linear fit (shown in gray in Figure A1A), as well as the regular residuals of $\sigma_{5\%}$ with respect to R_2 as an independent variable in Figure A1B, both for a chosen target size of 2.3×3.4 nm². Both graphs demonstrate that the linear dependence effectively captures the variability in the data, with approximately half of the points lying above and half below the best fit line, while also showing an expected increase in deviation as the R_2 values increase.

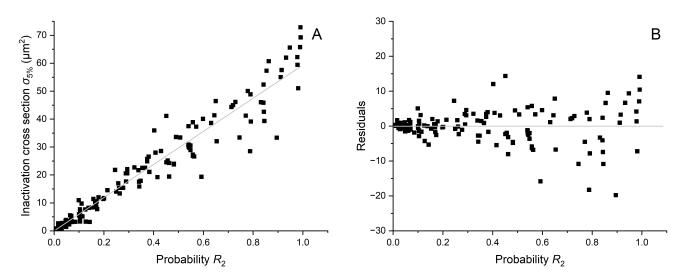


Figure A1. Linear fit between $\sigma_{5\%}$ and R_2 (**A**) and regular residuals of $\sigma_{5\%}$ in a function of an independent variable R_2 (**B**). Coefficient of determination equal to 0.971.

To illustrate that R_2 correlates better with radiobiological data than F_k , we present both R_2 and F_k curves alongside radiobiological data as functions of M_1 for 2.3 × 3.4 nm² (Figure A2B) and 1 × 1 nm² (Figure A2A). In all cases, we selected R_2 for p that provided the best fit, and F_k for k that resulted in the best fit (with k up to 7 tested). For the 2.3 × 3.4 nm² target size, the best fit was obtained for R_2 with p = 0.35 and F_5 , while for the target of 1 × 1 nm², it was achieved for R_2 with p = 0.8 and F_2 .

As shown in Figure A2, F_k proves to be a suitable candidate only for a limited range of M_1 where we observe a linear dependence between $\sigma_{5\%}$ and M_1 . However, at higher M_1 values where saturation occurs, F_k no longer provides an ideal fit. Specifically, for higher M_1 , F_k tends to lie below the biological data. Adjusting the factor K could improve the model's performance for M_1 values above the average, yet it tends to reduce the model's accuracy, especially for average M_1 values at which the shift from a linear to a saturation phase happens. This crucial range is heavily represented with biological data points and substantially impacts the model's fit. The discrete options provided by F_k for choosing k index result in limited curve slopes, unlike the continuous parameter p selection in R_2 , which allows for more precise fitting across a wide range of M_1 values, including within the saturation region.

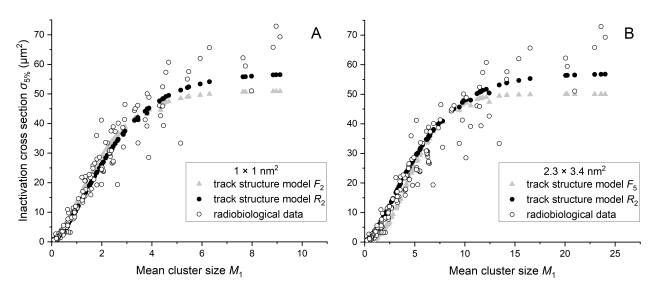


Figure A2. Comparison of R_2 and F_k curves yielding the best fit with radiobiological data for target sizes of 1×1 nm² (**A**) and 2.3×3.4 nm² (**B**). In (**A**), the optimal fit is achieved with F_2 and R_2 for p equal to 0.8, while in (**B**), the best fit is observed for F_5 and R_2 for p equal to 0.35. In both cases, R_2 provides a better fit than F_k .

To provide comparison with F_k yielding best fit, Figure A3 shows the relationship between $\sigma_{5\%}$ and F_5 with the best linear fit (shown in gray in Figure A3A), as well as the regular residuals of $\sigma_{5\%}$ with respect to F_5 as an independent variable in Figure A3B, both for a chosen target size of 2.3 × 3.4 nm². We also included similar results for F_2 in Figure A4 showing that F_2 for a given target size does not provide a satisfying fit.

