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Role of Native Defects in Fe-Doped β-Ga$_2$O$_3$

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Abstract: Iron impurities are believed to act as deep acceptors that can compensate for the n-type conductivity in as-grown Ga$_2$O$_3$, but several scientific issues, such as the site occupation of the Fe heteroatom and the complexes of Fe-doped β-Ga$_2$O$_3$ with native defects, are still lacking. In this paper, based on first-principle density functional theory calculations with the generalized gradient approximation approach, the controversy regarding the preferential Fe incorporation on the Ga site in the β-Ga$_2$O$_3$ crystal has been addressed, and our result demonstrates that Fe dopant is energetically favored on the octahedrally coordinated Ga site. The structural stabilities are confirmed by the formation energy calculations, the phonon dispersion relationships, and the strain-dependent analyses. The thermodynamic transition level Fe^{3+}/Fe^{2+} is located at 0.52 eV below the conduction band minimum, which is consistent with Ingebrigtsen's theoretical conclusion, but slightly smaller than some experimental values between 0.78 eV and 1.2 eV. In order to provide direct guidance for material synthesis and property design in Fe-doped β-Ga$_2$O$_3$, the defect formation energies, charge transitional levels, and optical properties of the defective complexes with different kinds of native defects are investigated. Our results show that V$_{Ga}$ and O$_i$ can be easily formed for the Fe-doped β-Ga$_2$O$_3$ crystals under O-rich conditions, where the +3 charge state Fe$_{Ga}$Ga$_i$ and −2 charge state Fe$_{Ga}$O$_i$ are energetically favorable when the Fermi level approaches the valence and conduction band edges, respectively. Optical absorption shows that the complexes of Fe$_{Ga}$Ga$_i$ and Fe$_{Ga}$V$_{Ga}$ can significantly enhance the optical absorption in the visible-infrared region, while the energy-loss function in the β-Ga$_2$O$_3$ material is almost negligible after the extra introduction of various intrinsic defects.

Keywords: first-principles; β-Ga$_2$O$_3$; doping; impurity levels; defect formation energies; optical properties

1. Introduction

Gallium oxides (Ga$_2$O$_3$) have received a lot of attention due to their exceptional physical and chemical features with a variety of applications such as solar-blind ultraviolet photodetectors [1,2], high-power transistors [3,4], Schottky diodes [5,6], as well as photocatalysts [7]. Due to the inevitable insertion of native defects (such as Ga$_i$ [8,9]) and extrinsic impurities (such as Si [10], H [11]) during the growth of materials, perfect Ga$_2$O$_3$ exhibits n-type conductivity, which severely impedes its further applications. Doping engineering, in general, can be a valuable approach to manipulating conductivity, which influences electrical and optical performance by modifying the microscopic crystalline structure [12–16]. As a result, studies of acceptors in β-Ga$_2$O$_3$ materials are required. The n-type conductivity in perfect β-Ga$_2$O$_3$ can be compensated by the introduction of deep acceptors, such as Fe dopant. Fe impurity is one of the most attractive dopants because it

not only exists unintentionally during the synthesis of β-Ga_2O_3 crystals but also possesses the same tri-valence states with comparable ionic radii as host Ga^{3+} [17].

β-Ga_2O_3 exhibits a monoclinic structure with two nonequivalent tetrahedrally and octahedrally coordinated Ga sites. Regarding the replacement of Ga by Fe dopant in the β-Ga_2O_3 system, one general question would be what is the preferential substitution location for Fe, the tetrahedrally or the octahedrally coordinated Ga sites? Previous studies showed that the specified site location and local symmetry may determine the microscopic structure as well as the optical and electronic properties [18]. Zhang et al. reported the preferential occupation of Fe^{3+} ions in the octahedral over the tetrahedral sites in the Fe-doped β-Ga_2O_3 crystal based on electron paramagnetic resonance (EPR) analyses [19]. Trooster et al. reported that Fe-doped $Ga_{2-x}Fe_xO_3$ powder with high doping concentrations (i.e., x = 0.8, 0.9, 1.08, and 1.15) grown with the flux method of Remeika exhibited ferrimagnetic spin configuration. Based on the Mossbauer measurements of ^{57}Fe in different compositions, they concluded that Fe^{3+} ions mainly replaced Ga^{3+} in the octahedral sites, with only a small fraction of Fe ions at the tetrahedral Ga sites [20]. Büscher et al. revealed the occupation of Fe^{3+} in distorted tetrahedral sites in single β-Ga_2O_3 crystals for the first time by employing EPR measurements [21]. Recently, Bhandari et al. showed that the Fe-replaced tetrahedral and octahedral Ga sites were not distinguished since the photon-induced changes at two different Ga sites were the same based on steady-state photo-EPR measurements [22]. This controversy over the specified Fe location in β-Ga_2O_3 will be addressed theoretically as below. In addition, native defects are inevitable in Fe-doping in the β-Ga_2O_3 system. Zhang et al. revealed that, different from the as-grown Fe-doped β-Ga_2O_3 system, the air-annealing treatment can efficiently increase the crystalline quality and reduce oxygen vacancies, along with decreasing the conductivity and halving the spin susceptibility [19]. Zhou et al. found that for the Fe substituting of the Ga site in the β-Ga_2O_3 lattice, the main defects originated from oxygen vacancies at room temperatures, as suggested by the EPR spectra, which led to the high resistivity and the potential application for *x*-ray detection [23]. Hany et al. also reported the existence of V_O and V_{Ga} in Fe-doped β-Ga_2O_3 single crystals using optical absorption and temperature-dependent cathodoluminescence (CL) measurements [24].

In terms of the electronic structure variation due to Fe^{3+} substitution, a deep level between (0.78–1.2) eV relative to the conduction band minimum (CBM) has been reported. Ingebrigtsen et al. unfolded two similar deep levels located at 0.78 eV and 0.75 eV, which can be associated with Fe impurities and intrinsic defects, respectively, for both bulk β-Ga_2O_3 crystal growth by hydride vapor phase epitaxy and molecular beam epitaxy methods [25]. Lenyk et al. studied the Fe^{3+}/Fe^{2+} level in Fe-doped β-Ga_2O_3 crystals and observed a value of ~0.84 eV below the conduction band using noncontact spectroscopy methods including EPR, infrared absorption, and thermoluminescence [17]. Polyakov et al. ascertained that the Fermi level (E_f) in Fe-doped β-Ga_2O_3 crystals was pinned by the Fe acceptor level near the CBM of ~0.80 eV [26]. Bhandari et al. showed that Fe dopants act as deep acceptors, and the first optically induced change in Fe^{3+} occurred at 1.2 eV in a Fe-doped β-Ga_2O_3 single crystal [22].

To corroborate the experimentally resolved two similar deep levels, Ingebrigtsen et al. performed Heyd-Scuseria-Ernzerhof (HSE) hybrid functional calculations. Their results show that the Fe-replaced Ga site is energetically favored on the octahedral Ga site (Fe_{GaII}), while Fe substituted for the tetrahedral site (Fe_{GaI}) exhibits a slightly higher formation energy both under O-rich and Ga-rich conditions compared with the Fe_{GaII} state. Moreover, the thermodynamic transition level for the Fe^{3+}/Fe^{2+} is located at 0.61 eV below the CBM; the level falls to 0.40 eV if assuming the lower screening [25]. We can hardly find more theoretically calculated results for Fe-doped β-Ga_2O_3 to the best of our knowledge. Therefore, it is highly desirable to provide a fundamental understanding of the relationships between the local crystal structure in Fe-doped β-Ga_2O_3 and other electronic properties from different theoretical approaches. Aside from the Fe dopant, intrinsic defects, including vacancies and interstitials, have significant impacts on their physical properties. How-

ever, the correlations among the Fe-doped β-Ga$_2$O$_3$ with native defects, the local crystal structure, and the electronic and optical properties have not been extensively studied.

Herein, we performed density functional theory (DFT) calculations to investigate the defect formation energies, charge transitional levels, electronic structures, and optical properties of Fe-doped β-Ga$_2$O$_3$, as well as Fe-doped β-Ga$_2$O$_3$ with different kinds of native defects. Our results address the controversies regarding the preferential Fe incorporation on the tetrahedrally or octahedrally coordinated Ga site, as mentioned above. Moreover, since the absence of relevant reports in Fe-doped β-Ga$_2$O$_3$ lattices with native defects from theoretical studies, the defect formation energies, charge transitional levels, and optical properties of the defective complexes of Fe-doped β-Ga$_2$O$_3$ with different kinds of native defects, i.e., oxygen vacancy (V$_O$), gallium vacancy (V$_{Ga}$), oxygen interstitial (O$_i$), and gallium interstitial (Ga$_i$), are investigated. Our studies are beneficial for understanding the ground state properties of Fe-doped β-Ga$_2$O$_3$, as well as for providing theoretical guidance on the design of β-Ga$_2$O$_3$-based functional materials and the promising applications of β-Ga$_2$O$_3$ for innovative spin-electronic and optoelectronic devices.

