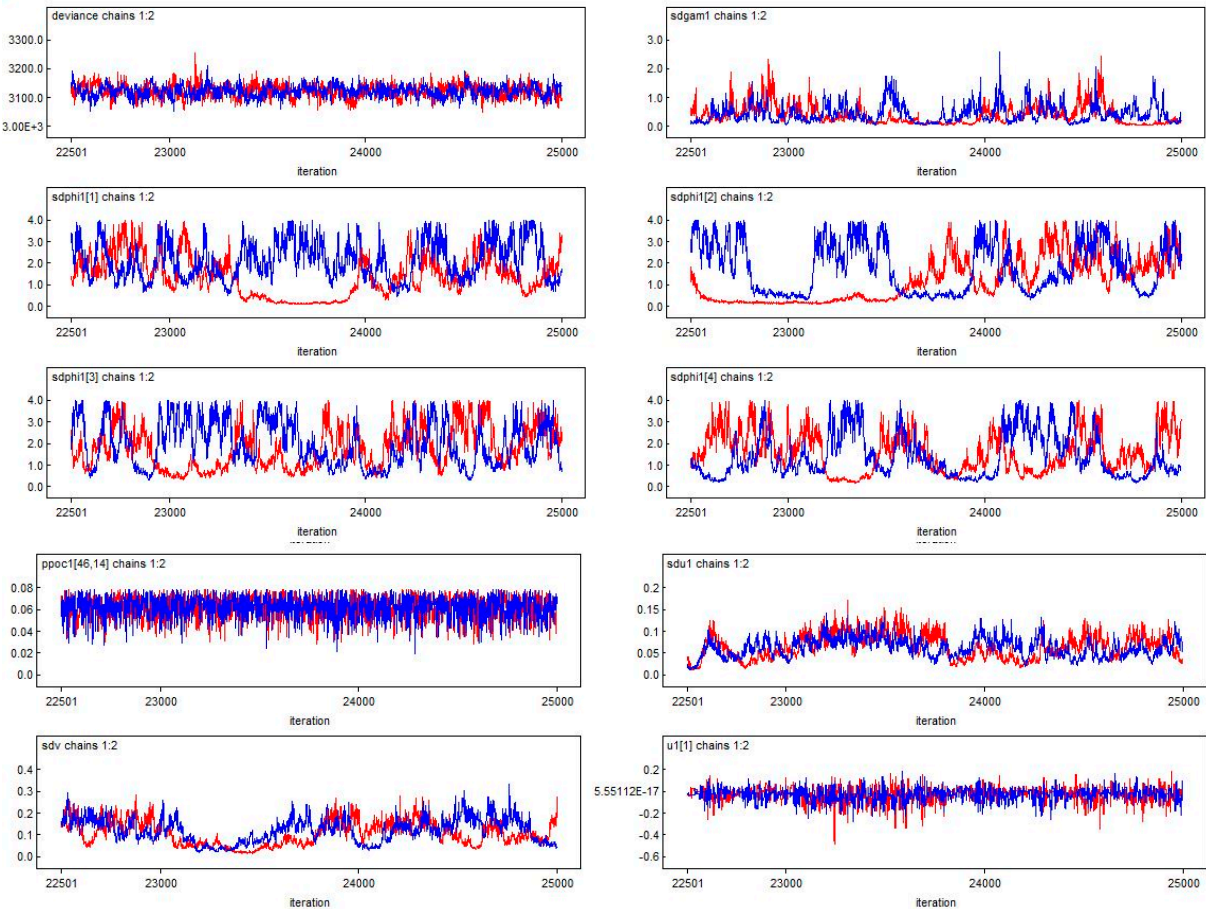


Supplemental Convergence Information

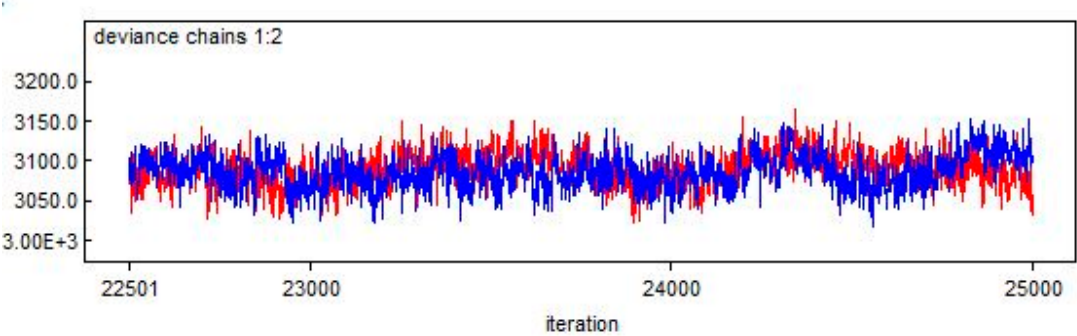
Trace plots of the deviance for all models, as well as some of the random effects' standard deviations are below. The univariate results are for oral/pharynx cancer. The deviance is also broken down by disease for the bivariate and multivariate plots such that d1 is lung, d2 is oral/pharynx, and d3 is melanoma.

