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A Multi-Information Spreading Model for One-Time Retweet Information in Complex Networks

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Abstract: In the realm of online social networks, the spreading of information is influenced by a complex interplay of factors. To explore the dynamics of one-time retweet information spreading, we propose a Susceptible–Infected–Completed (SIC) multi-information spreading model. This model captures how multiple pieces of information interact in online social networks by introducing inhibiting and enhancement factors. The SIC model considers the completed state, where nodes cease to spread a particular piece of information after transmitting it. It also takes into account the impact of past and present information received from neighboring nodes, dynamically calculating the probability of nodes spreading each piece of information at any given moment. To analyze the dynamics of multiple information pieces in various scenarios, such as mutual enhancement, partial competition, complete competition, and coexistence of competition and enhancement, we conduct experiments on BA scale-free networks and the Twitter network. Our findings reveal that competing information decreases the likelihood of its spread while cooperating information amplifies the spreading of mutually beneficial content. Furthermore, the strength of the enhancement factor between different information pieces determines their spread when competition and cooperation coexist. These insights offer a fresh perspective for understanding the patterns of information propagation in multiple contexts.

Keywords: multi-information spreading; online social network; inhibiting factor; enhancement factor; one-time retweet information



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1. Introduction

The emergence of online social networks has revolutionized the spreading of information. These platforms provide easy access to a wide range of information, including news, entertainment, and academic research. This accessibility not only enhances people's understanding of the world, but also facilitates the sharing and spread of knowledge, contributing to societal development and progress.

However, the rapid spread of information through online networks also brings about various challenges. Privacy breaches, exposure to false information, and the propagation of harmful rumors are among the negative impacts associated with this phenomenon [1–6]. Therefore, it is crucial to deeply explore different forms of information spreading. Understanding the mechanisms of information diffusion and implementing effective measures to mitigate its negative effects are essential for public opinion monitoring and information recommendation systems.

Drawing parallels between the spread of epidemics and information, researchers have often employed epidemic models to study information spreading. Previous research

primarily focused on single information spread within networks [7–14]. However, given the vast array of information types and complex interactions within online social networks, which significantly impact the dynamics of information diffusion, scholars have increasingly turned their attention to multi-information spreading models. These models aimed to simulate and comprehend the intricate mechanisms underlying information propagation in online social networks [15–22].

The commonly used epidemic models, such as SIR and SIS, have been applied to the research of single information spreading [23–26]. Zhu [27] introduced the concept of information priority and focused on the competitive relationship between original false information and updated information. Shang [28] investigated the influence of overlap among communities on epidemics. By constructing an SIS model, it was found that epidemics spread faster in networks with a higher level of overlapping communities. Wang [29] studied the information spreading dynamics on complex networks with cliques and proved that the phase transition was always continuous and independent of the cliques. Continuous phase transition implies that the total number of infections during an epidemic varies with the infectiousness, exhibiting more complex collective dynamics influenced by environmental factors, including discontinuous or explosive transitions [30]. Prakash [15] proposed an information competition spreading model and discovered that strong information with a high spreading probability completely supplanted weaker information. Beutel [31] investigated the conditions for the coexistence of two competing viruses (or products or ideas) in a network. Wei [32] examined the intertwined diffusion of two rival information in a composite network based on the SIS model. They established a non-linear dynamic system and conducted an eigenvalue analysis to identify the critical point of epidemic behavior. Fátima [17] used the SIS model to explore the interaction between the spread of epidemics and the spreading of disease knowledge information, showing that the knowledge of the disease helped to reduce the disease prevalence and increase the epidemic threshold of the disease. Zhang [18] proposed an information diffusion framework to analyze the overall interactive behavior of users. Xiao [19] explored the impact factor and the interrelation of network layers on the information diffusion process based on the SIS model. Fan [33] studied the impact of a hybrid information propagation model on the epidemic and its related information coupling dynamics in a multilayer network. In this multilayer network, the upper layer was composed of randomly generated simple complexes, while the lower layer consisted of either traditional scale-free or Erdős–Rényi (ER) random networks.

However, despite extensive research on multi-information spreading models, there are still several unresolved issues that warrant attention.

1. When examining the relationships between different types of information, it is important to acknowledge that cooperation and competition can coexist within a network. While many researchers tend to focus on either cooperation or competition, understanding the interplay between these two dynamics is crucial. Even when two pieces of information compete, the degree of competition can vary, ranging from complete to partial. By considering the dynamics of spreading between different types of information, we can enhance our theoretical foundation for managing and controlling information spreading in networks. This deeper understanding allows us to develop strategies and measures that effectively address the negative impacts associated with information spreading. By recognizing the intricate interactions and complex nature of information propagation, we can establish more robust frameworks for managing and mitigating the consequences of network information spread.
2. Certain types of information possess strong timeliness, users may choose to retweet a piece of information upon first encountering it, but then cease to engage in any further retweets of the same content. Integrating the SIR model with one-time retweet behavior is crucial for accurately simulating and understanding the mechanisms of information spreading in social networks. In terms of its impact on information spreading, this ‘one-time retweet’ behavior could inhibit further diffusion of information, affecting the

speed and breadth of information propagation. Therefore, this user behavior should be considered when constructing models of information propagation.

To address the above issues, we draw on the concept of influence factors [19] and propose a Susceptible–Infected–Completed (SIC) information-spreading dynamic model. We use the microscopic Markov chain approach (MMCA) [34,35] to establish the dynamic equation and discuss the information spreading mechanism under different relationships in both artificial and real networks. The main research results of this paper are as follows:

1. Proposal of the SIC model: We introduce a novel SIC model where nodes transition to a completed state after participating in information spreading. This model specifically focuses on one-time retweet information.
2. Examination of the impact factor: We incorporate the concept of influence factors to describe the interactions between different types of information. By considering free spreading, cooperative spreading, partial competitive spreading, complete competitive spreading, and the coexistence of competition and cooperation, we analyze how multiple pieces of information propagate within the network.
3. Utilization of the MMCA: We employ the MMCA to establish the dynamic equation of the SIC model. This mathematical framework allows us to dissect and understand the intricate dynamics of information spreading within the network.

By leveraging influence factors and employing the MMCA approach, we present a comprehensive analysis of information diffusion, shedding light on its mechanisms under diverse relationship scenarios. The proposed model is applied to analyze the spread of information in both simulated artificial networks and real-world network data.

The rest of this paper is organized as follows. In Section 2, we provide the problem definition. In Section 3, we describe the proposed model in detail. In Section 4, we present and analyze the experimental results of the model. Finally, in Section 5 we conclude the paper.

2. Problem Definition

In order to study the spreading of multiple pieces of information in a network and their interactions with each other, we first define a network $G = \{V, E\}$. $V = \{v_1, v_2, v_3, \dots, v_N\}$ represents the set of nodes in the network, v_i is specific nodes, and $E = e_{ij} = \{\langle v_i, v_j \rangle | i, j \in V\}$ represents the edges in the network, with e_{ij} indicating the edges between node i and node j . Information can spread along these edges. $Inf = \{Inf_1, Inf_2, \dots, Inf_M\}$ is employed to denote the collection of M distinct pieces of information.

