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Top-Down Design Method of a Time Domain Accelerometer with Adjustable Resolution

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Abstract: A top-down design methodology and implementation of a time domain sensor is presented in this paper. The acceleration resolution of the time domain sensor is equal to the time-measurement accuracy divided by the sensor sensitivity. Combined with the sensitivity formula, the acceleration resolution is proportional to the vibration amplitude, the time-measurement accuracy, and the third power of the resonant frequency. According to the available time-measurement accuracy and the desired acceleration resolution, the parameters including the vibration amplitude and the resonant frequency were theoretically calculated. The geometrical configuration of the time domain sensor device was designed based on the calculated parameters. Then, the designed device was fabricated based on a standard silicon-on-insulator process and a matched interface circuit was developed for the fabricated device. Experimental results demonstrated that the design methodology is effective and feasible. Moreover, the implemented sensor works well. In addition, the acceleration resolution can be tuned by adjusting the time-measurement accuracy and the vibration amplitude. All the reported results of this work can be expanded to other time domain inertial sensors, e.g., a gyroscope or tilt sensor.

Keywords: MEMS; inertial sensor; accelerometer; time domain measurement; design methodology; adjustable acceleration resolution



Citation: Li, E.; Jian, J. Top-Down Design Method of a Time Domain Accelerometer with Adjustable Resolution. *Micromachines* **2024**, *15*, 635. https://doi.org/10.3390/ mi15050635

Academic Editor: Ha Duong Ngo

Received: 9 March 2024 Revised: 28 April 2024 Accepted: 2 May 2024 Published: 9 May 2024



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1. Introduction

Microelectromechanical system (MEMS) accelerometers have gained widespread use in the consumer electronics and automobile industries and geophysical exploration due to their advantages of low cost, small size, light weight, and low power (CSWaP) [1–5]. The first MEMS accelerometer, a piezoresistive sensor, was developed by L. M. Roylance and J. B. Angel at Stanford University in 1979 [6]. Since then, researchers have developed various types of accelerometers based on different sensing mechanisms, including piezoelectric [7], resonant [8], mode-localized [9,10], tunneling [11], capacitive [12], etc. Piezoresistive accelerometers offer a measuring technique (widely using piezoresistive bridges) and exhibit good linearity and a wide dynamic response range. However, these sensors are sensitive to temperature variations, necessitating the implementation of temperature-compensation mechanisms [13]. Piezoelectric accelerometers demonstrate good linearity and a wide dynamic response range, but are not suitable for low-frequency or static measurements [14]. Resonant accelerometers provide excellent stability, high accuracy, and strong resistance to interference. However, they have a limited frequency response range [15,16]. Modelocalized accelerometers utilize the energy confinement of mode localization to enhance accuracy, with relative sensitivity to amplitude ratio 302 times higher than the resonance frequency shift [17]. Despite this improvement in accuracy, mode-localized accelerometers suffer from poor stability in amplitude ratio output, limiting their use in high-accuracy fields. Among these sensing mechanisms, capacitive accelerometers have emerged as a research hotspot and have gained favor in the commercial industry [18–20]. The state-ofthe-art resolution of capacitive sensors is currently around 0.44 µg [21] according to the

published literature. However, further improvements in the accuracy of capacitive sensors are challenging [21,22].

A time domain acceleration-sensing mechanism that converts acceleration perturbation into changes in time intervals was theoretically proposed by Space and Naval Warfare Systems Center Pacific (SSC Pacific). This sensing mechanism theoretically has the great potential to achieve a detection limit of $\sim 10^{-13}$ g [23,24] because the state-of-the-art time accuracy arrives at the level of 10^{-18} s [25]. A theoretical implementation method based on tunneling electrodes was also presented by SSC Pacific [26]. Based on the implementation method, some theoretical works have been reported, mainly focusing on the apparatus and appliance of in-plane inertial devices [27], the intelligent polynomial curve fitting method for inertial devices [28], modeling gyroscope devices, and the angular random walk estimation method for gyroscopes [29]. However, none of the time sensors were developed, due to the methods being hard to implement. As a result, the theoretical results have not been experimentally verified.

Since then, the literature with respect to time domain sensors has been seldom published except by our research group. In our previous works, several novel characteristics of time domain accelerometers have been identified and verified utilizing a self-developed sensor based on a standard silicon-on-insulator process. First, a virtual time domain accelerometer array using a single device was built [30]. Multiple acceleration measurements could be simultaneously performed using the built virtual time domain sensor array. The accuracy was improved by combining all the measurements. Second, the time domain sensor has the ability to measure acceleration perturbation during the process of attenuation vibration [24]. Third, two sensitivities exist in the time domain sensors, which can be enhanced by decreasing the amplitude and frequency [23].

However, the design method of time domain sensors and their new characteristics have seldom been reported in the published literature to data. In this paper, a top-down design methodology for a time domain sensor device is proposed. Based on this methodology, the structural topology of a self-developed sensor device was designed step by step and the parameters were optimized. In addition, a corresponding detection method was developed. Finally, utilizing the developed sensor device and the detection method, the time domain sensor with adjustable resolution was experimentally verified.

The rest of this paper is organized as follows. In Section 2, the adjustable resolution of the time domain accelerometer is theoretically analyzed. The design and fabrication of the time domain accelerometer device is presented in Section 3. In Section 4, the detection method of the developed time domain sensor is described. Measurement results and discussion are presented in Section 5. The final conclusions are summarized in Section 6.

2. Adjustable Resolution of Time Domain Accelerometer

The acceleration resolution caused by the time-measurement accuracy is equal to the ratio of the time-measurement accuracy Δt divided by the sensitivity S of the time domain sensor. Therefore, the acceleration resolution can be expressed by

$$\Delta a = \frac{\Delta t}{S} \tag{1}$$

where the sensitivity can be expressed by [23]

$$S \propto \frac{2}{A\omega^3} \tag{2}$$

where A and ω denote the vibration amplitude and resonant frequency of the time domain sensor, respectively. Submitting Equation (2) into Equation (1), the acceleration resolution can be rewritten as:

$$\Delta a \propto A\omega^3 \Delta t \tag{3}$$

It can be seen from Equation (3) that the acceleration resolution is proportional to the vibration amplitude, the third power of the resonant frequency, and the time-measurement accuracy. Therefore, Equation (3) is a theoretical foundation for designing a time domain sensor with adjustable resolution.

