

# Package ‘localift’

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**Type** Package

**Title** Functions to manipulate data in order to study the Local Lift Dependence (Beta Version)

**Version** 0.0.1

**URL** <http://github.com/dmarcondes/localift>

**BugReports** <https://github.com/dmarcondes/localift/issues>

**Description** Generates tables, plots and measures related to the Local Lift Dependence.

**Imports** ggplot2 (>= 2.2.1),  
MASS (>= 7.3-45),

**Depends** R (>= 3.3.2)

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 6.0.1

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heatmap.lift

*Lift Function Heatmap***Description**

Heatmap of the Lift Function.

**Usage**

```
heatmap.lift(x, y, xlab = "x", ylab = "y", plot.title = " ",
  palette = "Spectral", na.color = "red", contour = TRUE,
  contour.color = "white", contour.alpha = 0.5, contour.bin = 15,
  contour.binwidth = 1, critical.value = 3, quantilesx = c(1/3, 2/3),
  quantilesy = c(1/3, 2/3), breaks = c(1, 2), quantile.type = 7,
  n = length(x), grid = TRUE)
```

**Arguments**

x	A vector of data.
y	A vector of data.
xlab	Label of the x-axis.
ylab	Label of the y-axis.
plot.title	Title of the heatmap plot.
palette	The color palette to be used on the heatmap. Default is <i>'Spectral'</i> .
na.color	Color for <i>NA</i> values.
contour	Logical. Whether to plot the Lift Function contour.
contour.color	Color of the Lift Function contour.
contour.alpha	Transparency coefficient for the contour plot.
contour.bin	Number of bins for the contour plot.
contour.binwidth	Width of the bins for the contour plot.
critical.value	Critical value in which the Lift Function must be truncated.
quantilesx	Quantiles to be marked on the x-axis.
quantilesy	Quantiles to be marked on the y-axis.
breaks	Breaks of the heatmap legend. Must not contain <i>0</i> nor <i>critical.value</i> and all values must be less than the <i>critical.value</i> .
quantile.type	An integer between 1 and 9 selecting one of the nine quantile algorithms of the <i>quantile</i> function.
n	Number of equally spaced points at which the density is to be estimated. When $n > 512$ , it is rounded up to a power of 2 during the calculations (as <i>fft</i> is used) and the final result is interpolated by <i>approx</i> . So it almost always makes sense to specify <i>n</i> as a power of two
grid	Logical. Whether to plot grid lines representing the sample quantiles.

**Details**

Given two continuous random variables returns the heatmap of their estimated Lift Function. The heatmap paint the support of  $(x,y)$  according to the values of the Lift Function  $L(x, y) = f(x, y)/(g(x)*h(y))$  in which  $f(x,y)$  is the estimated joint density of  $(x,y)$  and  $g(x)$  and  $h(y)$  are the respective estimated marginal distributions. If  $L(x, y) > critical.value$  then  $L(x,y) = critical.value$ , i.e.,  $L(x,y)$  is truncated at  $critical.value$ .

**Value**

plot                    A ggplot2 heatmap.

**References**

Simonis, A., Marcondes, D., Barrera, J. (2017) Feature Selection based on the Local Lift Dependence Scale. *Submitted*

**Examples**

```
attach(requirement)
heatmap.lift(SP,P2)
```

---

lift.feats.selection    *Lift Featuring Selection Algorithm*

---

**Description**

Given two sets  $x$  and  $y$ , select the subsets of variables that are more dependent.

**Usage**

```
lift.feats.selection(y, x, block.x = NULL, block.y = NULL, fix.x = NULL,
  fix.y = NULL, reach.x = "all", reach.y = "all", cost = "eta",
  local = NULL, low.min = 0, windows = "all", trace = FALSE,
  se = FALSE, quantilesx = c(1/3, 2/3), quantile.type = 7,
  namesx = c("1 TertileX", "2 TertileX", "3 TertileX"), quantilesy = c(1/3,
  2/3), namesy = c("1 TertileY", "2 TertileY", "3 TertileY"),
  method = "mahalanobis", p.minkowski = 1, sample = "se",
  point = "zero", min.size = 0, right = TRUE)
```

**Arguments**

$y$                     Data frame in which each column is a sample of a random variable.