2. Calculation Methods

2.1. Computational Details

To implement the first-principles calculations, we use the Vienna ab initio Simulation Package (VASP) [27,28] based on DFT [29] with projected augmented wave (PAW) potentials. To characterize the exchange-correlation interactions, the generalized gradient approximation (GGA) parameterized by Perdew-Burke-Ernzerhof (PBE) [30] is used. The kinetic energy cutoff for the plane-wave basis set is 450 eV, the energy convergence criterion for the calculations is set to 1×10^{-5} eV/atom for the interactions between the electrons and ions, and all the atomic positions are fully optimized. When all components of the residual forces are less than 0.01 eV/Å, the relaxation will be terminated. A $4 \times 4 \times 2$ Monkhost-Pack grid is utilized for structural relaxation, whereas a $9 \times 9 \times 4$ Monkhost-Pack grid is used for the calculations of density of states (DOS) and optical properties. The so-called density function perturbation (DFPT) calculated method for phonon calculations is adopted in this work. Usually, phonon dispersion is needed to expand the supercell. However, we do not enlarge the supercell in this work considering the time-consuming nature, which may not influence our conclusions qualitatively. A $2 \times 4 \times 2$ Monkhost-Pack grid and a 1×10^{-6} eV/atom energy criterion have been used for the calculation of phonon dispersion and mechanical properties. The valence electronic configurations for Ga, O, and Fe are [Ar] 3d^{10}4s^{2}4p^1, [He] 2s^{2}2p^4, and [Ar] 3d^{7}4s^1, respectively.

A $1 \times 2 \times 2$ β-Ga$_2$O$_3$ supercell of 32 Ga atoms and 48 O atoms is modeled in this study, with one Fe impurity replacing the Ga atom, corresponding to a doping concentration of 3.125%, as shown in Figure 1a. β-Ga$_2$O$_3$ possesses two inequivalent Ga positions. Fe impurity incorporation on the tetrahedrally and octahedrally coordinated Ga sites is labeled 1 and 2, respectively. Different kinds of native defects in terms of oxygen vacancy, gallium vacancy, oxygen interstitial, and gallium interstitial in the β-Ga$_2$O$_3$ supercell are considered, which are denoted as V$_O$, V$_{Ga}$, O$_i$, and Ga$_i$, respectively. For the atomic positions of V$_O$ and V$_{Ga}$, we use the results by Dong et al. [31], i.e., the positions of 3 and 4 in Figure 1a, respectively. For the low-energy O$_i$ and Ga$_i$ doping sites in gallium oxide, we adopt the results given by Zacherle et al. [32], where the two interstitial sites are located at the same position (0.683, 0.500, 0.459) in the supercell before relaxation and labeled as 5 in Figure 1a. For simplicity, Fe impurities replacing tetrahedral and octahedral Ga atoms are named Fe$_{GaI}$ and Fe$_{GaII}$, respectively. Thus, their complexes of Fe$_{GaI}$ with V$_O$, V$_{Ga}$, O$_i$, and Ga$_i$ configurations are named Fe$_{GaI}$V$_O$, Fe$_{GaI}$V$_{Ga}$, Fe$_{GaI}$O$_i$, and Fe$_{GaI}$Ga$_i$, respectively, while complexes of Fe$_{GaII}$ with V$_O$, V$_{Ga}$, O$_i$, and Ga$_i$ configurations are labeled as Fe$_{GaII}$V$_O$, Fe$_{GaII}$V$_{Ga}$, Fe$_{GaII}$O$_i$, and Fe$_{GaII}$Ga$_i$, respectively. Besides, we also employ the value of U in accordance with the experimental band gap for the perfect β-Ga$_2$O$_3$ [33], and the U value of 4.09 eV is adopted for the 3d orbital of the Fe dopant as suggested by the literature [34].
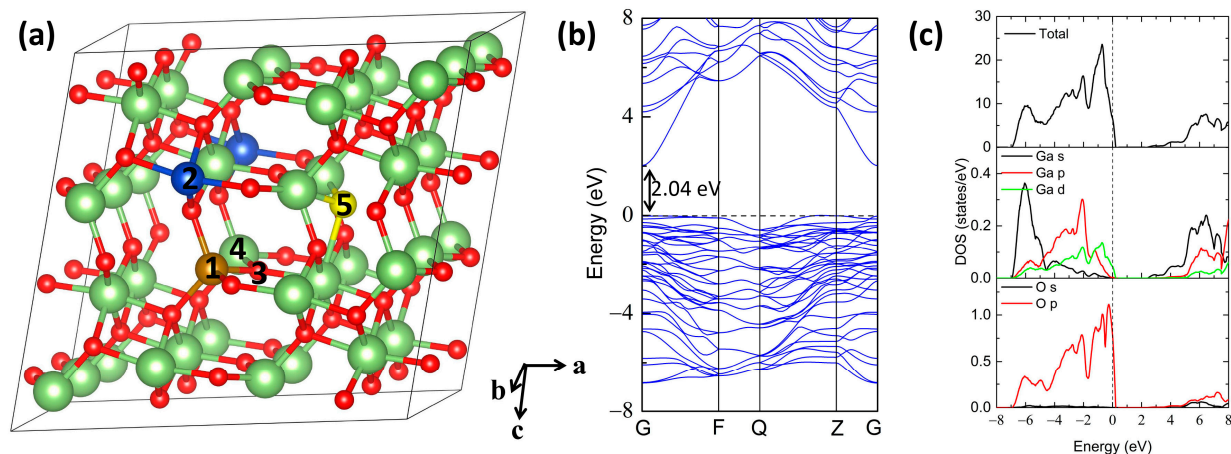
Figure 1. (**a**) The calculated complex model of a Fe-doped β-Ga$_2$O$_3$ supercell with native defects obtained from VESTA [35]. 1 and 2 denote the tetrahedrally and octahedrally coordinated Ga sites substituted by an iron atom, respectively. 3 and 4 show the vacancy sites for Ga and O, respectively, while 5 represents the interstitial positions for both Ga and O. The a, b, and c axes refer to the crystallographic a, b, and c directions, respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.) (**b**,**c**) exhibit the band structure and the density of states for perfect β-Ga$_2$O$_3$, respectively.

2.2. Formation Energies, Transitional Levels and Optical Calculations

The formation energy of the defect D in the charge state q is calculated as [36,37]

$$H_{D,q}(E_f, \mu) = [E_{D,q} - E_p] + \sum_i n_i \mu_i + q(E_{VBM} + E_f) + E_{corr} \tag{1}$$

where $E_{D,q}$ and E_p denote the total energy of the defect and perfect supercell, respectively. n_i represents the number of i atoms added ($n_i < 0$) or removed ($n_i > 0$) from the perfect supercell, and μ_i is the corresponding chemical potential. E_{VBM} is energy of the valence band maximum (VBM) for bulk Ga$_2$O$_3$. E_f is Fermi level, which is referenced to the VBM in the bulk. E_{corr} is the term that accounts for the finite-size corrections, which is determined by the potential alignment and is given as [36]

$$E_{corr} = q(V^r_{D,q} - V^r_p) \tag{2}$$

where the potential difference between the charged defect Ga$_2$O$_3$ supercell ($V^r_{D,q}$) and perfect Ga$_2$O$_3$ supercell (V^r_p) are calculated from the atomic-sphere-averaged potentials at the atomic sites farther away from the defect employed by the software of VASPKIT Standard Edition 1.3.5 [38].

Note that the chemical potential satisfies the boundary conditions as follows:

$$2\mu_{Ga} + 3\mu_O = \mu_{Ga_2O_3}, \qquad \mu_{Ga} \leq \mu_{Ga}^{Metal}, \qquad \mu_O \leq \frac{1}{2}\mu_{O_2} \tag{3}$$

Chemical potential varies according to different growth conditions. Under O-rich growth condition:

$$\mu_O = \frac{1}{2}\mu_{O_2}, \qquad \mu_{Ga} = \frac{1}{2}\left(\mu_{Ga_2O_3} - \frac{3}{2}\mu_{O_2}\right) \tag{4}$$

Under Ga-rich growth condition:

$$\mu_{Ga} = \mu_{Ga}^{Metal}, \qquad \mu_O = \frac{1}{3}\left(\mu_{Ga_2O_3} - 2\mu_{Ga}\right) \tag{5}$$

where, $\mu_{Ga_2O_3}$ is the chemical potential of the bulk β-Ga_2O_3. The chemical potential of μ_{Ga}^{Metal} and μ_{Fe} are calculated from the energies of the most stable bulk crystal of the Ga and Fe atoms, respectively. μ_O represents the chemical potential of O obtained from the energy of O_2. The chemical potentials of μ_O, μ_{Ga} and μ_{Fe} under O-rich condition are -4.92 eV, -7.55 eV, -8.24 eV, respectively, while the corresponding values are -8.01 eV, -2.90 eV, -8.24 eV for Ga-rich atmosphere.

The transition energy $\varepsilon(q_1/q_2)$ between charge state q_1 and q_2 for defect D doping configuration is calculated as [39]

$$\varepsilon(q_1/q_2) = \frac{E_D^{q_1}\big|_{E_f=0} - E_D^{q_2}\big|_{E_f=0}}{q_2 - q_1} \tag{6}$$

Here, the $E_D^q\big|_{E_f=0}$ represents the formation energy of the defect D in charge state q evaluated at $E_f = 0$. The $\varepsilon(q_1/q_2)$ denotes the Fermi-level position where the charge states q_1 and q_2 have equal formation energy.