3. Design and Fabrication of a Time Domain Accelerometer Device with Adjustable Resolution

3.1. Design of a Time Domain Accelerometer Device

3.1.1. Overall Design

The model of the time domain accelerometer is equivalent to a forced vibration of a mass–spring–damper single-freedom system, where the mass denotes inertial proof mass, the spring denotes elastic beam, and the damper refers to energy loss during the processing of microstructure motion. In addition, a set of (two) displacement reference points (DRPs) is necessary for implementing a time domain sensor, where the DRPs are used for generating the trigger events when the proof mass passes through them. Then, the acceleration is calculated through measuring the time intervals between the corresponding trigger events.

According to the model of the time domain sensor, the proposed senor device is shown in Figure 1. The harmonically oscillating proof mass is suspended by the four symmetrical elastic beams and is driven by an electrostatic force generated via area-varying drive capacitors. In addition, the amplitude of the proof mass can be adjusted by changing the drive voltage on the drive capacitors. The gap-varying sense capacitors, combined with a corresponding capacitance-to-voltage (C–V) interface circuit and a self-developed data post-processing algorithm, are utilized for defining the DRPs, generating the trigger events, measuring the time intervals, and further calculating applied acceleration perturbation.

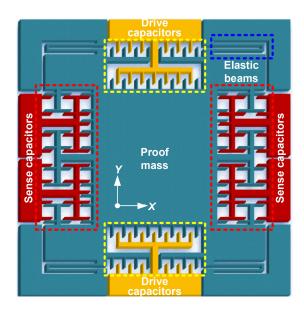


Figure 1. Schematic diagram of the proposed time domain accelerometer device.

When an inertial acceleration perturbation is applied in the Y-axis positive direction, the proof mass moves in the negative direction along the Y axis (Figure 1). The oscillation trajectory of the time domain sensor with acceleration perturbation is shown in Figure 2a. The data points (represented by the blue dots) on the oscillation trajectory denote the proof mass displacements relative to the rest position. The position relationships between the proof mass and the two preset DRPs at different times are illustrated in Figure 2b. The proof mass starts with the lowest position at time t_0 and then moves up to the DRP X_1 at time t_1 and the DRP X_2 at time t_2 . It reaches the highest position at time t_{\max} and then moves down to the DRP X_2 at time t_3 and the DRP X_1 at time t_4 . The proof mass returns to its original position at time t_{\min} . After that, it moves to the DRP X_1 again at time t_5 and

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continues this periodic repetitive motion. In a period, the time intervals ΔT_1 , ΔT_2 , and ΔT can be measured by the obtained five times t_1 , t_2 , t_3 , t_4 , and t_5 . Finally, the acceleration can be calculated from the measured ΔT_1 , ΔT_2 , and ΔT via the function $a = f(\Delta T_1, \Delta T_2, \Delta T)$.

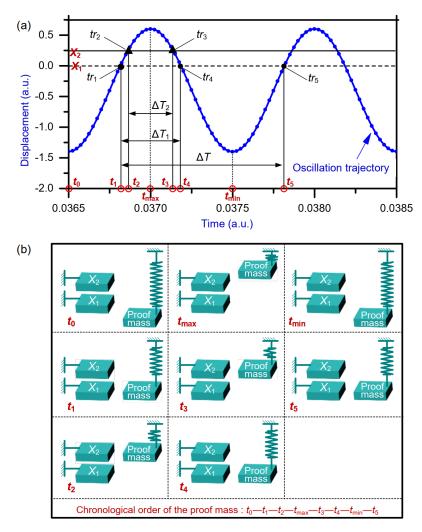


Figure 2. Schematic diagram: (a) time interval measurements, (b) position relationships between the proof mass and the DRPs at different times.

In this work, for acquiring these five time measurements and finally calculating the acceleration, the displacement of the proof mass is converted into measurable voltage. Because the movable electrodes of the sense capacitors are rigidly connected with the proof mass, they experience the same displacement as the proof mass (Figure 1). Therefore, the displacement of the proof mass caused by the acceleration perturbation is first converted into the change in capacitance. Then, the change in capacitance is converted into that in voltage by the aforementioned C–V interface circuit. As a result, a function relationship between the displacement and voltage is built. The displacement is represented by the output voltage. Correspondingly, the DRPs can be represented by the VRPs.

The National Instruments serial data acquisition (DAQ) system [31] is used to sample voltage signal from the C–V interface circuit. The sampling rate can be up to 2.5 million samples per second (MSPS). Correspondingly, the highest time-measurement accuracy (reciprocal of MSPS) is 400 ns. Thereinto, the time-measurement accuracy is adjustable through varying the sampling rate. Based on our experience from standard silicon-on-insulator processes, the resonance frequency of the developed sensor device should be larger than or equal to 1.2 kHz, in case the proof adheres to the handle layer. The desired acceleration resolution is ~5 mg. According to Equation (3), the maximum vibration

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amplitude of the time domain sensor is ~584 nm. The size of the device was designed to be 3.5 mm \times 4 mm and the sensing mass 1.8×10^{-7} kg. The overall parameters are listed in Table 1. Based on the parameters, the elastic beam, driving structure, and sensor structure were designed as follows.

Table 1. Overall	parameters of the	e designed time	domain acce	lerometer.

Parameters	Value	
Desired acceleration resolution	~5 mg	
Resonant frequency	1.2 kHz	
Maximum vibration amplitude	584 nm	
Highest time-measurement accuracy	400 ns	
Size	$3.5 \text{ mm} \times 4 \text{ mm}$	
Sensing mass	$1.8 imes 10^{-7} ext{ kg}$	

It should be noted that if some parameters of Equation (3) are constrained, the remaining ones can be calculated and optimized. Then, the corresponding parameters of the sensor device and detection circuit can be calculated and designed.