$x$                     Data frame in which each column is a sample of a random variable.

block.x              Block factor in which  $x$  must be discretize within. The quantiles will be taken inside each block.

block.y	Block factor in which y must be discretize within. The quantiles will be taken inside each block.
fix.x	Number of the columns of x that must be considered in all iterations.
fix.y	Number of the columns of y that must be considered in all iterations.
reach.x	Vector with the sizes of the subsets of x that must be considered. Default is all the power set of x.
reach.y	Vector with the sizes of the subsets of y that must be considered. Default is all the power set of y.
cost	Cost function to be used. Must be "MI" for Mutual Information, "eta" for eta on windows or 'max' for the local max.
local	If cost = 'max', must be the name of the category of y which the maximum of the lift must be searched for. Must be a level of y or one of the labels in <i>namesy</i> .
low.min	If cost = 'max', must be an lower bound for the profile relative frequency, so that the algorithm will search for the rows of the lift table with relative frequency greater than <i>low.min</i> .
windows	In what windows the eta coefficient must be calculated. Can be "all" for all windows or "cat" for the windows that are given by a single category of <i>U</i> .
trace	Logical. Whether to return a data frame with the mutual information and the eta coefficient, along with the Lift Table, for every subset of y and x.
se	Whether the standard error must be calculated for the lift table and the eta coefficients. If <i>TRUE</i> the computational time increases exponentially.
quantilex	Quantiles in which the variables x must be partitioned. Must not contain 0 nor 1.
quantile.type	An integer between 1 and 9 selecting one of the nine quantile algorithms of the <i>quantile</i> function.
namesx	Name of the partitions of x. Its length must equal $length(quantilex) + 1$ .
quantilesy	Quantiles in which the variables y must be partitioned. Must not contain 0 nor 1.
namesy	Name of the partitions of y. Its length must equal $length(quantilesy) + 1$ .
method	Method that should be used to calculate the distance between the sample points and zero or the sample mean. Must be 'mahalanobis', 'euclidean', 'maximum', 'manhattan', 'canberra', 'binary' or 'minkowski'.
p.minkowski	The power of the Minkowski distance, if <i>method</i> = 'minkowski'.
sample	What information about the sample to display in parenthesis on the Lift Table. Must 'size' for sample size, 'joint' for relative frequency and 'none' for displaying nothing.
point	Which point to calculate the distance from. Must be 'zero' or 'mean' for sample mean.
min.size	Minimum sample size that can be considered. It will skip all combinations of the x and y partitions in which the sample size is less than <i>min.size</i>
right	Logical, indicating if the quantile intervals should be closed on the right (and open on the left) or vice versa.

**Details**

Given two sets  $x$  and  $y$  of random variables, it returns the subsets  $x'$  of  $x$  and  $y'$  of  $x$  for which the Global Eta Coefficient, or W-Local Eta Coefficient, or the Lift Function at a given point is the greatest in comparison to all the other combination of subsets of  $x$  and  $y$ .

**Value**

lift	The <a href="#">LiftTable</a> of the selected features.
MI	The Mutual information between the returned subsets.
Eta	The dependence measures eta between the returned subsets.
EtaM	The maximum eta dependence measure in windows of the returned x subset.
Window	The window with maximum eta coefficient.
Max	The maximum of the lift on the considered category of $y$ .
LevelMax	The levels of $x$ for which the lift is <i>max</i> .
subsetx	The subset of $x$
subsety	The subset of $y$
xquantile	The quantile of each observation of $x$ .
yquantile	The quantile of each observation of $y$ .
trace	The table with the trace of the algorithm.
ltables	The Lift Tables of each iteration.

**References**

Simonis, A., Marcondes, D., Barrera, J. (2017) Feature Selection based on the Local Lift Dependence Scale. *Submitted*

**Examples**

```
attach(requirement)
lift.feat.selection(SP,data.frame(C1,C2,C3,P1,P2),cost = "eta",trace = TRUE,local = "3 TertileY")
```

---

LiftTable

*Lift Table*


---

**Description**

Lift Table between two groups of variables.

