

## Article

# Optimization of Two-Phase Ejector Mixing Chamber Length under Varied Liquid Volume Fraction

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**Abstract:** The ejector performance varies with the mixing chamber length which is largely dependent on the fluid liquid volume fraction at the inlet. In this study, numerical simulations are conducted to optimize two mixing chamber lengths of a two-phase ejector under varied liquid volume fractions of 0–0.1 in two inlet fluids. The main findings are as follows: (1) The two optimal lengths of constant-pressure and constant-area mixing chambers are identified within 23–44 mm and 15–18 mm, respectively, when the primary inlet fluid is in two-phase; (2) the two optimal lengths are 2–5 mm and 9–15 mm, respectively, when the secondary inlet fluid is in two-phase; (3) when both inlets are in two-phase, the two optimal lengths are ranged in 5–23 mm and 6–18 mm; (4) little liquid within inlet fluid has a significant influence on ejector performances; and (5) optimal constant-pressure mixing chamber length and the sum of the two optimal lengths increase with the primary flow inlet liquid volume fraction but decrease with that of the secondary flow inlet.

**Keywords:** ejector; entrainment ratio; liquid volume fraction; numerical simulation; mixing chamber length



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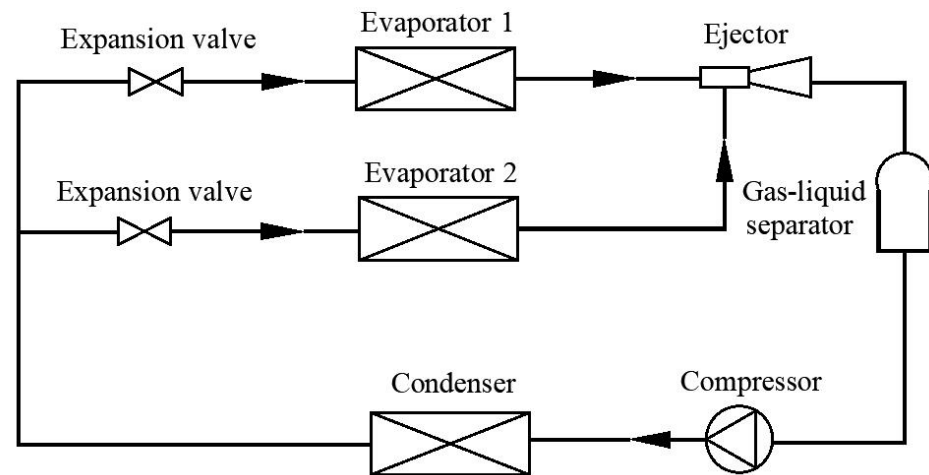
## 1. Introduction

With the rapid development of technology, energy consumption has restricted economic and social development. Therefore, it is quite urgent to improve energy efficiency in air-conditioning and refrigeration devices [1,2]. Various studies have been conducted to improve the performance of refrigeration systems and thus solve environmental issues [3–5]. Moreover, the performance of refrigeration systems has been enhanced by adopting advanced technologies [6–9]. For the refrigeration needed in refrigerated trucks that always need air-conditioning services and refrigerating or freezing purposes for food storage, a pressure regulating valve (PRV) is equipped between two evaporators to keep the required pressure difference [10,11], which causes many irreversible throttling losses. Therefore, an ejector is used to replace the PRV and partially recover the throttling losses [12–14]. The schematic of a typical simplified EMERS with two temperature levels is shown in Figure 1 [15]. An EMERS has some advantages such as low operating costs [16,17].

When the EMERS is used in refrigerated trucks, the essential device of the system is the ejector [18,19]. The two flows of the refrigerant flows mix in the ejector and enter the compressor with a pressure lift [20]. By optimizing the area ratio (AR) and the nozzle exit position (NXP) and so on, ejector performance can be improved [21,22].

High entrainment performance of the ejector can be achieved if the two flows are mixed well [23]. Nakagawa et al. [24] studied the effect of mixing the length of a trans-critical CO<sub>2</sub> two-phase ejector with a rectangular cross-section, and they claimed that the 15 mm of mixing length can produce good ejector performance. Sarkar et al. [25] showed that the constant-area mixing chamber cross-section area affects ejector performance mainly depending on the ejector inlet conditions. Banasiak et al. [26] also proved that the ejector performance largely depends on the mixing chamber length in a small ejector-based

R744 transcritical heat pump system. Jeon et al. [27] studied an ejector mixing length and improved system performance. Fu et al. [28] optimized the mixing chamber throat diameter to improve the steam ejector performance. By using three-dimensional numerical simulations, Dong et al. [29] studied the effects of the mixing chamber length, and the best ejector performance was obtained within a certain range of the mixing chamber length.



**Figure 1.** Schematic of a two-temperature evaporator-based EMERS.

In many cases, the ejector operates with a gas-liquid mixture of primary flow or gas-liquid mixture of secondary flow. Hemidi et al. [30] conducted the study when the water droplets were ejected into primary air flow, which improved off-design performance. Yuan et al. [31] investigated a two-phase ejector experimentally and numerically. Similarly, according to the study of Yuan et al. [31], Chen et al. [32] also studied the two-phase secondary flow ejector performance. They claimed that ER and PRR would decrease when the induced flow is accompanied by water. Aliabadi et al. [33] investigated the effects of primary nozzle inlet wetness in the range of 0–1%. Their results indicate that the water droplets make an ER improvement.

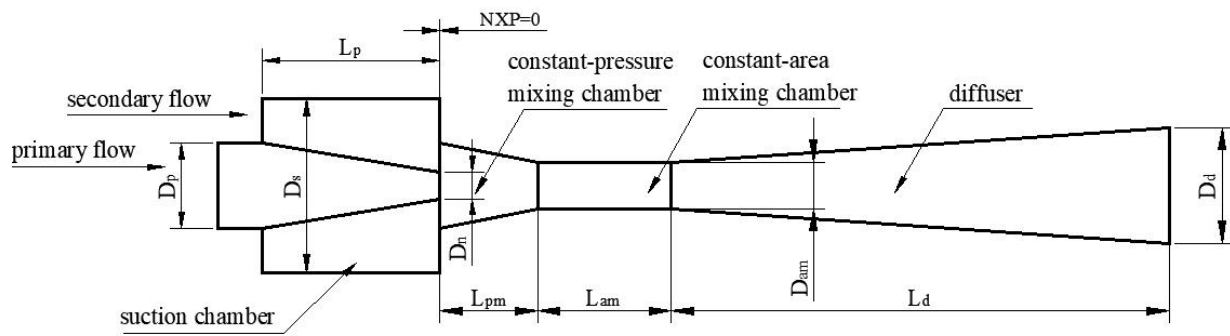
To the best of the authors' knowledge, there is no study on the effects of mixing chamber length under different liquid volume fractions (LVF) which means the liquid volume percentage in the two-phase flow on ejector performance used refrigerant of  $C_2H_2F_4$  as displayed in Figure 1. With our former study [15], it was known that when the LVF of the two inlet flows varies, it may have an undesirable effect on ejector performance, and thus, the ejector with original geometries may be in malfunction.

Thus, this study aims to optimize the constant-pressure mixing section length ( $L_{pm}$ ) and constant-area mixing section length ( $L_{am}$ ) of a two-phase ejector under different primary and secondary flow liquid volume fractions. The details of the work in this paper are:

- to identify optimal  $L_{pm}$  under varied secondary flow liquid volume fraction;
- to find the optimal  $L_{pm}$  under varied primary flow liquid volume fraction;
- with optimal  $L_{pm}$ , to search for the optimal  $L_{am}$  under varied secondary flow liquid volume fraction;
- with optimal  $L_{pm}$ , to optimize the  $L_{am}$  under varied primary flow liquid volume fraction.

## 2. CFD Modeling and Validation

The schematic of the ejector is presented in Figure 2 [15]. Its initial geometrical parameters are presented in Table 1, and boundary conditions are presented in Table 2.



**Figure 2.** Schematic of the ejector.

**Table 1.** Initial geometrical parameters of the ejector.

Parameters	Value (mm)
The suction chamber diameter, $D_s$	19.6
The primary nozzle inlet diameter, $D_p$	9.6
The primary nozzle outlet diameter, $D_n$	3
The constant-area mixing chamber diameter, $D_{am}$	5.2
The diffuser outlet diameter, $D_d$	10
The primary nozzle length, $L_p$	20
The constant-pressure mixing chamber length, $L_{pm}$	11
The constant-area mixing chamber length, $L_{am}$	15
The diffuser length, $L_d$	56

**Table 2.** Boundary conditions for the ejector.

Parameters	Type	Pressure (kPa)	Temperature (K)	
			Superheated Gas	Two-Phase
Primary inlet	Pressure inlet	374.6	290	280
Secondary inlet	Pressure inlet	243.3	278	268
Outlet	Pressure outlet	267.63	-	-

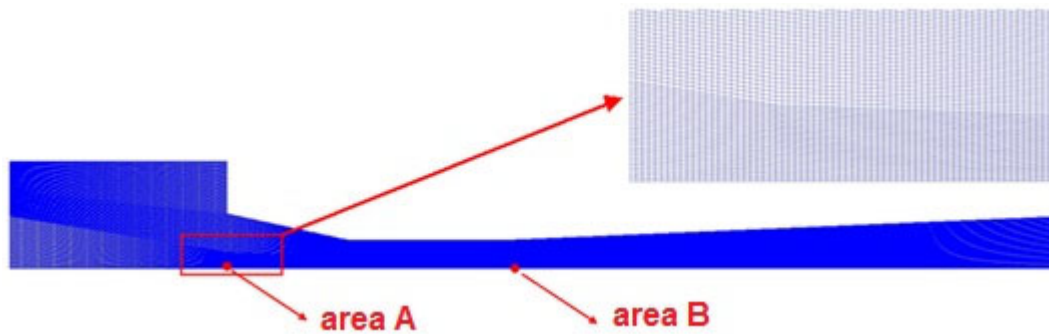
To simulate the complex flow regime, the governing equations are the steady Reynolds Averaged Navier-Stokes equations [34,35].

Fluent 19.0 is used for the simulation. According to Palacz et al. [36], the differences in the results for the 3-D and 2-D models are negligible; therefore, the axisymmetric two-dimensional model is utilized in this CFD simulation. The properties of the working fluid are derived from NIST. Besagni et al. [37], Exposito-Carrillo et al. [38], and Croquer et al. [39] found that the k- $\omega$  SST model generally performed better in simulating the single-phase ejector; however, the realizable k- $\epsilon$  model is employed for two-phase ejector [35]. Meanwhile, near-wall refinement is used in the regions where large pressure and temperature gradient are possible to better capture shock waves and complex internal flow details. In addition, sensitivity analysis on wall treatments is performed and the first grid locates at  $30 < y < 300$ , which gives accurate results [15].

The PRESTO algorithm is applied to pressure-solving. Moreover, the second-order upwind discretization scheme is employed for density, momentum, energy, turbulent kinetic energy, and turbulent dissipation rate solving. All equations are iterated until the residuals are below  $10^{-6}$ . In addition, for an optimization study, consistent convergence of the CFD solution is sometimes difficult, especially when the solution is likely to be quasi-steady-state due to turbulence and the multi-phases. The convergence can often be slow, and the residual can remain stagnating or oscillating above-chosen convergence criteria.