Univariate

Alt 1

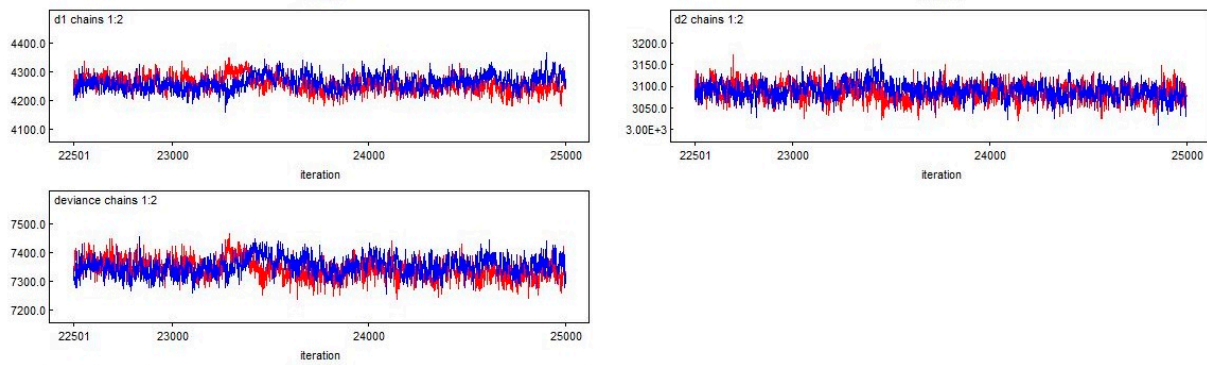


Alt 2

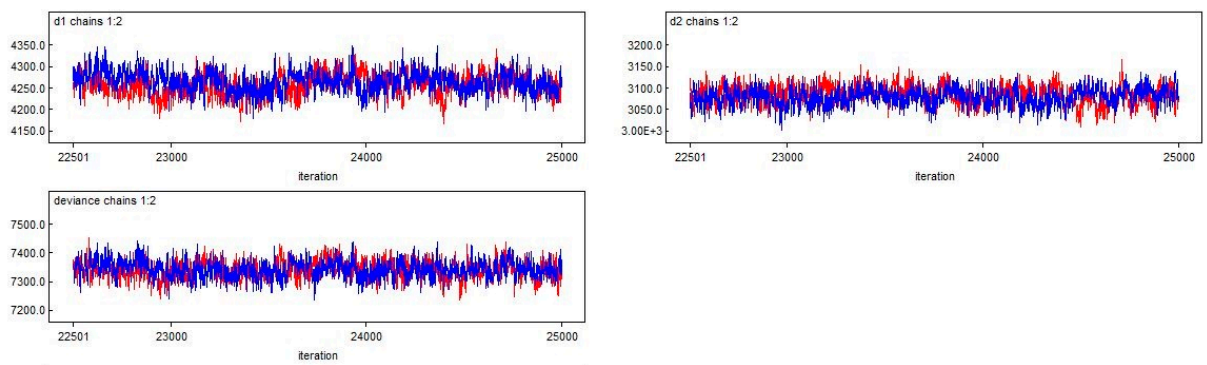


## Bivariate

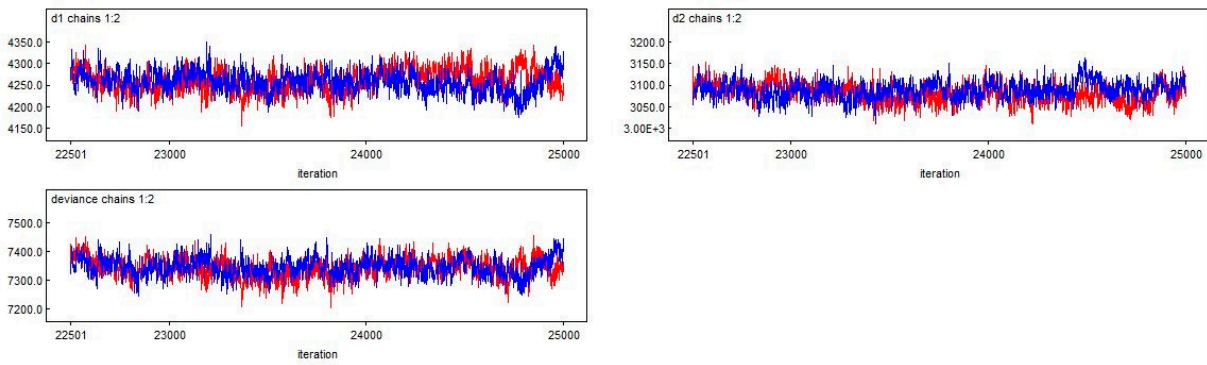
### Alt 1



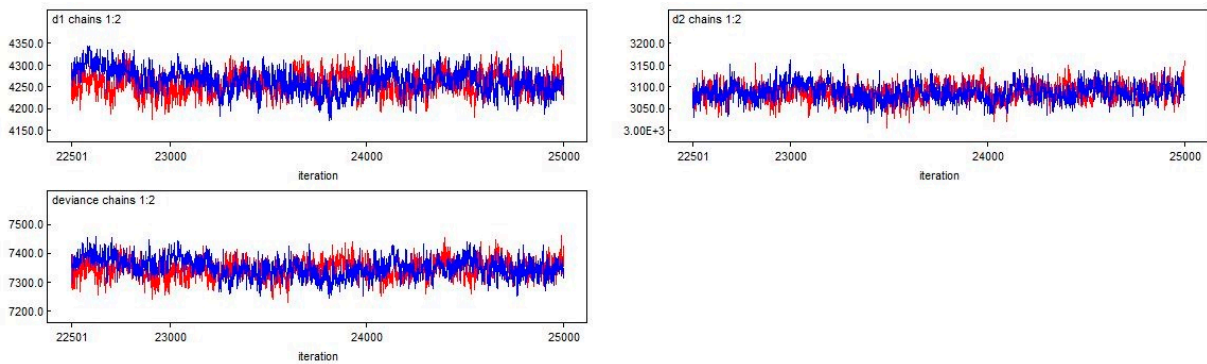
### Alt2



### Alt 3a

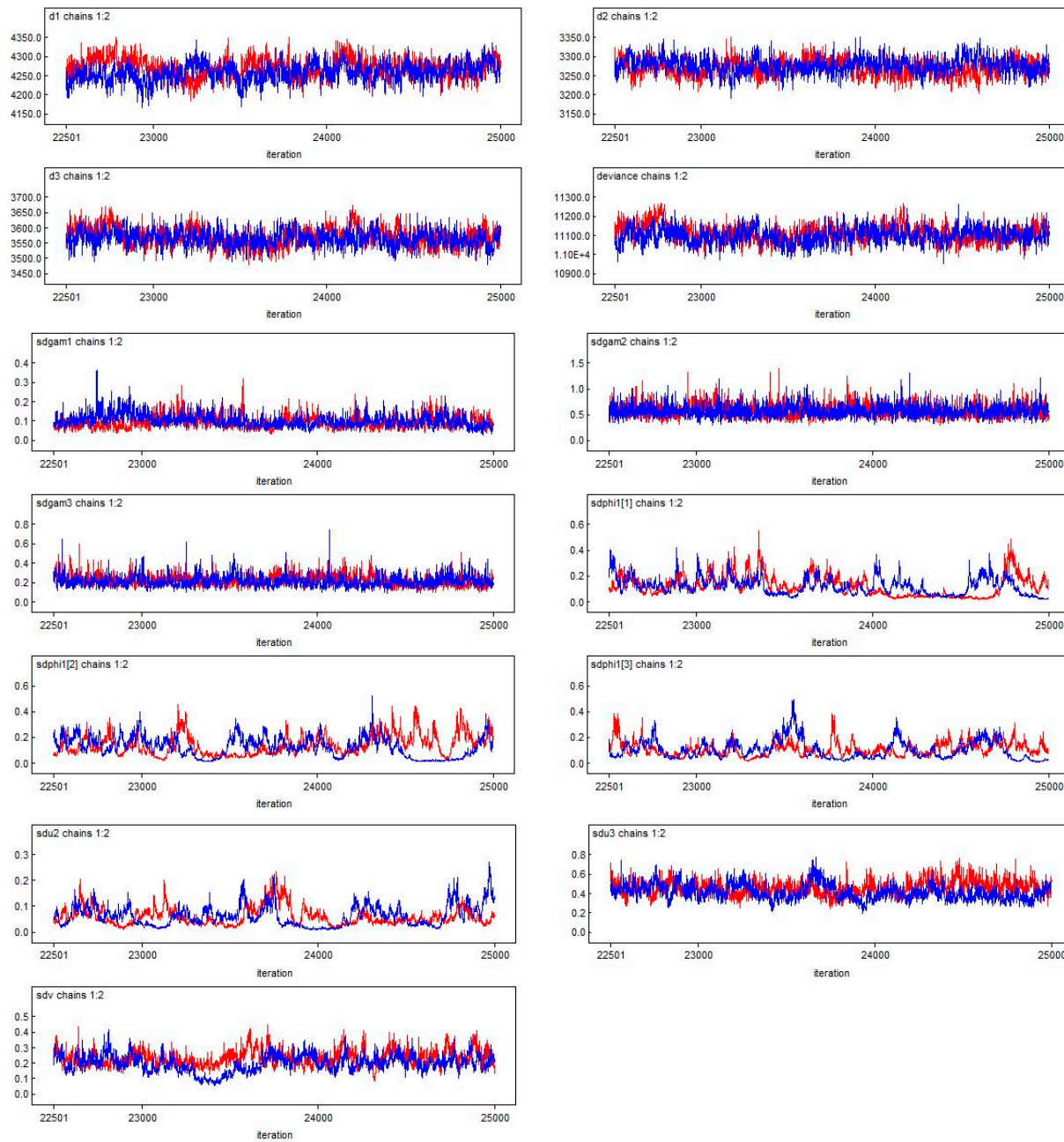


### Alt 3b

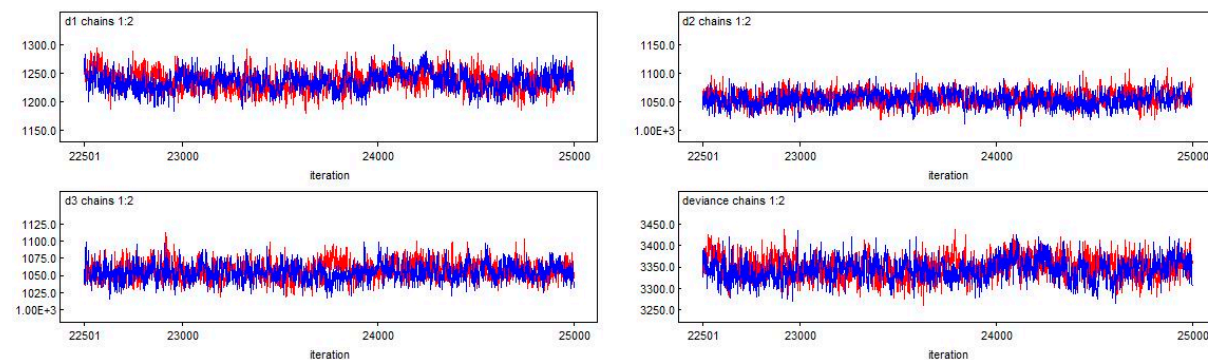