In this paper, the focus is on analyzing the spreading of information in a network that has a lasting impact once it is disseminated. To address this, the proposed model is called the SIC model. The node status is divided into three categories: S (Susceptible), I (Infected), and C (Completed). Nodes in the S_i state refer to those who have not yet been exposed to Inf_i and are susceptible to its influence. Nodes in the I_i state indicate those who receive Inf_i from their neighbors and are interested in it. They are willing to spread Inf_i to their friends. Nodes in the C_i state indicate that the node has already spread a certain Inf_i and maintains a memory of it, but the Inf_i will no longer be spread by them. This state is similar to the “recovered” state in the SIR model. However, nodes in the C_i state only mean that the node will no longer spread Inf_i , but there is still a possibility of spreading other information on the network. Moreover, because nodes in the C_i state maintain a memory of Inf_i , this affects the probability of the node spreading other information in the future.

Table 1 displays the symbols used in our paper. The cooperative and competitive relationships between information are controlled by parameters a_1 and a_2 . a_1 represents the influence factor between information in a competitive relationship, with $0 \leq a_1 \leq 1$. The larger the value of a_1 , the greater the inhibit strength. When $a_1 = 1$, it means that the information completely repels other information, and the node only accepts certain information that repels others. When $a_1 = 0$, the information does not compete with other information. a_2 represents the influence factor between information in a cooperative

relationship, and the larger the value of a_2 , the stronger the cooperative strength. We use $\beta = \{\beta_1, \beta_2, \dots, \beta_M\}$ to represent the infection rate, where β_i denotes the infection rate of Inf_i . The infection rate is defined as the probability that a node in the susceptible state (S state) will be influenced by a neighboring node in the infected state (I state)

Table 1. Symbols and definitions.

Symbols	Definitions
Inf	Information
β_i	Infection rate of inf_i
γ_i	Completed rate of inf_i
a_1	The influence parameter of the competitive information, and satisfies $a_1 \in [0, 1]$
a_2	The influence parameter of the cooperative information, and satisfies $a_2 \in [0, \infty)$
V	The set of nodes
E	The set of edges
N	The number of nodes
M	The number of information
A	The adjacency matrix of the network
λ	The largest eigenvalue of matrix A
S_i	Susceptible state for information i
I_i	Infected state for information i
C_i	Completed state for information i

3. Proposed Model

In this paper, the focus is on discussing five different types of information spreading within networks. These categories include free spreading, mutual enhancement, partial competition, complete competition, and the coexistence of competition and enhancement.

- (1) Free spreading: In this scenario, there is no mutual influence between different pieces of information. Each piece of information spreads independently throughout the network without any direct interaction or impact from other information items.
- (2) Mutual enhancement: When information spreads through mutual enhancement, the probability of a node spreading cooperative information increases after it disseminates a piece of information. This means that the act of spreading one piece of information enhances the likelihood of that node also spreading additional cooperative information.
- (3) Partial competition: In the case of local competition between information, the probability of a node spreading competitive information is inhibited after it spreads a piece of information. This implies that when multiple pieces of information compete, the spreading of one piece of information inhibits the node's tendency to spread other competitive information.
- (4) Complete competition: when there is complete competition between information, a node will not spread competitive information after it spreads a piece of information.
- (5) Coexistence of competition and enhancement: in the case of the coexistence of competition and enhancement between different kinds of information, the probability of a node spreading cooperative information increases, and at the same time, the probability of spreading competitive information is inhibited after it spreads a piece of information.

By exploring these different types of information spreading and their dynamics, we aim to provide a comprehensive understanding of how information disseminates within networks. This knowledge can contribute to the development of effective strategies for managing and controlling the spread of network information.

The Markov chain approach is utilized in this paper to analyze the five types of information spreading mentioned earlier. To facilitate discussion and explanation, let us consider an example with three pieces of information. The principles can be extended to include more than three pieces of information.

In this model, the initial node can receive any of the M pieces of information present in the network. For the sake of simplicity, we refer to the three pieces of information as Inf_1 , Inf_2 , and Inf_3 . For further analysis, the subsequent content assumes that Inf_1 and Inf_3 have a cooperative relationship, while Inf_2 has a competitive relationship with both Inf_1 and Inf_3 . We will explore their relationships within the context of the SIC model. Here are some examples of states within this model: when a node is in the state of $S_1S_2S_3$, it indicates that the node has not received any of the three pieces of information; when a node is in the state of $I_1S_2S_3$, it means that the node has only spread Inf_1 ; when a node is in the state of $C_1I_2S_3$, it means that the node has already spread Inf_1 , and now it spreads Inf_2 , which has a competitive relationship with Inf_1 ; and when a node is in the state of $C_1S_2I_3$, it means that the node has already spread Inf_1 , and now it spreads Inf_3 , which has a cooperative relationship with Inf_1 . These states and their relationships are part of the SIC model, which aims to analyze the spread of information in a network while considering the effects of cooperation and competition among different pieces of information.

When the infection rate of Inf_i is β_i , if the node is in $S_1S_2S_3$ state at time t , it will change to $I_1S_2S_3$, $S_1I_2S_3$, $S_1S_2I_3$ with probabilities $f_i^{(1)}$, $f_i^{(2)}$, $f_i^{(3)}$ [36], which are:

$$f_i^{(1)}(t) = 1 - \prod_{j=1}^N (1 - \beta_1 A_{ji} s_j^1(t)) \tag{1}$$

$$f_i^{(2)}(t) = 1 - \prod_{j=1}^N (1 - \beta_2 A_{ji} s_j^2(t)) \tag{2}$$

$$f_i^{(3)}(t) = 1 - \prod_{j=1}^N (1 - \beta_3 A_{ji} s_j^3(t)) \tag{3}$$

The variable N denotes the total number of nodes in the network. A is the adjacency matrix of the network. $A_{ji} = 1$ indicates that individual i has an edge directed towards individual j , while $A_{ji} = 0$ signifies that there is no directed edge between them. The variables $s_j^1(t)$, $s_j^2(t)$, and $s_j^3(t)$, respectively, indicate whether individual j is in an infected state with Inf_1 , Inf_2 , and Inf_3 at time t . If individual j is in an infected state, we have $s_j^1(t) = 1$, otherwise $s_j^1(t) = 0$. Similarly, $s_j^2(t)$ and $s_j^3(t)$ are defined.

The spreading mechanism operates as follows: Every node in states $I_1S_2S_3$ transmits information inf_1 to each of its adjacent nodes at time t . Each of these attempts has an independent success rate, represented by the probability β_1 . Concurrently, nodes in states $S_1I_2S_3$ and $S_1S_2I_3$ also aim to disseminate information Inf_2 and Inf_3 to each of their neighboring nodes with probabilities β_2 and β_3 , respectively. Therefore, $f_i^{(1)}$, $f_i^{(2)}$, and $f_i^{(3)}$ represent the probabilities that a given node i receives information Inf_1 , Inf_2 , and Inf_3 from its neighboring nodes.

We construct a state transition diagram for the nodes, with Figure 1 represents the state transition diagram for prioritizing the reception of Inf_1 , Inf_2 , and Inf_3 .