Figure 3 presents the 2-D axisymmetric quadrilateral grid configuration for the baseline ejector. As shown in Figure 3, the pressure and velocity at Point A and Point B are used

to detect the influence of the cell number. Tables 3 and 4 display the grid independence verification results. Pressure and velocity errors with area A and area B are less than 0.5%, indicating that the results are within the acceptable ranges; thus, the medium one with a grid number of 83,100 is selected.



**Figure 3.** Densified meshes of the ejector.

**Table 3.** Mesh sensitivity analysis of area A.

Grid Number	Pressure (Pa)	Error (%)	Velocity ( $\text{m}\cdot\text{s}^{-1}$ )	Error (%)
52,200	274,947	-	120.138	-
68,520	275,288	0.12	119.893	0.2
83,100	275,521	0.085	119.684	0.17
114,880	275,613	0.033	119.623	0.051

**Table 4.** Mesh sensitivity analysis of area B.

Grid Number	Pressure (Pa)	Error (%)	Velocity ( $\text{m}\cdot\text{s}^{-1}$ )	Error (%)
52,200	206,538	-	165.218	-
68,520	206,879	0.165	164.934	0.172
83,100	207,054	0.085	164.841	0.056
114,880	207,123	0.033	164.788	0.032

The CFD model is validated by the void fraction inside the ejector which is based on the experimental results [15]. Take a typical case as an example, when  $\text{LVF}_1$  is 0.1 and  $\text{LVF}_2$  is 0. As shown in Figure 4, the maximum discrepancy is within 7.9%. The maximum deviation of  $\alpha$  for many other ejector dimensions does not exceed 15%; thus, the model can be used in the following simulation.

As for the selection of a convergent nozzle, the comparison between the converging and the converging-diverging nozzle is presented below. For single-phase primary and secondary flow, based on the initial geometries, when the NXP is fixed at 0 mm and primary nozzle diverging section length is varied with 0 mm, 2 mm, 4 mm, and 6 mm, mass flow rates and ER are displayed in Figure 5. It is clear that, with the increase of the divergent section length,  $m_1$  has little change,  $m_2$  decreases significantly, and correspondingly, ER decreases with the increases in divergent section length. Moreover, the corresponding Mach number contours are shown in Figure 6. Hence, the converging nozzle is selected.

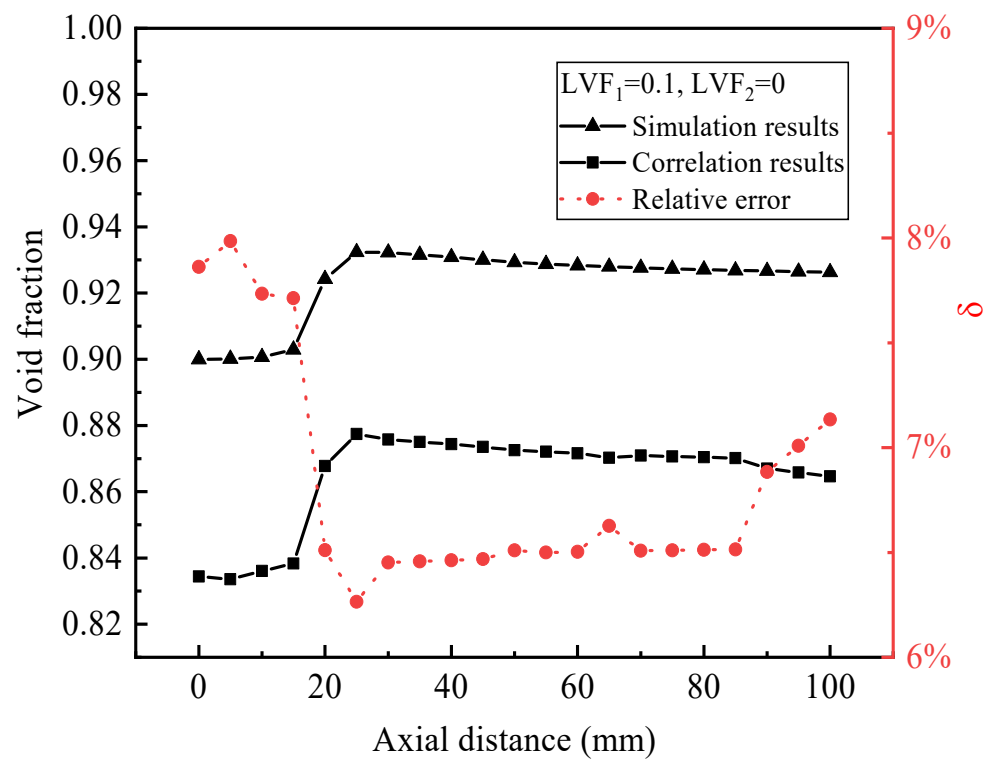


Figure 4. Comparison of  $\alpha$  between simulation and correlation results.

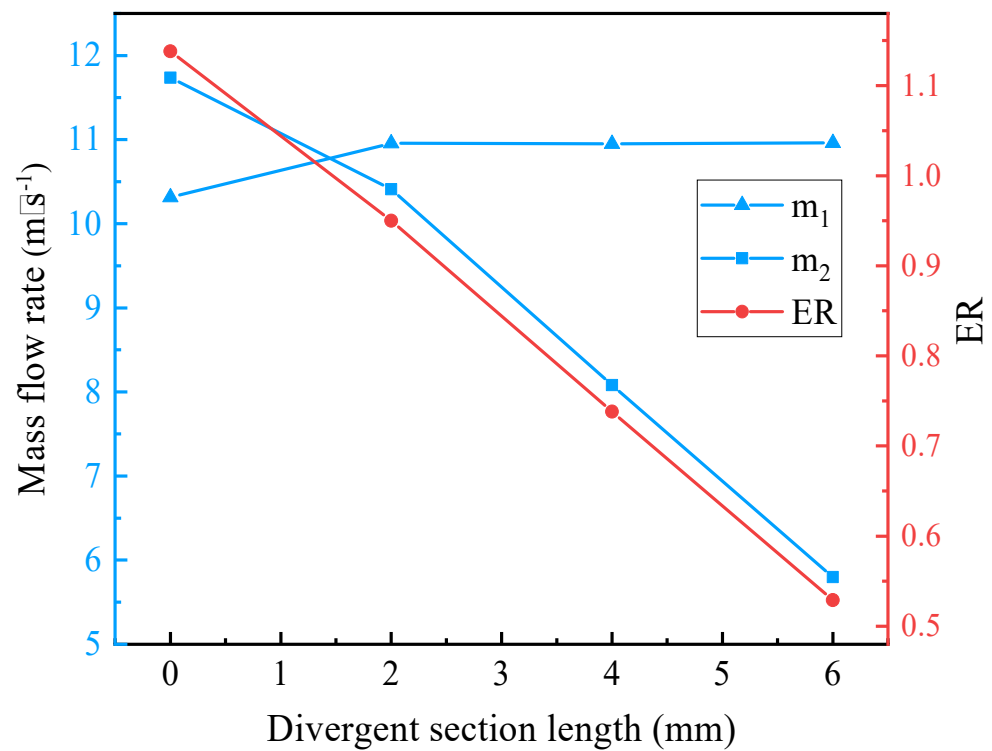
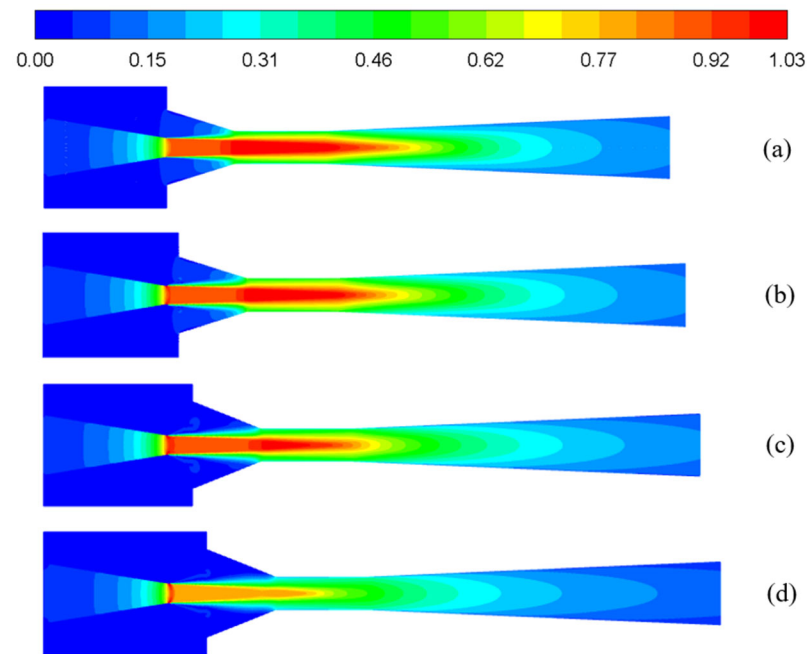


Figure 5. The relation of mass flow rate and ER with diverging section length of the primary nozzle.



**Figure 6.** The Mach number contours under different nozzle diverging section lengths: (a) 0 mm; (b) 2 mm; (c) 4 mm; and (d) 6 mm.

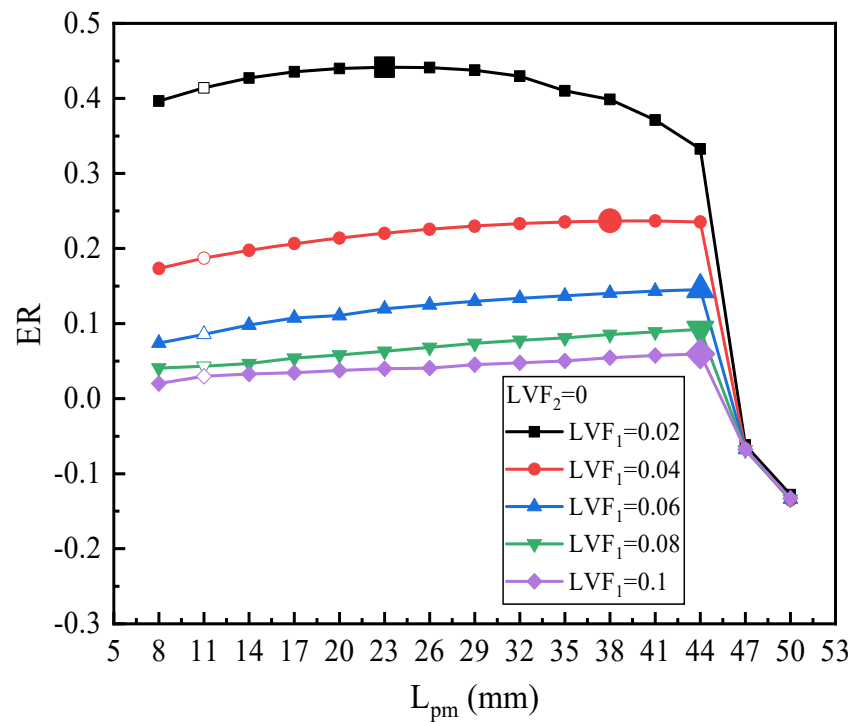
### 3. Results and Discussion

#### 3.1. Optimization of $L_{pm}$

##### 3.1.1. Effect of Two-Phase Primary Flow

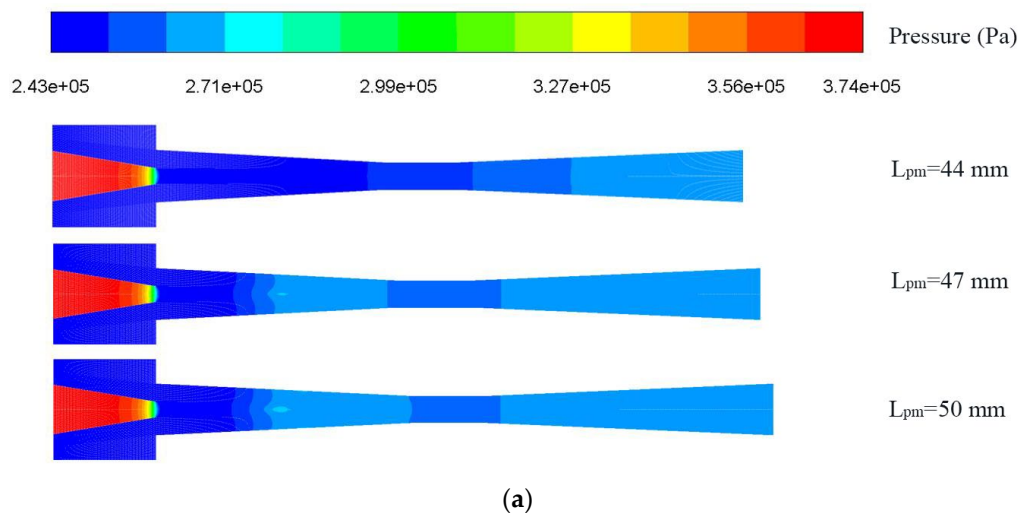
The  $L_{pm}$  is a key design parameter because it determines the mixing efficiency which indicates the ejector performance. Several groups of the  $L_{pm}$  are selected for analysis of the ejector performance under different LVFs of primary flow.