3.1.2. Elastic Beam

According to the resonant frequency f of 1.2 kHz and the sensing mass m of ~1.8 \times 10⁻⁷ kg (Table 1), the stiffness coefficient K of the elastic beam is ~10 N/m ($f = \sqrt{K/m}/2\pi$). There are various types of elastic beams, including folded elastic beam, L-shaped elastic beam, U-shaped elastic beam, serpentine elastic beam, and so on. Among them, the U-shaped elastic beam (Figure 3) was chosen due to the advantages of low stiffness coefficient in detection mode and good residual stress release [32].

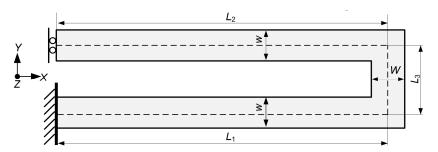


Figure 3. U-shaped elastic beam of this work.

The stiffness coefficients of the U-shaped elastic beam in X, Y, and Z direction, i.e., K_x , K_y , and K_z can be expressed via Equation (4) [32]:

$$K_x = \frac{EtwW^3}{2L_1W^3 + L_3^3w}, K_y = \frac{Etw^3W}{L_3w^3 + 2L_1^3W}, K_z = \frac{Et^3wW}{2L_1^3W + L_3^3w}$$
 (4)

In Equation (4), w and W denote the width of the beam while L_1 , L_2 , and L_3 denote the length of the beam, as shown in Figure 3. t denotes the height of the beam in the Z direction. Some parameters of the U-shaped elastic beam are constrained: $W=30~\mu m$; $L_3=30~\mu m$; $L_1/w=L_2/w=20\sim100$. According to Equation (4), the dependence of the stiffness coefficient in the Y direction on the aspect ratio L_1/w is displayed in Figure 4. As can be seen from Figure 4, the stiffness coefficient is 10~N/m when the aspect ratio is ~65 . In this work, the aspect ratio was taken as 70 for convenient design. For reducing the lateral interference, the ratio of the stiffness coefficients between the non-sensitive direction and sensitive direction should be kept to at least 10-fold. According to Equation (4), when the beam width w is equal to $10~\mu m$, the ratio of the stiffness coefficients of the X direction to the Y direction is ~5000 and the ratio of the stiffness coefficients of the Z direction to the Y

direction is ~10. The geometrical parameters of the designed U-shaped elastic beam are listed in Table 2.

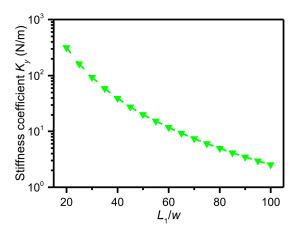


Figure 4. Dependence of the stiffness coefficient in the Y direction on the aspect ratio L_1/w .

Table 2. Geometrical parameters of the designed U-shaped elastic beam.

Parameters	Value (μm)
L_1	700
L_2	700
L_3	30
w	10
W	30
t	30

3.1.3. Electrostatic Driving Structure

Area-varying capacitors are used as the electrostatic driving structure (Figure 5). When there is no applied acceleration perturbation, the movable combs, being fixedly connected to the proof mass, are located in the middle of the fixed combs. When there is an applied acceleration perturbation, the gap d_{d0} remains unchanged while the overlapping length l_d changes.

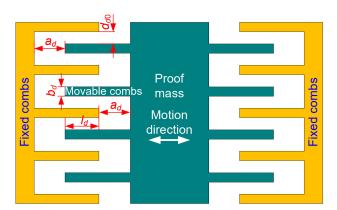


Figure 5. Schematic diagram of driving structure.

When the proof mass shifts with a displacement caused by an acceleration perturbation in the sensing direction, the differential of the drive capacitance (Figure 5) to the displacement can be expressed as:

$$\frac{\partial C_d}{\partial y} = 2n_d \varepsilon \frac{h_d}{d_{d0}} + (2n+1)\varepsilon \frac{b_d h_d}{a_d^2} \tag{5}$$

where n_d denotes the number of combs, h_d refers to the height of the combs, and b_d denotes the width of the combs. The first term of Equation (5) is a constant while the second term varies with the changing a_d . Thus, the second term brings a nonlinearity to $\partial C_d/\partial y$. The ratio of the second term to the first term, i.e., the nonlinearity, is given as:

$$R = \frac{(2n+1)\varepsilon \frac{b_d h_d}{a_d^2}}{2n\varepsilon \frac{h_d}{d_{d0}}} \approx \frac{b_d d_{d0}}{a_d^2}$$
 (6)

As can be seen from Equation (6), the ratio is proportional to the comb width b_d and the gap d_{d0} and inversely proportion to gap a_d^2 . Some parameters of the drive capacitors are constrained: $b_d=5~\mu m$; $l_d=40~\mu m$; $d_{d0}=2.5~\mu m$. The nonlinearity decreases while the gap a_d increases. However, increasing the gap a_d reduces the driving capacitance. Therefore, in this work, the nonlinearity is limited to less than 2%. The dependence of the nonlinearity on the gap a_d is displayed in Figure 6. When the gap a_d is greater than or equal to 25 μm , the nonlinearity R is less than 2%. As a result, the gap a_d of 25 μm was chosen. The geometrical parameters of the designed driving structure are listed in Table 3.

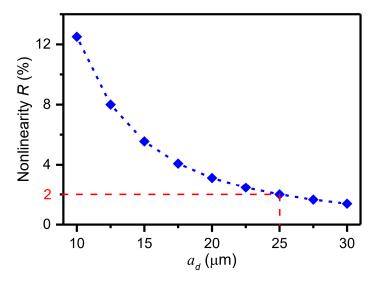


Figure 6. Dependence of the nonlinearity on the gap a_d .

Table 3. Geometrical parameters of the designed driving structure.