## Multivariate

### Alt 1

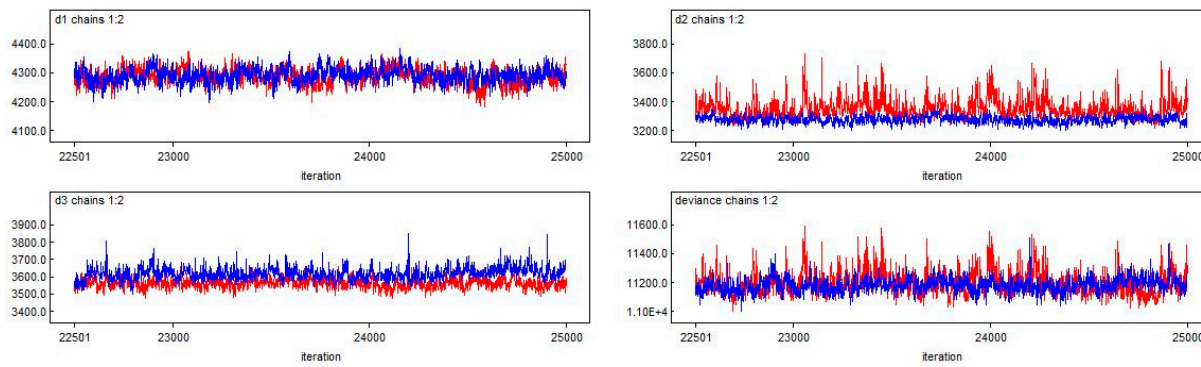


### Alt 2

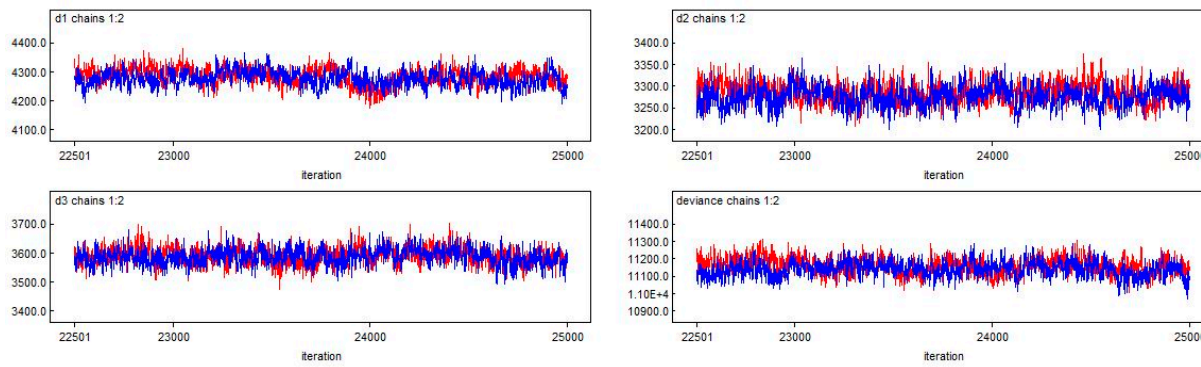




### Alt 3a



### Alt 3b



Supplemental Tables and Figures

The following Tables S1–S3 display the goodness of fit measures for overall, lung, and melanoma over all models respectively.