Figure 7 displays the ER with  $L_{pm}$  under  $LVF_2 = 0$  and varied  $LVF_1$  (the unfilled point indicates the baseline ejector model). It can be observed that for different  $LVF_1$ , ER always first rises moderately and then decreases steeply. To be specific, for  $LVF_1$  of 0.02, when  $L_{pm}$  is increased from 8 mm to 50 mm, ER increases and peaks at  $L_{pm}$  of 23 mm which is magnified for the legend. After the peak value, ER drops slowly at first, then it falls suddenly, and even backflow occurs. Similarly, ER under  $LVF_1$  of 0.04 also rises first and then reaches the peak of 0.237 at  $L_{pm} = 38$  mm; the maximum ER increases by 26.58% over the baseline ejector. When  $LVF_1$  are 0.06, 0.08, and 0.1, all the highest ER (0.145, 0.0922, and 0.0596, respectively) are achieved with  $L_{pm}$  of 44 mm. In addition, after the maximum value, the ER decreases suddenly to a negative value. To elucidate the abrupt drop of ER, contours of static pressure and axial static pressure distribution for the  $L_{pm}$  of 44 mm, 47 mm, and 50 mm are displayed in Figure 8a,b, respectively. Note that the amount of secondary fluid mass flow depends on how much pressure drop is induced at the outlet of the primary nozzle. Obviously, for  $L_{pm} = 44$  mm, the static pressure rises smoothly, which can improve ejector performance. While for  $L_{pm}$  of 47 mm and 50 mm, higher pressure is generated, which weakens the ejector performance. When  $L_{pm}$  increases to 50 mm, the area of the high-pressure region increases, which further results in a decrease in ER. In addition, from another perspective, with the increase of  $L_{pm}$ , these two fluids mix more sufficiently, and correspondingly, the entrainment performance is enhanced; however, the increase of  $L_{pm}$  will also lead to the increase of frictional loss. Therefore, ejector performance suddenly decreases as  $L_{pm}$  increases to a certain value. As displayed by the velocity contours in Figure 8c, the energy loss increases largely when  $L_{pm}$  increases from 44 mm to 47 mm. For this purpose,  $L_{pm}$  should not exceed 44 mm for a proper operation of the ejector.



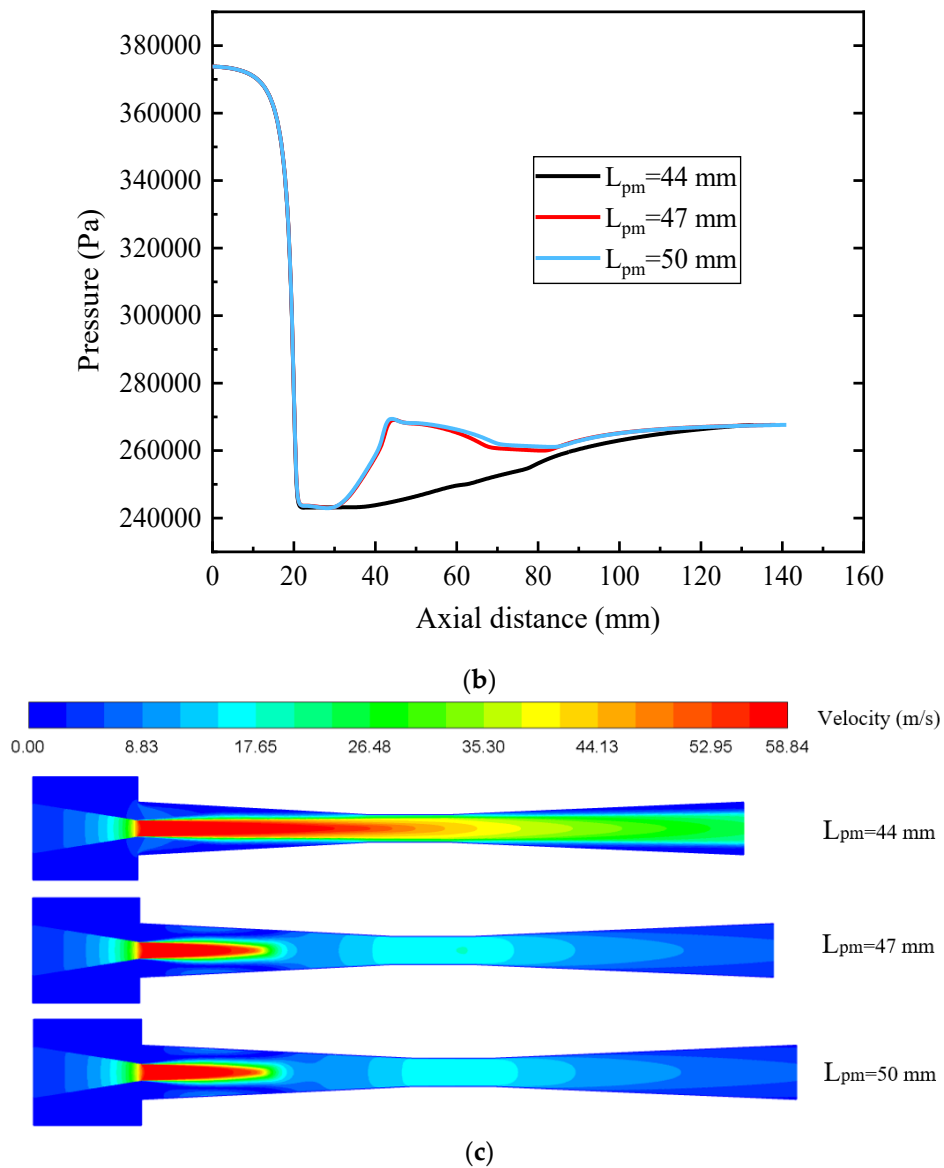
**Figure 7.** Optimization of  $L_{pm}$  on ER under  $LVF_1 = 0.02\sim 0.1$  ( $LVF_2 = 0$ ).

In addition, compared with the baseline ejector model with an  $L_{pm}$  of 11 mm, the ejector under two-phase primary flow operation has a much longer optimal  $L_{pm}$ . That is to say, the optimal  $L_{pm}$  seriously deviates from the baseline ejector model, but when  $L_{pm}$  is more than 44 mm, the performance of the ejector drops drastically, which should be avoided.



**Figure 8.** Cont.



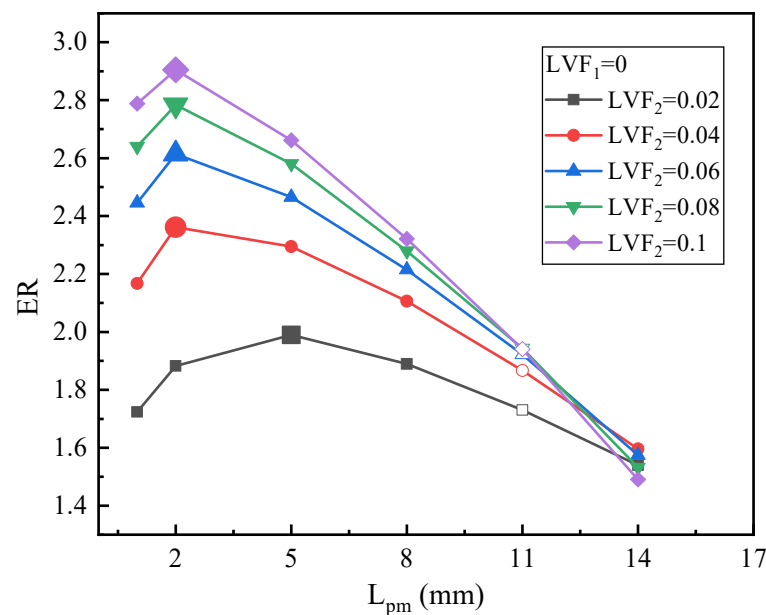


**Figure 8.** Pressure inside the ejector with different  $L_{pm}$  under  $LVF_1 = 0.06$  and  $LVF_2 = 0$ : (a) Contour of static pressure; (b) Static pressure along the centerline; (c) Contour of velocity.

### 3.1.2. Effect of Two-Phase Secondary Flow

Optimization of  $L_{pm}$  under different  $LVF_2$  and fixed  $LVF_1$  of 0 is conducted in this section. Figure 9 portrays the change trends of ER with  $L_{pm}$ . To be specific, when  $LVF_2$  is 0.02, ER first increases and then peaks at 1.99 when  $L_{pm}$  equals 5 mm. That is to say, for  $LVF_2$  of 0.02, there exists an optimal  $L_{pm}$  of 5 mm, which is less than the  $L_{pm}$  of the baseline ejector of 11 mm. When  $LVF_2$  varies from 0.04 to 0.1, all ERs rise first and then decrease with an increase in  $L_{pm}$ . Moreover, as displayed by the magnified point in Figure 9, the optimal  $L_{pm}$  are the same and all equal 2 mm, which is less than the  $L_{pm}$  of the baseline ejector as well. The maximum ERs are 2.36, 2.62, 2.78, and 2.91 for  $LVF_2$  of 0.04, 0.06, 0.08, and 0.1, respectively, or the maximum ER increases with increasing  $LVF_2$ . Therefore, a higher ER is generated with a shorter  $L_{pm}$  under a two-phase secondary flow. Furthermore, it can be found that the optimal  $L_{pm}$  of a two-phase secondary flow is much shorter than the optimal  $L_{pm}$  of a two-phase primary flow.





**Figure 9.** Optimization of  $L_{pm}$  on ER with  $LVF_1 = 0$  and  $LVF_2 = 0.02\sim 0.1$ .

With the results of Sections 3.1.1 and 3.1.2, the optimal  $L_{pm}$  is in the range of 23–44 mm when  $LVF_1 = 0.02\sim 0.1$  and  $LVF_2 = 0$ , and the longest optimal  $L_{pm}$  of 44 mm is obtained at  $LVF_1 = 0.1$  and  $LVF_2 = 0$ . Moreover, the optimal  $L_{pm}$  is in the range of 2–5 mm when  $LVF_2 = 0.02\sim 0.1$  and  $LVF_1 = 0$ , and it can be said that the shortest optimal  $L_{pm}$  of 2 mm is obtained at  $LVF_1 = 0$  and  $LVF_2 = 0.1$ . That is, when the LVF of both inlets are very different, the optimal  $L_{pm}$  also has a striking difference.