Parameters	Value (μm)
b_d	5
$l_d^{\cdot \cdot}$	40
d_{d0}	2.5
a_d	25

3.1.4. Detection Structure of the Oscillation Trajectory of the Proof Mass

Gap-varying capacitors (Figure 7) are used for the detection structure of the oscillation trajectory of the proof mass. When there is no applied acceleration perturbation, the movable combs, being fixedly connected to the proof mass, are located in the middle of the fixed combs. When there is an applied acceleration perturbation, the overlapping length l_s remains unchanged while the gaps d_1 and d_2 change. The detection structure converts the proof mass displacement into detectable capacitance, which is necessary for representing DRPs, measuring time intervals, and further calculating acceleration.

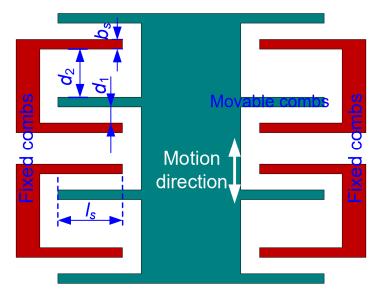


Figure 7. Schematic diagram of detection structure based on sense capacitors.

The ratio of d_1 to d_2 is defined as a variable η . Based on the parameters (Figure 7), the detection capacitance ΔC can be expressed as:

$$\Delta C = n\varepsilon lh_s \left(\frac{1}{d_1 - \Delta y} + \frac{1}{d_2 + \Delta y} \right) - n\varepsilon lh_s \left(\frac{1}{d_1 + \Delta y} + \frac{1}{d_2 - \Delta y} \right)
= \frac{2n\varepsilon lh_s}{d_1} \left(1 - \frac{1}{\eta^2} \right) \left[\frac{\Delta y}{d_1} + \left(\frac{\Delta y}{d_1} \right)^3 + \left(\frac{\Delta y}{d_1} \right)^5 + \cdots \right]$$
(7)

In the Equation (7), the part containing the first-order term of $\Delta y/d_1$ represents the linear capacitance variation. The other part containing the high-order terms of $\Delta y/d_1$ represents nonlinear capacitance variation. In this work, the nonlinearity is limited to less than 5%. Some parameters of the sense capacitors are constrained: $b_s=6$ µm; $l_s=60$ µm; $d_1=2.5$ µm. The dependence of the linear capacitance variation on the ratio η is displayed in Figure 8. When the ratio η is equal to 3, the linear capacitance variation reaches a maximum. Moreover, when the displacement Δy is less than 540 µm, the nonlinearity of the capacitance variation is less than 5% (Equation (7)). The resulting geometrical parameters of the designed detection structure are listed in Table 4.

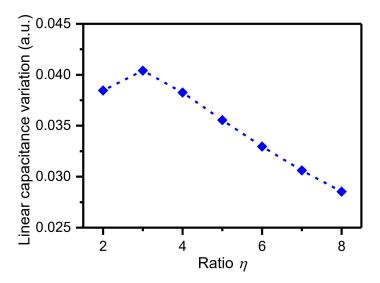


Figure 8. Dependence of the linear capacitance variation on the ratio η .

Table 4. Geometrical	parameters of the	e designed (detection structure.

Parameters	Value (µm)		
d_1	2.5		
d_2	7.5		
η	3		
l_3	60		
$b_{\scriptscriptstyle S}$	6		

3.2. Fabrication of Time Domain Sensor Device Using One Photomask

Based on the designed geometrical parameters described in Part 3.1, the device was fabricated using a typical silicon-on-insulator (SOI) process, as illustrated in Figure 9 [23]. The thickness of the device layer, handle layer, and oxide layer was 30, 400, and 4 μm , respectively (Figure 4a). The fabrication process involved steps such as spin coating of photoresist (b), patterning (c), deep reactive-ion etching (DRIE) (d), notching (e), removing the photoresist (f), dicing (g), and releasing the structure using dry HF (h). In the whole process, only one photomask was used. After the DRIE, the step of notching was employed for the purpose of rapidly releasing device layer. At the same time, the oxide layer below the anchors prevented over-etching. The SEM image is shown in Figure 10. The schematic diagram of wire bonding and the packaged sensor device is shown in Figure 11.

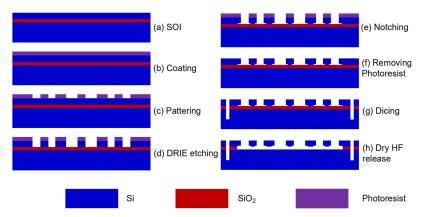


Figure 9. SOI fabrication process of the sensor device [23].

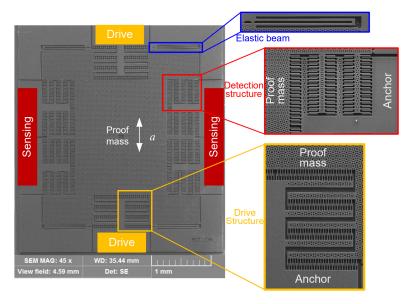


Figure 10. SEM image and close-up of the fabricated sensor device [23,24,30].

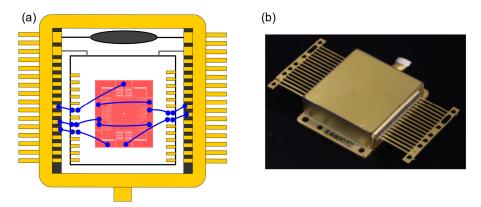


Figure 11. Schematic diagram of wire bonding (a) and the packaged device (b).

4. Detection Method of Developed Time Domain Acceleration Sensor

Based on the fabricated sensor device, an acceleration detection method is proposed. The detection method consists of a push–pull electrostatic drive circuit, detection circuit for the oscillation trajectory of the proof mass, and time-interval measurement based on data post-processing. The push–pull electrostatic drive is used to actuate the proof mass under a resonant state. The detection of the oscillation trajectory converts the displacement of the proof mass into a voltage. As a result, a functional relationship is built between the displacement and the voltage. The DRPs are indirectly characterized by the VRPs. The data post-processing method is used to judge the times when the proof mass passes the DRPs, extract the corresponding time intervals, and calculate the acceleration perturbation.