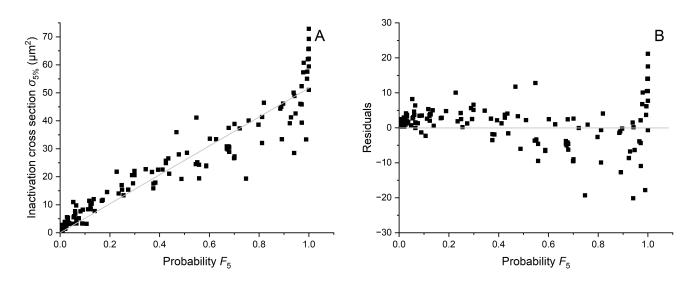


Figure A3. Linear fit between $\sigma_{5\%}$ and F_5 (**A**) and regular residuals of $\sigma_{5\%}$ in a function of an independent variable F_5 (**B**). Coefficient of determination equal to 0.955.

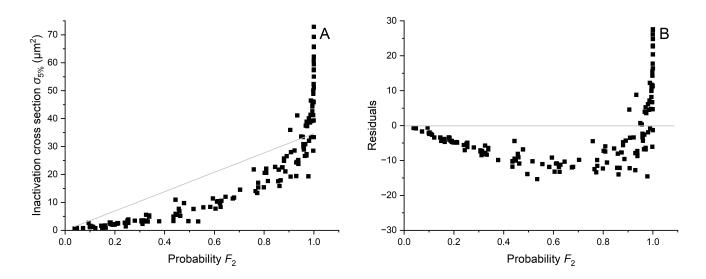


Figure A4. Linear fit between $\sigma_{5\%}$ and F_2 (**A**) and regular residuals of $\sigma_{5\%}$ in a function of an independent variable F_2 (**B**). Coefficient of determination equal to 0.839.

Appendix B

As the study relies on findings derived from Monte Carlo (MC) simulations, we aim to demonstrate the comparability between simulation outcomes for various particles and experimental results obtained using nanodosimeter. The comparison between ICSDs obtained using Geant4-DNA MC code and those measured with Jet Counter nanodosimeter (JC) is presented in Figure A5.

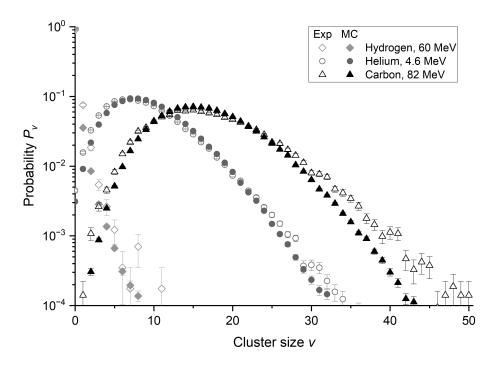


Figure A5. Comparison of ionization cluster size distributions obtained in experiments (Exp) with the Jet Counter device (empty shapes) and in Monte Carlo (MC) simulations (filled shapes) for hydrogen, helium, and carbon ions with different energies. All data are for a $2.3 \times 3.4 \text{ nm}^2$ target size. Uncertainties are due to statistical fluctuations.

Details of the performed simulations and experiments can be found in [24,39]. The discrepancy between experimental data and simulations is more noticeable in the tails of

the ionization cluster size distribution corresponding to large ionization clusters. This is primarily due to the increased experimental uncertainty of the Jet Counter and the reduced statistical uncertainty of simulations. The probability of large cluster sizes is relatively low, which is why the input for the cumulative probability does not cause significant differences.

The prediction of ICSD and their parameters based on Geant4-DNA simulations is satisfying and accurate enough to describe experimental data collected with Jet Counter for different charged particles (protons, alpha particles, and carbon ions) in a wide range of energies [24,39]. Our results indicate that the prediction of ICSD and their parameters based on Geant4-DNA Monte Carlo simulations is precise and opens the possibility of its application for other kinds and energies of the ionizing particles presented in this study.