The absorption coefficients in optical properties can be described as [31,40]

$$\alpha(\omega) = \sqrt{2}\omega\left[\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega)\right]^{1/2} \tag{7}$$

where $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ indicate the real and imaginary parts of the dielectric function, respectively. The $\varepsilon_2(\omega)$ can be calculated by summing up the transitions between occupied and unoccupied states using the following equation

$$\varepsilon_2(\omega) = \left(\frac{4\pi^2 e^2}{m\omega^2}\right)\sum_{i,j}\int \langle i|M|j\rangle^2 f_i(1 - f_i) \times \delta(E_{jk} - E_{ik} - \omega)d^3k \tag{8}$$

Here, m, e, M, and ω denote the mass of free electrons, the electron charge, the dipole matrix, and the frequency of incident photons, respectively. i, j, f_i, and k represent the initial state, the final state, the Fermi distribution function, and the wave function vector, respectively. The $\varepsilon_2(\omega)$ is related to the absorption of light and dielectric loss of energy, while $\varepsilon_1(\omega)$ is associated with the stored energy.

The energy loss function (ELF) can be described by the following equation [41]

$$L(\omega) = Im[\frac{-1}{\varepsilon(\omega)}] = \frac{\varepsilon_2(\omega)}{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} \tag{9}$$

3. Results and Discussions

3.1. Structural Stability

The calculated lattice parameters of perfect β-Ga_2O_3 are a = 12.412 Å, b = 3.076 Å, c = 5.872 Å, and the unique angle β = 103.702°, which are in excellent accordance with the theoretically calculated values obtained by PBE [41] and B3PW [42] approaches, as well as with the experimental values [43], as shown in Table 1. The optimized structural parameters for the Fe-doped cases are also summarized in Table 1. The lattice constants of Fe-doped β-Ga_2O_3 exhibit a slight decrease, which can be ascribed to the comparable ionic radii and local structures between Fe and Ga atoms. The relative difference of the radii between Fe^{3+} (Fe^{2+}) and Ga^{3+} ions is -1.61% (-11.3%). Fe_{GaII} is endowed with smaller lattice parameter variations in terms of all three lattice vectors and the unique angle β compared with Fe_{GaI}, implying that small distortions may be easily formed in the experimental growth.

Table 1. The calculated lattice constants for perfect and Fe-doped β-Ga$_2$O$_3$. The values in parentheses indicate the changes in lattice parameters compared with these of the perfect β-Ga$_2$O$_3$.

Lattice Constants	Perfect (This Work)	Perfect (Literature)	Fe$_{GaI}$	Fe$_{GaII}$
a (Å)	12.412	12.494 [41]/12.28 [42]/12.214 [43]	12.387 (−0.20%)	12.393 (−0.15%)
b (Å)	3.076	3.096 [41]/3.05 [42]/3.037 [43]	3.076 (0.02%)	3.075 (−0.05%)
c (Å)	5.872	5.898 [41]/5.82 [42]/5.798 [43]	5.888 (0.28%)	5.868 (−0.07%)
β (°)	103.702	103.705 [41]/103.83 [43]	103.835 (0.13%)	103.700 (0%)

To study the structural stability of Fe-doped β-Ga$_2$O$_3$ supercells, the defect formation energies under different conditions are calculated, as shown in Figure 2. Meanwhile, the transition levels are also employed to assess the ionization energies and the effectiveness of the doped systems. Our calculated value of the band gap for perfect β-Ga$_2$O$_3$ is 2.04 eV, as denoted by the dashed line in Figure 1b, which is consistent with the values obtained by the DFT calculated method but smaller than the experimental values [44]. The underestimated band gap for DFT calculation is a common phenomenon; however, it does not affect our conclusions qualitatively [45,46]. In addition, Figure 1c illustrates the calculated total density of states (TDOS) and partial density of states (PDOS) for perfect β-Ga$_2$O$_3$; the VBM is predominantly composed of O 2p orbital-derived states with minor hybridization with Ga 3d and 4p orbitals, while the CBM is mainly formed by Ga 4s orbitals.
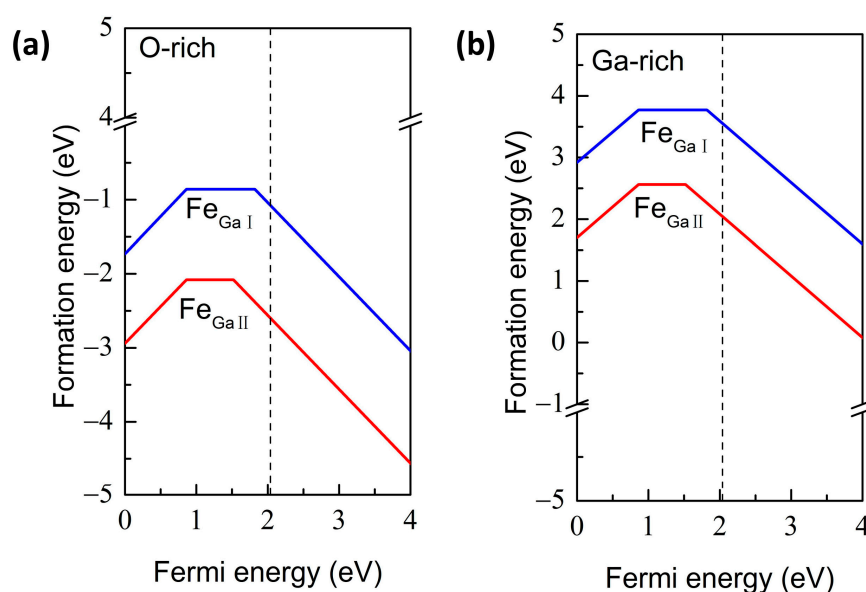

Figure 2. The defect formation energies of Fe-doped β-Ga$_2$O$_3$ under (**a**) the O-rich and (**b**) Ga-rich conditions. The dash line represents the calculated band gap of perfect β-Ga$_2$O$_3$.

Figure 2a indicates the formation energies for Fe-doped β-Ga$_2$O$_3$ under O-rich conditions. Fe$_{GaII}$ case has lower formation energy, suggesting the preferential occupation of Fe$_{Ga}$ at the octahedrally coordinated Ga site, which is in agreement with Ingebrigtsen's conclusion by theoretical calculation [25] and other experimental results [19,20]. The thermodynamic transition level Fe^{3+}/Fe^{2+} for Fe$_{GaII}$, i.e., $\varepsilon(0/-)$, is located at 0.52 eV below CBM, which is comparable to the theoretical value calculated by HSE hybrid functions (0.61 eV or 0.40 eV [25]), but slightly smaller than the reported experimental values (0.78 eV [25], 0.80 eV [26], 0.84 eV [17], 1.2 eV [22]). The transition level Fe^{3+}/Fe^{2+} for Fe$_{GaI}$ measured from VBM is 0.24 eV below CBM, thus deep acceptors are expected for both Fe-doped β-Ga$_2$O$_3$ configurations in the n-type β-Ga$_2$O$_3$ conditions, which can compensate for the free electrons caused by native defects or extrinsic impurities. In addition, the tran-

sition level $\varepsilon(+/0)$ for both Fe_{GaI} and Fe_{GaII} is 0.86 eV above the VBM, which demonstrates that both doping cases generate deep donors even in the p-type β-Ga_2O_3 crystals. For the Ga-rich condition, i.e., the O-poor condition, as shown in Figure 2b, the tendency is the same as for the O-rich atmosphere, with the exception of higher formation energies. This suggests that Fe impurity is more easily substituted for Ga sites under O-rich conditions.

The mechanical characteristics of β-Ga_2O_3 are evaluated by employing a complete set of elastic constants. There are thirteen independent elastic constants (C_{11}, C_{22}, C_{33}, C_{44}, C_{55}, C_{66}, C_{12}, C_{13}, C_{23}, C_{15}, C_{25}, C_{35}, and C_{46}) in the monoclinic symmetry crystal. The mechanical stability criteria of β-Ga_2O_3 are described as follows [47]:

$$C_{ii} > 0, \quad i = 1 - 6. \tag{10}$$

$$[C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})] > 0 \tag{11}$$

$$\left(C_{33}C_{55} - C_{35}^2\right) > 0 \tag{12}$$

$$\left(C_{44}C_{66} - C_{46}^2\right) > 0 \tag{13}$$

$$(C_{22} + C_{33} - 2C_{23}) > 0 \tag{14}$$

$$[C_{22}\left(C_{33}C_{55} - C_{35}^2\right) + 2C_{23}C_{25}C_{35} - C_{23}^2C_{55} - C_{25}^2C_{33}] > 0 \tag{15}$$

$$\begin{aligned} \Omega \quad &= 2[C_{15}C_{25}(C_{33}C_{12} - C_{13}C_{23}) + C_{15}C_{35}(C_{22}C_{13} - C_{12}C_{23}) \\ &+ C_{25}C_{35}(C_{11}C_{23} - C_{12}C_{13})] - [C_{15}^2(C_{22}C_{33} - C_{23}^2) \\ &+ C_{25}^2(C_{11}C_{33} - C_{13}^2) + C_{35}^2(C_{11}C_{22} - C_{12}^2)] + C_{55}g > 0 \end{aligned} \tag{16}$$

$$g = C_{11}C_{22}C_{33} - C_{11}C_{23}^2 - C_{22}C_{13}^2 - C_{33}C_{12}^2 + 2C_{12}C_{13}C_{23} \tag{17}$$

In this study, the mechanical property calculations are carried out for the perfect and energetically favorable Fe_{GaII} doping configuration. The calculated elastic stiffness constants of prefect and Fe-doped β-Ga_2O_3 are shown in Table 2. For comparisons, available theoretical and experimental results are also listed. The elastic stiffness of prefect and Fe-doped β-Ga_2O_3 meets the mechanical stability criteria presented above, suggesting that prefect and Fe-doped β-Ga_2O_3 are mechanically stable at ambient conditions.