4.1. Push-Pull Electrostatic Drive Circuit

As shown in Figure 12, area-varying capacitors serve as differential drive electrodes. An AC drive voltage with a DC bias voltage is applied to the drive electrodes, where the DC bias voltages are equal in magnitude but opposite in direction. In addition, a high-frequency sinusoidal carrier wave is applied to the proof mass. Typically, the frequency of the carrier wave is about three orders higher than that of the AC drive signal. There is a potential difference between the movable combs fixed to the proof mass and the fixed combs connected to the drive electrodes, forming a normal electrostatic force (perpendicular to the direction of motion) and a tangential electrostatic force (along the direction of motion). The tangential electrostatic force provides the driving force while the normal electrostatic forces cancel each other. The tangential electrostatic force is given as:

$$F_{d} = \frac{1}{2} \frac{\partial C_{d}}{\partial y} (V_{a} \sin \omega_{d} t + V_{d} - V_{0} \sin \omega_{m} t)^{2} - \frac{1}{2} \frac{\partial C_{d}}{\partial y} (V_{a} \sin \omega_{d} t - V_{d} - V_{0} \sin \omega_{m} t)^{2}$$

$$= \frac{1}{2} \frac{\partial C_{d}}{\partial y} \left[(V_{a} \sin \omega_{d} t + V_{d})^{2} - (V_{a} \sin \omega_{d} t - V_{d})^{2} + 2V_{0} \sin \omega_{m} t (-2V_{d}) \right]$$

$$= \frac{1}{2} \frac{\partial C_{d}}{\partial y} (4V_{a} V_{d} \sin \omega_{d} t - 4V_{0} V_{d} \sin \omega_{m} t)$$
(8)

where $V_a \sin \omega_d t$ denotes the AC component of the drive voltage, V_d denotes the DC component of the drive voltage, $V_0 \sin \omega_m t$ denotes the high-frequency sinusoidal carrier wave.

The frequency of the AC drive voltage is equal to the resonant frequency of the time domain sensor for the purpose of the device resonance. As mentioned above, the frequency of the carrier wave is about three orders higher than that of the AC drive voltage, and the response of the time domain sensor to the carrier wave, i.e., the second term of Equation (8), is greatly attenuated and can be neglected according to the amplitude-frequency characteristic of the second-order system. As a result, the effective electrostatic force is reduced to:

$$F_{deff} = \frac{1}{2} \frac{\partial C_d}{\partial y} 4V_d V_a \sin \omega_d t \tag{9}$$

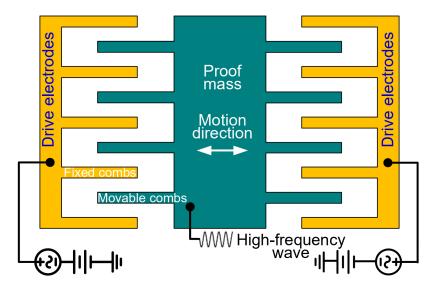


Figure 12. Push–pull electrostatic drive.

It can be seen from Equation (9) that the magnitude of the effective electrostatic force is proportional to the differential of the drive capacitance, the DC bias voltage, and the amplitude of the AC component of the drive voltage. The frequency of the effective electrostatic force is the same as the frequency of the AC drive voltage. Correspondingly, the displacement x (i.e., the vibration amplitude A) caused by the electrostatic force is given as:

$$x = A = \frac{F_{deff}}{K}Q\tag{10}$$

where *Q* refers to the quality factor of the sensor.

Submitting Equations (4), (5), (9) and (10) into Equation (3), the acceleration resolution can be rewritten as:

$$\Delta a \propto \frac{\left[2n_{d}\varepsilon\frac{h_{d}}{d_{d0}} + (2n+1)\varepsilon\frac{b_{d}h_{d}}{a_{d}^{2}}\right]\sqrt{\frac{Etw^{3}W}{L_{3}w^{3} + 2L_{1}^{3}W}}4V_{d}V_{a}\sin\omega_{d}t}{2m_{2}^{3}}Q\Delta t \tag{11}$$

It can be seen from Equation (11) that the resolution can be expressed by the structural parameters of the designed time domain accelerometer. As a result, a relationship between the acceleration resolution and the structural parameters can be built, which provides a theoretical foundation for time domain sensor device design.

4.2. Detection Circuit of the Oscillation Trajectory of the Proof Mass

4.2.1. Representation of DRPs

For a forced vibration of a mass–spring–damper single-freedom system, when an acceleration perturbation a is applied, the center position of the oscillation trajectory of the proof mass shifts a displacement d, $d = a/\omega_0^2$ [30]. Therefore, when the acceleration perturbations, -1 g and +1 g, are applied, the shifted displacement of the center position can be expressed as:

$$x_a = \frac{2g}{\omega_0^2} \tag{12}$$

The shifted displacement causes a change in the spacing between the movable and fixed combs of the sense capacitors (Figure 7), which further results in a change in capacitance. Through the displacement extraction circuit based on a charge amplifier (Figure 13), the change in displacement is reflected by the change in output voltage. Notably, it is necessary carry out signal modulation and demodulation for the output voltage because the AC drive voltage is fed through to the output.

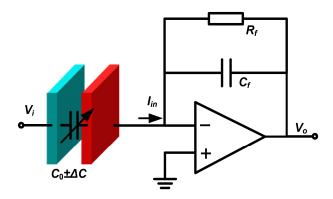


Figure 13. Displacement extraction based on a charge amplifier.