References

- Goodhead, D.T. Initial Events in the Cellular Effects of Ionizing Radiations: Clustered Damage in DNA. Int. J. Radiat. Biol. 1994, 65, 7–17. [CrossRef]
- Brenner, D.; Ward, J. Constraints on energy deposition and target size of multiply damaged sites associated with DNA doublestrand breaks. *Int. J. Radiat. Biol.* 1992, 61, 737–748. [CrossRef]
- Michalik, V. Energy Deposition Clusters in Nanometer Regions of Charged-Particle Tracks. *Radiat. Res.* 1993, 134, 265–270. [CrossRef]
- 4. Schulte, R.W. Nanodosimetry: Principle and Current Status. Aip Conf. Proc. 2011, 1345, 249–261. [CrossRef]
- Palmans, H.; Rabus, H.; Belchior, A.L.; Bug, M.U.; Galer, S.; Giesen, U.; Gonon, G.; Gruel, G.; Hilgers, G.; Moro, D.; et al. Future Development of Biologically Relevant Dosimetry. *Br. J. Radiol.* 2015, *88*, 20140392. [CrossRef]
- 6. Conte, V.; Selva, A.; Colautti, P.; Hilgers, G.; Rabus, H.; Bantsar, A.; Pietrzak, M.; Pszona, S. Nanodosimetry: Towards a New Concept of Radiation Quality. *Radiat. Prot. Dosim.* **2018**, *180*, 150–156. [CrossRef]
- Faddegon, B.; Blakely, E.A.; Burigo, L.; Censor, Y.; Dokic, I.; Domínguez Kondo, N.; Ortiz, R.; Ramos Méndez, J.; Rucinski, A.; Schubert, K.; et al. Ionization Detail Parameters and Cluster Dose: A Mathematical Model for Selection of Nanodosimetric Quantities for Use in Treatment Planning in Charged Particle Radiotherapy. *Phys. Med. Biol.* 2023, *68*, 175013. [CrossRef]
- 8. Grosswendt, B. Nanodosimetry, the Metrological Tool for Connecting Radiation Physics with Radiation Biology. *Radiat. Prot. Dosim.* 2006, 122, 404–414. [CrossRef]
- Conte, V.; Selva, A.; Colautti, P.; Hilgers, G.; Rabus, H. Track structure characterization and its link to radiobiology. *Radiat. Meas.* 2017, 106, 506–511. [CrossRef]
- 10. Rucinski, A.; Biernacka, A.; Schulte, R. Applications of nanodosimetry in particle therapy planning and beyond. *Phys. Med. Biol.* **2021**, *66*, 24TR01. [CrossRef]
- Conte, V.; Bianchi, A.; Selva, A. Track Structure of Light Ions: The Link to Radiobiology. Int. J. Mol. Sci. 2023, 24, 5826. [CrossRef] [PubMed]
- 12. Incerti, S.; Kyriakou, I.; Bernal, M.A.; Bordage, M.C.; Francis, Z.; Guatelli, S.; Ivanchenko, V.; Karamitros, M.; Lampe, N.; Lee, S.B.; et al. Geant4-DNA Example Applications for Track Structure Simulations in Liquid Water: A Report from the Geant4-DNA Project. *Med. Phys.* **2018**, *45*, e722–e739. [CrossRef] [PubMed]