### 3.1.3. Effect of Two-Phase Primary and Secondary Flows

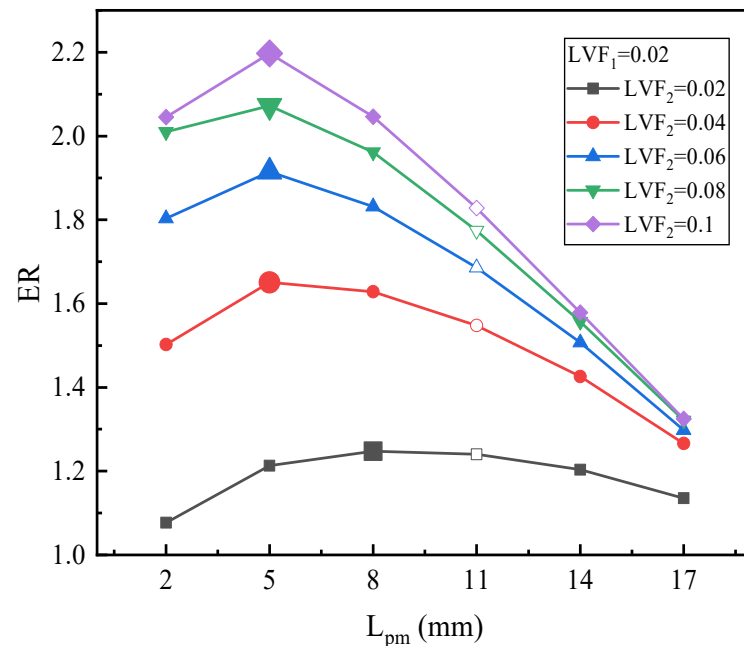
The above two sections are carried out under the circumstance that one of the ejector inlets does not contain liquid. Optimization of  $L_{pm}$  when both the primary and secondary flows contain liquid, by varying the  $LVF_1$  and  $LVF_2$ , respectively, relevant simulation results are given below.

#### (a). Varied $LVF_2$ with fixed $LVF_1$

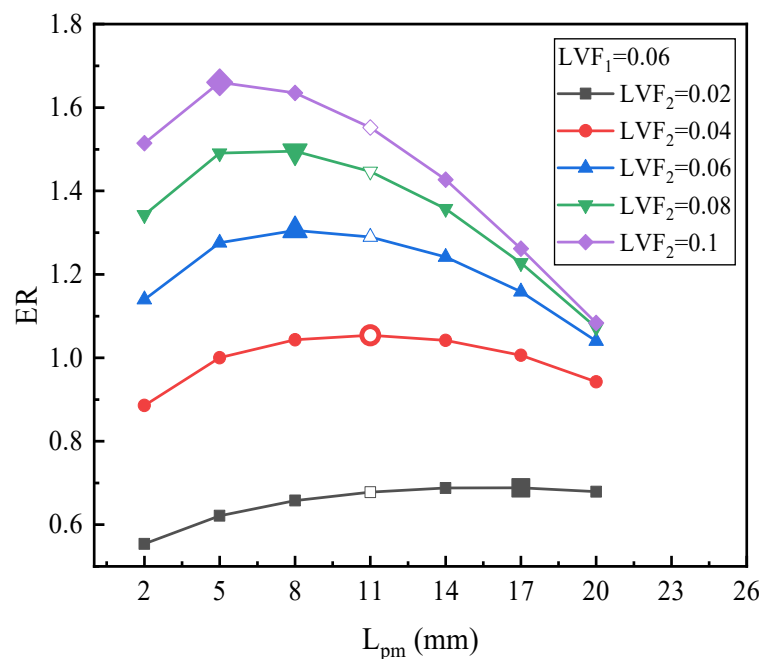
Figure 10 depicts the relationship between  $L_{pm}$  and ER under  $LVF_1 = 0.02$  and  $LVF_2 = 0.02\sim 0.1$ . It is readily found that for diversified  $LVF_2$ , ER always initially increases and then decreases along with the increase of  $L_{pm}$ . When  $LVF_2$  changes from 0.04 to 0.1, the optimal  $L_{pm}$  are all 5 mm, which is less than the  $L_{pm}$  of the baseline ejector. The highest values of ER for  $LVF_2$  from 0.04 to 0.1 are 1.65, 1.91, 2.07, and 2.2, respectively. In addition, in comparison with the baseline ejector, the corresponding maximum ERs increase by 6.64%, 13.58%, 16.81%, and 20.2%, respectively.

Figure 11 is the ER with  $L_{pm}$  under fixed  $LVF_1$  of 0.06 and various  $LVF_2$ . For different  $LVF_2$ , ER always rises first and then consistently reduces along with the increase of  $L_{pm}$ . To be specific, for  $LVF_2$  of 0.02, when  $L_{pm}$  increases from 2 mm to 20 mm, ER increases and arrives at its peak value of 0.68 at the  $L_{pm}$  of 17 mm. Furthermore, the maximum ER increases by 1.54% over the baseline ejector. Similarly, the changing trend of ER for  $LVF_2 = 0.04$  is basically the same as that of  $LVF_2 = 0.02$ . The difference is that the optimal  $L_{pm}$  for  $LVF_2 = 0.04$  is 11 mm, which is less than the  $L_{pm}$  of  $LVF_2 = 0.02$ . For  $LVF_2$  of 0.06 and 0.08, both the peak values of ERs are obtained at the  $L_{pm}$  of 8 mm, which is less than the  $L_{pm}$  of the baseline ejector. Moreover, the maximum ER increases by 1.24% and 3.34%, respectively. As for the  $LVF_2$  of 0.1, the maximum ER is 1.66 with the  $L_{pm} = 5$  mm, and the maximum ER increases by 6.98%. It is worth mentioning that when  $L_{pm}$  deviates from the optimal value, the performance of the ejector will be greatly reduced. Furthermore, it is obviously observed that when  $LVF_2$  increases, the optimal  $L_{pm}$  gets smaller. Compared

with Figure 10, it can also be found that when  $LVF_1$  increases from 0.02 to 0.06, for each  $LVF_2$ , the optimal  $L_{pm}$  increases a little.



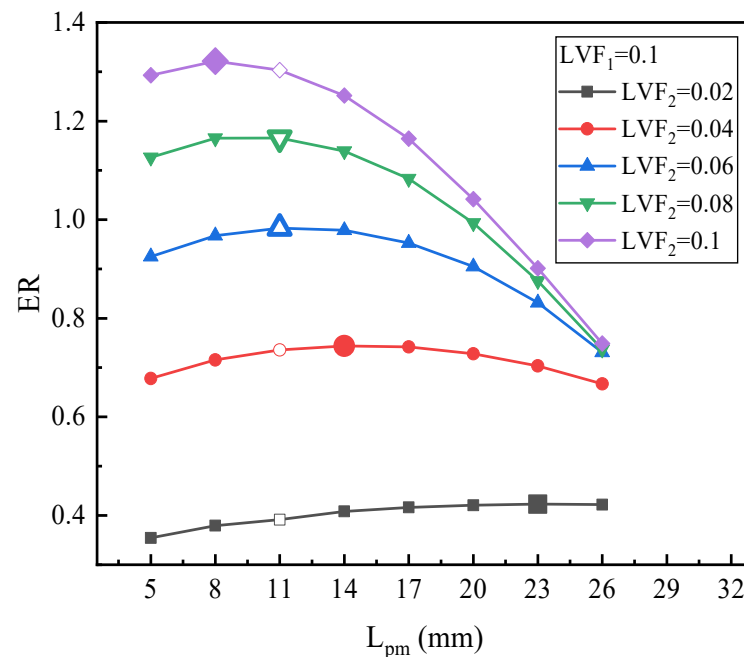
**Figure 10.** The relation of ER with  $L_{pm}$  under  $LVF_1 = 0.02$  and  $LVF_2 = 0.02\sim 0.1$ .



**Figure 11.** The relation of ER with  $L_{pm}$  under  $LVF_1 = 0.06$  and  $LVF_2 = 0.02\sim 0.1$ .

Figure 12 illustrates the changing trend of ER with  $L_{pm}$  under fixed  $LVF_1$  of 0.1 and various  $LVF_2$ . For  $LVF_2$  of 0.02, the maximum ER is 0.423 with  $L_{pm} = 23$  mm, which increases by 9.59%. For  $LVF_2$  of 0.04, the highest value of ER, 0.744, is achieved at the  $L_{pm}$  of 14 mm. Both for  $LVF_2$  of 0.06 and 0.08, the maximum ERs (0.983 and 1.166, respectively) are obtained when  $L_{pm}$  reaches 11 mm. Moreover, similar to Figure 10, as  $LVF_2$  increases from 0.02 to 0.1, the optimal  $L_{pm}$  is reduced gradually, since the optimal  $L_{pm}$  is 23 mm, 14 mm, 11 mm, 11 mm, and 8 mm, respectively. However, compared with Figure 10, namely when

$LVF_1$  increases from 0.06 to 0.1, for each fixed  $LVF_2$ , each optimal  $L_{pm}$  increases slightly, but the maximum ER drops.



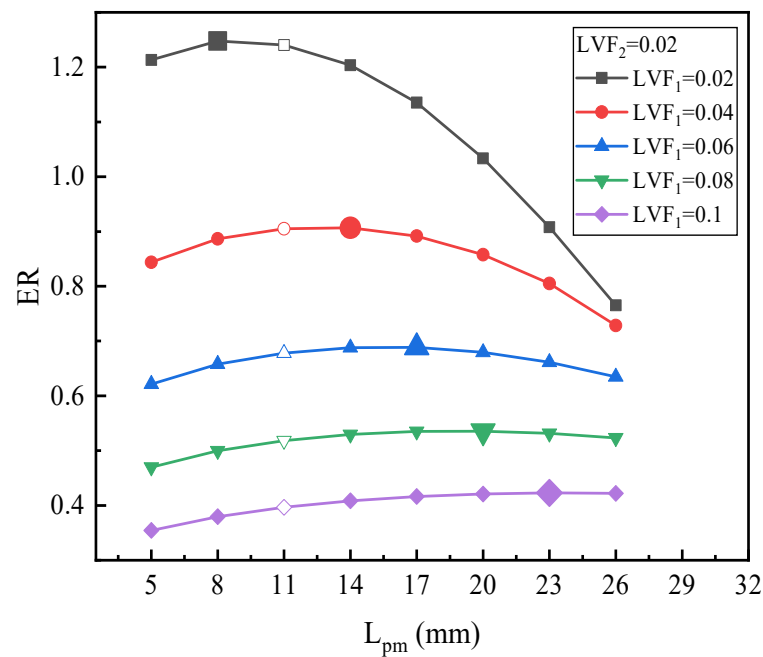
**Figure 12.** The relation of ER with  $L_{pm}$  under  $LVF_1 = 0.1$  and various  $LVF_2$ .

