



Proceeding Paper

Testing General Relativity vs. Alternative Theories of Gravitation with the SaToR-G Experiment [†]

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Abstract: A new experiment in the field of gravitation, SaToR-G, is presented. The experiment aims to compare the predictions of different theories of gravitation in the limit of weak field and slow motion. The ultimate goal of the experiment is to look for possible "new physics" beyond the current *standard model* of gravitation based on the predictions of general relativity. A key role in the above perspective is the theoretical and experimental framework within which to confine our work. To this end, we make our best efforts to exploit the framework suggested by Dicke over 50 years ago.

Keywords: general relativity; alternative theories of gravitation; weak fields; LAGEOS and LARES satellites



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1. The Goals of SaToR-G

Satellites tests of relativistic gravity (SaToR-G)) is a new fundamental physics project that aims to test gravitation beyond the predictions of Einstein's general relativity (GR) theory [1] in search for effects foreseen by alternative theories of gravitation (ATGs) [2] and possibly connected with "new physics." In particular, SaToR-G is dedicated to measurements of the gravitational interaction in the weak field and slow motion (WFSM) limit of GR by means of laser tracking to geodetic passive satellites orbiting Earth. Indeed, this new experiment exploits—as quasi-ideal proof masses—the geodynamic laser-ranged satellites LAGEOS [3,4], LAGEOS II [5], and LARES [6] tracked by the powerful satellite laser ranging (SLR) technique [7,8].

The activities of SaToR-G mainly, but not exclusively, focus on metric theories of gravitation, GR being the first of this category. In the context of theories of gravitation alternative to GR, scalar–tensor and vector–tensor theories are of considerable importance. In particular, scalar–tensor theories are metric theories of gravitation quite interesting to be further investigated as ATG [9–11]. The main focus of SaToR-G is twofold: (i) measurement of possible deviations of gravity from the inverse square law for the distance between Earth and the satellites considered, with possible constraints on a Yukawa-like, long-range interaction [12–14], with a typical range correlated to the semi-major axis of satellites [15–17]; (ii) precise and accurate measurements of some post-Newtonian parameters according to the parameterized post–Newtonian (PPN) formalism [18–20]. These are, in fact, in this context, the most powerful tools for testing the predictions of different theories beyond GR itself.

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2. The Theoretical Framework of SaToR-G

Precisely measuring the orbits of artificial satellites allows testing GR vs. other metric theories in their most profound aspects related to the curvature of spacetime, geodesic motion, and field equations. Metric theories of gravitation share Einstein's equivalence principle (EEP) [21], the Lorentzian structure of spacetime and equations of motion. In other words, in all metric theories of gravitation, the structure of spacetime is the same, as is the way in which the geometry of spacetime determines the way mass—energy moves in it. What instead profoundly distinguishes GR from the other metric theories of gravitation are the equations of the gravitational field, that is, how the mass—energy of the field orders the geometry of spacetime to curve [2].

As mentioned above, testing for the values of the PPN parameters represents a powerful tool to discriminate among different theories of gravitation. Nevertheless, within the SaToR-G strategy to test a theory of gravity, we are also interested in recovering the more general approach from which the PPN formalism itself, in its current version, was basically born. In fact, here, we make our best efforts to test the different theories in the theoretical/experimental framework conceived by Robert Dicke around the mid-1960s [22]. The main idea at the basis of this framework is to build up a set of experiments to be as unbiased as possible, both from classical Newtonian physics and from Einstein's GR. The continuing experimental successes of GR predictions in recent decades made this quest less pressing.

On the other hand, during the 1960s and 1970s (and, partly, the 1980s), when experimental evidence for the validity of general relativity was still very weak [23,24], several alternative theories were proposed with a certain degree of continuity [25]. Indeed, in the early 1970s, Kip Thorne and Clifford Will proposed [26]—as a strategy for testing GR—a scheme based on both a Dicke-like approach and an approach based on the at-the-time nascent PPN formalism.

However, from a practical point of view, it appears that Dicke's framework has not been fully exploited in the past, and the main tests and measurements of GR have actually been based on measurements of PPN parameters. This aspect is largely true in the case of gravitational measurements within the solar system, that is, in the case of weak fields (that Thorne and Will were primarily concerned with, in 1971), but it is also valid in the context of almost strong fields such as those tested more recently in relativistic astrophysics [27,28]. Indeed, even in the cases of non-weak fields, the post-Newtonian formalism provides an excellent description of gravitational measurements [29].