According to state transmission, we use the MMCA to describe the collaborative evolution process of all information sources. MMCA pivots on the fundamental principles of Markov chains, where the future state of a system is dependent solely on its current state. At the heart of this approach is the consideration of each individual in the population as a distinct entity, with a set of possible states. The transitions between these states are governed by probabilities:

$$\left\{ \begin{aligned}
 P_i^{I_1 S_2 S_3}(t+1) &= P_i^{S_1 S_2 S_3}(t) f_i^1 (1-f_i^2)(1-f_i^3) + P_i^{I_1 S_2 S_3}(t)(1-r_i^1)(1-f_i^2)(1-f_i^3) \\
 P_i^{S_1 I_2 S_3}(t+1) &= P_i^{S_1 S_2 S_3}(t) f_i^2 (1-f_i^1)(1-f_i^3) + P_i^{S_1 I_2 S_3}(t)(1-r_i^2)(1-f_i^1)(1-f_i^3) \\
 P_i^{S_1 S_2 I_3}(t+1) &= P_i^{S_1 S_2 S_3}(t) f_i^3 (1-f_i^1)(1-f_i^2) + P_i^{S_1 S_2 I_3}(t)(1-r_i^3)(1-f_i^1)(1-f_i^2) \\
 P_i^{C_1 S_2 S_3}(t+1) &= P_i^{I_1 S_2 S_3}(t) r_i^1 (1-f_i^2)(1-f_i^3) + P_i^{C_1 S_2 S_3}(t)(1-f_i^2)(1-f_i^3) \\
 P_i^{S_1 C_2 S_3}(t+1) &= P_i^{S_1 I_2 S_3}(t) r_i^2 (1-f_i^1)(1-f_i^3) + P_i^{S_1 C_2 S_3}(t)(1-f_i^1)(1-f_i^3) \\
 P_i^{S_1 S_2 C_3}(t+1) &= P_i^{S_1 S_2 I_3}(t) r_i^3 (1-f_i^1)(1-f_i^2) + P_i^{S_1 S_2 C_3}(t)(1-f_i^1)(1-f_i^2) \\
 P_i^{I_1 I_2 S_3}(t+1) &= P_i^{S_1 I_2 S_3}(t)(1-r_i^2) f_i^1 (1-f_i^3)(1-a_1) + P_i^{I_1 S_2 S_3}(t)(1-r_i^1) f_i^2 (1-f_i^3)(1-a_1) \\
 &+ P_i^{I_1 I_2 S_3}(t)(1-r_i^1)(1-r_i^2)(1-f_i^3) \\
 P_i^{I_1 S_2 I_3}(t+1) &= P_i^{I_1 S_2 I_3}(t)(1-r_i^1)(1-r_i^3)(1-f_i^2) + P_i^{S_1 S_2 I_3}(t)(1-r_i^3) f_i^1 (1-f_i^2)(1+a_2) \\
 &+ P_i^{I_1 S_2 S_3}(t)(1-r_i^1) f_i^2 (1-f_i^3)(1+a_2) \\
 P_i^{S_1 I_2 I_3}(t+1) &= P_i^{S_1 I_2 I_3}(t)(1-f_i^1)(1-r_i^2)(1-r_i^3) + P_i^{S_1 S_2 I_3}(t)(1-r_i^3) f_i^2 (1-f_i^1)(1-a_1) \\
 &+ P_i^{S_1 I_2 S_3}(t)(1-r_i^2) f_i^3 (1-f_i^1)(1-a_1) \\
 P_i^{C_1 I_2 S_3}(t+1) &= P_i^{I_1 I_2 S_3}(t) r_i^1 (1-r_i^2)(1-f_i^3) + P_i^{C_1 S_2 S_3}(t) f_i^2 (1-f_i^3)(1-a_1) \\
 &+ P_i^{C_1 I_2 S_3}(t)(1-r_i^2)(1-f_i^3) \\
 P_i^{I_1 C_2 S_3}(t+1) &= P_i^{I_1 I_2 S_3}(t)(1-r_i^1) r_i^2 (1-f_i^3) + P_i^{S_1 C_2 S_3}(t) f_i^1 (1-f_i^3)(1-a_1) \\
 &+ P_i^{I_1 C_2 S_3}(t)(1-r_i^1)(1-f_i^3) \\
 P_i^{I_1 S_2 C_3}(t+1) &= P_i^{I_1 S_2 I_3}(t)(1-r_i^1)(1-f_i^2) r_i^3 + P_i^{S_1 S_2 C_3}(t) f_i^1 (1-f_i^2) \\
 &+ P_i^{I_1 S_2 C_3}(t)(1-r_i^1)(1-f_i^2) \\
 P_i^{C_1 S_2 I_3}(t+1) &= P_i^{I_1 S_2 I_3}(t) r_i^1 (1-f_i^2)(1-r_i^3) + P_i^{C_1 S_2 S_3}(t)(1-f_i^2) f_i^3 (1+a_2) \\
 &+ P_i^{C_1 S_2 I_3}(t)(1-f_i^2)(1-r_i^3) \\
 P_i^{S_1 I_2 C_3}(t+1) &= P_i^{S_1 I_2 C_3}(t)(1-f_i^1)(1-r_i^2) + P_i^{S_1 S_2 C_3}(t)(1-f_i^1) f_i^2 (1-a_1) \\
 &+ P_i^{S_1 I_2 I_3}(t)(1-f_i^1)(1-r_i^2) r_i^3 \\
 P_i^{S_1 C_2 I_3}(t+1) &= P_i^{S_1 C_2 I_3}(t)(1-f_i^1)(1-r_i^3) + P_i^{S_1 I_2 I_3}(t)(1-f_i^1) r_i^2 (1-r_i^3) \\
 &+ P_i^{S_1 C_2 S_3}(t)(1-f_i^1) f_i^3 (1+a_2) \\
 P_i^{C_1 C_2 S_3}(t+1) &= P_i^{I_1 C_2 S_3}(t) r_i^1 (1-f_i^3) + P_i^{C_1 I_2 S_3}(t) r_i^2 (1-f_i^3) \\
 &+ P_i^{C_1 C_2 S_3}(t)(1-f_i^3) \\
 P_i^{S_1 C_2 C_3}(t+1) &= P_i^{S_1 C_2 C_3}(t)(1-f_i^1) + P_i^{S_1 I_2 C_3}(t)(1-f_i^1) r_i^2 \\
 &+ P_i^{S_1 C_2 I_3}(t)(1-f_i^1) r_i^3 \\
 P_i^{C_1 S_2 C_3}(t+1) &= P_i^{I_1 S_2 C_3}(t) r_i^1 (1-f_i^2) + P_i^{C_1 S_2 C_3}(t)(1-f_i^2) \\
 &+ P_i^{C_1 S_2 I_3}(t)(1-f_i^2) r_i^3 \\
 P_i^{I_1 I_2 I_3}(t+1) &= P_i^{I_1 I_2 I_3}(t)(1-r_i^1)(1-r_i^2)(1-r_i^3) + P_i^{S_1 I_2 I_3}(t) f_i^1 (1-r_i^2)(1-r_i^3)(1-a_1)(1+a_2) \\
 &+ P_i^{I_1 S_2 I_3}(t)(1-r_i^1) f_i^2 (1-r_i^3)(1-a_1)^2 + P_i^{I_1 I_2 S_3}(t)(1-r_i^1)(1-r_i^2) f_i^3 (1-a_1)(1+a_2) \\
 P_i^{I_1 I_2 C_3}(t+1) &= P_i^{S_1 I_2 C_3}(t) f_i^1 (1-r_i^2)(1-a_1)(1+a_2) + P_i^{I_1 S_2 C_3}(t)(1-r_i^1) f_i^2 (1-a_1)^2 \\
 &+ P_i^{I_1 I_2 I_3}(t)(1-r_i^1)(1-r_i^2) r_i^3 + P_i^{I_1 I_2 C_3}(t)(1-r_i^1)(1-r_i^2) \\
 P_i^{C_1 I_2 I_3}(t+1) &= P_i^{I_1 I_2 I_3}(t) r_i^1 (1-r_i^2)(1-r_i^3) + P_i^{C_1 S_2 I_3}(t) f_i^2 (1-r_i^3)(1-a_1)^2 \\
 &+ P_i^{C_1 I_2 S_3}(t)(1-r_i^2) f_i^3 (1-a_1)(1+a_2) + P_i^{C_1 I_2 I_3}(t)(1-r_i^2)(1-r_i^3) \\
 P_i^{C_1 C_2 I_3}(t+1) &= P_i^{I_1 C_2 I_3}(t) r_i^1 (1-r_i^3) + P_i^{C_1 I_2 I_3}(t) r_i^2 (1-r_i^3) \\
 &+ P_i^{C_1 C_2 S_3}(t) f_i^3 (1-a_1)(1+a_2) + P_i^{C_1 C_2 I_3}(t)(1-r_i^3) \\
 P_i^{C_1 I_2 C_3}(t+1) &= P_i^{I_1 I_2 C_3}(t) r_i^1 (1-r_i^2) + P_i^{C_1 S_2 C_3}(t) f_i^2 (1-a_1)^2 \\
 &+ P_i^{C_1 I_2 I_3}(t)(1-r_i^2) r_i^3 + P_i^{C_1 I_2 C_3}(t)(1-r_i^2) \\
 P_i^{I_1 C_2 C_3}(t+1) &= P_i^{S_1 C_2 C_3}(t) f_i^1 (1-a_1)(1+a_2) + P_i^{I_1 I_2 C_3}(t)(1-r_i^1) r_i^2 \\
 &+ P_i^{I_1 C_2 I_3}(t)(1-r_i^1) r_i^3 + P_i^{I_1 C_2 C_3}(t)(1-r_i^1) \\
 P_i^{C_1 C_2 C_3}(t+1) &= P_i^{I_1 C_2 C_3}(t) r_i^1 + P_i^{C_1 I_2 C_3}(t) r_i^2 + P_i^{C_1 C_2 I_3}(t) r_i^3 \\
 P_i^{S_1 S_2 S_3}(t+1) &= 1 - \text{Above}
 \end{aligned} \right. \tag{4}$$