In general, with the results of Figures 10–12, it can be concluded that: (1) for each fixed  $LVF_1$ , when  $LVF_2$  increases from 0.02 to 0.1, the optimal  $L_{pm}$  decreases to different degrees; (2) the optimal  $L_{pm}$  is in 5–23 mm; (3) with the increases of  $LVF_1$ , the optimal  $L_{pm}$  generally increases; (4) combined with the operating condition of two-phase primary flow ( $LVF_2 = 0.02 \sim 0.1$ ) as presented in Section 3.1.2, the optimal  $L_{pm}$  and ER decrease with an increase of  $LVF_1$ .

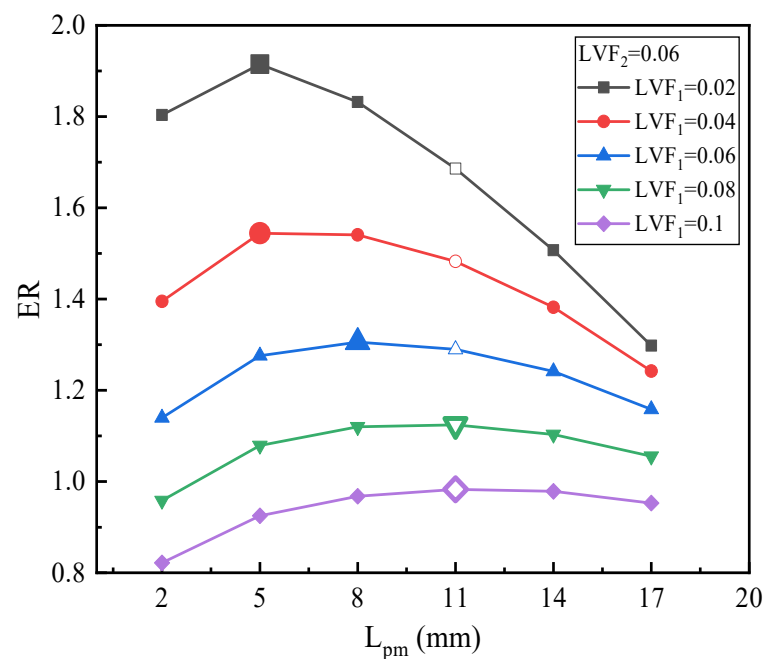
(b). Varied  $LVF_1$  with fixed  $LVF_2$

Figure 13 is the ER with  $L_{pm}$  under fixed  $LVF_2$  of 0.02 and various  $LVF_1$ . Specifically speaking, for  $LVF_1$  of 0.02, the ER reaches the peak value of 1.248 at  $L_{pm} = 8$  mm. The maximum ER increases by 0.61% compared with the baseline ejector. In terms of  $LVF_1 = 0.04$ , the ER increases slightly from 0.844 to 0.907, after the highest value, ER drops gradually, and the optimal  $L_{pm}$  is 14 mm in this condition. When  $LVF_1$  is in the range of 0.06 to 0.1, as  $L_{pm}$  increases, the increments of the ER do not change a lot. The optimal  $L_{pm}$  are 17 mm, 20 mm, and 23 mm for  $LVF_1$  of 0.06, 0.08, and 0.1, respectively. The corresponding maximum ER increases by 1.54%, 3.34%, and 6.65%, respectively. Generally speaking, for  $LVF_2$  of 0.02, as  $LVF_1$  varies from 0.02 to 0.1, the optimal  $L_{pm}$ , as displayed by the magnified point in Figure 13, becomes larger and larger.

Figure 14 depicts the effect of  $L_{pm}$  on the ER under fixed  $LVF_2$  of 0.06 and various  $LVF_1$ . ERs always increase initially and then decrease. To be specific, for  $LVF_1$  of 0.02 and 0.04, both the ERs obtain the maximum value (1.915 and 1.544, respectively) at the  $L_{pm}$  of 5 mm, and the maximum ER increases by 13.58% and 4.17%, respectively. When  $LVF_1$  changes from 0.08 to 0.1, ER increases along with the increase of  $L_{pm}$  and obtain the maximum of 1.12 and 0.98, respectively, both the optimum  $L_{pm}$  are 11 mm. Overall, when  $LVF_1$  changes from 0.02 to 0.1, the optimal  $L_{pm}$  increases gradually, but all the optimal  $L_{pm}$  are no more than the  $L_{pm}$  of the baseline ejector. Compared with  $LVF_1 = 0.02$  as displayed in Figure 13, when  $LVF_2$  is 0.06, for each  $LVF_1$ , all the maximum ERs increase, but optimal  $L_{pm}$  decrease.

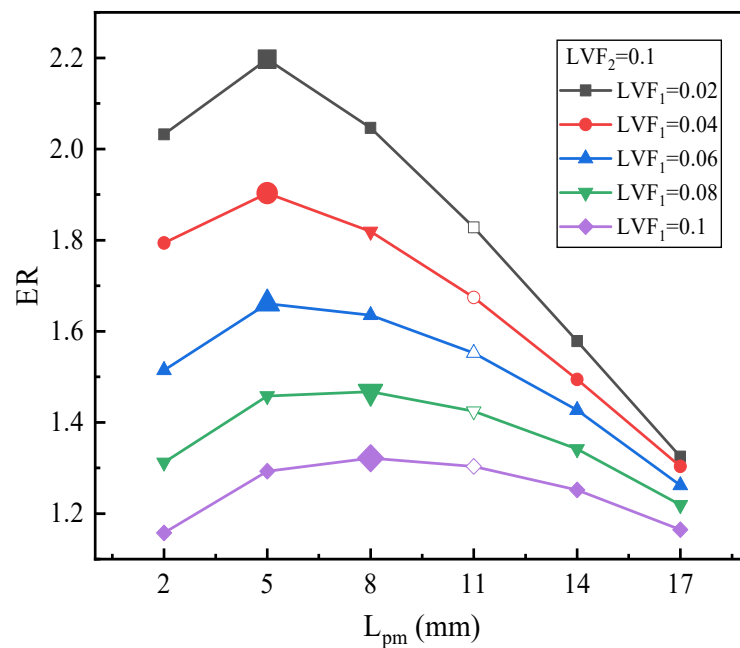


**Figure 13.** The relation of ER with  $L_{pm}$  under  $L_{VF2} = 0.02$  and  $L_{VF1} = 0.02 \sim 0.1$ .



**Figure 14.** The relation of ER with  $L_{pm}$  under  $L_{VF2} = 0.06$  and  $L_{VF1} = 0.02 \sim 0.1$ .

Figure 15 displays the impact of  $L_{pm}$  on the ER under  $L_{VF2} = 0.1$  and various  $L_{VF1}$ . The results reveal that all the Ers follow a similar pattern, namely, they increase first and then decrease with the growth of  $L_{pm}$ . For  $L_{VF1}$  varied from 0.02 to 0.06, the maximum Ers (2.2, 1.9, and 1.66, respectively) are all achieved at the  $L_{pm}$  of 5 mm, which is slightly less than the baseline ejector. The maximum ER has an increase of 20.2%, 13.68%, and 6.98%, respectively. Moreover, when  $L_{VF1}$  increases from 0.08 to 0.1, the optimal  $L_{pm}$  increases to 8 mm. The corresponding maximum ERs are 1.47 and 1.32 for  $L_{VF1}$  of 0.08 and 0.1, respectively. In addition, the maximum ER increases by 3.01% and 1.4%, respectively. It is noteworthy that for fixed  $L_{VF2}$  of 0.1 and various  $L_{VF1}$ , all the optimal  $L_{pm}$  are less than 11 mm. Compared with Figure 14 in which  $L_{VF2}$  is 0.06, for each  $L_{VF1}$ , the maximum ER increases. Moreover, for  $L_{VF1} = 0.06 \sim 0.1$ , the optimal  $L_{pm}$  also increases.



**Figure 15.** The variation of ER with  $L_{pm}$  under  $LVF_2 = 0.1$  and  $LVF_1 = 0.02\sim 0.1$ .

Overall, from Figures 13–15, it can be inferred that: (1) for each fixed  $LVF_2$ , the optimal  $L_{pm}$  increases with the growth of  $LVF_1$ ; (2) with the increase of  $LVF_2$ , the optimal  $L_{pm}$  is generally reduced; (3) when both  $LVF_1$  and  $LVF_2$  are in the range of 0.02–0.1, the optimal  $L_{pm}$  is in the range of 5–23 mm; (4) and, combined with Figure 6 in which  $LVF_2$  is 0, it can also be concluded that when  $LVF_1$  is fixed in the range of 0–0.1, the optimal  $L_{pm}$  improves with the growth of  $LVF_1$ , and the ER rises with the rise of  $LVF_2$ .

### 3.2. Optimization of $L_{am}$

Based on the optimal  $L_{pm}$  determined in Section 3.1, the following simulations are performed to seek the optimal  $L_{am}$ .

#### 3.2.1. Effect of Two-Phase Primary Flow

Figure 16 reveals the influence of  $L_{am}$  on ER under various  $LVF_1$  ( $LVF_2 = 0$ ). For  $LVF_1$  of 0.02 and 0.04, when  $L_{am}$  increases from 9 mm to 24 mm, the influence of  $L_{am}$  is not evident. The ER for  $LVF_1 = 0.02$  increases from 0.438 at the  $L_{am}$  of 9 mm to the maximum of 0.442 at the  $L_{am}$  of 18 mm and then drops. For  $LVF_1 = 0.04$ , the ER rises first and reaches the maximum of 0.24 at  $L_{am} = 15$  mm and then drops gradually. The optimal  $L_{am}$  for  $LVF_1$  of 0.02 and 0.04 are 18 mm and 15 mm, respectively. For  $LVF_1$  of 0.06 and 0.08, the optimal  $L_{am}$  are both 15 mm. Nonetheless, when  $L_{am}$  exceeds 15 mm, ER decreases abruptly. For  $LVF_1$  of 0.1, the peak value of ER is 0.064 at the  $L_{am}$  of 18 mm, which means the  $LVF_1 = 0.1$  has a more evident effect on the ER, the reason is that the liquid density is much higher than the vapor density. Likewise, after the peak value, ER drops suddenly. To avoid the malfunction of the ejector, the  $L_{am}$  should not exceed 15 mm, and the primary flow should not contain liquid. To identify the cause for the abrupt decrease, contours of static pressure, axial static pressure distribution, velocity contours, and the velocity vector field are displayed in Figure 17a–d, respectively. It can be observed from Figure 17a,b that the static pressure monotonically increases in the mixing chamber when  $L_{am}$  is 15 mm and 18 mm. In addition, when  $L_{am}$  rises to 21 mm, the mixed fluids have a momentum drop since the increase of the resistance weakens the ejector performance. In other words, when the friction loss caused by the increase of  $L_{am}$  exceeds the performance enhanced by the effect of more sufficient mixing, the ejector performance will decrease. Moreover, reflux occurs as illustrated in Figure 17d.

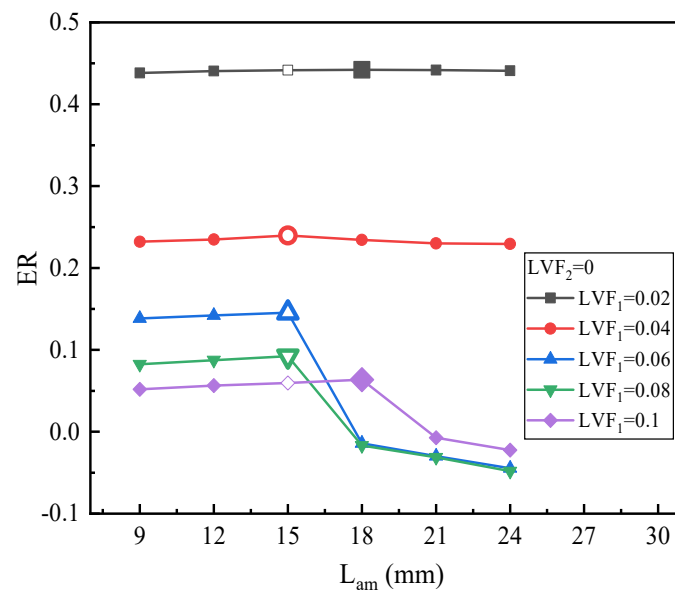


Figure 16. ER with  $L_{am}$  under  $LVF_1 = 0.02 \sim 0.1$  ( $LVF_2 = 0$ ).