Table S1. Overall goodness of fit results for all cancers.

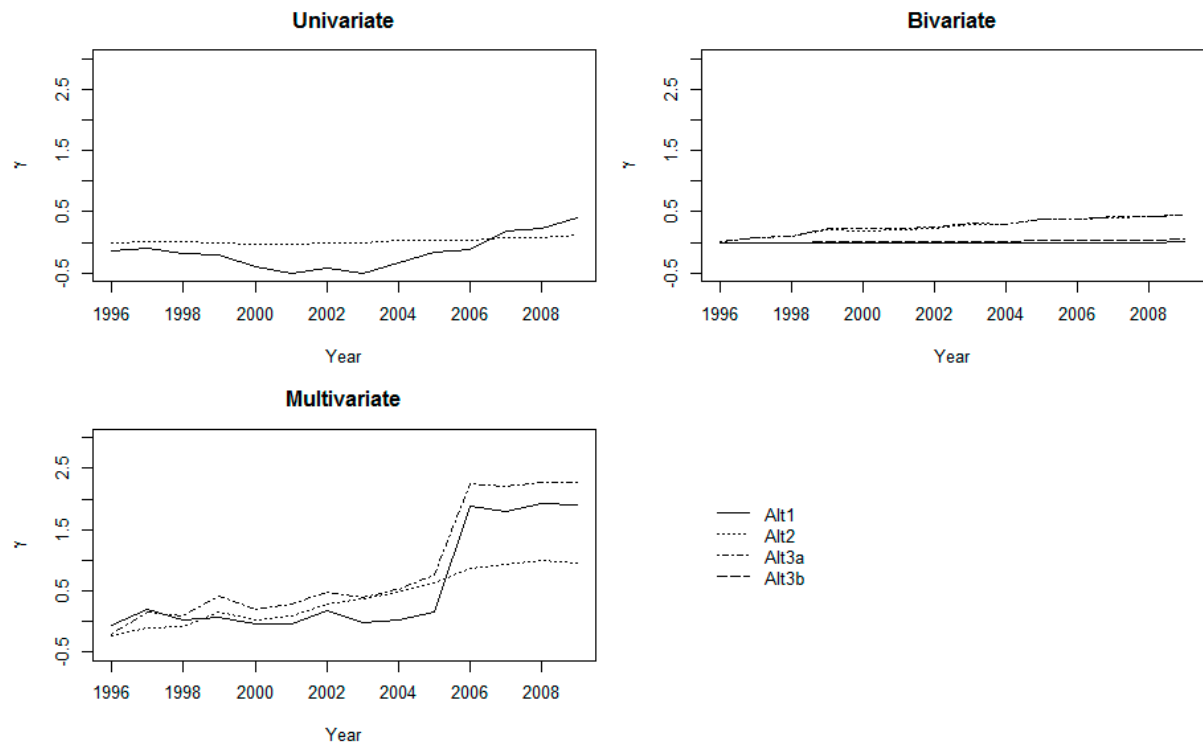
		Univariate, Sum of Oral/Pharynx and Lung		Bivariate				Univariate, Sum of All 3		Multivariate			
		Alt1	Alt2	Alt1	Alt2	Alt3a	Alt3b	Alt1	Alt2	Alt1	Alt2	Alt3a	Alt3b
WAIC	'96-'09	7695.81	8869.27	7615.10	<b>7609.03</b>	7618.74	<b>7611.42</b>	<b>11,494.82</b>	12,676.63	11,772.66	11,796.13	11,588.21	12,328.05
pD	'96-'09	245.14	291.71	228.80	229.98	231.15	228.89	433.04	490.93	490.42	505.69	467.66	835.92
MSPE	'96-'09	915.95	<b>735.50</b>	770.49	746.56	771.59	784.32	<b>1081.03</b>	934.77	14,975.96	14,807.69	14,809.43	14,425.79

Table S2. Goodness of fit results for melanoma cancer of the skin.

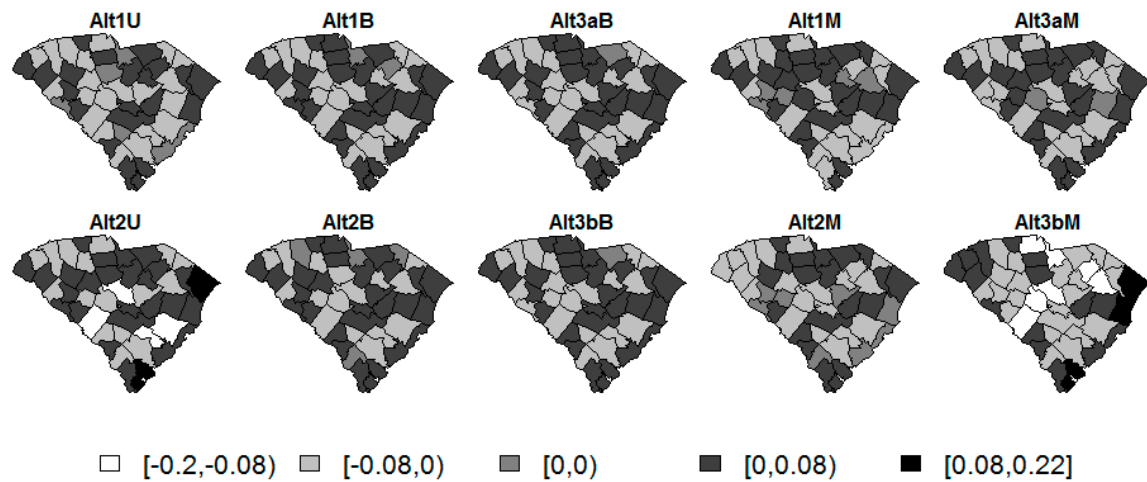
		Univariate		Multivariate			
		Alt1	Alt2	Alt1	Alt2	Alt3a	Alt3b
WAIC	'96-'09	3799.01	3807.36	3839.02	3826.78	<b>3737.80</b>	3781.34
	'96-'05	<b>2659.56</b>	2675.25	2689.43	2683.93	2672.38	2698.71
	'06-'09	1139.45	1132.12	1137.36	1155.09	<b>1065.42</b>	1082.62
pD	'96-'09	187.90	199.22	197.10	206.69	176.61	194.37
	'96-'05	135.59	145.21	151.16	138.74	125.79	137.55
	'06-'09	52.30	54.01	55.53	58.36	50.82	56.82
MSPE	'96-'09	<b>165.08</b>	199.27	172.32	195.25	<b>164.75</b>	187.11
	'96-'05	<b>103.88</b>	140.41	112.26	135.74	104.99	122.26
	'06-'09	61.20	<b>58.86</b>	60.06	59.51	59.76	64.85