where $P_i^{I_1 S_2 S_3}(t+1)$ represents the probability of node i in the $I_1 S_2 S_3$ state at time $t+1$. A node is set in one of all different states, so $P_i^{S_1 S_2 S_3}(t+1) = 1 - \text{Above}$. The epidemic

threshold is the critical point for information explosion. To determine the threshold, we first simplify Equation (4) to a general expression $\vec{P}(t + 1) = g(\vec{P}(t))$, where

$$\begin{aligned} \vec{P}(t) = & (\bar{P}^{I_1S_2S_3}(t), \bar{P}^{S_1I_2S_3}(t), \bar{P}^{S_1S_2I_3}(t), \bar{P}^{S_1I_2I_3}(t), \bar{P}^{I_1S_2I_3}(t), \bar{P}^{I_1I_2S_3}(t), \bar{P}^{I_1S_2C_3}(t), \\ & \bar{P}^{I_1C_2S_3}(t), \bar{P}^{S_1I_2C_3}(t), \bar{P}^{C_1I_2S_3}(t), \bar{P}^{C_1S_2I_3}(t), \bar{P}^{S_1C_2I_3}(t), \bar{P}^{I_1I_2C_3}(t), \\ & \bar{P}^{I_1C_2I_3}(t), \bar{P}^{C_1I_2I_3}(t), \bar{P}^{I_1C_2C_3}(t), \bar{P}^{C_1I_2C_3}(t), \bar{P}^{C_1C_2I_3}(t), \bar{P}^{I_1I_2I_3}(t)) \end{aligned} \tag{5}$$

$\bar{P}^{I_1S_2S_3}(t) = (P_1^{I_1S_2S_3}(t), P_2^{I_1S_2S_3}(t), \dots, P_N^{I_1S_2S_3}(t))$ and others are similarly.

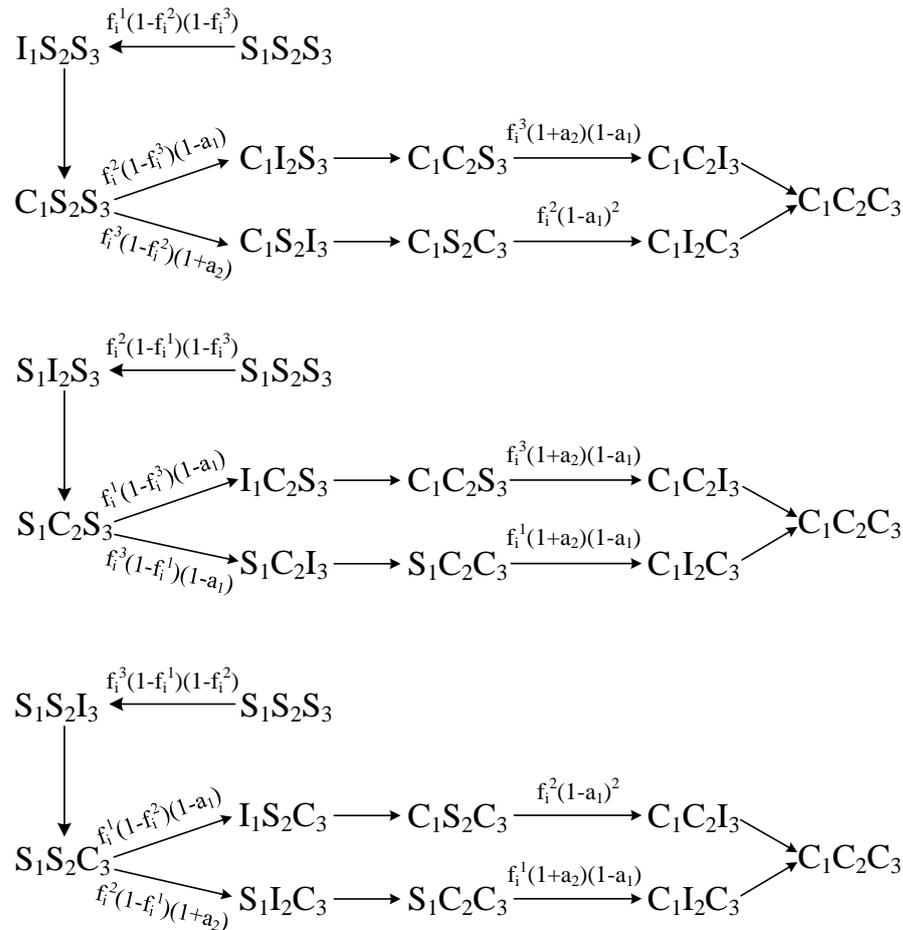


Figure 1. The state transition diagram for prioritizing the spreading of Inf_1 , Inf_2 and Inf_3 .

