

Supplementary materials

Bio-mathematical two-pathway model. The initial number of fragments $n_0 = n_0(t)$ is assumed to be produced proportional to the dose rate R and a cleavage constant k_{cleav} . The number of fragments $n_{1,fast} = n_{1,fast}(t)$ represents fragments recruited for the fast repair-pathway by a first order kinetics process with the speed constant $k_{0,fast}$. Following the fast repair pathway, the number $n_{2,fast} = n_{2,fast}(t)$ is counting fragments prepared for the fast final repair process by a “delayed” first order kinetics process with the speed constant $k_{1,fast}$, the delay time $t_{r,fast}$. These fragments are removed by a second order process (two fragments are linked together) with the repair constant $k_{2,fast}$. The slow repair pathway has the same structure with the number of fragments recruited for the slow repair pathway $n_{1,slow} = n_{1,slow}(t)$ by a first order kinetics process with the speed constant $k_{0,slow}$ and the number of fragments $n_{2,slow} = n_{2,slow}(t)$ prepared for the slow final repair process by a “delayed” first order kinetics process (speed constant $k_{1,slow}$; delay time $t_{r,slow}$) and removed by second order repair (repair constant $k_{2,slow}$). The total number of free fragments (visible in the Comet tail) is calculated by:

$$n_{Comet} = n_0 + \sum_i (n_{i,fast} + n_{i,slow}) + b_n \quad (1)$$

where b_n is the base line number of fragments that can be estimated along with the other parameters. All numbers of fragments are scaled to the percentage of DNA in tail (%DNA fragments in tail, corresponding to the experimental data). The induction-, production-, and repair rates are given by the following system of ordinary (ODE) and delay differential equations (DDE):

$$\begin{aligned} \frac{dn_0}{dt} &= k_{cleav} R - (k_{0,fast} + k_{0,slow}) \cdot n_0 \\ \frac{dn_{1,fast}}{dt} &= k_{0,fast} n_0 - k_{1,fast} n_{1,fast} (t - t_{r,fast}) \\ \frac{dn_{2,fast}}{dt} &= k_{1,fast} n_{1,fast} (t - t_{r,fast}) - k_{2,fast} n_{2,fast}^2 \\ \frac{dn_{1,slow}}{dt} &= k_{0,slow} n_0 - k_{1,slow} n_{1,slow} (t - t_{r,slow}) \\ \frac{dn_{2,slow}}{dt} &= k_{1,slow} n_{1,slow} (t - t_{r,slow}) - k_{2,slow} n_{2,slow}^2 \end{aligned} \tag{2}$$

With the initial conditions:

$$n_0(0) = n_{2,fast}(0) = n_{2,slow}(0) = 0$$

and

$$n_{1,fast}(t < 0) = n_{1,slow}(t < 0) = 0$$