- Bernal, M.A.; Bordage, M.C.; Brown, J.M.C.; Davídková, M.; Delage, E.; Bitar, Z.E.; Enger, S.A.; Francis, Z.; Guatelli, S.; Ivanchenko, V.N.; et al. Track Structure Modeling in Liquid Water: A Review of the Geant4-DNA Very Low Energy Extension of the Geant4 Monte Carlo Simulation Toolkit. *Phys. Med. Eur. J. Med. Phys.* 2015, *31*, 861–874. [CrossRef] [PubMed]
- Incerti, S.; Ivanchenko, A.; Karamitros, M.; Mantero, A.; Moretto, P.; Tran, H.N.; Mascialino, B.; Champion, C.; Ivanchenko, V.N.; Bernal, M.A.; et al. Comparison of GEANT4 Very Low Energy Cross Section Models with Experimental Data in Water. *Med. Phys.* 2010, 37, 4692–4708. [CrossRef] [PubMed]
- 15. Incerti, S.; Baldacchino, G.; Bernal, M.; Capra, R.; Champion, C.; Francis, Z.; Guèye, P.; Mantero, A.; Mascialino, B.; Moretto, P.; et al. The Geant4-Dna Project. *Int. J. Model. Simul. Sci. Comput.* **2010**, *1*, 157–178. [CrossRef]
- 16. Belloni, F.; Bettega, D.; Calzolari, P.; Cherubini, R.; Massariello, P.; Tallone, L. Inactivation Cross Sections for Mammalian Cells Exposed to Charged Particles: A Phenomenological Approach. *Radiat. Prot. Dosim.* **2002**, *99*, 199–202. [CrossRef]
- 17. Grosswendt, B. Recent Advances of Nanodosimetry. Radiat. Prot. Dosim. 2004, 110, 789–799. [CrossRef]
- 18. Friedrich, T.; Pfuhl, T.; Scholz, M. Update of the Particle Irradiation Data Ensemble (PIDE) for Cell Survival. *J. Radiat. Res.* **2021**, 62, 645–655. [CrossRef] [PubMed]
- Vasi, F.; Schneider, U. First measurements of ionization cluster-size distributions with a compact nanodosimeter. *Med. Phys.* 2021, 48, 2566–2571. [CrossRef]
- 20. Vasi, F.; Kempf, I.; Besserer, J.; Schneider, U. FIRE: A compact nanodosimeter detector based on ion amplification in gas. *Nucl. Instrum. Methods Phys. Res. Sect. A Accel. Spectrometers Detect. Assoc. Equip.* **2021**, 999, 165116. [CrossRef]
- Garty, G.; Schulte, R.; Shchemelinin, S.; Grosswendt, B.; Leloup, C.; Assaf, G.; Breskin, A.; Chechik, R.; Bashkirov, V. First attempts at prediction of DNA strand-break yields using nanodosimetric data. *Radiat. Prot. Dosim.* 2006, 122, 451–454. [CrossRef] [PubMed]