**Table S3.** Goodness of fit results for lung and bronchus cancer.

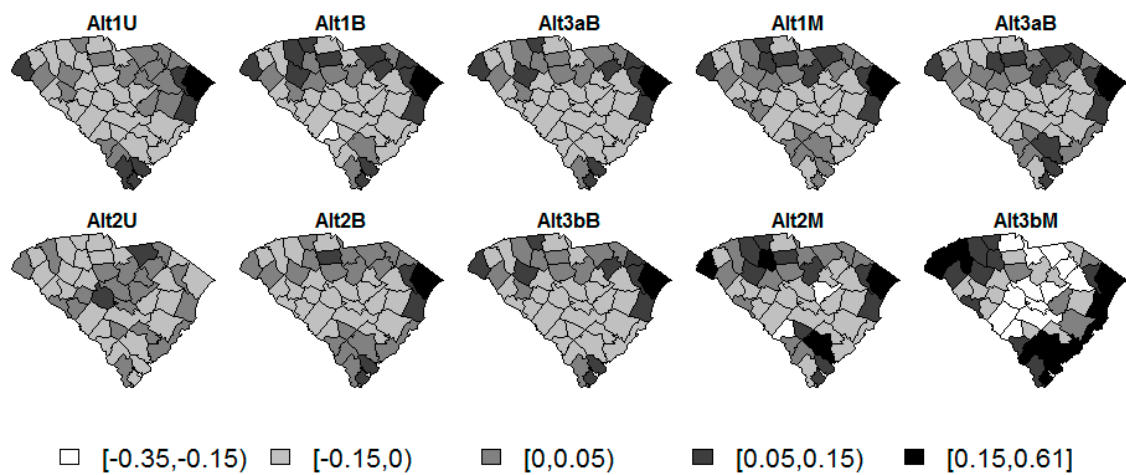
		Univariate		Bivariate				Multivariate			
		Alt1	Alt2	Alt1	Alt2	Alt3a	Alt3b	Alt1	Alt2	Alt3a	Alt3b
WAIC	'96-'09	4456.72	4420.56	4429.08	4416.26	4423.77	4419.24	4506.70	4448.71	4380.12	<b>4362.04</b>
	'96-'05	3131.58	3115.17	3116.14	3109.59	3115.81	3114.61	3136.12	3102.10	3113.24	<b>3096.35</b>
	'06-'09	1325.13	1305.40	1302.94	1306.66	1307.97	1304.63	1316.34	1302.10	<b>1266.89</b>	<b>1265.69</b>
pD	'96-'09	139.85	134.40	134.49	133.32	137.71	135.13	162.25	157.31	141.62	140.54
	'96-'05	81.93	81.97	81.16	81.90	82.68	82.20	82.20	82.20	100.17	98.85
	'06-'09	57.92	52.43	53.33	51.42	55.03	52.92	52.92	52.92	41.45	41.68
MSPE	'96-'09	761.92	618.50	652.56	634.92	654.78	669.09	766.56	616.84	690.71	<b>559.89</b>
	'96-'05	503.08	429.78	460.65	431.01	455.44	458.66	<b>511.05</b>	442.33	484.87	<b>392.09</b>
	'06-'09	258.84	188.73	191.91	203.91	247.26	210.44	255.51	174.51	205.83	<b>167.80</b>



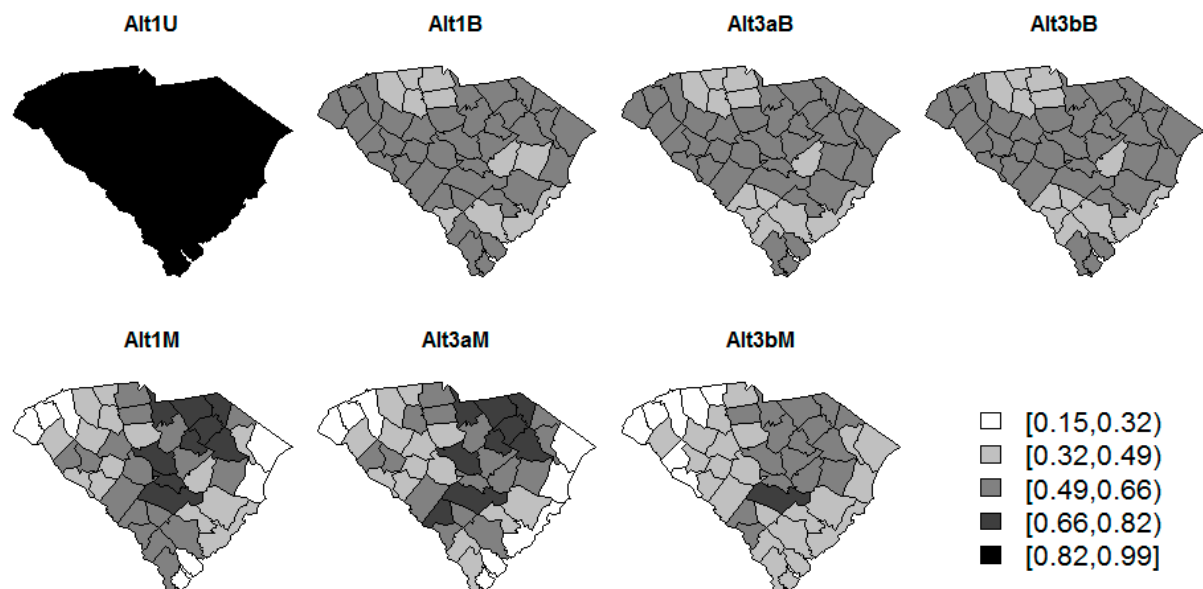
**Figure S1.**  $\gamma_{jk}$ ,  $\gamma_j$ , and  $f(\gamma_j, \rho_k)$  posterior mean estimates for univariate and multivariate fits of Alt1, Alt2, and Alt3 for oral cavity and pharynx cancer.