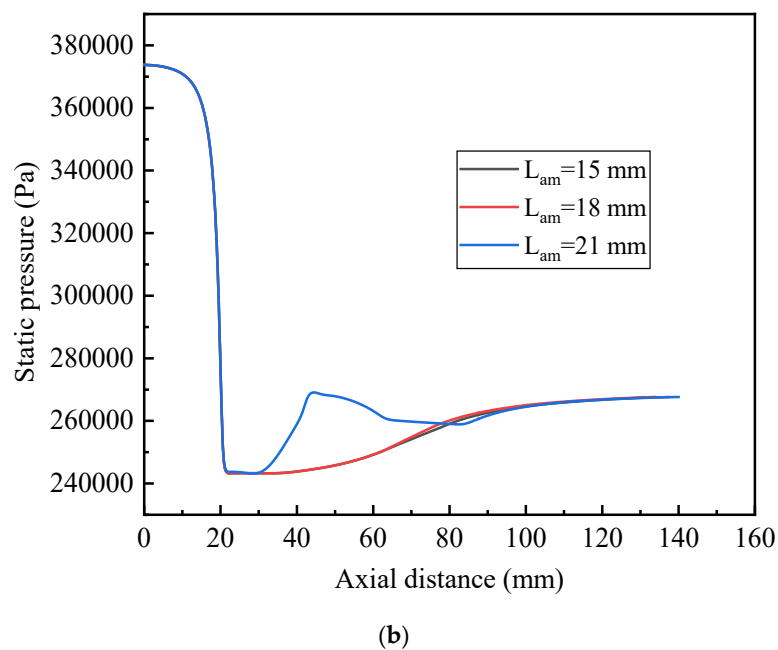
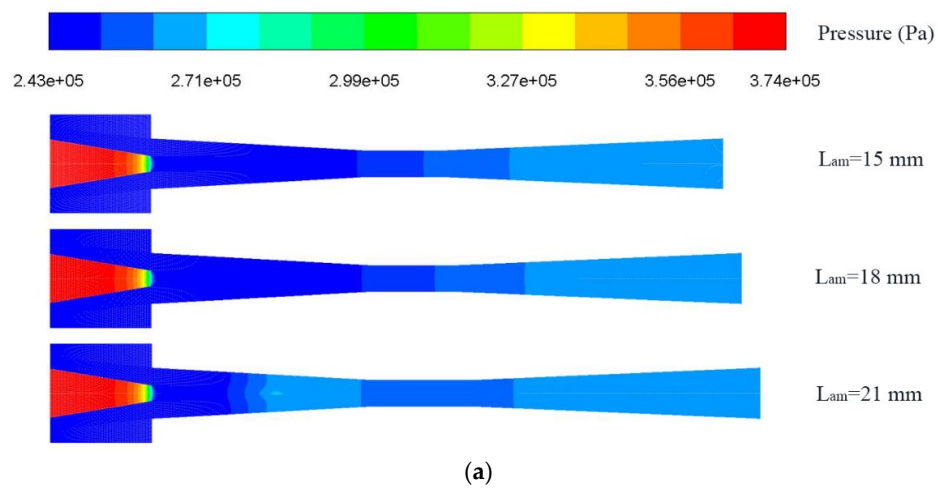
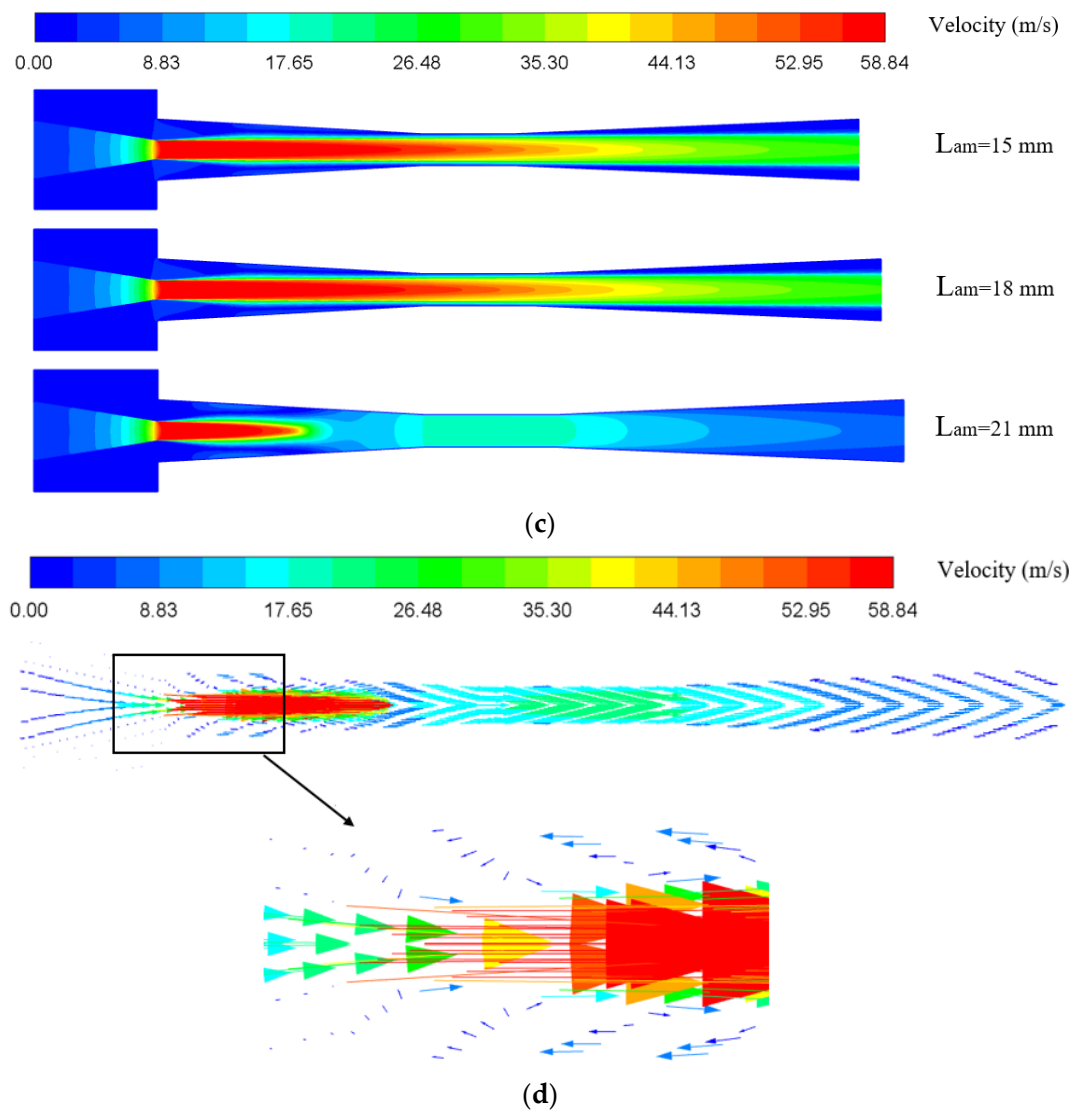


Figure 17. Cont.

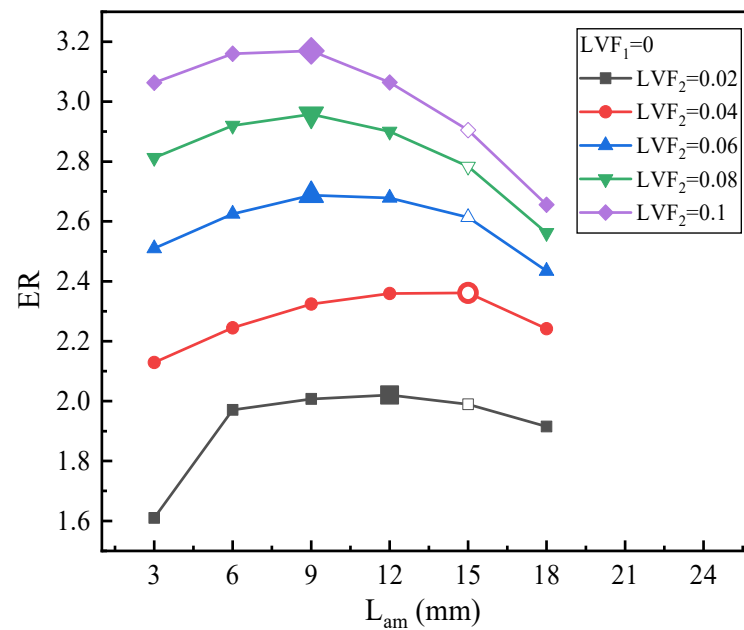


**Figure 17.** Pressure inside the ejector with different  $L_{am}$  under  $LVF_1 = 0.1$  and  $LVF_2 = 0$ : (a) Contour of static pressure; (b) Static pressure along the centerline; (c) Contour of velocity and (d) Velocity vector field of  $L_{am} = 21$  mm.

### 3.2.2. Effect of Two-Phase Secondary Flow

Figure 18 displays the effect of  $L_{am}$  on ER under fixed  $LVF_1$  of 0 and various  $LVF_2$ . Obviously, under all the  $LVF_2$ , ER increases first and then decreases. Nevertheless, for various  $LVF_2$ , the optimal  $L_{am}$  is not always the same. Specifically, for  $LVF_2 = 0.02$ , the maximum ER of 2.02 peaks at the  $L_{am}$  of 12 mm. For  $LVF_2 = 0.04$ , the optimal  $L_{am}$  of 15 mm is the same as that of the baseline ejector. When  $LVF_2$  is in the range of 0.06–0.1, the optimal  $L_{am}$  is at 9 mm.



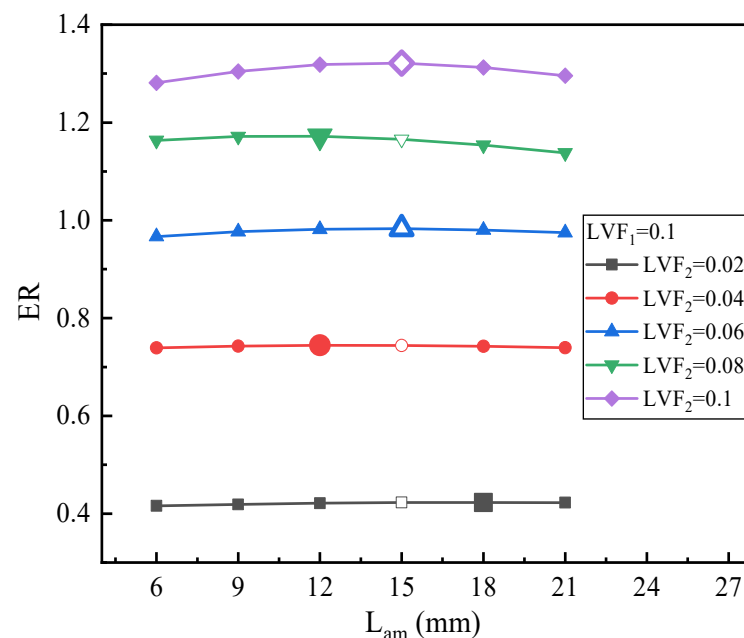


**Figure 18.** ER with  $L_{am}$  under  $LVF_2 = 0.02\sim 0.1$  ( $LVF_1 = 0$ ).

### 3.2.3. Effect of Two-Phase Primary and Secondary Flows

All the  $L_{am}$  are optimized under  $LVF_1 = 0.02\sim 0.1$  and  $LVF_2 = 0.02\sim 0.1$  with an interval of 0.02. Considering the limited space, only two cases ( $LVF_1 = 0.1$  and  $LVF_2 = 0.02\sim 0.1$ ,  $LVF_2 = 0.1$  and  $LVF_1 = 0.02\sim 0.1$ ) are displayed here.