- Pietrzak, M.; Pszona, S.; Bantsar, A. Measurements of spatial correlations of ionisation clusters in the track of carbon ions-first results. *Radiat. Prot. Dosim.* 2018, 180, 162–167. [CrossRef] [PubMed]
- 23. Hilgers, G.; Rabus, H. Correlated ionisations in two spatially separated nanometric volumes in the track structure of 241Am alpha particles: Measurements with the PTB ion counter. *Radiat. Phys. Chem.* **2020**, *176*, 109025. [CrossRef]
- Pietrzak, M. Nanodosimetric Characteristic of Carbon Ion Beam—Experiments and Monte Carlo Simulations. Ph.D. Thesis, Faculty of Physics, University of Warsaw, Warsaw, Poland, 2023.
- Mao, H.; Zhang, H.; Luo, Y.; Yang, J.; Liu, Y.; Zhang, S.; Chen, W.; Li, Q.; Dai, Z. Primary Study of the Relative and Compound Biological Effectiveness Model for Boron Neutron Capture Therapy Based on Nanodosimetry. *Med. Phys.* 2024, *51*, 3076–3092. [CrossRef] [PubMed]
- 26. Durante, M. New Challenges in High-Energy Particle Radiobiology. Br. J. Radiol. 2014, 87, 20130626. [CrossRef] [PubMed]
- Mazzone, A.; Finocchiaro, P.; Meo, S.L.; Colonna, N. On the (Un)Effectiveness of Proton Boron Capture in Proton Therapy. *arXiv* 2018, arXiv:1802.09482.
- Mastromarco, M.; Digennaro, A.; Mazzone, A.; Finocchiaro, P.; Praena, J.; Porras, I.; Colonna, N. Proton Boron Capture Therapy: Dose Calculations and a Possible New Measurement. *Rad Conf. Proc.* 2020, *4*, 185–189. [CrossRef]
- Ahmadi Ganjeh, Z.; Mosleh-Shirazi, M.A. Macroscopic and Microscopic Investigation of Maximum Effectiveness of Proton-Boron Capture Therapy Using Monte Carlo Simulation. *Radiat. Phys. Chem.* 2024, 214, 111289. [CrossRef]
- Manti, L.; Attili, A.; Bláha, P.; Bortolussi, S.; Cuttone, G.; Postuma, I. Increasing Particle Therapy Biological Effectiveness by Nuclear Reaction-Driven Binary Strategies. In *Monte Carlo in Heavy Charged Particle Therapy*; CRC Press: Boca Raton, FL, USA, 2024.
- Safavi-Naeini, M.; Chacon, A.; Guatelli, S.; Franklin, D.R.; Bambery, K.; Gregoire, M.C.; Rosenfeld, A. Opportunistic Dose Amplification for Proton and Carbon Ion Therapy via Capture of Internally Generated Thermal Neutrons. *Sci. Rep.* 2018, *8*, 16257. [CrossRef]
- 32. Grosswendt, B.; De Nardo, L.; Colautti, P.; Pszona, S.; Conte, V.; Tornielli, G. Experimental Equivalent Cluster-Size Distributions in Nanometric Volumes of Liquid Water. *Radiat. Prot. Dosim.* 2004, *110*, 851–857. [CrossRef]
- 33. Pszona, S.; Bantsar, A.; Kula, J. Charge cluster distribution in nanosites traversed by a single ionizing particle—An experimental approach. *Nucl. Instrum. Methods Phys. Res. Sect. B-Beam Interact. Mater. At.* **2008**, *266*, 4911–4915. [CrossRef]
- 34. Bantsar, A. Ionization Cluster Size Distributions Created by Low Energy Electrons and Alpha Particles in Nanometric Track Segment in Gases. Ph.D. Thesis, The Andrzej Sołtan Institute for Nuclear Studies, Świerk, Poland, 2010. [CrossRef]
- Bantsar, A.; Grosswendt, B.; Pszona, S.; Kula, J. Single track nanodosimetry of low energy electrons. Nucl. Instrum. Methods Phys. Res. Sect. A Accel. Spectrometers Detect. Assoc. Equip. 2009, 599, 270–274. [CrossRef]