**Figure S2.** Posterior mean  $u_i$  estimates for Alt1 and Alt2 in the univariate and multivariate framework.

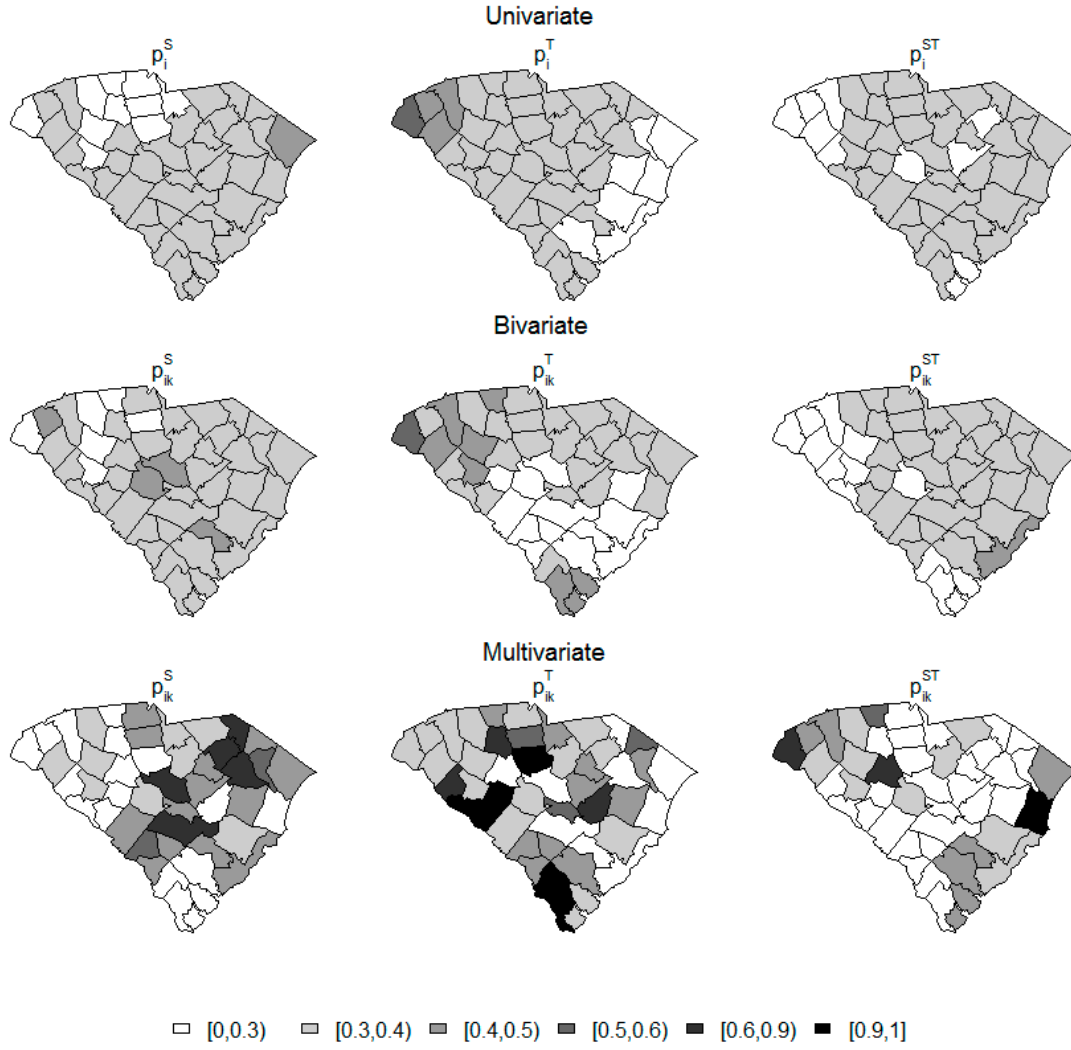


**Figure S3.** Posterior mean  $v_i$  estimates for Alt1 and Alt2 as well as univariate and multivariate.



**Figure S4.** Alt1 oral cavity and pharynx cancer posterior mean mixture parameter estimates in the univariate, bivariate, and multivariate settings.





**Figure S5.** Alt2 oral/pharynx posterior mean mixture parameter estimates ( $p_i^S$ ,  $p_i^T$ ,  $p_i^{ST}$ ,  $p_{ik}^S$ ,  $p_{ik}^T$ , and  $p_{ik}^{ST}$ ) in the univariate, bivariate, and multivariate settings.