If the extracted DC voltages are V_{-1g} and V_{+1g} when the acceleration perturbations are -1 g and +1 g, the sensitivity of displacement to voltage is given as:

$$S_{xV} = \frac{2g/\omega_0^2}{V_{-1g} - V_{+1g}} \tag{13}$$

Then, the functional relationship between displacement and voltage can be expressed as:

$$x = \left(V - \frac{V_{-1g} + V_{1g}}{2}\right) \times S_{xV} \tag{14}$$

Correspondingly, the functional relationship between the DRPs and the VRPs can be expressed as:

$$X_{i} = \left(V_{i} - \frac{V_{-1g} + V_{1g}}{2}\right) \times S_{xV} \ (i = 1, 2) \tag{15}$$

4.2.2. Relationship between Displacement and Capacitance

The proof mass works under a resonant state. Thus, the movable combs of the sense capacitors fixed to the proof mass also work under a resonant state. As a result, the varying sense capacitance (Figure 14) consists of three parts: the initial capacitance C_{s0} ($C_{s0} = \varepsilon_0 l_s h_s / d_{s0}$), the capacitance change caused by acceleration perturbation ΔC_{sd} ($\Delta C_{sd} = C_{s0} d / d_{s0}$), and the capacitance change caused by the simple harmonic oscillation ΔC_{sv} ($\Delta C_{sv} = C_{s0} A \cos \omega_d t / d_{s0}$).

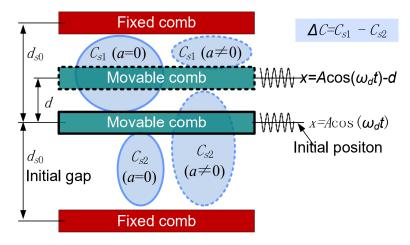


Figure 14. Varying sense capacitance [30].

The sense capacitances C_{s1} and C_{s2} (Figure 14) can be expressed as:

$$C_{s1} = C_{s0} + \Delta C_{sd} + \Delta C_{sv}, \ C_{s2} = C_{s0} - \Delta C_{sd} - \Delta C_{sv}$$
 (16)

The difference ΔC_s between C_{s1} and C_{s2} can be expressed as:

$$\Delta C_s = C_{s1} - C_{s1} = 2(\Delta C_{sd} + \Delta C_{sv}) = 2C_{s0}\frac{d}{d_{s0}} + 2C_{s0}\frac{A\cos\omega_d t}{d_{s0}}$$
(17)

It can be seen from Equation (17) that the change of differential sense capacitance is caused by the external acceleration perturbation and the harmonically oscillating proof mass.

4.2.3. Differential Capacitance Detection Method of Suppressing the Same-Frequency Interference

The differential capacitance ΔC_s consists of two terms (Equation (17)). However, only the first term corresponds to the acceleration perturbation. Consequently, the second term must be suppressed. First, the differential capacitance ΔC_s is converted into high-frequency AC voltage by a single-carrier dual-channel integrated amplifier (Figure 15), where the integrated amplifier consists of two identical charge amplifiers and an instrument amplifier. The commercial chips AD8065 and AD8221 were chosen to build the two charge amplifiers and the instrument amplifier, respectively. The designed sensing capacitance C_{s1} and C_{s2} are both equal to 1.5 pF. The feedback capacitance C_f is set as 2.2 pF. The resistor R_{INA} is set as 51 k Ω . The amplitude and frequency of the sinusoidal carrier wave are 0.5 V and 100 kHz.

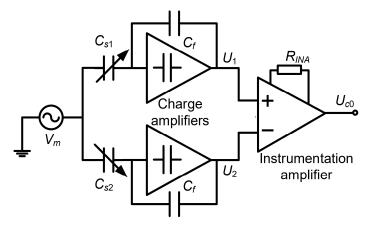


Figure 15. Single-carrier dual-channel integrated amplifier.

The high-frequency voltage can be expressed as:

$$U_{c0} = K_{INA}(U_2 - U)_1 = K_{INA} \frac{C_{s1} - C_{s2}}{C_f} V_m = K_{INA} V_m \frac{\Delta C_s}{C_f}$$
(18)

where V_m denotes carrier voltage ($V_m = V_0 \sin \omega_m t$) and C_f denotes feedback capacitance. The block diagram of suppression of the same-frequency interference is shown in Figure 16. Demodulation is performed on the high-frequency AC voltage U_{c0} for the purpose of obtaining a voltage. The voltage is proportional to the capacitance or displacement caused by the acceleration perturbation. In addition, same-frequency interference is prevented by the high-pass filter (HPF) before the demodulation. After the demodulation, the high-frequency carrier is isolated through a low-pass filter (LPF).

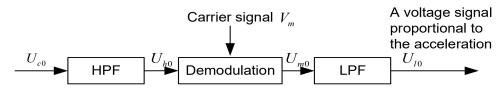


Figure 16. Block diagram of suppression of the same-frequency interference.

The output voltages of the high-pass filter, demodulation, and low-pass filter can be expressed as:

$$\begin{cases} U_{h0} = U_{c0}\dot{A}_{uh} = \dot{A}_{uh}K_{INA}V_{m}\frac{\Delta C_{s}}{C_{f}} \\ V_{m0} = K_{m}V_{m}U_{h0} = K_{m}\dot{A}_{uh}K_{INA}V_{m}^{2}\frac{\Delta C_{s}}{C_{f}} = \frac{1}{2}K_{m}\dot{A}_{uh}K_{INA}V_{0}^{2}\frac{\Delta C_{s}}{C_{f}}[1 - \cos(2\omega_{m}t)] \\ U_{l0} = \frac{1}{2}K_{m}\dot{A}_{uh}\dot{A}_{ul}K_{INA}V_{0}^{2}\frac{\Delta C_{s}}{C_{f}} \end{cases}$$
(19)

where A_{uh} denotes the amplification factor of the HPF, K_m refers to the amplification factor of the demodulation, and A_{ul} denotes the amplification factor of the LPF. The output voltage U_{l0} from the LPF is proportional to the capacitance or displacement caused by the acceleration perturbation.