The formation energies as a function of the biaxial strain with q = 0 under O-rich conditions are shown in Figure 3a to assess the mechanical stability of Fe_{GaII} as well. It can be seen that the unstrained Fe_{GaII} is endowed with the smallest formation energy of -2.07 eV, indicating the Fe_{GaII} structure is in a stable state. Moreover, the formation energies are strongly dependent on the biaxial strain. As the tensile or compressive stress increases, it increases dramatically. When the compressive strain is greater than 2% or the tensile strain is higher than 3%, the defect formation energy is greater than 0, denoting that it may be difficult to materialize in the experiment. The defect formation energy increases more rapidly under compressive strain, which indicates that the defect is more difficult to realize under compressive strain.

Table 2. Calculated elastic coefficients C_{ij}, bulk modulus B_H, Yong modulus E_H and shear modulus G_H (all in GPa) for perfect and Fe_{GaII} structures, as well as the literature values for comparison. The subscript H is responding to Voigt-Reuss-Hill notation.

		C_{11}	C_{12}	C_{13}	C_{15}	C_{22}	C_{23}	C_{25}	C_{33}
Perfect	This work (PBE)	215	109	119	−15	317	72	14	312
	PBE [48]	208	118	146	0	335	83	0	318
	B3LYP [49]	235	124	138	−13	357	76	7	357
	Exp [50]	238	130	152	−4	359	78	2	346
Fe_{GaII}		217	107	118	−17	322	72	9	315
		C_{35}	C_{44}	C_{46}	C_{55}	C_{66}	B_H	E_H	G_H
Perfect	This work (PBE)	6	48	14	64	94	159	188	72
	PBE [48]	19	50	9	77	96	171	192	73
	B3LYP [49]	12	55	15	81	101	179	214	82
	Exp [50]	19	49	6	91	107	184	213	82
Fe_{GaII}		7	51	18	67	90	160	190	73
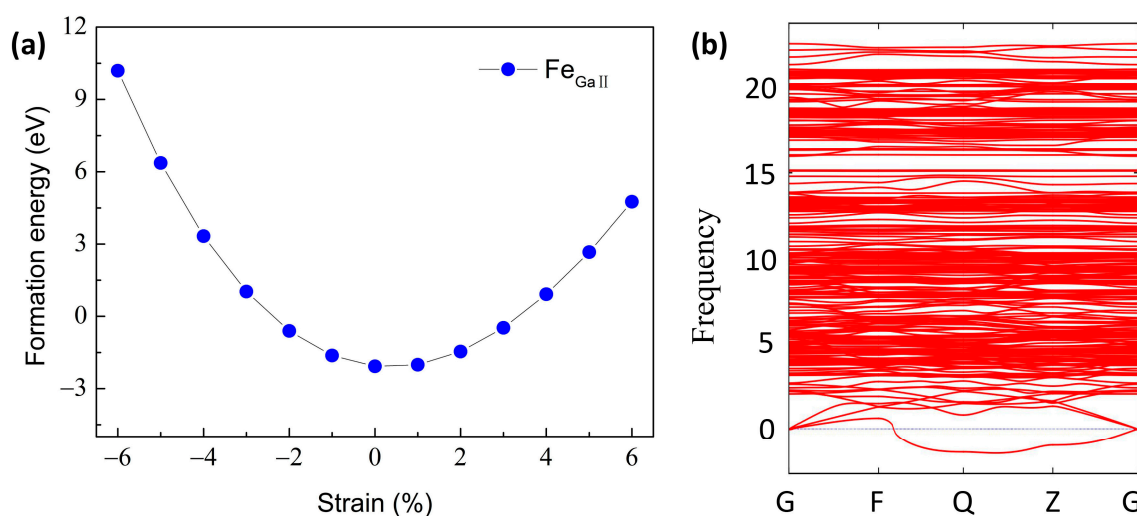
Figure 3. (**a**) The formation energies of Fe_{GaII} as a function of the biaxial strain with q = 0 under O-rich conditions. (**b**) The phonon dispersion calculations for the Fe_{GaII} doping configuration.

Phonon analysis has proven to be an effective approach to predicting structural stability [51]. The phonon dispersion calculation for Fe_{GaII} doping structure is shown in Figure 3b. We observe three small imaginary frequencies, i.e., 0.64, 0.78, and 1.10 cm^{-1}, locating at the non-gamma point (G). In general, imaginary frequencies at the gamma point can be related to structural instability, whereas the presence of imaginary frequencies at the non-gamma point can be responsible for the finite size of the simulation crystal cell, which can be eliminated by expanding the calculated supercell. Therefore, the Fe-doped β-Ga$_2$O$_3$ with small imaginary frequencies at the non-gamma point is predicted to be structurally stable, which agrees well with the results as suggested by the low formation energies.

Figure 4a shows the complexes of Fe_{GaII} and Fe_{GaI} with native defects under different growth condition limits. For these defective Fe_{GaII} complexes under O-rich conditions, positively charged $Fe_{GaII}Ga_i$ and negatively charged $Fe_{GaII}O_i$ are energetically favorable when the E_f approaches the VBM and CBM, respectively, while positively charged $Fe_{GaII}Ga_i$ is

expected throughout the whole band gap under Ga-rich condition. Moreover, the formation energies of $Fe_{Ga_{II}}Ga_i$ (Ga-rich condition) and $Fe_{Ga_{II}}O_i$ (O-rich condition) are lower compared with those of $Fe_{Ga_{II}}$ case, suggesting that $Fe_{Ga_{II}}Ga_i$ and $Fe_{Ga_{II}}O_i$ complexes are easily formed under Ga-rich and O-rich conditions during experimental growth, respectively. For the $Fe_{Ga_{II}}V_O$ case, under O-rich conditions, the transition levels $\varepsilon(+2/+1)$ and $\varepsilon(+1/0)$ are 1.29 and 0.62 eV below CBM, respectively, indicating that the complex acts as a deep donor and cannot contribute to n-type conductivity. Different from the intrinsic Vo defect investigated in literature [10], we observe the +1 charge state rather than +2 and 0 charge states, which may be attributed to the combination of −1 charge state Fe dopant and +2 charge state V_O. The similar results are inspected under Ga-rich conditions except for the lower formation energies, suggesting the $Fe_{Ga_{II}}V_O$ complex is easily formed in the O-poor growth atmosphere. For the $Fe_{Ga_{II}}V_{Ga}$ case, the transition levels $\varepsilon(0/-2)$, $\varepsilon(-2/-3)$ and $\varepsilon(-3/-4)$ are located at 1.34, 0.57, and 2.04 eV below CBM, which demonstrate that the complexes act as deep acceptors with −4 or −3 charge state, respectively. Compared with the Ga-rich condition, the $Fe_{Ga_{II}}V_{Ga}$ complex possesses lower formation energies in n-type Ga_2O_3 materials, which demonstrates that the V_{Ga} is more likely produced in Fe-doped Ga_2O_3 under an O-rich growth atmosphere in experiments. It is in excellent agreement with the reported experimental result by Hany et al. [24]. Either under O-rich or Ga-rich conditions, positively charged and negatively charged $Fe_{Ga_{II}}O_i$ is energetically favorable when the Fermi level approaches the VBM and CBM, respectively. Moreover, $Fe_{Ga_{II}}O_i$ complex is more susceptible to being produced under O-rich conditions. For the $Fe_{Ga_{II}}Ga_i$ case, both under O-rich and Ga-rich conditions, positively charged are energetically favorable when the E_f is located throughout the whole band gap, which demonstrates that the complex exhibits n-type conductivity. The transition levels $\varepsilon(+4/+3)$ and $\varepsilon(+3/+2)$ are 1.47 and 3.02 eV above the VBM under O-rich condition and Ga-rich condition, which indicates that the +3 charge state for the $Fe_{Ga_{II}}Ga_i$ complex is expected. In addition, the higher formation energies under the O-rich condition for the $Fe_{Ga_{II}}Ga_i$ illustrate that the complex is more likely to be found under the Ga-rich conditions. It is worth mentioning that the Ga_i is the main origin of the native defect to form the n-type conductive β-Ga_2O_3 crystal, as illustrated in Refs. [8,9], while a low formation energy is gained for the $Fe_{Ga_{II}}Ga_i$ complex. The E_f always tends to be positioned at the higher region of the bandgap in β-Ga_2O_3 and gives rise to the n-type conduction characteristic due to unintentionally introduced native defects during the growth of β-Ga_2O_3. Therefore, our calculated results illustrate that the +3 charge state $Fe_{Ga_{II}}Ga_i$ under O-poor condition and −2 charge state $Fe_{Ga_{II}}O_i$ under O-rich condition are easily formed for the growth of β-Ga_2O_3 crystals.