**Table S4.** Posterior mean fixed effect coefficient estimates for the best fitting model, Alt2B.

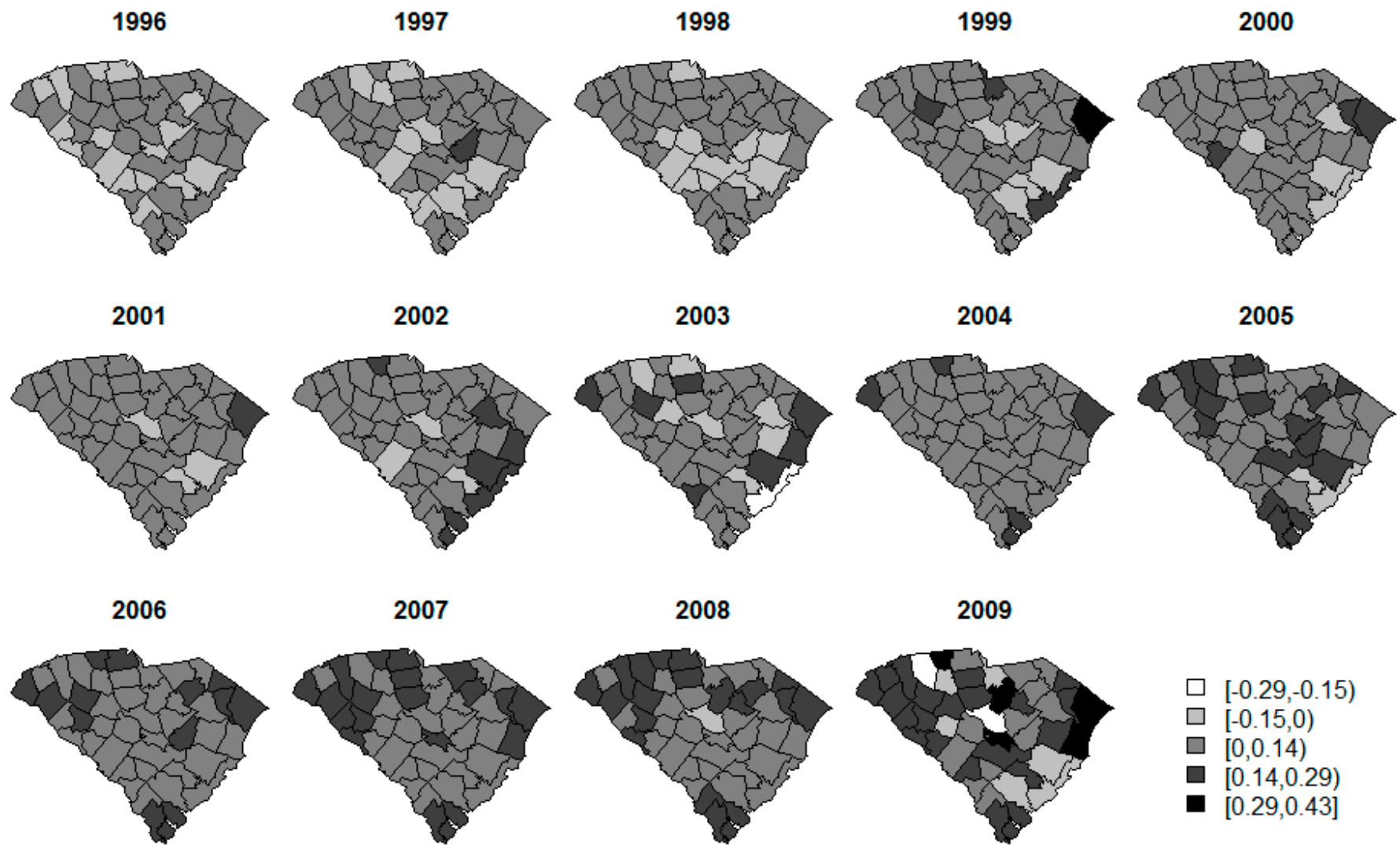
Parameter	Mean	2.5%	97.5%
$\beta_{1,1}^S$	0.030819	-0.12271	0.203728
$\beta_{1,2}^S$	-0.02111	-0.1741	0.1677
$\beta_{1,3}^S$	-0.00107	-0.16281	0.1538
$\beta_{2,1}^S$	0.077557	-0.1123	0.2907
$\beta_{2,2}^S$	-0.16376	-0.43809	0.02683
$\beta_{2,3}^S$	0.080206	-0.11041	0.2881
$\beta_1^T$	-0.02091	-0.06491	0.018883
$\beta_2^T$	0.036927	-0.0375	0.1182
$\beta_{1,1,1}^{ST}$	-0.01605	-0.13121	0.061783
$\beta_{1,1,2}^{ST}$	0.013176	-0.05502	0.113015
$\beta_{1,1,3}^{ST}$	0.014457	-0.06366	0.117518
$\beta_{1,1,4}^{ST}$	-0.00554	-0.10001	0.077849
$\beta_{1,1,5}^{ST}$	0.01349	-0.06014	0.1165
$\beta_{1,1,6}^{ST}$	0.019758	-0.04797	0.126813
$\beta_{1,1,7}^{ST}$	0.00132	-0.07664	0.086639

$\beta_{1,1,8}^{ST}$	-0.01403	-0.10851	0.054963
$\beta_{1,1,9}^{ST}$	-0.00505	-0.09051	0.066932
$\beta_{1,1,10}^{ST}$	0.014129	-0.06109	0.115305
$\beta_{1,1,11}^{ST}$	-0.01349	-0.1151	0.057241
$\beta_{1,1,12}^{ST}$	-0.013	-0.10792	0.059841
$\beta_{1,1,13}^{ST}$	0.016244	-0.059	0.126113
$\beta_{1,1,14}^{ST}$	0.018128	-0.05227	0.1194
$\beta_{1,2,1}^{ST}$	-0.00153	-0.06074	0.054125
$\beta_{1,2,2}^{ST}$	0.008101	-0.03138	0.075319
$\beta_{1,2,3}^{ST}$	0.002473	-0.04271	0.063052
$\beta_{1,2,4}^{ST}$	0.003228	-0.04446	0.05606
$\beta_{1,2,5}^{ST}$	-0.00214	-0.05152	0.05026
$\beta_{1,2,6}^{ST}$	0.003596	-0.0421	0.064112
$\beta_{1,2,7}^{ST}$	0.005881	-0.03408	0.067362
$\beta_{1,2,8}^{ST}$	-0.00212	-0.06005	0.04479
$\beta_{1,2,9}^{ST}$	-0.0166	-0.09529	0.019074
$\beta_{1,2,10}^{ST}$	0.003702	-0.04558	0.06968
$\beta_{1,2,11}^{ST}$	-0.00713	-0.07584	0.036534
$\beta_{1,2,12}^{ST}$	-0.00947	-0.08793	0.0347
$\beta_{1,2,13}^{ST}$	-0.00921	-0.09105	0.036513
$\beta_{1,2,14}^{ST}$	0.003427	-0.04512	0.06183
$\beta_{1,3,1}^{ST}$	0.012069	-0.0942	0.146218
$\beta_{1,3,2}^{ST}$	-0.01506	-0.1226	0.079462
$\beta_{1,3,3}^{ST}$	0.002684	-0.1073	0.117008
$\beta_{1,3,4}^{ST}$	-0.0209	-0.1437	0.067091
$\beta_{1,3,5}^{ST}$	0.048153	-0.03964	0.222
$\beta_{1,3,6}^{ST}$	-0.01909	-0.14021	0.08059
$\beta_{1,3,7}^{ST}$	0.001756	-0.1052	0.108913
$\beta_{1,3,8}^{ST}$	-0.02004	-0.1352	0.06988
$\beta_{1,3,9}^{ST}$	0.042302	-0.04044	0.187503
$\beta_{1,3,10}^{ST}$	0.033306	-0.04981	0.1691
$\beta_{1,3,11}^{ST}$	-0.00688	-0.12351	0.1031
$\beta_{1,3,12}^{ST}$	0.012898	-0.0857	0.136613
$\beta_{1,3,13}^{ST}$	0.020966	-0.07667	0.169603
$\beta_{1,3,14}^{ST}$	-0.01256	-0.12871	0.087511
$\beta_{2,1,1}^{ST}$	0.010562	-0.1787	0.2209
$\beta_{2,1,2}^{ST}$	0.043124	-0.13	0.290205
$\beta_{2,1,3}^{ST}$	-0.05771	-0.3073	0.102505
$\beta_{2,1,4}^{ST}$	0.008362	-0.18223	0.201705
$\beta_{2,1,5}^{ST}$	0.07509	-0.0825	0.3578
$\beta_{2,1,6}^{ST}$	0.040369	-0.13681	0.262725
$\beta_{2,1,7}^{ST}$	0.039854	-0.13432	0.2703
$\beta_{2,1,8}^{ST}$	0.052673	-0.1228	0.318603
$\beta_{2,1,9}^{ST}$	-0.0162	-0.2189	0.156125
$\beta_{2,1,10}^{ST}$	-0.02632	-0.25393	0.147433
$\beta_{2,1,11}^{ST}$	0.051826	-0.09616	0.280005
$\beta_{2,1,12}^{ST}$	-0.05075	-0.26898	0.09944