The circuits of the HPF, demodulation, and low-pass filter are shown in Figure 17. Commercial chips from Analog Devices, Inc. were used to implement the circuits. An operational amplifier AD847 was chosen for the HPF circuit. Therein, the resistors R_f , R_1 , and R are equal to $1~\rm k\Omega$. The capacitor C is set as $1.5~\rm pF$. As a result, the amplification factor and cut-off frequency are 2 and 234 kHz in the HPF. A demodulator AD630 was chosen for the demodulation circuit. An operational amplifier AD847 is also chosen for the LPF circuit. Therein, the resistors R_2 , R_3 , and R_4 are equal to $1~\rm k\Omega$. The capacitor C_1 is set as 33 pF. As a result, the amplification factor and cut-off frequency in the LPF are 2 and $4.8~\rm kHz$.

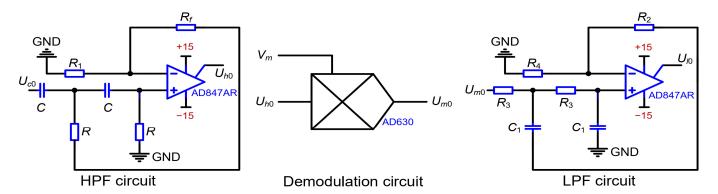


Figure 17. Circuits of the HPF, demodulation, and low-pass filter.

4.3. Time Intervals Measurement Based on Data Post-Processing

The output voltage signal from LPF is sampled using DAQ [31]. Sampling data are post-processed using MATLAB 2012b (Figure 18). As depicted in Figure 18, the trajectory oscillation of the time domain sensor is sampled. Assuming that the sampling rate is S_R , the time-measurement accuracy is $\Delta t = 1/S_R$. Thus, the time-measurement accuracy is tunable through varying the sampling rate. We take time interval ΔT_1 as an example for explaining how the time intervals are measured. When DRP X_1 is between two adjacent sampling data, the first datum is chosen as the trigger event. Thus, the first trigger event tr_1 and the second trigger event tr_4 are chosen in an oscillation period. The event tr_1 corresponds to sampling datum numbered N_{tr_1} while the event tr_4 corresponds to sampling datum numbered N_{tr_4} . The difference between the two trigger events, tr_1 and tr_4 , is extracted as the measured time interval ΔT_1 , i.e., $\Delta T_1 = (N_{tr_4} - N_{tr_1}) \times \Delta t$. Utilizing the same method, the time intervals

 ΔT_2 and ΔT are measured. With reference to Figures 2a and 18, submitting the measured time intervals ΔT_1 , ΔT_2 , and ΔT into Equation 19, the acceleration is calculated as [24]:

$$a = \left(\frac{2\pi}{\Delta T}\right)^2 \left[\frac{(X_1 - X_2)}{\cos\left(\pi \frac{\Delta T_1}{\Delta T}\right) - \cos\left(\pi \frac{\Delta T_2}{\Delta T}\right)} \cos\left(\pi \frac{\Delta T_1}{\Delta T}\right) - X_1\right]$$
(20)

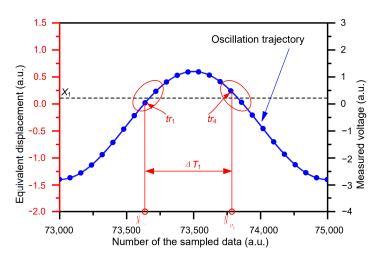


Figure 18. Schematic diagram of time-interval measurement [24,30].

5. Measurement Results and Discussion

5.1. Dependence of Acceleration Resolution on Time-Measurement Accuracy and Vibration Amplitude

5.1.1. Dependence of the Acceleration Resolution on the Time-Measurement Accuracy

The performance of the time domain accelerometer was evaluated via the standard deviation (1σ) of the measured acceleration values [30]. Different time-measurement accuracies were achieved by sampling rate. When the sampling rates were 2.5 MHz, 1.25 MHz, 0.5 MHz, 0.25 MHz respectively, the corresponding time-measurement accuracies were 4×10^{-7} s, 8×10^{-7} s, 2×10^{-6} s, 4×10^{-6} s. The time domain sensor is mounted on dividing head to respond to external acceleration of -1 g. When the DC component of drive voltage, V_d, is 1 V and both the peak-peak amplitude and frequency of the AC component of drive voltage are 0.3 V and ~1245.88 Hz, the sensor works under resonant state with a vibration amplitude of ~342 nm and a frequency of ~1245.88 Hz. The analog signal of the sensor was sampled with different sampling rates for 3.2 s. The DRPs were set as 0 nm and 130 nm. Using the data post-processing method [30], the solved acceleration is shown in Figure 19. The 1σ noises of the solved acceleration were 6.23 mg, 7.07 mg, 12.07 mg, 24.6 mg at the time-measurement accuracies of 4×10^{-7} s, 8×10^{-7} s, 2×10^{-6} s, 4×10^{-6} s. When the time-measurement accuracies were equal to or lower than 8×10^{-7} s ($\ge 8 \times 10^{-7}$ s), the measured 1σ noises were almost proportional to the time-measurement accuracies (Figure 20). The results are consistent with the theoretical analysis (Equation (3)), which indicates that the sensor noises were mainly dependent on time-measurement accuracy. When the time-measurement accuracies were higher than or equal to 8×10^{-7} s ($\leq 8 \times 10^{-7}$ s), the measured 1σ noises were not proportional to the time-measurement accuracies. We can infer that the sensor noise was affected by not only the time-measurement accuracy but also the C-V interface circuit. Limited by the DAQ, higher time accuracies ($<4 \times 10^{-7}$ s) could not be obtained and the corresponding 1σ noises of acceleration were not measured.

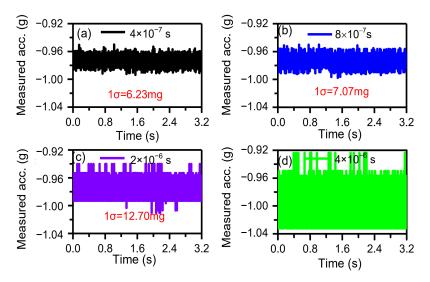


Figure 19. Dependence of the solved acceleration on different time-measure accuracies: (a) 4×10^{-7} s, (b) 8×10^{-7} s, (c) 2×10^{-6} s, (d) 4×10^{-6} s.