　Figure 4b shows the defect formation energies for the complexes of Fe_{Ga_I} with native defects. Different from the case of $Fe_{Ga_{II}}$ complexes, under O-rich conditions, +4 charge state $Fe_{Ga_I}Ga_i$ and −2 charge state $Fe_{Ga_I}O_i$ are dominated when the E_f is located near the VBM and CBM, respectively, while −4 charge state $Fe_{Ga_I}Ga_i$ is easily generated throughout the whole band gap under Ga-rich conditions. Thus, different local structures can influence the electron transfer. As shown in Figure 4b, these defective complexes are characterized by similar tendencies with those of $Fe_{Ga_{II}}$ complexes in exception for different formation energies both under O-rich and Ga-rich conditions.
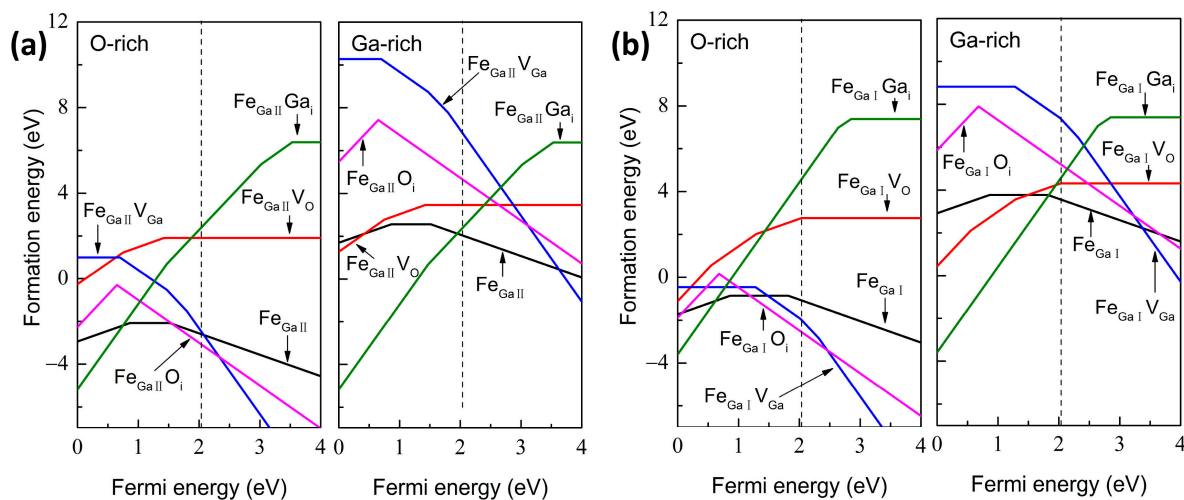
Figure 4. The defect formation energies under the O-rich and Ga-rich conditions for the complexes of (**a**) Fe_{GaII} and (**b**) Fe_{GaI} with native defects. The dash line represents the calculated band gap of perfect β-Ga_2O_3.

3.2. Optical Property

For wide-band gap semiconductor materials, optical parameters of dielectric function $\varepsilon(\omega)$ can be employed to clarify the linear response of the system to electromagnetic radiation, which is crucial to assessing the interactions between photons and electrons. The imaginary part $\varepsilon_2(\omega)$ of the dielectric constant is related to the absorption of light and the dielectric energy-loss function, while $\varepsilon_1(\omega)$ is associated with the stored energy. Figure 5 denotes the optical absorption coefficient of perfect, Fe-doped, and various Fe_{GaII}/Fe_{GaI} complexes in the energy range between 0 and 30 eV. Figure 5b,d exhibits the enlarged plots at the (0–5) eV region. The strong absorption peaks are located at 11.8 and 10.9 eV for perfect β-Ga_2O_3, as shown in Figure 5a, which originate from the inter-band transitions from O 2p states to Ga 4s states, illustrating that the bulk material is characterized by its deep ultraviolet properties. The calculated data is consistent with Yan and Pan's results [52,53]. Compared with perfect β-Ga_2O_3, the profiles of Fe-doped β-Ga_2O_3 and various complexes in Figure 5a,c are endowed with similar absorption peaks in the high-energy ultraviolet region, indicating that these dopants can hardly decrease the optical absorption coefficients of β-Ga_2O_3 in the deep ultraviolet region. The slightly red shift for $Fe_{GaII}V_{Ga}$, $Fe_{GaI}V_{Ga}$, $Fe_{GaII}O_i$, and $Fe_{GaI}O_i$ can be ascribed to hole doping, while the blue shift for the $Fe_{GaII}Ga_i$, $Fe_{GaI}Ga_i$ cases can be associated with the introduction of electrons, which is consistent with our formation energy calculations above. In addition, one can obviously notice that new peaks appear in the low-energy region for these Fe_{GaII}/Fe_{GaI} complexes, as shown in the amplified plots shown in Figure 5b,d.

The perfect β-Ga_2O_3 possesses an optical band gap of about 2 eV, which is in good agreement with the value observed from electronic structure calculations in Figure 1b. For the Fe_{GaII} and Fe_{GaI} cases, the optical absorption spectra remain almost unchanged in the visible region, which can be associated with the deep acceptor doping for the Fe foreigner atom. When introducing extra V_O into the β-Ga_2O_3 crystal, the absorption coefficients become relatively low for both $Fe_{GaII}V_O$ and $Fe_{GaI}V_O$ cases in the low-energy region (0–5 eV), whereas a new wide peak for $Fe_{GaII}V_{Ga}$ configuration is generated, leading to the optical migration from the ultraviolet light region to the visible-infrared region. The new peak for $Fe_{GaII}V_{Ga}$ configuration originated from the inter-band transitions of O 2p from the VBM to the induced impurity levels. Similarly, a new peak appears at a high energy level of ~1.42 eV and ~0.84 eV for $Fe_{GaII}Ga_i$ and $Fe_{GaI}Ga_i$ complexes, respectively, which are originated by the transitions from impurity levels to Ga 4s orbitals. These new peaks are expected to benefit the optical transformation from ultraviolet light to the visible-infrared region. In the low-energy region in Figure 5b,d, the $Fe_{GaII}O_i$ case exhibits the absence of a

clear optical absorption peak, while a few small oscillation peaks are present for the $Fe_{GaI}O_i$ combination. Therefore, $Fe_{GaII}Ga_i$, $Fe_{GaI}Ga_i$, and $Fe_{GaII}V_{Ga}$ complexes can significantly enhance the optical absorption in the visible-infrared region.
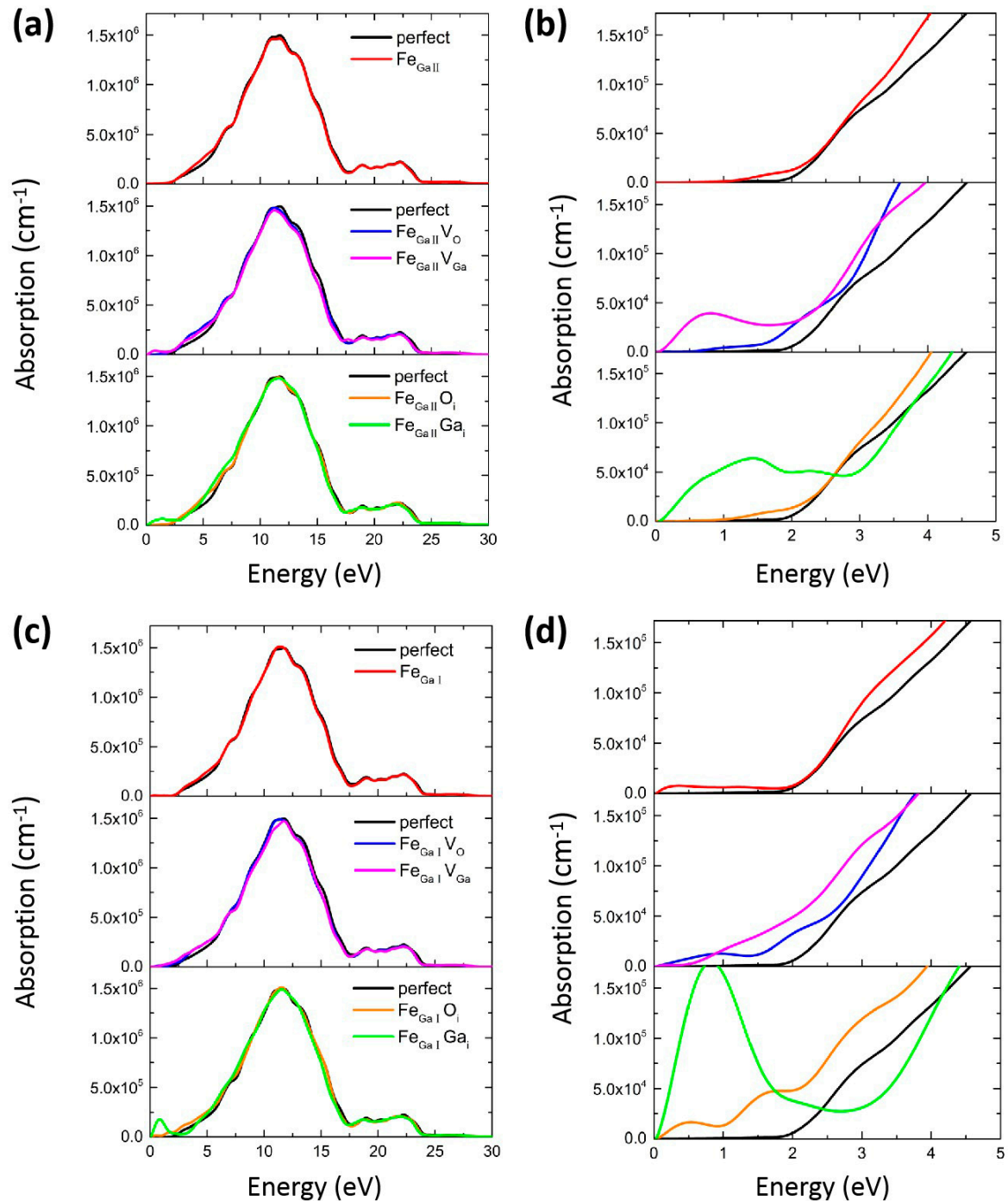

Figure 5. Comparison of the optical absorption spectra of perfect, Fe-doped, as well as various Fe_{GaII} and Fe_{GaI} complexes in energy range from 0–30 eV (**a**,**c**). Panels (**b**,**d**) show the corresponding amplified spectra at the low-energy region (0–5 eV).