**Usage**

```
LiftTable(table = NULL, x, y, se = TRUE, local = NULL, w = TRUE,
  windows = "all", block.x = 1, block.y = 1, quantilex = c(1/3, 2/3),
  namesx = c("1 TertileX", "2 TertileX", "3 TertileX"), quantilesy = c(1/3,
  2/3), namesy = c("1 TertileY", "2 TertileY", "3 TertileY"),
  quantile.type = 7, point.x = "zero", point.y = "zero",
  method = "mahalanobis", p.minkowski = 1, low.min = 0, sample = "se",
  right = TRUE, digits = 3)
```

**Arguments**

table	A contingency table without margins and with row and column names. Needed only if the factor variables are already tabulated.
x	A numeric matrix, a factor vector or a numeric vector.
y	A numeric matrix, a factor vector or a numeric vector.
se	Whether the standard error must be calculated for the lift table and the eta coefficients.
local	Must be the name of the category of y in which the maximum of the lift must be searched for. Must be a level of y or one of the labels in <i>namesy</i> . The <i>default</i> is the first category of y.
w	Whether the <i>eta</i> coefficient must be calculated for the <i>windows</i> of the support of <i>U</i> .
windows	In what windows the eta coefficient must be calculated. Must be a list of vectors, in which each vector contain the name of the categories of <i>U</i> . Can be "all" for all windows or "cat" for the windows that are given by a single category of <i>U</i>
block.x	Block factor in which x must be discretize within. The quantiles will be taken inside each block.
block.y	Block factor in which y must be discretize within. The quantiles will be taken inside each block.
quantilex	Quantiles in which the variable x must be partitioned. Must not contain 0 nor 1.
namesx	Name of the partitions of x. Its length must equal $length(quantilex) + 1$ .
quantilesy	Quantiles in which the variables y must be partitioned. Must not contain 0 nor 1.
namesy	Name of the partitions of y. Its length must equal $length(quantilesy) + 1$ .
quantile.type	An integer between 1 and 9 selecting one of the nine quantile algorithms of the <a href="#">quantile</a> function.
point.x	Which point to calculate the distances of x from. Must be 'zero', 'mean' for sample mean or a vector with the dimension of x.
point.y	Which point to calculate the distances of y from. Must be 'zero', 'mean' for sample mean or a vector with the dimension of y.
method	Method that should be used to calculate the distance. Must be 'mahalanobis', 'euclidean', 'maximum', 'manhattan', 'canberra', 'binary' or 'minkowski'.
p.minkowski	The power of the Minkowski distance, if <i>method</i> = 'minkowski'.

low.min	If <i>cost</i> = 'max', must be an lower bound for the profile relative frequency, so that the algorithm will search for the rows of the lift table with relative frequency greater than <i>low.min</i> .
sample	What information about the sample to display in parenthesis on the Lift Table. Must be 'size' for sample size, 'joint' for relative frequency, 'se' for standard error and 'none' for displaying nothing.
right	Logical, indicating if the quantile intervals should be closed on the right (and open on the left) or vice versa.
digits	Integer indicating the number of significant digits (signif) to be used on the Lift Table.

### Details

If  $x$  and  $y$  are numeric vectors, it computes the Lift Table between the discrete random variables  $U$  and  $V$  determined from the sample quantiles of  $x$  and  $y$ , inside each level of the block variables. If  $x$  or  $y$  are numerical *matrices*, then the Lift Table is computed from the discrete random variables  $U$  and  $V$  determined from the partition of  $(x,y)$  by the selected distance method based on the sample quantiles, within each level of the block factors. If  $x$  or  $y$  are factor vectors, the Lift Function is calculated directly from  $x$  and  $y$ . If  $x$  or  $y$  contain numerical and factor variables then the discretization process is made by the quantile discretization of the sample distances from the given point, within each level of the factor and block variables.