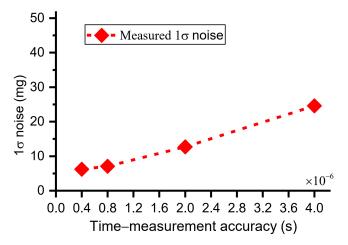


Figure 20. Dependence of 1σ noise on different time-measurement accuracies.

5.1.2. Dependence of the Acceleration Resolution on the Vibration Amplitudes

The DC component of the drive voltage, V_d , remained the same, i.e., V_d = 1 V, while the peak–peak amplitudes of the AC component of the drive voltage were set as 0.3 V, 0.35 V, 0.40 V, and 0.45 V; the driving forces varied and different vibration amplitudes of ~342 nm, ~399 nm, ~455 nm, and ~512 nm were achieved. The sensor operated in a resonant state with a frequency of ~1245.88 Hz, responding to external acceleration of -1 g. The sampling rate was 2.5 MHz and the corresponding time-measurement accuracy was 4×10^{-7} s. The analog signal of the sensor was sampled with different vibration amplitudes for 3.2 s. Then, the DRPs were set as 0 nm and 130 nm. The solved acceleration via data post-processing is shown in Figure 21. The 1σ noises of the solved acceleration were 6.23 mg, 7.02 mg, 7.76 mg, 8.59 mg at vibration amplitudes of ~342 nm, ~399 nm, ~455 nm, and ~512 nm (Figure 21). The measured 1σ noise was almost proportional to the vibration amplitude (Figure 22). This result is consistent with the theoretical analysis (Equation (3)).

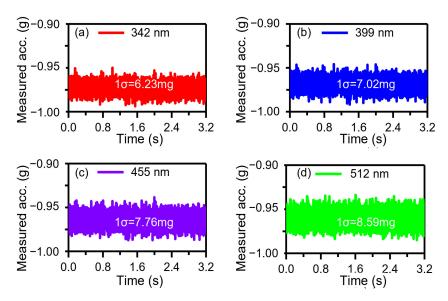


Figure 21. Dependence of the solved acceleration on different vibration amplitudes: (a) 342 nm, (b) 399 nm, (c) 455 nm, (d) 512 nm.

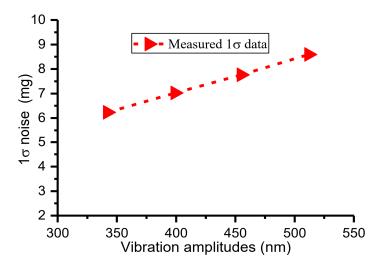


Figure 22. Dependence of 1σ noise on different vibration amplitudes.

It should be noted that the displacement and DRPs are indirectly represented by voltage and VRPs. The voltage is obtained from the varying capacitance of the sense capacitors in the C–V circuit. If the developed device rotates around the Z axis, the Coriolis force acts on the oscillating proof mass and the proof mass moves along the X direction (non-sensing direction). Then, an additional capacitance caused by the Coriolis force is coupled to the effective capacitance caused by the acceleration perturbation. Therefore, the rotation of the developed device around the Z axis affects the measured acceleration. If the displacement and DRPs of the device are physically defined as stacked tunneling electrodes [26], the trigger events are not influenced by the certain X-direction displacement caused by the Coriolis force. Therefore, the rotation of the device based on tunneling electrodes does not affect the measured acceleration. In future work, time domain sensors based on tunneling electrodes will be developed and new characteristics of the time domain sensors studied.

For the time domain sensor, the measurement range can be expressed as $a_{\rm max} = \omega^2(A-d_0)$ [30]. Combining this with the resolution expression $\Delta a \propto A\omega^3\Delta t$ (Equation (3)), we can conclude that when the vibration amplitude and resonant frequency vary, both the measurement range and resolution vary. Furthermore, when the resolution grows low, the measurement range grows large. Generally, two or more separate traditional accelerom-

eters are required for the sensing or measurement of parameter values of significantly different amplitude, thereby increasing the cost and complexity of systems capable of wide measurement ranges. On the contrary, if a developed time domain sensor with adjustable resolution and measurement range could be utilized to sense or measure the significantly different amplitude, it would be a promising technique because the cost and complexity would be lowered.

6. Conclusions

A top-down design methodology and the implementation of a time domain accelerometer have been presented in this paper. The acceleration resolution of the time domain sensor can be tuned by varying the time-measurement accuracy, vibration amplitude, and resonant frequency. The desired resolution was taken as the design target. Some parameters were calculated under the constrained parameters. In this work, the time-measurement accuracy and resonant frequency were constrained, and the vibration amplitude was calculated. Then, a time domain sensor device including driving and detecting structures was detailed, designed according to the parameters, and the device was fabricated utilizing a standard SOI process. In addition, a detection method matched to the fabricated device was developed. Experimental results show that the developed time domain sensor works well, verifying the effectiveness and feasibility of the design methodology and the implementation. The acceleration resolution can be tuned by varying the time-measurement accuracies and vibration amplitudes. Representing a limitation to the current device and test platform, the resonant frequency in the acceleration resolution adjustment test cannot be tuned. In future work, a device with a special port for tuning resonant frequency will be designed for acceleration resolution enhancement and adjustment tests. The top-down design methodology can be expanded to other time domain inertial sensors, e.g., a time domain gyroscope or tilt sensor, and the results of this work can also be applied to other time domain inertial sensors.

Author Contributions: Conceptualization, E.L. and J.J.; methodology, J.J.; software, E.L.; investigation, J.J.; data curation, E.L.; writing—original draft preparation, E.L.; writing—review and editing, E.L. and J.J.; visualization, J.J.; supervision, E.L.; funding acquisition, E.L. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Natural Science Foundation of Huzhou City under Grant 2023YZ12.

Data Availability Statement: Data are contained within the article.

Conflicts of Interest: The authors declare no conflicts of interest.

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