The energy-loss function (ELF) is calculated based on Equation (9) from the dynamic dielectric constant at small scattering angles, which can determine the energy loss of free electrons across the material. This ELF function allows a direct comparison between theoretical conclusions and experimental spectroscopy measurements such as EELS [54].

Figure 6 shows the ELF spectra for $Fe_{Ga\text{II}}$ and $Fe_{Ga\text{I}}$ complexes. The major peak for perfect β-Ga_2O_3 is located at 16.7 eV. The peak positions remain at the same locations for $Fe_{Ga\text{II}}$ and $Fe_{Ga\text{I}}$, while accompanying with higher ELF value. This indicates that the induced Fe dopant tends to increase its energy loss and decreases its emission of peak energy efficiency under the high energy region in the material. The changes in the primary peaks for these $Fe_{Ga\text{II}}$ and $Fe_{Ga\text{I}}$ complexes are also minor, showing that the energy loss in the β-Ga_2O_3 material is almost negligible after the extra introduction of various native defects. Additionally, a seemingly little peak develops in the low-energy region for the $Fe_{Ga\text{I}}Ga_i$ case, which may be attributed to the optical absorption peak of ~0.84 eV in Figure 5d.
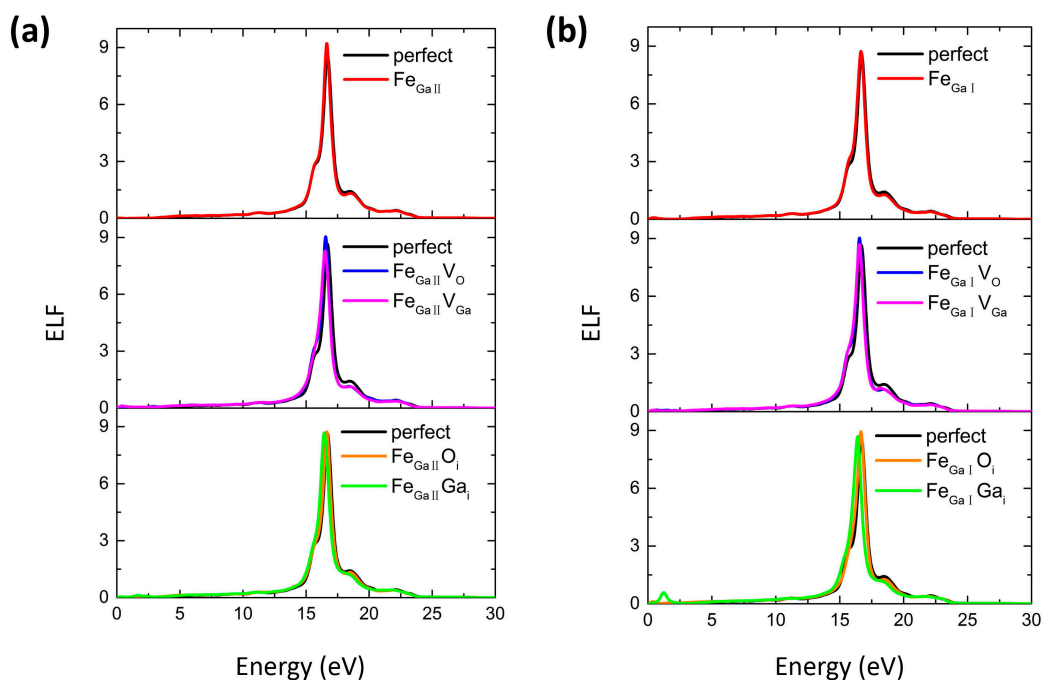
Figure 6. The energy-loss function (ELF) for (**a**) $Fe_{Ga\text{II}}$ and (**b**) $Fe_{Ga\text{I}}$ complexes.

3.3. GGA + U

We further carried out the GGA + U calculations to gain insight into the influences on the electronic structure of Fe-doped β-Ga_2O_3, considering the strong electron-electron interactions. GGA + U calculations are usually applied to deal with strong correlations in localized d- or f- electron systems and thus partially solve the band gap underestimation. We employ the values of U in the literature to accord with the experimental band-gap for the perfect β-Ga_2O_3 [33]. Besides, the U value of 4.09 eV has been chosen for the 3d orbital of the Fe dopant based on the literature [34].

The GGA + U calculated spin-up and spin-down band structures of the perfect β-Ga_2O_3 configuration are shown in Figure 7a,d. The perfect β-Ga_2O_3 is endowed with a band gap of 4.77 eV accompanied by a direct semiconductor structure, which is in good agreement with the experimental band-gap value of 4.78 eV [55]. The much flat valence bands illustrate a large effective mass and low mobility, which prevent the formation of p-type β-Ga_2O_3. The main orbital compositions of the VBM and CBM are consistent with those from GGA calculations, as mentioned before. Figure 7b,c,e,f show the spin-up and spin-down band structures of $Fe_{Ga\text{II}}$ and $Fe_{Ga\text{I}}$ structures, respectively, where the Fe impurity bands of 3d characters are located above the E_f near CBM. The $Fe_{Ga\text{II}}$ and $Fe_{Ga\text{I}}$ exhibit semiconductor ferromagnetic ground states. The magnetic moment mainly originates from the uncompensated spin-down orbitals of Fe impurities, where no extra band has been observed in the spin-up channel. In the spin-down channel, several isolated bands originated from Fe 3d orbitals are located above the E_f, which exhibit deep acceptor levels and give rise to a magnetic moment of 5 μ_B. The induced deep acceptor levels of Fe

3d orbitals are 0.63 eV lower than the CBM and 3.20 eV higher than the VBM in the Fe_{GaII} structure. For the Fe_{GaI} configuration, in the spin-down channel, several isolated bands originated from Fe 3d orbitals are located at 3.31 eV, 3.49 eV, 3.57 eV, 3.59 eV, and 3.70 eV above the E_f. The induced deep acceptor levels of Fe 3d orbitals are 1.09 eV lower than the CBM. The larger values below CBM compared with these of GGA calculations can be attributed to the more localized Ga and Fe 3d orbitals under GGA + U calculations, which are reasonable compared with the experimentally measured results, i.e., the EPR results of 0.84 eV observed from Polyakov et al. [26] and 1.2 eV from Bhandari et al. [22].
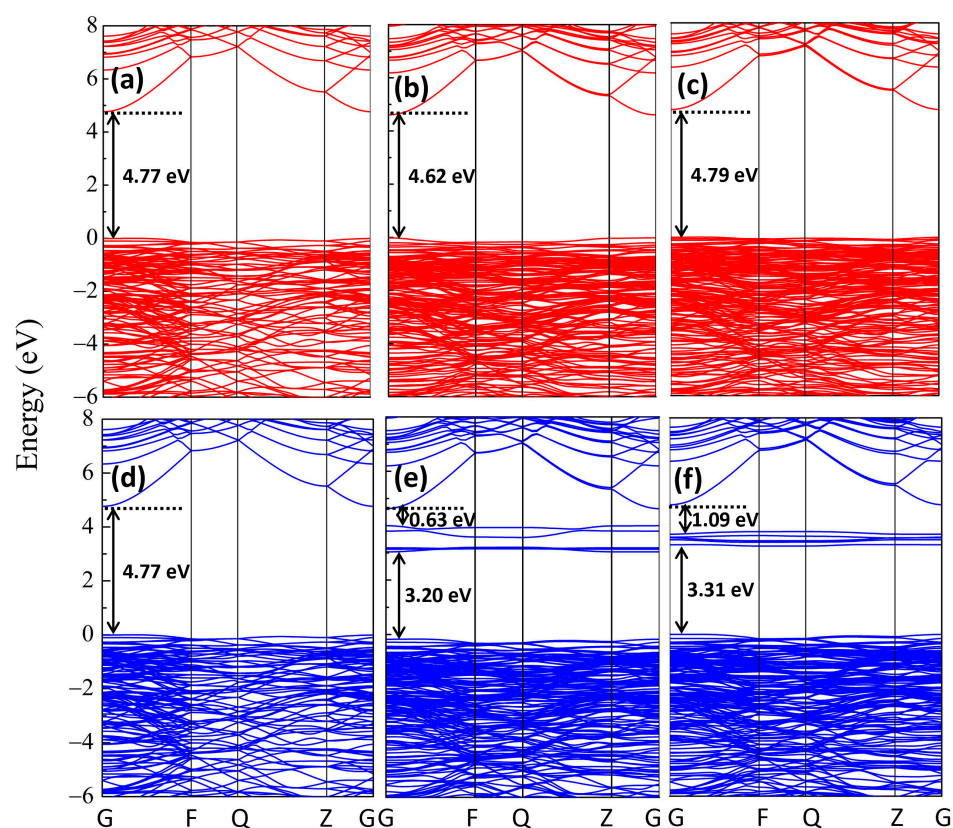
Figure 7. GGA + U calculated the band structures of (**a**) spin-up channel and (**d**) spin-down channel for perfect β-Ga_2O_3, (**b**) spin-up channel and (**e**) spin-down channel for Fe_{GaII} structure, as well as (**c**) spin-up channel and (**f**) spin-down channel for perfect Fe_{GaI} structure.