Theorem 1. The system is asymptotically stable at $\vec{P}(t) = \vec{0}$ when the eigenvalues of $\nabla g(\vec{0})$ are less than 1 in absolute value, where Jacobian matrix is calculated as follows:

$$J = [\nabla g(\vec{0})]_{m,n} = \left. \frac{\partial g_{m,t+1}}{\partial P_{n,t}} \right|_{\vec{P}_n = \vec{0}} \tag{6}$$

In order to compute the epidemic threshold, it is necessary to solve the Jacobian matrix of the system. Based on $\vec{P} = \vec{0}$, the eigenvalues of its Jacobian matrix are as follows:

$$\begin{cases} (1 - \gamma_1)E + \beta_1 A \\ (1 - \gamma_2)E + \beta_2 A \\ (1 - \gamma_3)E + \beta_3 A \\ (1 - \gamma_1)(1 - \gamma_2)E \\ (1 - \gamma_1)(1 - \gamma_3)E \\ (1 - \gamma_2)(1 - \gamma_3)E \\ (1 - \gamma_1)E \\ (1 - \gamma_2)E \\ (1 - \gamma_3)E \end{cases} \tag{7}$$

According to Theorem 1, there are

$$\begin{aligned} & \text{Max}(|(1 - \gamma_1) + \beta_1 \lambda|, |(1 - \gamma_2) + \beta_2 \lambda|, |(1 - \gamma_3) + \beta_3 \lambda|, |(1 - \gamma_1)(1 - \gamma_2)|, \\ & |(1 - \gamma_1)(1 - \gamma_3)|, |(1 - \gamma_2)(1 - \gamma_3)|, |(1 - \gamma_1)|, |(1 - \gamma_2)|, |(1 - \gamma_3)|) < 1 \end{aligned} \tag{8}$$

where λ represents the maximum eigenvalue of the adjacency matrix. When the system attains stability, no information can spread through the network.

$\gamma_1, \gamma_2, \gamma_3, \beta_1, \beta_2, \beta_3$ all range from 0 to 1. In the context of undirected networks, the adjacency matrix possesses the properties of irreducibility, non-negativity, and symmetry. In accordance with the Perron–Frobenius Theorem, its largest eigenvalue is a positive real number, therefore $(1 - \gamma_1) + \beta_1 \lambda > 0$, $(1 - \gamma_2) + \beta_2 \lambda > 0$ and $(1 - \gamma_3) + \beta_3 \lambda > 0$ and condition (8) can be rewritten as follows:

$$\begin{cases} (1 - \gamma_1) + \beta_1 \lambda < 1 \\ (1 - \gamma_2) + \beta_2 \lambda < 1 \\ (1 - \gamma_3) + \beta_3 \lambda < 1 \end{cases} \Rightarrow \begin{cases} \beta_1 / \gamma_1 < 1 / \lambda \\ \beta_2 / \gamma_2 < 1 / \lambda \\ \beta_3 / \gamma_3 < 1 / \lambda \end{cases} \tag{9}$$

When $\beta_i / \gamma_i < 1 / \lambda$, the spreading of information within the network has completed. It is evident from the derived results that the epidemic threshold remains independent of the interaction factors.

4. Results and Analysis

In this section, we verify the influence of the relationships between different pieces of information on multiple information propagation processes separately on real-world networks and synthetic networks.

4.1. Experimental Datasets

We conduct simulations of the proposed model based on both real and synthetic networks. The dataset for the real network is extracted from the Twitter dataset. The details are as follows:

1. **Twitter:** Twitter serves as a platform for real-time global event tracking and discussions on trending topics. Users can engage in open, real-time conversations and interact with other users. The dataset is collected from 5000 users and their social circles, where users and their social relationships are represented as nodes and connections, respectively. The statistical characteristics of the Twitter network are shown in Table 2.
2. **Synthetic network:** The synthetic network is generated using the Barabási–Albert (BA) network [37] and consists of 1000 nodes. The parameter m is set to 3, indicating the number of connected edges when a new node is added.

Table 2. Features of the Twitter network.

Number of Nodes	Number of Edges	Average Path Length	Clustering Coefficient
5000	185,433	3.2597	0.1178

4.2. Multiple Information Analysis

In this section, we explore the influence of interaction factors on propagation. Given that the emphasis of this section is on the interaction between pieces of information, we primarily observe the impact of changes in the values of α_1 and α_2 on the spreading, where $\alpha_1 \in [0, 1]$, $\alpha_2 \in [0, \infty)$. This ensures the generality of the experiments as we randomly select five initial nodes for information propagation experiments with each experiment repeated 100 times, and the results averaged.

In Figure 2a, we depict the relationship between the number of individuals involved in the spreading of information and the enhancement factor a_2 in the synthetic network, considering the parameters $\beta_1 = 0.1$, $\beta_3 = 0.1$. The information in the network mutually enhances each other. With an increase in a_2 , the number of individuals involved in the spreading of information grows. The positive correlation between the enhancement factor and the number of individuals engaged in spreading information implies that as the strength of mutual enhancement increases, a larger segment of the network actively participates in the propagation of information.

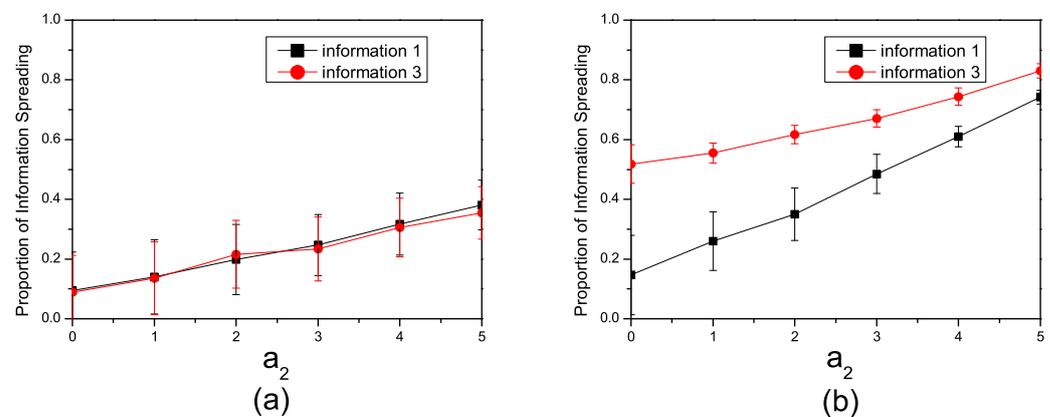


Figure 2. (a) The relationship in the synthetic network between the proportion of individuals spreading information and the enhancement factor a_2 with $\beta_1 = 0.1$ and $\beta_3 = 0.1$. (b) The relationship in the synthetic network between the proportion of individuals spreading information and enhancement factor a_2 with $\beta_1 = 0.1$, $\beta_3 = 0.3$.