For the above reasons, we believe that an effort to reconsider the Dicke framework is appropriate and of interest, even these days, to test the foundation of gravitation, especially in those aspects that are not fully covered by the PPN framework.

3. The Legacy from LARASE

SaToR-G builds on the improved dynamical model of the two LAGEOS and LARES satellites achieved within the previous project LAser RAnged Satellites Experiment (LARASE)) [30]. The improvements mainly concern the modeling of the nonconservative forces (NCFs) acting on the surface of the three satellites [31–34] and that of the Earth's gravitational field and tides in their precise orbit determination (POD) [34–36]. Regarding the NCF, the main improvements were the development of a model for the spin of the satellites (LASSOS: LArase Satellites Spin mOdel Solutions) and a model for thermal thrust forces (LATOS: LArase Thermal mOdel Solutions). For the gravitational field, the monthly solutions of the GRACE mission [37–39] have been implemented in the code used for the POD.

The main results of LARASE in the field of gravitational effects measurements were a precise and accurate measurement of the precession of the argument of pericenter of LAGEOS II [17] and of the Lense–Thirring precession from the analysis of the orbits of the two LAGEOS and LARES satellites [34,40,41]. In particular, in the case of the first measurement, constraints on nonsymmetric [42,43] and torsional [44,45] theories of gravitation were set with improvements with respect to previous results in the literature.

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In this regard, a significant result was the constraint on a Yukawa-like interaction with a characteristic range λ close to the radius of the Earth and a strength $|\alpha|=|0.5\pm 8\pm 101|\times 10^{-12}$. In the case of the Lense–Thirring precession, the parameter μ that is used to parameterize the relativistic precession (with $\mu=1$ in GR and $\mu=0$ in Newtonian physics) was measured very accurately with an error budget of about 1.6%: $\mu_{\rm meas}-1=(1.5\pm 7.4\pm 16)\times 10^{-3}$, where the first uncertainty represents the statistical formal error, at a 95% confidence level, while the second uncertainty represents the estimate of the systematic sources of error.

4. Conclusions

A number of activities have been initiated with the aim of setting new kinds of measurements in the field of gravitation with Earth-bound laser-ranged satellites. This activity will be based on a theoretical/experimental framework that is not "simply" described by PPN parameters but also as close as possible to the original framework proposed by Professor R.H. Dicke. See supplementary materials with more relevant information.

Supplementary Materials: The following are available online at https://www.mdpi.com/article/10 .3390/ECU2021-09274/s1.

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References

- 1. Einstein, A. Die Grundlage der allgemeinen Relativitätstheorie. Ann. Phys. 1916, 354, 769–822. [CrossRef]
- 2. Will, C.M. Theory and Experiment in Gravitational Physics; Cambridge University Press: Cambridge, UK, 2018.
- 3. Johnson, C.W.; Lundquist, C.A.; Zurasky, J.L. (Eds.) The Lageos Satellite. In Proceedings of the Anaheim International Astronautical Federation Congress, Anaheim, CA, USA, 10–16 October 1976.
- 4. National Aeronautics and Space Administration. *LAGEOS Phase B Technical Report, NASA Technical Memorandum X-64915*; Technical Report TMX-64915; Marshall Space Flight Center: Huntsville, AL, USA, 1975.
- 5. Fontana, F. *Physical Properties of LAGEOS II Satellite*; Technical Report LG-TN-AI-037; Aeritalia: Torino, Italy, 1989.
- 6. Paolozzi, A.; Ciufolini, I. LARES successfully launched in orbit: Satellite and mission description. *Acta Astronaut.* **2013**, 91, 313–321. [CrossRef]
- 7. Degnan, J.J. Satellite laser ranging: Current status and future prospects. *IEEE Trans. Geosci. Remote Sens.* **1985**, 23, 398–413. [CrossRef]
- 8. Pearlman, M.R.; Degnan, J.J.; Bosworth, J.M. The International Laser Ranging Service. *Adv. Space Res.* **2002**, *30*, 135–143. [CrossRef]
- 9. Brans, C.; Dicke, R.H. Mach's Principle and a Relativistic Theory of Gravitation. Phys. Rev. 1961, 124, 925–935. [CrossRef]
- 10. Sotiriou, T.P.; Faraoni, V. f(R) theories of gravity. Rev. Mod. Phys. 2010, 82, 451–497. [CrossRef]
- 11. De Felice, A.; Tsujikawa, S. f(R) Theories. Living Rev. Relativ. 2010, 13, 3. [CrossRef]
- 12. Fujii, Y. Dilaton and Possible Non-Newtonian Gravity. Nat. Phys. Sci. 1971, 234, 5–7. [CrossRef]
- 13. Damour, T.; Piazza, F.; Veneziano, G. Runaway Dilaton and Equivalence Principle Violations. *Phys. Rev. Lett.* **2002**, *89*, 081601. [CrossRef] [PubMed]
- 14. Fischbach, E.; Sudarsky, D.; Szafer, A.; Talmadge, C.; Aronson, S.H. Reanalysis of the Eotvos experiment. *Phys. Rev. Lett.* **1986**, 56, 3–6. [CrossRef] [PubMed]
- 15. Lucchesi, D.M. The LAGEOS satellites orbit and Yukawa-like interactions. Adv. Space Res. 2011, 47, 1232–1237. [CrossRef]