- 36. Bantsar, A.; Hilgers, G.; Pszona, S.; Rabus, H.; Szeflinski, Z. Experimental investigation of ionisation track structure of carbon ions at HIL Warsaw. *Radiat. Prot. Dosim.* 2015, 166, 253–256. [CrossRef]
- Bantsar, A.; Pietrzak, M.; Jaskóła, M.; Korman, A.; Pszona, S.; Szefliński, Z. Status report: Nanodosimetry of carbon ion beam at HIL. *Rep. Pract. Oncol. Radiother.* 2014, 19, S42–S46. [CrossRef]
- Selva, A.; De Nadal, V.; Cherubini, R.; Colautti, P.; Conte, V. Towards the use of nanodosimetry to predict cell survival. *Radiat.* Prot. Dosim. 2019, 183, 192–196. [CrossRef]
- 39. Pietrzak, M.; Mietelska, M.; Bancer, A.; Rucinski, A.; Brzozowska, B. Geant4-DNA modeling of nanodosimetric quantities in the Jet Counter for alpha particles. *Phys. Med. Biol.* **2021**, *66*, 225008. [CrossRef]
- Agostinelli, S.; Allison, J.; Amako, K.; Apostolakis, J.; Araujo, H.; Arce, P.; Asai, M.; Axen, D.; Banerjee, S.; Barrand, G.; et al. Geant4—A simulation toolkit. *Nucl. Inst. Meth. Phys. Res. A* 2003, 506, 250–303. [CrossRef]
- Allison, J.; Amako, K.; Apostolakis, J.; Arce, P.; Asai, M.; Aso, T.; Bagli, E.; Bagulya, A.; Banerjee, S.; Barrand, G.; et al. Recent developments in Geant4. Nucl. Instrum. Methods Phys. Res. Sect. A Accel. Spectrometers Detect. Assoc. Equip. 2016, 835, 186–225. [CrossRef]
- Kyriakou, I.; Šefl, M.; Nourry, V.; Incerti, S. The Impact of New Geant4-DNA Cross Section Models on Electron Track Structure Simulations in Liquid Water. J. Appl. Phys. 2016, 119, 194902. [CrossRef]
- Ivanchenko, V.; Apostolakis, J.; Bagulya, A.; Abdelouahed, H.B.; Black, R.; Bogdanov, A.; Burkhard, H.; Chauvie, S.; Cirrone, P.; Cuttone, G.; et al. Recent Improvements in Geant4 Electromagnetic Physics Models and Interfaces. *Prog. Nucl. Sci. Technol.* 2011, 2,898–903. [CrossRef]
- Arce, P.; Bolst, D.; Bordage, M.C.; Brown, J.M.C.; Cirrone, P.; Cortés-Giraldo, M.A.; Cutajar, D.; Cuttone, G.; Desorgher, L.; Dondero, P.; et al. Report on G4-Med, a Geant4 Benchmarking System for Medical Physics Applications Developed by the Geant4 Medical Simulation Benchmarking Group. *Med. Phys.* 2021, 48, 19–56. [CrossRef]
- Ziegler, J.F.; Ziegler, M.D.; Biersack, J.P. SRIM—The Stopping and Range of Ions in Matter (2010). Nucl. Instrum. Methods Phys. Res. Sect. B Beam Interact. Mater. At. 2010, 268, 1818–1823. [CrossRef]
- 46. Friedrich, T.; Scholz, U.; ElsäSser, T.; Durante, M.; Scholz, M. Systematic Analysis of RBE and Related Quantities Using a Database of Cell Survival Experiments with Ion Beam Irradiation. *J. Radiat. Res.* **2013**, *54*, 494–514. [CrossRef]
- Hall, E.J.; Gross, W.; Dvorak, R.F.; Kellerer, A.M.; Rossi, H.H. Survival Curves and Age Response Functions for Chinese Hamster Cells Exposed to X-rays or High LET Alpha-Particles. *Radiat. Res.* 1972, 52, 88–98. [CrossRef] [PubMed]
- Bird, R.P.; Burki, H.J. Survival of Synchronized Chinese Hamster Cells Exposed to Radiation of Different Linear-Energy Transfer. Int. J. Radiat. Biol. 1975, 27, 105–120. [CrossRef]