Figure 2b illustrates the impact of facilitation factors on information propagation under different spreading probabilities. With $\beta_1 = 0.1$, $\beta_3 = 0.3$, we initially observed that the propagation range of both pieces of information increases with the strengthening of the facilitation factor. Additionally, the enhancement amplitude for Inf_1 is greater, while the enhancement amplitude for Inf_3 is smaller. In scenarios of mutual enhancement, the information with a higher inherent tendency to spread can act as a catalyst, facilitating the dissemination of less infectious information.

Figure 3 illustrates the variation in individuals participating in information propagation in the Twitter network under different enhancement factors. Given the structural disparities between the Twitter network and a synthetic network, we set the infection rate $\beta_1 = 0.08$, $\beta_3 = 0.08$. It can be observed that with an increase in the enhancement factor, the propagation range of Inf_1 and Inf_3 becomes larger. These findings align with the results observed in studies of synthetic networks.

To investigate the impact of the inhibition factor, we disregard the enhancement relationship between Inf_1 and Inf_3 by setting $a_2 = 0$. Figure 4a illustrates the influence of the inhibition factor on information propagation in a synthetic network. We set the infection rates as $\beta_1 = 0.15$, $\beta_3 = 0.15$, $\beta_2 = 0.3$. When the inhibition factor $a_1 = 0$, there is no competition among the three pieces of information. Therefore, all three pieces of information can be spread freely. As the inhibition factor increases, the propagation of all three pieces of information becomes constrained.

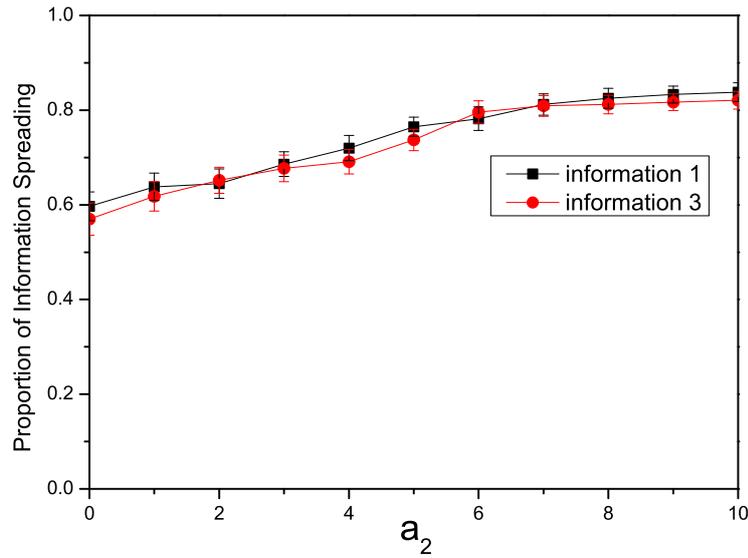


Figure 3. The relationship in the Twitter network between the proportion of individuals spreading information and the enhancement factor a_2 with $\beta_1 = 0.08, \beta_3 = 0.08$.

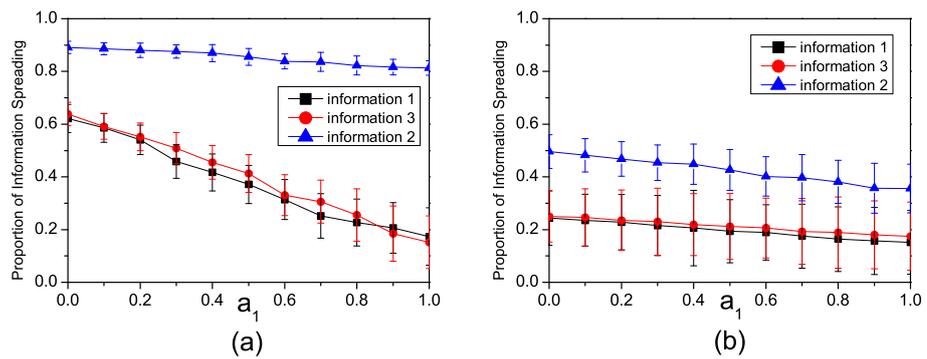


Figure 4. (a) The relationship in the synthetic network between the proportion of individuals spreading information and the inhibiting factor a_1 with $\beta_1 = 0.15, \beta_3 = 0.15, \beta_2 = 0.3$. (b) The relationship in the Twitter network between the proportion of individuals spreading information with the inhibiting factor $a_1, \beta_1 = 0.08, \beta_3 = 0.08$ and $\beta_2 = 0.3$.

Figure 4b illustrates the impact of the inhibition factor a_1 on information propagation in the Twitter network. We set the infection rates as $\beta_1 = 0.08, \beta_3 = 0.08$ and $\beta_2 = 0.3$. When $a_1 = 0$, the influence range of all three pieces of information, which propagate freely, is significantly large. However, as a_1 increases, the propagation range of information with lower infection rates notably decreases, while the impact on information with higher infection rates is comparatively lower.

Figure 5a illustrates the variation in information propagation with changes in a_2 when both inhibition and enhancement factors coexist in a synthetic network. It can be observed that when the infection rates $\beta_1 = 0.15, \beta_3 = 0.15$ and $\beta_2 = 0.3$, and the inhibition factor is $a_1 = 1$, the propagation range of Inf_2 decreases with an increase in the enhancement factor. In contrast, the propagation ranges of Inf_1 and Inf_3 increase with the enhancement factor.

Figure 5b illustrates the variation in information propagation with changes in a_2 when both inhibition and enhancement factors coexist in the Twitter network. The infection rate is set as $\beta_1 = 0.08, \beta_3 = 0.08$ and $\beta_2 = 0.3$. When a_2 is small, the number of individuals spreading Inf_1 and Inf_3 is lower than that of Inf_2 . However, as a_2 continues to increase, the number of individuals spreading Inf_1 and Inf_3 gradually surpasses the number of individuals

spreading Inf_2 . This dynamic signifies a critical turning point—when the enhancement factor is small, information with a higher infection rate impedes the dissemination of information with a lower infection rate. However, as the enhancement factor increases, a more complex interplay emerges. Information with a higher infection rate becomes subject to joint inhibition by multiple pieces of information characterized by lower influence probabilities.