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16. Lucchesi, D.M.; Peron, R. Accurate Measurement in the Field of the Earth of the General-Relativistic Precession of the LAGEOS II Pericenter and New Constraints on Non–Newtonian Gravity. *Phys. Rev. Lett.* **2010**, *105*, 231103. [CrossRef]

- 17. Lucchesi, D.M.; Peron, R. LAGEOS II pericenter general relativistic precession (1993-2005): Error budget and constraints in gravitational physics. *Phys. Rev. D* **2014**, *89*, 082002. [CrossRef]
- 18. Nordtvedt, K. Equivalence Principle for Massive Bodies. II. Theory. Phys. Rev. 1968, 169, 1017–1025. [CrossRef]
- 19. Will, C.M. Theoretical Frameworks for Testing Relativistic Gravity. II. Parametrized Post–Newtonian Hydrodynamics, and the Nordtvedt Effect. *Astrophys. J.* **1971**, *163*, 611–628. [CrossRef]
- 20. Will, C.M.; Nordtvedt, J.K. Conservation Laws and Preferred Frames in Relativistic Gravity. I. Preferred-Frame Theories and an Extended PPN Formalism. *Astrophys. J.* **1972**, 177, 757–774. [CrossRef]
- 21. Schwartz, H.M. Einstein's comprehensive 1907 essay on relativity, part III. Am. J. Phys. 1977, 45, 899–902. [CrossRef]
- 22. Dicke, R.H. The Theoretical Significance of Experimental Relativity; Blackie and Son Ltd.: London/Glasgow, UK, 1964.
- 23. Bertotti, B.; Brill, D.; Krotkov, R. Gravitation: An Introduction to Current Research; Wiley: Hoboken, NJ, USA, 1962.
- 24. Whitrow, G.J.; Morduch, G.E. Relativistic theories of gravitation: A comparative analysis with particular reference to astronomical tests. *Vistas Astron.* **1965**, *6*, 1–67. [CrossRef]
- 25. Will, C.M. Theory and Experiment in Gravitational Physics; Cambridge University Press: Cambridge, UK, 1993.
- Thorne, K.S.; Will, C.M. Theoretical Frameworks for Testing Relativistic Gravity. I. Foundations. Astrophys. J. 1971, 163, 595.
 [CrossRef]
- 27. Abbott, B.P.; Abbott, R.; Abbott, T.D.; Abernathy, M.R.; Acernese, F.; Ackley, K.; Adams, C.; Adams, T.; Addesso, P.; Adhikari, R.X.; et al. Observation of Gravitational Waves from a Binary Black Hole Merger. *Phys. Rev. Lett.* **2016**, *116*, 061102. [CrossRef]
- 28. Abbott, B.P.; Abbott, R.; Abbott, T.D.; Acernese, F.; Ackley, K.; Adams, C.; Adams, T.; Addesso, P.; Adhikari, R.X.; Adya, V.B.; et al. Multi-messenger Observations of a Binary Neutron Star Merger. *APJL* 2017, 848, L12. [CrossRef]
- 29. Will, C.M. Inaugural Article: On the unreasonable effectiveness of the post-Newtonian approximation in gravitational physics. *Proc. Natl. Acad. Sci. USA* **2011**, *108*, 5938–5945. [CrossRef]
- 30. Lucchesi, D.; Anselmo, L.; Bassan, M.; Pardini, C.; Peron, R.; Pucacco, G.; Visco, M. Testing the gravitational interaction in the field of the Earth via satellite laser ranging and the Laser Ranged Satellites Experiment (LARASE). *Class. Quantum Grav.* **2015**, 32, 155012. [CrossRef]