- Cox, R.; Thacker, J.; Goodhead, D.T.; Masson, W.K.; Wilkinson, R.E. Inactivation and Mutation of Cultured Mammalian Cells by Aluminium Characteristic Ultrasoft X-Rays: II. Dose-responses of Chinese Hamster and Human Diploid Cells to Aluminium X-rays and Radiations of Different LET. *Int. J. Radiat. Biol.* 1977, *31*, 561–576. [CrossRef]
- 50. Thacker, J.; Stretch, A.; Stephens, M.A. Mutation and Inactivation of Cultured Mammalian Cells Exposed to Beams of Accelerated Heavy Ions. II. Chinese Hamster V79 Cells. *Int. J. Radiat. Biol. Relat. Stud. Phys. Chem. Med.* **1979**, *36*, 137–148. [CrossRef]
- 51. Schlag, H.; Lücke-Huhle, C. The Influence of Ionization Density on the DNA Synthetic Phase and Survival of Irradiated Mammalian Cells. *Int. J. Radiat. Biol.* **1981**, *40*, 75–85. [CrossRef]
- 52. Perris, A.; Pialoglou, P.; Katsanos, A.A.; Sideris, E.G. Biological Effectiveness of Low Energy Protons. I. Survival of Chinese Hamster Cells. *Int. J. Radiat. Biol.* **1986**, *50*, 1093–1101. [CrossRef]
- Folkard, M.; Prise, K.M.; Vojnovic, B.; Davies, S.; Roper, M.J.; Michael, B.D. The Irradiation of V79 Mammalian Cells by Protons with Energies below 2 Mev: Part I: Experimental Arrangement and Measurements of Cell Survival. *Int. J. Radiat. Biol.* 1989, 56, 221–237. [CrossRef]
- 54. Folkard, M.; Prise, K.M.; Vojnovic, B.; Newman, H.C.; Roper, M.J.; Michael, B.D. Inactivation of V79 Cells by Low-Energy Protons, Deuterons and Helium-3 Ions. *Int. J. Radiat. Biol.* **1996**, *69*, 729–738. [CrossRef]
- Prise, K.M.; Folkard, M.; Davies, S.; Michael, B.D. The Irradiation of V79 Mammalian Cells by Protons with Energies below 2 Mev. Part II. Measurement of Oxygen Enhancement Ratios and DNA Damage. *Int. J. Radiat. Biol.* 1990, 58, 261–277. [CrossRef] [PubMed]
- Raju, M.R.; Eisen, Y.; Carpenter, S.; Inkret, W.C. Radiobiology of *α* Particles. III. Cell Inactivation by *α*-Particle Traversals of the Cell Nucleus. *Radiat. Res.* 1991, 128, 204–209. [CrossRef]
- 57. Jenner, T.J.; DeLara, C.M.; O'Neill, P.; Stevens, D.L. Induction and Rejoining of DNA Double-Strand Breaks in V79-4 Mammalian Cells Following *γ* and *A*irradiation. *Int. J. Radiat. Biol.* **1993**, *64*, 265–273. [CrossRef]
- 58. Weber, K.J.; Flentje, M. Lethality of Heavy Ion-Induced DNA Double-Strand Breaks in Mammalian Cells. *Int. J. Radiat. Biol.* **1993**, 64, 169–178. [CrossRef]
- Stenerlöw, B.; Pettersson, O.A.; Essand, M.; Blomquist, E.; Carlsson, J. Irregular Variations in Radiation Sensitivity When the Linear Energy Transfer Is Increased. *Radiother. Oncol.* 1995, *36*, 133–142. [CrossRef]
- Belli, M.; Cera, F.; Cherubini, R.; Dalla Vecchia, M.; Haqjue, A.M.; Ianzini, F.; Moschini, G.; Sapora, O.; Simone, G.; Tabocchini, M.A.; et al. RBE-LET Relationships for Cell Inactivation and Mutation Induced by Low Energy Protons in V79 Cells: Further Results at the LNL Facility. *Int. J. Radiat. Biol.* 1998, 74, 501–509. [CrossRef]
- 61. Belli, M.; Bettega, D.; Calzolari, P.; Cherubini, R.; Cuttone, G.; Durante, M.; Esposito, G.; Furusawa, Y.; Gerardi, S.; Gialanella, G.; et al. Effectiveness of Monoenergetic and Spread-out Bragg Peak Carbon-Ions for Inactivation of Various Normal and Tumour Human Cell Lines. *J. Radiat. Res.* **2008**, *49*, 597–607. [CrossRef]