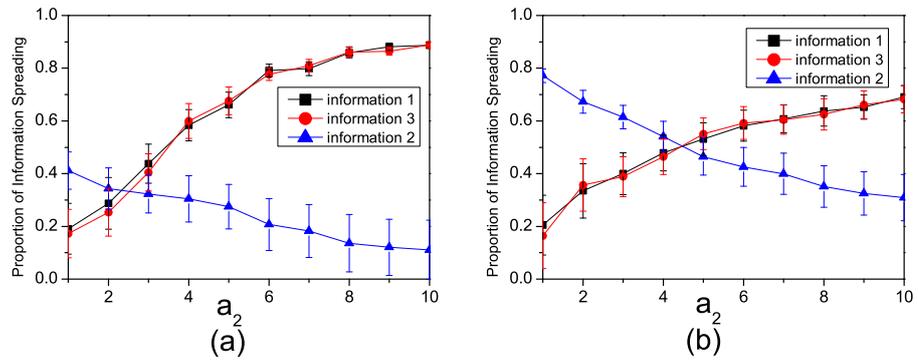


Figure 5. (a) The relationship in the synthetic network between the proportion of individuals spreading information and enhancement factor a_2 with $\beta_1 = 0.15, \beta_3 = 0.15, \beta_2 = 0.3, a_1 = 1$. (b) The relationship in the Twitter network between the proportion of individuals spreading information and the enhancement factor a_2 with $\beta_1 = 0.08, \beta_3 = 0.08, \beta_2 = 0.3, a_1 = 1$.

Next, we explore the impact of enhancement and inhibiting factors on information spreading in networks constructed with different BA model parameters m . Figure 6a illustrates the changes in the propagation of Inf_1 in synthetic networks for different m values. The infection rate is set as $\beta_1 = 0.1, \beta_3 = 0.1$. When m is small, the spreading of information faces significant challenges. Sparse networks typically feature limited connectivity among nodes, which hinders the efficient spread of information. In such scenarios, even with an increase in the enhancement factor, the impact on information propagation remains minimal. As m increases, the number of individuals involved in the propagation of Inf_1 gradually increases. The amplifying effect of the enhancement factor a_2 also becomes more pronounced, indicating that improving the connectivity of the network has a positive impact on information propagation.

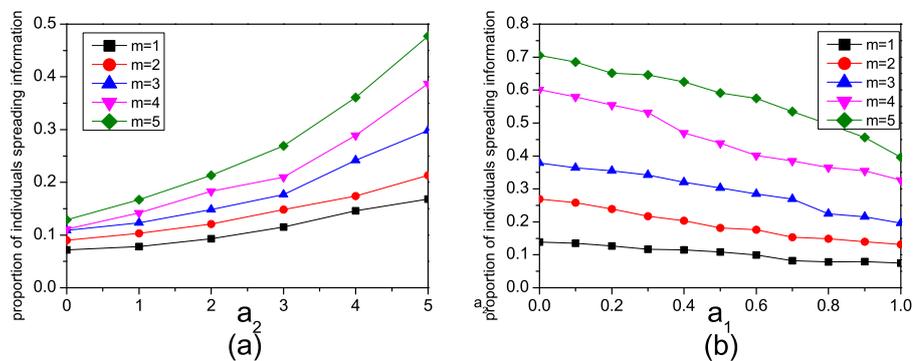


Figure 6. (a) The relationship in the synthetic network between the proportion of individuals spreading Inf_1 and the parameter m with $\beta_1 = 0.1, \beta_3 = 0.1$. (b) The relationship in the synthetic network between the proportion of individuals spreading Inf_2 and the inhibiting factor a_1 with $\beta_1 = 0.15, \beta_3 = 0.15, \beta_2 = 0.3$ and different m .

Figure 6b illustrates the varying impact of the inhibition factor a_1 on the propagation of Inf_2 in synthetic networks for different values of m . The infection rate is set as $\beta_1 = 0.15$, $\beta_3 = 0.15$ and $\beta_2 = 0.3$. When m is large, an increase in the inhibition factor leads to a gradual reduction in the proportion of individuals involved in the diffusion of Inf_2 . Conversely, when m is small, the influence of an increased inhibition factor on the diffusion of Inf_2 is small. These findings suggest that in networks with higher connectivity, the inhibition factor has a more significant impact on the propagation of Inf_2 , while in networks with lower connectivity, the effect of the inhibition factor on Inf_2 propagation is less pronounced.

5. Conclusions

In this paper, we propose a SIC multi-information spreading model that incorporates enhancement and inhibiting factors to analyze their influence on the spread of multiple pieces of information. Through our experiments, several significant findings have emerged: (1) When multiple pieces of information mutually enhance each other, information with a higher infection rate can amplify the spread of information with a lower infection rate. This highlights the interplay between different pieces of information and how they can synergistically contribute to the overall spread. (2) The presence of competition among pieces of information hinders their spread. Moreover, the lower the infection rate of a piece of information, the more it is inhibited by competing information. This emphasizes the impact of competition on the spreading of individual pieces of information. (3) In cases where there is cooperation and competition among pieces of information, the one with a higher infection rate exerts a dominant influence on information spreading. This showcases the power dynamics at play when multiple pieces of information interact within a network. (4) In sparse networks with limited connectivity, the challenges in spreading information are more pronounced. Additionally, the impact of enhancement and inhibiting factors on information transmission becomes less significant in such networks. Overall, we provide valuable insights into understanding and predicting the dynamics of multi-information spreading in various contexts.

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References

1. Moreno, Y.; Nekovee, M.; Pacheco, A.F. Dynamics of rumor spreading in complex networks. *Phys. Rev. E* **2004**, *69*, 066130. [[CrossRef](#)]
2. Doerr, B.; Fouz, M.; Friedrich, T. Why rumors spread so quickly in social networks. *Commun. ACM* **2012**, *55*, 70–75. [[CrossRef](#)]
3. Chierichetti, F.; Lattanzi, S.; Panconesi, A. Rumor spreading in social networks. *Theor. Comput. Sci.* **2011**, *412*, 2602–2610. [[CrossRef](#)]
4. Zan, Y.; Wu, J.; Li, P.; Yu, Q. SICR rumor spreading model in complex networks: Counterattack and self-resistance. *Phys. A Stat. Mech. Its Appl.* **2014**, *405*, 159–170. [[CrossRef](#)]
5. Xu, C.; Ding, A.S.; Zhao, K. A novel POI recommendation method based on trust relationship and spatial–temporal factors. *Electron. Commer. Res. Appl.* **2021**, *48*, 101060. [[CrossRef](#)]
6. Wang, Y.; Ding, A.S.; Xu, C. The impact of paid social Q&A on panic buying and digital hoarding at the stage of coexistence with COVID-19: The moderating role of sensitivity to pain of payment. *Int. J. Disaster Risk Reduct.* **2023**, *84*, 103472.