- 31. Visco, M.; Lucchesi, D.M. Review and critical analysis of mass and moments of inertia of the LAGEOS and LAGEOS II satellites for the LARASE program. *Adv. Space Res.* **2016**, *57*, 1928–1938. [CrossRef]
- 32. Pardini, C.; Anselmo, L.; Lucchesi, D.M.; Peron, R. On the secular decay of the LARES semi-major axis. *Acta Astronaut.* 2017, 140, 469–477. [CrossRef]
- 33. Visco, M.; Lucchesi, D.M. Comprehensive model for the spin evolution of the LAGEOS and LARES satellites. *Phys. Rev. D* **2018**, 98, 044034. [CrossRef]
- 34. Lucchesi, D.M.; Anselmo, L.; Bassan, M.; Magnafico, C.; Pardini, C.; Peron, R.; Pucacco, G.; Visco, M. General Relativity Measurements in the Field of Earth with Laser-Ranged Satellites: State of the Art and Perspectives. *Universe* **2019**, *5*, 141. [CrossRef]
- 35. Pucacco, G.; Lucchesi, D.M.; Anselmo, L.; Bassan, M.; Magnafico, C.; Pardini, C.; Peron, R.; Stanga, R.; Visco, M. Earth gravity field modeling and relativistic measurements with laser-ranged satellites and the LARASE research program. In Proceedings of the EGU Conference, Geophysical Research Abstracts, Vienna, Austria, 23–28 April 2017; Volume 19.
- 36. Pucacco, G.; Lucchesi, D.M. Tidal effects on the LAGEOS-LARES satellites and the LARASE program. *Celest. Mech. Dyn. Astron.* **2018**, *130*, 66. [CrossRef]
- 37. Tapley, B.D.; Flechtner, F.; Bettadpur, S.V.; Watkins, M.M. The status and future prospect for GRACE after the first decade. In Proceedings of the Eos Transactions Fall Meeting Supplement Abstract G32A-01, San Francisco, CA, USA, 9–13 December 2013.
- 38. Cheng, M.; Tapley, B.D.; Ries, J.C. Deceleration in the Earth's oblateness. J. Geophys. Res. Solid Earth 2013, 118, 740–747. [CrossRef]
- 39. Cheng, M.; Ries, J.C. Decadal variation in Earth's oblateness (J₂) from satellite laser ranging data. *Geophys. J. Int.* **2018**, 212, 1218–1224. [CrossRef]
- 40. Lucchesi, D.M.; Visco, M.; Peron, R.; Bassan, M.; Pucacco, G.; Pardini, C.; Anselmo, L.; Magnafico, C. An improved measurement of the Lense-Thirring precession on the orbits of laser-ranged satellites with an accuracy approaching the 1% level. *arXiv* **2019**, arXiv:gr-qc/1910.01941.
- 41. Lucchesi, D.; Visco, M.; Peron, R.; Bassan, M.; Pucacco, G.; Pardini, C.; Anselmo, L.; Magnafico, C. A 1% Measurement of the Gravitomagnetic Field of the Earth with Laser-Tracked Satellites. *Universe* **2020**, *6*, 139. [CrossRef]
- 42. Moffat, J.W. New theory of gravitation. Phys. Rev. D 1979, 19, 3554–3558. [CrossRef]
- 43. Moffat, J.W.; Woolgar, E. Motion of massive bodies: Testing the nonsymmetric gravitation theory. *Phys. Rev. D* **1988**, *37*, 918–930. [CrossRef] [PubMed]
- 44. Hehl, F.W.; von der Heyde, P.; Kerlick, G.D.; Nester, J.M. General relativity with spin and torsion: Foundations and prospects. *Rev. Mod. Phys.* **1976**, *48*, 393–416. [CrossRef]
- 45. Hammond, R.T. Torsion gravity. Rep. Prog. Phys. 2002, 65, 599–649. [CrossRef]