3.4. Conclusions

Based on first-principle DFT calculations with the GGA approach, we illustrate that Fe dopant is energetically favored for the octahedrally coordinated Ga site in Fe-doped Ga_2O_3 material. The controversy regarding the preferential Fe incorporation on the Ga site in the β-Ga_2O_3 crystal has been addressed; our result demonstrates that Fe dopant is energetically favored for the octahedrally coordinated Ga site, while analyses based on phonon dispersion mechanical characteristics, strain-dependent analyses, and formation energies are used to confirm the structural stability. Moreover, Fe impurities are more easily substituted for Ga sites under O-rich conditions. Our calculated results illustrate that the +3 charge state $Fe_{GaII}Ga_i$ under O-poor conditions and −2 charge state $Fe_{GaII}O_i$ under O-rich conditions are easily formed for the growth of β-Ga_2O_3 crystals. The formation energy calculations predict that the V_{Ga} and O_i in Fe-doped Ga_2O_3 are more likely to be formed under an O-rich growth environment. When the E_f approaches the valence and conduction band edges, the +3 charge state $Fe_{Ga}Ga_i$ and −2 charge state $Fe_{Ga}O_i$ are energetically advantageous, respectively. Moreover, V_O and Ga_i are expected under Ga-rich conditions with the preferred −4 charge sate $Fe_{Ga}Ga_i$ complex throughout the whole

band gap. $Fe_{Ga\Pi}Ga_i$, $Fe_{GaI}Ga_i$, and $Fe_{Ga\Pi}V_{Ga}$ complexes can significantly enhance the optical absorption in the visible-infrared region. The changes in the primary peaks for these $Fe_{Ga\Pi}$ and Fe_{GaI} complexes are all minor, showing that the energy loss in the β-Ga_2O_3 material is almost negligible after the introduction of various native defects. The GGA + U calculations show that the induced deep acceptor levels of Fe 3d orbitals are 0.63 eV and 1.09 eV lower than the CBM for $Fe_{Ga\Pi}$ and Fe_{GaI} configurations, respectively, which are reasonable compared with the experimentally measured results, i.e., the EPR results of 0.84 eV observed from Polyakov et al. [26] and 1.2 eV from Bhandari et al. [22].

References

1. Tang, R.; Li, G.; Li, C.; Li, J.; Zhang, Y.; Huang, K.; Ye, J.; Li, C.; Kang, J.Y.; Zhang, R.; et al. Localized surface plasmon enhanced Ga_2O_3 solar blind photodetectors. *Opt. Express* **2020**, *28*, 5731–5740. [CrossRef] [PubMed]
2. Jiang, Z.X.; Wu, Z.Y.; Ma, C.C.; Deng, J.N.; Zhang, H.; Xu, Y.; Ye, J.D.; Fang, Z.L.; Zhang, G.Q.; Kang, J.Y.; et al. P-type β-Ga_2O_3 metal-semiconductor-metal solar-blind photodetectors with extremely high responsivity and gain-bandwidth product. *Mater. Today Phys.* **2020**, *14*, 100226. [CrossRef]
3. Tadjer, M.J. Toward gallium oxide power electronics. *Science* **2022**, *378*, 724–725. [CrossRef] [PubMed]
4. Zhang, J.; Dong, P.; Dang, K.; Zhang, Y.; Yan, Q.; Xiang, H.; Su, J.; Liu, Z.; Si, M.; Gao, J.; et al. Ultra-wide bandgap semiconductor Ga_2O_3 power diodes. *Nat. Commun.* **2022**, *13*, 3900. [CrossRef] [PubMed]
5. Harada, T.; Ito, S.; Tsukazaki, A. Electric dipole effect in $PdCoO_2/β$-Ga_2O_3 Schottky diodes for high-temperature operation. *Sci. Adv.* **2019**, *5*, eaax5733. [CrossRef]
6. Harada, T.; Tsukazaki, A. Dynamic characteristics of $PdCoO_2/β$-Ga_2O_3 Schottky junctions. *Appl. Phys. Lett.* **2020**, *116*, 232104. [CrossRef]
7. Pang, R.; Teramura, K.; Morishita, M.; Asakura, H.; Hosokawa, S.; Tanaka, T. Enhanced CO evolution for photocatalytic conversion of CO_2 by H_2O over Ca modified Ga_2O_3. *Commun. Chem.* **2020**, *3*, 137. [CrossRef]
8. Kyrtsos, A.; Matsubara, M.; Bellotti, E. Migration mechanisms and diffusion barriers of vacancies in Ga_2O_3. *Phys. Rev. B* **2017**, *95*, 245202. [CrossRef]
9. Deák, P.; Ho, Q.D.; Seemann, F.; Aradi, B.; Lorke, M.; Frauenheim, T. Choosing the correct hybrid for defect calculations: A case study on intrinsic carrier trapping in β-Ga_2O_3. *Phys. Rev. B* **2017**, *95*, 075208. [CrossRef]
10. Varley, J.B.; Weber, J.R.; Janotti, A.; Van de Walle, C.G. Oxygen vacancies and donor impurities in β-Ga_2O_3. *Appl. Phys. Lett.* **2010**, *97*, 142106. [CrossRef]
11. Jiang, Q.; Meng, J.; Shi, Y.; Yin, Z.; Chen, J.; Zhang, J.; Wu, J.; Zhang, X. Electrical and optical properties of hydrogen plasma treated β-Ga_2O_3 thin films. *J. Semicond.* **2022**, *43*, 092802. [CrossRef]
12. Simon, J.; Protasenko, V.; Lian, C.; Xing, H.; Jena, D. Polarization-Induced Hole Doping in Wide-Band-Gap Uniaxial Semiconductor Heterostructures. *Science* **2010**, *327*, 60–64. [CrossRef] [PubMed]
13. Werner, P.; Casula, M.; Miyake, T.; Aryasetiawan, F.; Millis, A.J.; Biermann, S. Satellites and large doping and temperature dependence of electronic properties in hole-doped $BaFe_2As_2$. *Nat. Phys.* **2012**, *8*, 331–337. [CrossRef]
14. Zeng, H.; Wu, M.; Wang, H.Q.; Zheng, J.C.; Kang, J.Y. Tuning the Magnetism in Boron-Doped Strontium Titanate. *Materials* **2020**, *13*, 5686. [CrossRef] [PubMed]
15. Euvrard, J.; Yan, Y.; Mitzi, D.B. Electrical doping in halide perovskites. *Nat. Rev. Mater.* **2021**, *6*, 531–549. [CrossRef]
16. Zeng, H.; Wu, M.; Wang, H.Q.; Zheng, J.C.; Kang, J.Y. Tuning the magnetic and electronic properties of strontium titanate by carbon doping. *Front. Phys.* **2021**, *16*, 43501. [CrossRef]

17. Lenyk, C.A.; Gustafson, T.D.; Halliburton, L.E.; Giles, N.C. Deep donors and acceptors in β-Ga$_2$O$_3$ crystals Determination of the Fe$^{2+/3+}$ level by a noncontact method. *J. Appl. Phys.* **2019**, *126*, 245701. [CrossRef]

18. Gunsser, W.; Rohwer, K. Determination of the correlation between the crystal field axis system and the crystallographic axes in chromium-doped β-Ga$_2$O$_3$ by EPR. *Phys. Status Solidi B* **1983**, *116*, 275–278. [CrossRef]

19. Zhang, N.; Liu, H.; Sai, Q.; Shao, C.; Xia, C.; Wan, L.; Feng, Z.C.; Mohamed, H.F. Structural and electronic characteristics of Fe-doped β-Ga$_2$O$_3$ single crystals and the annealing effects. *J. Mater. Sci.* **2021**, *56*, 13178–13189. [CrossRef]

20. Tbooster, J.M.; Dymanus, A. Mossbauer Mössbauer effect in Ga$_{2-x}$Fe$_x$O$_3$ and related compounds. *Phys. Status Solidi B* **1967**, *24*, 487–499. [CrossRef]

21. Büscher, R.; Lehmann, G. Correlation of zero-field splittings and site distortions. IX. Fe^{3+} and Cr^{3+} in β-Ga$_2$O$_3$. Z. *Naturforsch. A* **1987**, *42*, 67–71. [CrossRef]

22. Bhandari, S.; Zvanut, M.E.; Varley, J.B. Optical absorption of Fe in doped Ga$_2$O$_3$. *J. Appl. Phys.* **2019**, *126*, 165703. [CrossRef]