7. Liu, D.; Chen, X. Rumor propagation in online social networks like twitter—A simulation study. In Proceedings of the 2011 Third International Conference on Multimedia Information Networking and Security, Shanghai, China, 4–6 November 2011; pp. 278–282.
8. Xu, X.-D.; Xiao, Y.-T.; Zhu, S.-R. Simulation investigation of rumor propagation in microblogging community. *Comput. Eng.* **2011**, *37*, 272–274.
9. Wang, H.; Li, Y.; Feng, Z.; Feng, L. ReTweeting analysis and prediction in microblogs: An epidemic inspired approach. *China Commun.* **2013**, *10*, 13–24. [[CrossRef](#)]
10. Xu, B.; Liu, L. Information diffusion through online social networks. In Proceedings of the 2010 IEEE International Conference on Emergency Management and Management Sciences, Beijing, China, 8–10 August 2010; pp. 53–56.
11. Wei, Z.; Yanqing, Y.; Hanlin, T.; Qiwei, D.; Taowei, L. Information diffusion model based on social network. In Proceedings of the Proceedings of the 2012 International Conference of Modern Computer Science and Applications, Wuhan, China, 8 September 2012; Springer: Berlin/Heidelberg, Germany, 2013; pp. 145–150.
12. Zanette, D.H. Critical behavior of propagation on small-world networks. *Phys. Rev. E* **2001**, *64*, 050901. [[CrossRef](#)]
13. Zanette, D.H. Dynamics of rumor propagation on small-world networks. *Phys. Rev. E* **2002**, *65*, 041908. [[CrossRef](#)]
14. Leskovec, J.; McGlohon, M.; Faloutsos, C.; Gance, N.; Hurst, M. Patterns of cascading behavior in large blog graphs. In Proceedings of the 2007 SIAM International Conference on Data Mining, Minneapolis, MN, USA, 26–28 April 2007; SIAM: Philadelphia, PA, USA, 2007; pp. 551–556.
15. Prakash, B.A.; Beutel, A.; Rosenfeld, R.; Faloutsos, C. Winner takes all: Competing viruses or ideas on fair-play networks. In Proceedings of the 21st International Conference on World Wide Web, Lyon, France, 16–20 April 2012; pp. 1037–1046.
16. Wang, J.; Xiong, W.; Wang, R.; Cai, S.; Wu, D.; Wang, W.; Chen, X. Effects of the information-driven awareness on epidemic spreading on multiplex networks. *Chaos Interdiscip. J. Nonlinear Sci.* **2022**, *32*, 073123. [[CrossRef](#)] [[PubMed](#)]
17. Velásquez-Rojas, F.; Ventura, P.C.; Connaughton, C.; Moreno, Y.; Rodrigues, F.A.; Vazquez, F. Disease and information spreading at different speeds in multiplex networks. *Phys. Rev. E* **2020**, *102*, 022312. [[CrossRef](#)] [[PubMed](#)]
18. Zhang, X.; Su, Y.; Qu, S.; Xie, S.; Fang, B.; Philip, S.Y. IAD: Interaction-aware diffusion framework in social networks. *IEEE Trans. Knowl. Data Eng.* **2018**, *31*, 1341–1354. [[CrossRef](#)]
19. Xiao, Y.; Zhang, L.; Li, Q.; Liu, L. MM-SIS: Model for multiple information spreading in multiplex network. *Phys. A Stat. Mech. Its Appl.* **2019**, *513*, 135–146. [[CrossRef](#)]
20. Danziger, M.M.; Bonamassa, I.; Boccaletti, S.; Havlin, S. Dynamic interdependence and competition in multilayer networks. *Nat. Phys.* **2019**, *15*, 178–185. [[CrossRef](#)]
21. Alvarez-Zuzek, L.G.; La Rocca, C.E.; Vazquez, F.; Braunstein, L.A. Interacting social processes on interconnected networks. *PLoS ONE* **2016**, *11*, e0163593. [[CrossRef](#)]
22. Kahr, M.; Leitner, M.; Ruthmair, M.; Sinnl, M. Benders decomposition for competitive influence maximization in (social) networks. *Omega* **2021**, *100*, 102264. [[CrossRef](#)]
23. Zhang, Y.; Zhou, S.; Zhang, Z.; Guan, J.; Zhou, S. Rumor evolution in social networks. *Phys. Rev. E* **2013**, *87*, 032133. [[CrossRef](#)]
24. Zhou, X.; Hu, Y.; Wu, Y.; Xiong, X. Influence analysis of information erupted on social networks based on SIR model. *Int. J. Mod. Phys. C* **2015**, *26*, 1550018. [[CrossRef](#)]
25. Xiong, X.; Qiao, S.; Han, N.; Li, Y.; Xiong, F.; He, L. Affective impression: Sentiment-awareness POI suggestion via embedding in heterogeneous LBSNs. *IEEE Trans. Affect. Comput.* **2019**, *13*, 272–284. [[CrossRef](#)]
26. Xiong, X.; Li, Y.; Qiao, S.; Han, N.; Wu, Y.; Peng, J.; Li, B. An emotional contagion model for heterogeneous social media with multiple behaviors. *Phys. A Stat. Mech. Its Appl.* **2018**, *490*, 185–202. [[CrossRef](#)]
27. Zhu, H.; Wu, H.; Cao, J.; Fu, G.; Li, H. Information dissemination model for social media with constant updates. *Phys. A Stat. Mech. Its Appl.* **2018**, *502*, 469–482. [[CrossRef](#)]
28. Shang, J.; Liu, L.; Li, X.; Xie, F.; Wu, C. Epidemic spreading on complex networks with overlapping and non-overlapping community structure. *Phys. A Stat. Mech. Its Appl.* **2015**, *419*, 171–182. [[CrossRef](#)]
29. Wang, W.; Wang, Z.X.; Cai, S.M. Critical phenomena of information spreading dynamics on networks with cliques. *Phys. Rev. E* **2018**, *98*, 052312. [[CrossRef](#)]
30. Scarselli, D.; Budanur, N.B.; Timme, M.; Hof, B. Discontinuous epidemic transition due to limited testing. *Nat. Commun.* **2021**, *12*, 2586. [[CrossRef](#)] [[PubMed](#)]
31. Beutel, A.; Prakash, B.A.; Rosenfeld, R.; Faloutsos, C. Interacting viruses in networks: Can both survive? In Proceedings of the Proceedings of the 18th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, Beijing, China, 12–16 August 2012; pp. 426–434.
32. Wei, X.; Valler, N.C.; Prakash, B.A.; Neamtii, I.; Faloutsos, M.; Faloutsos, C. Competing memes propagation on networks: A network science perspective. *IEEE J. Sel. Areas Commun.* **2013**, *31*, 1049–1060. [[CrossRef](#)]
33. Fan, J.; Zhao, D.; Xia, C.; Tanimoto, J. Coupled spreading between information and epidemics on multiplex networks with simplicial complexes. *Chaos Interdiscip. J. Nonlinear Sci.* **2022**, *32*, 113115. [[CrossRef](#)] [[PubMed](#)]
34. Gómez, S.; Arenas, A.; Borge-Holthoefer, J.; Meloni, S.; Moreno, Y. Discrete-time Markov chain approach to contact-based disease spreading in complex networks. *Europhys. Lett.* **2010**, *89*, 38009. [[CrossRef](#)]
35. Guo, Q.; Lei, Y.; Jiang, X.; Ma, Y.; Huo, G.; Zheng, Z. Epidemic spreading with activity-driven awareness diffusion on multiplex network. *Chaos Interdiscip. J. Nonlinear Sci.* **2016**, *26*, 043110. [[CrossRef](#)] [[PubMed](#)]

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36. Trpevski, D.; Tang, W.K.; Kocarev, L. Model for rumor spreading over networks. *Phys. Rev. E* **2010**, *81*, 056102. [[CrossRef](#)] [[PubMed](#)]
 37. Barabási, A.L.; Albert, R. Emergence of scaling in random networks. *Science* **1999**, *286*, 509–512. [[CrossRef](#)] [[PubMed](#)]

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