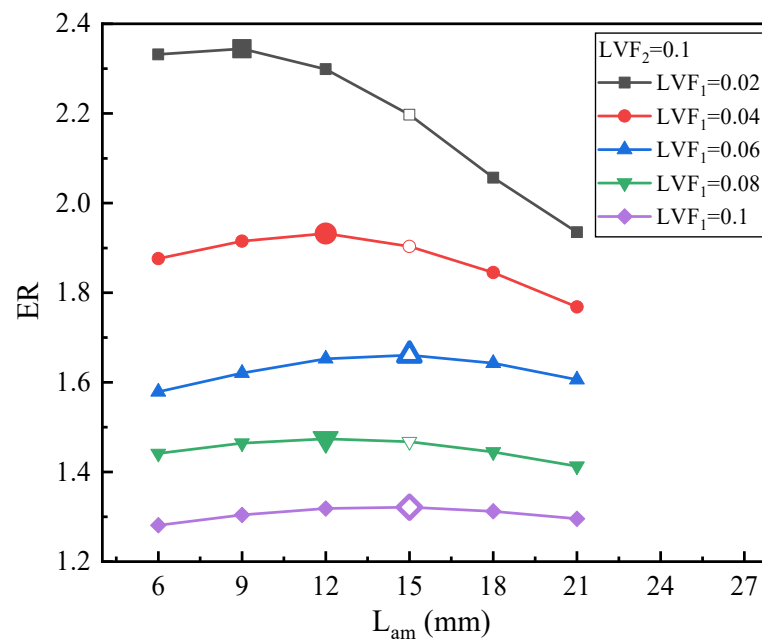
Figure 19 displays the effect of  $L_{am}$  on ER under fixed  $LVF_1$  of 0.1 and various  $LVF_2$  (0.02–0.1). When  $L_{am}$  increases from 6 mm to 21 mm, for a fixed  $LVF_2$ , the optimal  $L_{am}$  can be achieved.



**Figure 19.** The relation of ER with  $L_{am}$  under  $LVF_1 = 0.1$  and  $LVF_2 = 0.02\sim 0.1$ .

Figure 20 presents the effect of  $L_{am}$  on ER under fixed  $LVF_2$  of 0.1 and various  $LVF_1$  (0.02–0.1). Obviously, for  $LVF_1 = 0.02, 0.04$ , and  $0.06$ , it can be seen that the change in ER is relatively evident, while for  $LVF_1 = 0.08$  and  $0.1$ , the change in ER is pretty small. The

results are similar to the variation of the optimal  $L_{am}$  with LVF in Figures 16, 18 and 19, namely the changing trend of optimal  $L_{am}$  is irregular.



**Figure 20.** The relation of ER with  $L_{am}$  under  $LVF_2 = 0.1$  and  $LVF_1 = 0.02\sim 0.1$ .

In addition, the results of optimal  $L_{am}$  and ER under other LVF are presented in Tables 5 and 6.

**Table 5.** Results of optimal  $L_{am}$  and maximum ER under varied  $LVF_1$  for a given  $LVF_2$ .

	$LVF_2 = 0$ (ER)	$LVF_2 = 0.02$ (ER)	$LVF_2 = 0.06$ (ER)	$LVF_2 = 0.1$ (ER)
$LVF_1 = 0.02$	18 (0.442)	15 (1.248)	12 (1.941)	9 (2.344)
$LVF_1 = 0.04$	21 (0.24)	9 (0.912)	15 (1.544)	12 (1.932)
$LVF_1 = 0.06$	15 (0.145)	6 (0.693)	15 (1.306)	15 (1.661)
$LVF_1 = 0.08$	15 (0.092)	12 (0.536)	12 (1.128)	12 (1.474)
$LVF_1 = 0.1$	18 (0.065)	18 (0.423)	15 (0.983)	15 (1.321)

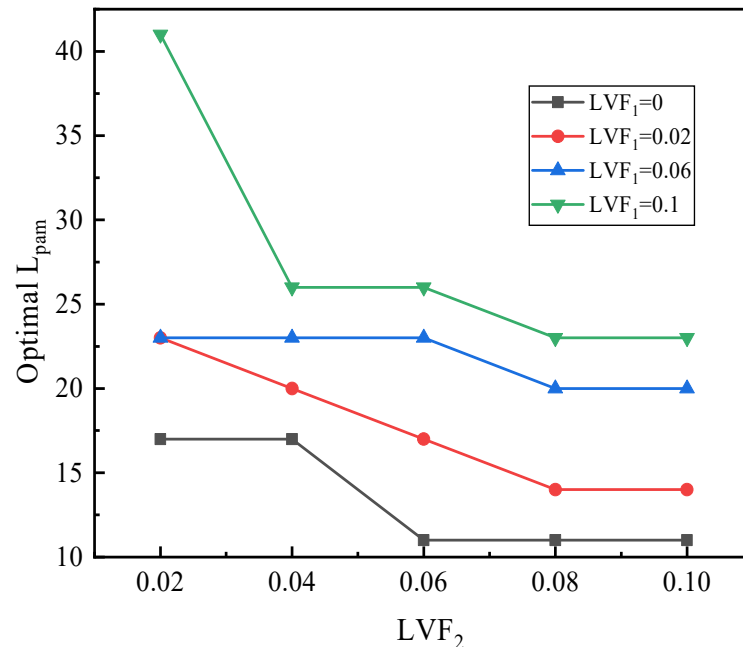
**Table 6.** Results of optimal  $L_{am}$  and maximum ER under varied  $LVF_2$  for a given  $LVF_1$ .

	$LVF_1 = 0$ (ER)	$LVF_1 = 0.02$ (ER)	$LVF_1 = 0.06$ (ER)	$LVF_1 = 0.1$ (ER)
$LVF_2 = 0.02$	12 (2.02)	15 (1.248)	6 (0.693)	18 (0.423)
$LVF_2 = 0.04$	15 (2.362)	15 (1.651)	12 (1.055)	12 (0.744)
$LVF_2 = 0.06$	9 (2.687)	12 (1.941)	15 (1.306)	15 (0.983)
$LVF_2 = 0.08$	9 (2.958)	9 (2.158)	12 (1.504)	12 (1.172)
$LVF_2 = 0.1$	9 (3.17)	9 (2.344)	15 (1.661)	15 (1.321)

With the results of Section 3.2, it can be found that the relation of optimal  $L_{am}$  with  $LVF_1$  and  $LVF_2$  is irregular since optimal  $L_{am}$  is influenced by optimal  $L_{pm}$ . When the optimal  $L_{pm}$  is more than 8 mm, the optimization of  $L_{am}$  is not evident, or the influence of  $L_{am}$  is not distinct. Nevertheless, when the optimal  $L_{pm}$  is less than 8 mm, the influence of  $L_{am}$  will be significant. The optimum  $L_{am}$  are in the range of 6–21 mm, and they do not deviate much from the  $L_{am}$  of the baseline ejector model (15 mm).

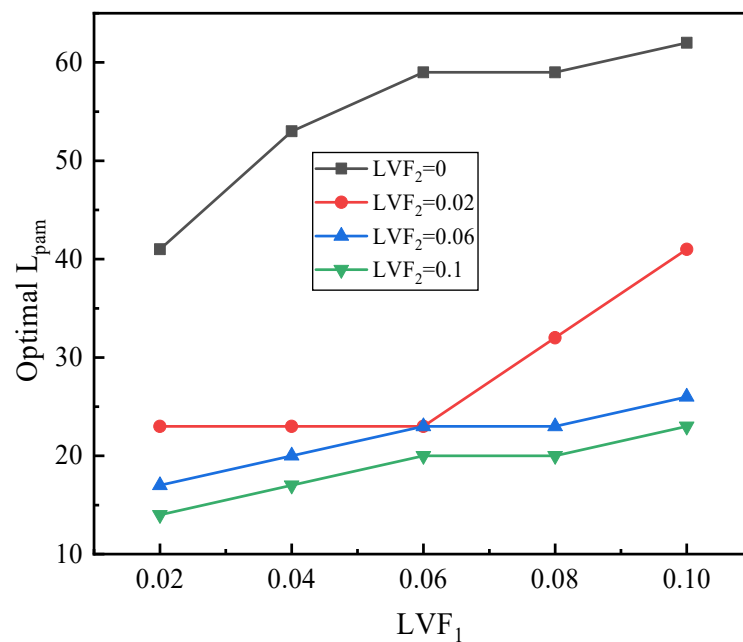
### 3.3. A Combination of Optimal $L_{pm}$ and $L_{am}$

Figure 21 depicts the relation of the sum of optimal  $L_{pm}$  and  $L_{am}$  ( $L_{pam}$ ) with  $LVF_2$  under changed  $LVF_1$ . It can be observed that for each  $LVF_1$ , the optimal  $L_{pam}$  decreases with  $LVF_2$ . Furthermore, the optimal  $L_{pam}$  increases with  $LVF_1$ .



**Figure 21.** The relation of optimal  $L_{pam}$  with  $LVF_2$  under different  $LVF_1$ .

Figure 22 indicates the relation of the sum of optimal  $L_{pm}$  and  $L_{am}$  with  $LVF_1$  under different  $LVF_2$ . Generally speaking, the optimal  $L_{pam}$  increases with  $LVF_1$  but reduces with  $LVF_2$ , and the relation between optimal  $L_{pm}$  and  $L_{pam}$  is regular.



**Figure 22.** The relation of optimal  $L_{pam}$  with  $LVF_1$  under given  $LVF_2$ .

#### 4. Conclusions

This paper numerically optimizes two mixing chamber geometries of a two-phase ejector under various primary and secondary inlet LVFs. The most important findings are given below:

- (1) When the primary inlet of the ejector contains liquid while the secondary inlet does not, the optimal  $L_{pm}$  and  $L_{am}$  are ranged between 23–44 mm and 15–18 mm. When the secondary inlet contains liquid while primary inlet does not, these two optimal lengths are ranged 2–5 mm and 9–15 mm, while when both the primary inlet and secondary inlet contain liquid, they are in the range of 5–23 mm and 6–18 mm, respectively. Thus, two mixing chamber lengths largely depend on the vapor or liquid state of the two inlets;
- (2) When primary inlet LVF is fixed and secondary inlet LVF increases from 0 to 0.1, the optimal  $L_{pm}$  decreases along with the growth of secondary inlet LVF; when secondary inlet LVF is fixed and primary inlet LVF varies from 0 to 0.1, the optimal  $L_{pm}$  increases along with the growth of primary inlet LVF;
- (3) The sum of optimal  $L_{pm}$  and optimal  $L_{am}$  increases with the increase of primary inlet LVF but decreases with the increase of secondary inlet LVF.