23. Zhou, L.; Chen, L.; Ruan, J.; Lu, X.; Liu, B.; Gao, R.; Li, Y.; Geng, L.; Ouyang, X. Pulsed X-ray detector based on Fe doped β-Ga$_2$O$_3$ single crystal. *J. Phys. D Appl. Phys.* **2021**, *54*, 274001. [CrossRef]

24. Hany, I.; Yang, G.; Zhou, C.E.; Sun, C.; Gundogdu, K.; Seyitliyev, D.; Danilov, E.O.; Castellano, F.N.; Sun, D.; Vetter, E. Low temperature cathodoluminescence study of Fe-doped β-Ga$_2$O$_3$. *Mater. Lett.* **2019**, *257*, 126744. [CrossRef]

25. Ingebrigtsen, M.E.; Varley, J.B.; Kuznetsov, A.Y.; Svensson, B.G.; Alfieri, G.; Mihaila, A.; Badstübner, U.; Vines, L. Iron and intrinsic deep level states in Ga$_2$O$_3$. *Appl. Phys. Lett.* **2018**, *112*, 04210. [CrossRef]

26. Polyakov, A.Y.; Smirnov, N.B.; Schemerov, I.V.; Chernykh, A.V.; Yakimov, E.B.; Kochkova, A.I.; Tereshchenko, A.N.; Pearton, S.J. Electrical Properties, Deep Levels and Luminescence Related to Fe in Bulk Semi-Insulating β-Ga$_2$O$_3$ Doped with Fe. *ECS J. Solid State Sci. Technol.* **2019**, *8*, Q3091–Q3096. [CrossRef]

27. Kresse, G.; Furthmuller, J. Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set. *Comp. Mater. Sci.* **1996**, *6*, 15–50. [CrossRef]

28. Kresse, G.; Furthmuller, J. Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set. *Phys. Rev. B* **1996**, *54*, 169–186. [CrossRef]

29. Kohn, W.; Sham, L.J. Self-Consistent Equations Including Exchange and Correlation Effects. *Phys. Rev.* **1965**, *140*, A1133–A1138. [CrossRef]

30. Perdew, J.P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868. [CrossRef]

31. Dong, L.; Jia, R.; Li, C.; Xin, B.; Zhang, Y. Ab initio study of N-doped β-Ga$_2$O$_3$ with intrinsic defects: The structural, electronic and optical properties. *J. Alloys Compd.* **2017**, *712*, 379–385. [CrossRef]

32. Zacherle, T.; Schmidt, P.C.; Martin, M. Ab initio calculations on the defect structure of β-Ga$_2$O$_3$. *Phys. Rev. B* **2013**, *87*, 235206. [CrossRef]

33. Dong, L.; Jia, R.; Xin, B.; Peng, B.; Zhang, Y. Effects of oxygen vacancies on the structural and optical properties of β-Ga$_2$O$_3$. *Sci. Rep.* **2017**, *7*, 40160. [CrossRef] [PubMed]

34. Muratahan, A.; Wolverton, C. Local environment dependent GGA + Umethod for accurate thermochemistry of transition metal compounds. *Phys. Rev. B* **2014**, *90*, 115105.

35. Momma, K.; Izumi, F. VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Cryst.* **2011**, *4*, 1272–1276. [CrossRef]

36. Goyal, A.; Gorai, P.; Peng, H.; Lany, S.; Stevanović, V. A computational framework for automation of point defect calculations. *Comput. Mater. Sci.* **2017**, *130*, 1–9. [CrossRef]

37. Kobayashi, T.; Gake, T.; Kumagai, Y.; Oba, F.; Matsushita, Y.-I. Energetics and electronic structure of native point defects in α-Ga$_2$O$_3$. *Appl. Phys. Express* **2019**, *12*, 091001. [CrossRef]

38. Wang, V.; Xu, N.; Liu, J.-C.; Tang, G.; Geng, W.-T. VASPKIT: A user-friendly interface facilitating high-throughput computing and analysis using VASP code. *Comput. Phys. Commun.* **2021**, *267*, 108033. [CrossRef]

39. Sun, D.; Gao, Y.; Xue, J.; Zhao, J. Defect stability and electronic structure of doped β-Ga$_2$O$_3$: A comprehensive ab initio study. *J. Alloys Compd.* **2019**, *794*, 374–384. [CrossRef]

40. Mondal, A.K.; Mohamed, M.A.; Ping, L.K.; Mohamad Taib, M.F.; Samat, M.H.; Mohammad Haniff, M.A.S.; Bahru, R. First-principles studies for electronic structure and optical properties of p-type calcium doped α-Ga$_2$O$_3$. *Materials* **2021**, *14*, 604. [CrossRef]

41. Kean Ping, L.; Mohamed, M.A.; Kumar Mondal, A.; Mohamad Taib, M.F.; Samat, M.H.; Berhanuddin, D.D.; Menon, P.S.; Bahru, R. First-Principles Studies for Electronic Structure and Optical Properties of Strontium Doped β-Ga$_2$O$_3$. *Micromachines* **2021**, *12*, 348. [CrossRef] [PubMed]

42. Usseinov, A.; Platonenko, A.; Koishybayeva, Z.; Akilbekov, A.; Zdorovets, M.; Popov, A.I. Pair vacancy defects in β-Ga$_2$O$_3$ crystal: Ab initio study. *Opt. Mater. X* **2022**, *16*, 100200. [CrossRef]

43. Mykhaylyk, V.B.; Kraus, H.; Kapustianyk, V.; Rudko, M. Low temperature scintillation properties of Ga$_2$O$_3$. *Appl. Phys. Lett.* **2019**, *115*, 081103. [CrossRef]

44. Yan, H.; Guo, Y.; Song, Q.; Chen, Y.; Shi, Y. Electronic Structure and Magnetic Interactions in Ti-Doped and Ti-V$_O$-Co-Doped β-Ga$_2$O$_3$ from First-Principles Calculations. *J. Supercond. Nov. Magn.* **2016**, *29*, 2607–2613. [CrossRef]

45. Ao, L.; Pham, A.; Xiang, X.; Li, S.; Zu, X. Defect induced charge trapping in C-doped α-Al$_2$O$_3$. *J. Appl. Phys.* **2017**, *122*, 025702. [CrossRef]

46. Goyal, A.; Gorai, P.; Toberer, E.S.; Stevanović, V. First-principles calculation of intrinsic defect chemistry and self-doping in PbTe. *NPJ Comput. Mater.* **2017**, *3*, 42. [CrossRef]

47. Wu, Z.-j.; Zhao, E.-j.; Xiang, H.-p.; Hao, X.-f.; Liu, X.-j.; Meng, J. Crystal structures and elastic properties of superhard IrN$_2$ and IrN$_3$ from first principles. *Phys. Rev. B* **2007**, *76*, 054115. [CrossRef]

48. Osipov, A.V.; Grashchenko, A.S.; Kukushkin, S.A.; Nikolaev, V.I.; Osipova, E.V.; Pechnikov, A.I.; Soshnikov, I.P. Structural and elastoplastic properties of β-Ga$_2$O$_3$ films grown on hybrid SiC/Si substrates. *Contin. Mech. Thermodyn.* **2018**, *30*, 1059–1068. [CrossRef]

49. Usseinov, A.; Koishybayeva, Z.; Platonenko, A.; Pankratov, V.; Suchikova, Y.; Akilbekov, A.; Zdorovets, M.; Purans, J.; Popov, A.I. Vacancy Defects in Ga$_2$O$_3$: First-Principles Calculations of Electronic Structure. *Materials* **2021**, *14*, 7384. [CrossRef]

50. Miller, W.; Böttcher, K.; Galazka, Z.; Schreuer, J. Numerical Modelling of the Czochralski Growth of β-Ga$_2$O$_3$. *Crystals* **2017**, *7*, 26. [CrossRef]

51. Wei, Y.; Wang, T.; Zhang, Y.; Qi, C.; Luan, J.; Ma, G.; Tsai, H.-S.; Liu, C.; Huo, M. Effects of carbon related defects on opto-electronic properties of β-Ga$_2$O$_3$: The first principle calculation. *J. Appl. Phys.* **2020**, *17*, 103060. [CrossRef]

52. Yan, H.; Guo, Y.; Song, Q.; Chen, Y. First-principles study on electronic structure and optical properties of Cu-doped β-Ga$_2$O$_3$. *Phys. B* **2014**, *434*, 181–184. [CrossRef]

53. Pan, Y. First-principles investigation of the influence of point defect on the electronic and optical properties of α-Ga$_2$O$_3$. *Int. J. Energy Res.* **2022**, *46*, 13070–13078. [CrossRef]

54. He, H.; Orlando, R.; Blanco, M.A.; Pandey, R.; Amzallag, E.; Baraille, I.; Rérat, M. First-principles study of the structural, electronic, and optical properties of Ga$_2$O$_3$ in its monoclinic and hexagonal phases. *Phys. Rev. B* **2006**, *74*, 195123. [CrossRef]

55. Zachinskis, A.; Grechenkov, J.; Butanovs, E.; Platonenko, A.; Piskunov, S.; Popov, A.I.; Purans, J.; Bocharov, D. Ir impurities in α- and β-Ga$_2$O$_3$ and their detrimental effect on p-type conductivity. *Sci. Rep.* **2023**, *13*, 8522. [CrossRef]