- Tilly, N.; Brahme, A.; Carlsson, J.; Glimelius, B. Comparison of Cell Survival Models for Mixed LET Radiation. *Int. J. Radiat. Biol.* 1999, 75, 233–243. [CrossRef] [PubMed]
- Weyrather, W.K.; Ritter, S.; Scholz, M.; Kraft, G. RBE for Carbon Track-Segment Irradiation in Cell Lines of Differing Repair Capacity. Int. J. Radiat. Biol. 1999, 75, 1357–1364. [CrossRef] [PubMed]
- 64. Aoki, M.; Furusawa, Y.; Yamada, T. LET Dependency of Heavy-Ion Induced Apoptosis in V79 Cells. J. Radiat. Res. 2000, 41, 163–175. [CrossRef]
- Furusawa, Y.; Fukutsu, K.; Aoki, M.; Itsukaichi, H.; Eguchi-Kasai, K.; Ohara, H.; Yatagai, F.; Kanai, T.; Ando, K. Inactivation of Aerobic and Hypoxic Cells from Three Different Cell Lines by Accelerated 3He-, 12C- and 20Ne-Ion Beams. *Radiat. Res.* 2000, 154, 485–496. [CrossRef]
- 66. Böhrnsen, G.; Weber, K.J.; Scholz, M. Measurement of Biological Effects of High-Energy Carbon Ions at Low Doses Using a Semi-Automated Cell Detection System. *Int. J. Radiat. Biol.* **2002**, *78*, 259–266. [CrossRef]
- Scholz, M. Effects of Ion Radiation on Cells and Tissues. In Advances in Polymer Science; Springer: Berlin/Heidelberg, Germany, 2003; Volume 162, pp. 95–155. [CrossRef]
- Hill, M.A.; Herdman, M.T.; Stevens, D.L.; Jones, N.J.; Thacker, J.; Goodhead, D.T. Relative Sensitivities of Repair-Deficient Mammalian Cells for Clonogenic Survival after *α*-Particle Irradiation. *Radiat. Res.* 2004, 162, 667–676. [CrossRef]
- Staab, A.; Zukowski, D.; Walenta, S.; Scholz, M.; Mueller-Klieser, W. Response of Chinese Hamster V79 Multicellular Spheroids Exposed to High-Energy Carbon Ions. *Radiat. Res.* 2004, 161, 219–227. [CrossRef]
- Zhou, G.; Kawata, T.; Furusawa, Y.; Aoki, M.; Hirayama, R.; Ando, K.; Ito, H. Protective Effects of Melatonin against Low- and High-LET Irradiation. J. Radiat. Res. 2006, 47, 175–181. [CrossRef]
- 71. Hirayama, R.; Ito, A.; Tomita, M.; Tsukada, T.; Yatagai, F.; Noguchi, M.; Matsumoto, Y.; Kase, Y.; Ando, K.; Okayasu, R.; et al. Contributions of Direct and Indirect Actions in Cell Killing by High-LET Radiations. *Radiat. Res.* 2009, 171, 212–218. [CrossRef]
- Claesson, K.; Magnander, K.; Kahu, H.; Lindegren, S.; Hultborn, R.; Elmroth, K. RBE of α-Particles from 211At for Complex DNA Damage and Cell Survival in Relation to Cell Cycle Position. *Int. J. Radiat. Biol.* 2011, *87*, 372–384. [CrossRef]
- 73. Doria, D.; Kakolee, K.F.; Kar, S.; Litt, S.K.; Fiorini, F.; Ahmed, H.; Green, S.; Jeynes, J.C.; Kavanagh, J.; Kirby, D.; et al. Biological Effectiveness on Live Cells of Laser Driven Protons at Dose Rates Exceeding 109 Gy/s. *AIP Adv.* **2012**, *2*, 11209. [CrossRef]
- Jeynes, J.C.; Merchant, M.J.; Barazzuol, L.; Barry, M.; Guest, D.; Palitsin, V.V.; Grime, G.W.; Tullis, I.D.; Barber, P.R.; Vojnovic, B.; et al. "Broadbeam" Irradiation of Mammalian Cells Using a Vertical Microbeam Facility. *Radiat. Environ. Biophys.* 2013, 52, 513–521. [CrossRef]

- 75. Tracy, B.L.; Stevens, D.L.; Goodhead, D.T.; Hill, M.A. Variation in RBE for Survival of V79-4 Cells as a Function of Alpha-Particle (Helium Ion) Energy. *Radiat. Res.* 2015, *184*, 33–45. [CrossRef]
- 76. Furusawa, Y.; Nakano-Aoki, M.; Matsumoto, Y.; Hirayama, R.; Kobayashi, A.; Konishi, T. Equivalency of the Quality of Sublethal Lesions after Photons and High-Linear Energy Transfer Ion Beams. *J. Radiat. Res.* **2017**, *58*, 803–808. [CrossRef]

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