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#### Nomenclature

$L_{pm}$	constant-pressure mixing chamber length, mm
$L_{am}$	constant-area mixing chamber length, mm
$L_{pam}$	sum of mixing chamber length, mm
$P$	pressure, kPa
$T$	temperature, K or °C
$m_1$	primary mass flow rate, $g \cdot s^{-1}$
$m_2$	secondary mass flow rate, $g \cdot s^{-1}$
$\chi$	quality
$\alpha$	void fraction
AR	area ratio
ER	entrainment ratio
PRR	pressure recovery ratio
$LVF_1$	liquid volume fraction of primary flow
$LVF_2$	liquid volume fraction of secondary flow
NXP	nozzle exit position
MERS	multi-evaporator refrigeration system

#### References

1. Besagni, G.; Mereu, R.; Inzoli, F. Ejector refrigeration: A comprehensive review. *Renew. Sustain. Energy Rev.* **2016**, *53*, 373–407. [[CrossRef](#)]
2. Wang, J.; Qv, D.; Yao, Y.; Ni, L. The difference between vapor injection cycle with flash tank and intermediate heat exchanger for air source heat pump: An experimental and theoretical study. *Energy* **2021**, *221*, 119796. [[CrossRef](#)]
3. Cuong, L.N.; Oh, J.T. The Comparison of Experiment Results and CFD Simulation in the Heat Pump System Using Thermobank and Two-Phase Ejector for Heating Room and Cold Storage. *Int. J. Air-Cond. Refrig.* **2016**, *24*, 1650004. [[CrossRef](#)]

4. Shi, Y.; Guo, X.; Zhang, X. Study on Economized Vapor Injection Heat Pump System Using Refrigerant R32. *Int. J. Air-Cond. Refrig.* **2016**, *24*, 1650006. [\[CrossRef\]](#)
5. Gullo, P.; Kærn, M.R.; Haida, M.; Smolka, J.; Elbel, S. A review on current status of capacity control techniques for two-phase ejectors. *Int. J. Refrig.* **2020**, *119*, 64–79. [\[CrossRef\]](#)
6. Chen, Q.; Hwang, Y.; Yan, G.; Yu, J. Theoretical investigation on the performance of an ejector enhanced refrigeration cycle using hydrocarbon mixture R290/R600a. *Appl. Therm. Eng.* **2020**, *164*, 114456. [\[CrossRef\]](#)
7. Dokandari, D.A.; Khoshkhoo, R.H.; Bidi, M.; Mafi, M. Thermodynamic investigation and optimization of two novel combined power-refrigeration cycles using cryogenic LNG energy. *Int. J. Refrig.* **2021**, *124*, 167–183. [\[CrossRef\]](#)
8. Barta, R.B.; Dhillon, P.; Braun, J.E.; Ziviani, D.; Groll, E.A. Design and Optimization Strategy for Ejectors Applied in Refrigeration Cycles. *Appl. Therm. Eng.* **2021**, *189*, 116682. [\[CrossRef\]](#)
9. Liu, J.; Lin, Z. A novel dual-temperature ejector-compression heat pump cycle-exergetic and economic analyses. *Int. J. Refrig.* **2021**, *126*, 155–167. [\[CrossRef\]](#)
10. Elliott, M.S.; Rasmussen, B.P. Decentralized model predictive control of a multi-evaporator air conditioning system. *Control Eng. Pract.* **2013**, *21*, 1665–1677. [\[CrossRef\]](#)
11. Li, C.; Yan, J.; Li, Y.; Cai, W.; Lin, C.; Chen, H. Experimental study on a multi-evaporator refrigeration system with variable area ratio ejector. *Appl. Therm. Eng.* **2016**, *102*, 196–203. [\[CrossRef\]](#)
12. Li, S.; Yan, J.; Liu, Z.; Yao, Y.; Li, X.; Wen, N.; Zou, G. Optimization on crucial ejector geometries in a multi-evaporator refrigeration system for tropical region refrigerated trucks. *Energy* **2019**, *189*, 116347. [\[CrossRef\]](#)
13. Yan, J.; Li, S.; Li, R. Numerical study on the auxiliary entrainment performance of an ejector with different area ratio. *Appl. Therm. Eng.* **2020**, *185*, 116369. [\[CrossRef\]](#)
14. Wen, N.; Wang, L.; Yan, J.; Li, X.; Liu, Z.; Li, S.; Zou, G. Effects of operating conditions and cooling loads on two-stage ejector performances. *Appl. Therm. Eng.* **2019**, *150*, 770–780. [\[CrossRef\]](#)
15. Wen, H.; Yan, J.; Li, X. Influence of liquid volume fraction on ejector performance: A numerical study. *Appl. Therm. Eng.* **2021**, *190*, 116845. [\[CrossRef\]](#)
16. Kumar, V.; Sachdeva, G. 1-D model for finding geometry of a single phase ejector. *Energy* **2018**, *165*, 75–92. [\[CrossRef\]](#)
17. Ramesh, A.S.; Sekhar, S.J. Experimental and numerical investigations on the effect of suction chamber angle and nozzle exit position of a steam-jet ejector. *Energy* **2018**, *164*, 1097–1113. [\[CrossRef\]](#)
18. Palacz, M.; Haida, M.; Smolka, J.; Nowak, A.J.; Banasiak, K.; Hafner, A. HEM and HRM accuracy comparison for the simulation of CO<sub>2</sub> expansion in two-phase ejectors for supermarket refrigeration systems. *Appl. Therm. Eng.* **2017**, *115*, 160–169. [\[CrossRef\]](#)
19. Aidoun, Z.; Ameer, K.; Falsafioon, M.; Badache, M. Current advances in ejector modeling, experimentation and applications for refrigeration and heat pumps. Part 2: Two-phase ejectors. *Inventions* **2019**, *4*, 16. [\[CrossRef\]](#)
20. Fu, W.; Li, Y.; Liu, Z.; Wu, H.; Wu, T. Numerical study for the influences of primary nozzle on steam ejector performance. *Appl. Therm. Eng.* **2016**, *106*, 1148–1156. [\[CrossRef\]](#)
21. Chunnanond, K.; Aphornratana, S. Ejectors: Applications in refrigeration technology. *Renew. Sustain. Energy Rev.* **2004**, *8*, 129–155. [\[CrossRef\]](#)
22. Jeon, Y.; Kim, D.; Jung, J.; Jang, D.S.; Kim, Y. Comparative performance evaluation of conventional and condenser outlet split ejector-based domestic refrigerator-freezers using R600a. *Energy* **2018**, *161*, 1085–1095. [\[CrossRef\]](#)
23. Tang, Y.; Liu, Z.; Li, Y.; Huang, Z.; Jon, K. Study on fundamental link between mixing efficiency and entrainment performance of a steam ejector. *Energy* **2021**, *215*, 119128. [\[CrossRef\]](#)
24. Nakagawa, M.; Marasigan, A.R.; Matsukawa, T.A. Kurashina, Experimental investigation on the effect of mixing length on the performance of two-phase ejector for CO<sub>2</sub> refrigeration cycle with and without heat exchanger. *Int. J. Refrig.* **2011**, *34*, 1604–1613. [\[CrossRef\]](#)
25. Sarkar, J. Ejector enhanced vapor compression refrigeration and heat pump systems—A review. *Renew. Sustain. Energy Rev.* **2012**, *16*, 6647–6659. [\[CrossRef\]](#)
26. Banasiak, K.; Hafner, A.; Andresen, T. Experimental and numerical investigation of the influence of the two-phase ejector geometry on the performance of the R744 heat pump. *Int. J. Refrig.* **2012**, *35*, 1617–1625. [\[CrossRef\]](#)
27. Jeon, Y.; Kim, S.; Kim, D.; Chung, H.J.; Kim, Y. Performance characteristics of an R600a household refrigeration cycle with a modified two-phase ejector for various ejector geometries and operating conditions. *Appl. Energy* **2017**, *205*, 1059–1067. [\[CrossRef\]](#)
28. Fu, W.; Liu, Z.; Li, Y.; Wu, H.; Tang, Y. Numerical study for the influences of primary steam nozzle distance and mixing chamber throat diameter on steam ejector performance. *Int. J. Therm. Sci.* **2018**, *132*, 509–516. [\[CrossRef\]](#)
29. Dong, J.; Hu, Q.; Yu, M.; Han, Z.; Cui, W.; Liang, D.; Ma, H.; Pan, X. Numerical investigation on the influence of mixing chamber length on steam ejector performance. *Appl. Therm. Eng.* **2020**, *174*, 115204. [\[CrossRef\]](#)
30. Hemidi, A.; Henry, F.; Leclaire, S.; Seynhaeve, J.M.; Bartosiewicz, Y. CFD analysis of a supersonic air ejector. Part I: Experimental validation of single-phase and two-phase operation. *Appl. Therm. Eng.* **2009**, *29*, 1523–1531. [\[CrossRef\]](#)
31. Yuan, G.; Zhang, L.; Zhang, H.; Wang, Z. Numerical and experimental investigation of performance of the liquid-gas and liquid jet pumps in desalination systems. *Desalination* **2011**, *276*, 89–95. [\[CrossRef\]](#)
32. Chen, W.; Huang, C.; Bai, Y.; Chong, D.; Yan, J.; Liu, J. Experimental and numerical investigation of two phase ejector performance with the water injected into the induced flow. *Int. J. Adv. Nucl. React. Des. Technol.* **2020**, *2*, 15–24. [\[CrossRef\]](#)

33. Aliabadi, M.A.F.; Bahiraei, M. Effect of water nano-droplet injection on steam ejector performance based on non-equilibrium spontaneous condensation: A droplet number study. *Appl. Therm. Eng.* **2021**, *184*, 116236. [[CrossRef](#)]
34. Yan, J.; Li, S.; Liu, Z. Numerical investigation on optimization of ejector primary nozzle geometries with fixed/varied nozzle exit position. *Appl. Therm. Eng.* **2020**, *175*, 115426. [[CrossRef](#)]
35. Li, C.; Li, Y.Z. Investigation of entrainment behavior and characteristics of gas-liquid ejectors based on CFD simulation. *Chem. Eng. Sci.* **2011**, *66*, 405–416. [[CrossRef](#)]
36. Palacz, M.; Smolka, J.; Kus, W.; Fic, A.; Bulinski, Z.; Nowak, A.J.; Banasiak, K.; Hafner, A. CFD-based shape optimisation of a CO<sub>2</sub> two-phase ejector mixing section. *Appl. Therm. Eng.* **2016**, *95*, 62–69. [[CrossRef](#)]
37. Besagni, G.; Cristiani, N.; Croci, L.; Guédon, G.R.; Inzoli, F. Computational fluid-dynamics modelling of supersonic ejectors: Screening of modelling approaches, comprehensive validation and assessment of ejector component efficiencies. *Appl. Therm. Eng.* **2021**, *186*, 116431. [[CrossRef](#)]
38. Carrillo, J.A.E.; de la Flor, F.J.S.; Lissén, J.M.S. Single-phase ejector geometry optimisation by means of a multi-objective evolutionary algorithm and a surrogate CFD model. *Energy* **2018**, *164*, 46–64. [[CrossRef](#)]
39. Croquer, S.; Poncet, S.; Aidoun, Z. Turbulence modeling of a single-phase R134a supersonic ejector. Part 1: Numerical benchmark. *Int. J. Refrig.* **2016**, *61*, 140–152. [[CrossRef](#)]

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