If  $(U,V)$  are discrete and  $(u,v)$  is a category of  $(U,V)$  then the Lift Function at such category is given by  $L(u,v) = p(u,v)/(pU(u) * pV(v))$  in which  $p$  is the relative joint frequency of  $(U,V)$  and  $pU$  and  $pV$  are the respective marginal relative frequencies. For more details see the References.

### Value

ltable	The Lift Table. Rows are related to $x$ and columns to $y$ .
eta	The dependence measures eta.
MI	The normalized Mutual Information of the Lift Table.
max	The maximum of the lift on the considered category of $y$ .
xquantile	The quantile of each observation of $x$ .
yquantile	The quantile of each observation of $y$ .
se	The standard error for each lift value.
cov	The covariance matrix of the lift function in lexicographical order.

### References

Simonis, A., Marcondes, D., Barrera, J. (2017) Feature Selection based on the Local Lift Dependence Scale. *Submitted*

### Examples

```
attach(requirement)
LiftTable(x = SP,y = data.frame(C3,P1))
LiftTable(x = data.frame(C1,C2,C3),y = data.frame(P1,P2))
LiftTable(x = data.frame(iris[,1:4]),y = iris$Species)
```

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mahalanobis.plot      *Mahalanobis Plot*

---

### Description

Dispersion plot with the Mahalanobis partition ellipses.

### Usage

```
mahalanobis.plot(x, y, g = NULL, g.color = "black", g.name = "Group",
  xlab = "x", ylab = "y", xlim = c(min(data[, 1]), max(data[, 1])),
  ylim = c(min(data[, 2]), max(data[, 2])), quantiles = c(1/3, 2/3),
  names = c("1 Tertile", "2 Tertile", "3 Tertile"), partition = TRUE,
  rectangle = TRUE, rectangle.color = "black", plot.title = " ",
  point = "zero", quantile.type = 7, shape = 16, size = 1.5,
  color = "black")
```

### Arguments

x	A vector of data.
y	A vector of data.
g	Grouping factor.
g.color	A vector with color names for the ellipses. It must present one color for each level of the grouping factor.
g.name	Name of the grouping factor.
xlab	Label of the x-axis.
ylab	Label of the y-axis.
xlim	Limits of the x-axis.
ylim	Limits of the y-axis.
quantiles	Quantiles of the Mahalanobis partition.
names	Name of the partitions. Its length must equal $length(quantiles) + 1$ .
partition	Logical. Whether the Mahalanobis ellipses are plotted.
rectangle	Logical. Whether a rectangle is plotted around the data.
rectangle.color	Color of the rectangle.
plot.title	Title of the plot.
point	Which point to calculate the distance from. Must be 'zero' or 'mean' for sample mean.
quantile.type	Integer between 1 and 9 selecting one of the nine quantile algorithms of the <i>quantile</i> function.
shape	ggplot2 shape.
size	ggplot2 size.
color	Points point color.

**Details**

Dispersion plot of two random variables with the ellipses of the Mahalanobis partition given by the quantiles of a distances to a given point inside each level of a grouping factor.

**Value**

plot	The dispersion plot.
quantiles	The quantile of each observation of <i>data</i> .

**References**

Simonis, A., Marcondes, D., Barrera, J. (2017) Feature Selection based on the Local Lift Dependence Scale. *Submitted*

**Examples**

```
attach(requirement)
mahalanobis.plot(C1,C2,xlim = c(0,10),ylim = c(0,10))
```

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requirement	<i>Requirement data set</i>
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**Description**

Data set containing the performance of 61 undergraduate Statistics students in Stochastic Process and its required courses.

**Usage**

```
requirement
```

**Format**

An object of class `data.frame` with 61 rows and 8 columns.

**Details**

The performance in each course is taken as the grade in the course, a number between 0 and 10.

**Value**

C1	The performance in Calculus I.
C2	The performance in Calculus II.
C3	The performance in Calculus III.
P1	The performance in Probability I.
P2	The performance in Probability II.
SP	Performance in Stochastic Process.
Year	The year each student enrolled in the undergraduate course.

**References**

Simonis, A., Marcondes, D., Barrera, J. (2017) Feature Selection based on the Local Lift Dependence Scale. *Submitted*

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