---

$\beta_{2,1,13}^{ST}$	0.022996	-0.14102	0.229403
$\beta_{2,1,14}^{ST}$	0.02791	-0.15713	0.26839
$\beta_{2,2,1}^{ST}$	-0.00019	-0.12242	0.1247
$\beta_{2,2,2}^{ST}$	0.014576	-0.08649	0.16042
$\beta_{2,2,3}^{ST}$	0.018992	-0.08161	0.168015
$\beta_{2,2,4}^{ST}$	0.045032	-0.03691	0.2533
$\beta_{2,2,5}^{ST}$	0.024071	-0.06888	0.190618
$\beta_{2,2,6}^{ST}$	-0.00977	-0.14371	0.08895
$\beta_{2,2,7}^{ST}$	0.051478	-0.02805	0.2759
$\beta_{2,2,8}^{ST}$	-0.02054	-0.20052	0.083313
$\beta_{2,2,9}^{ST}$	0.014638	-0.07873	0.149015
$\beta_{2,2,10}^{ST}$	-0.02902	-0.2058	0.05692
$\beta_{2,2,11}^{ST}$	0.007344	-0.0882	0.130708
$\beta_{2,2,12}^{ST}$	-0.00346	-0.12452	0.1102
$\beta_{2,2,13}^{ST}$	-0.02393	-0.1796	0.065083
$\beta_{2,2,14}^{ST}$	0.008337	-0.1115	0.1573
$\beta_{2,3,1}^{ST}$	-0.05394	-0.30442	0.1208
$\beta_{2,3,2}^{ST}$	0.012937	-0.17571	0.233808
$\beta_{2,3,3}^{ST}$	-0.04308	-0.30924	0.1407
$\beta_{2,3,4}^{ST}$	-0.02199	-0.2552	0.1668
$\beta_{2,3,5}^{ST}$	0.03514	-0.14971	0.2894
$\beta_{2,3,6}^{ST}$	0.029794	-0.13982	0.26782
$\beta_{2,3,7}^{ST}$	0.019208	-0.1622	0.236208
$\beta_{2,3,8}^{ST}$	0.086876	-0.07877	0.412903
$\beta_{2,3,9}^{ST}$	-0.04227	-0.26351	0.1117
$\beta_{2,3,10}^{ST}$	-0.03697	-0.27001	0.1383
$\beta_{2,3,11}^{ST}$	0.01105	-0.16391	0.199333
$\beta_{2,3,12}^{ST}$	-0.0206	-0.2455	0.15421
$\beta_{2,3,13}^{ST}$	0.030659	-0.15302	0.268328
$\beta_{2,3,14}^{ST}$	0.013567	-0.1862	0.2403

---



**Figure S6.** Sum of the posterior mean random effects times posterior mean mixture parameters ( $p_{ik}^S(u_{ik} + v_i) + p_{ik}^T\gamma_j + p_{ik}^{ST}\phi_{ijk}$ ) associated with oral cavity and pharynx cancer for Alt2B.

## Supplemental Code

Only multivariate code is included but the univariate equivalents can be deduced from these.

```
#Model Alt 1
model{
  for (i in 1: 46){
    for (j in 1: 14){
      #model set up
      exp1[i,j]<-POPL[i,j]*R1
      Y1[i,j]~dpois(mu1[i,j])
      log(mu1[i,j])<-log(exp1[i,j])+log(theta1[i,j])
      log(theta1[i,j])<-a01+p1[i]*modS1[i]+(1-p1[i])*modST1[i,j]
      ppoc1[i,j] <- exp(-mu1[i,j] + Y1[i,j]*log(mu1[i,j]) -
        logfact(Y1[i,j]) )
      # inverse of the conditional predictive ordinate
      icpoc1[i,j] <- 1/ppoc1[i,j]
      logppoc1[i,j]<-log(ppoc1[i,j])
      ll1[i,j]<-Y1[i,j]*log(mu1[i,j])-logfact(Y1[i,j])-mu1[i,j]
      exp2[i,j]<-POPL[i,j]*R2
      Y2[i,j]~dpois(mu2[i,j])
      log(mu2[i,j])<-log(exp2[i,j])+log(theta2[i,j])
      log(theta2[i,j])<-a02+p2[i]*modS2[i]+(1-p2[i])*modST2[i,j]
      ppoc2[i,j] <- exp(-mu2[i,j] + Y2[i,j]*log(mu2[i,j]) -
        logfact(Y2[i,j]) )
      # inverse of the conditional predictive ordinate
      icpoc2[i,j] <- 1/ppoc2[i,j]
      logppoc2[i,j]<-log(ppoc2[i,j])
      ll2[i,j]<-Y2[i,j]*log(mu2[i,j])-logfact(Y2[i,j])-mu2[i,j]
      exp3[i,j]<-POPL[i,j]*R3
      Y3[i,j]~dpois(mu3[i,j])
      log(mu3[i,j])<-log(exp3[i,j])+log(theta3[i,j])
      log(theta3[i,j])<-a03+p3[i]*modS3[i]+(1-p3[i])*modST3[i,j]
      ppoc3[i,j] <- exp(-mu3[i,j] + Y3[i,j]*log(mu3[i,j]) -
        logfact(Y3[i,j]) )
      # inverse of the conditional predictive ordinate
      icpoc3[i,j] <- 1/ppoc3[i,j]
      logppoc3[i,j]<-log(ppoc3[i,j])
      ll3[i,j]<-Y3[i,j]*log(mu3[i,j])-logfact(Y3[i,j])-mu3[i,j]
    }
  }
  #ST component
  modST1[i,j]<-gam1[j]+phi1[i,j]+aST1[1,j]*xST1[i,j]+aST1[2,j]*xST2[i,j]+
    aST1[3,j]*xST3[i,j]+aT1*xT[j]
```



```

      modST2[i,j]<-gam2[j]+phi2[i,j]+aST2[1,j]*xST1[i,j]+aST2[2,j]*xST2[i,j]+
        aST2[3,j]*xST3[i,j]+aT2*xT[j]
      modST3[i,j]<-gam3[j]+phi3[i,j]+aST3[1,j]*xST1[i,j]+aST3[2,j]*xST2[i,j]+
        aST3[3,j]*xST3[i,j]+aT3*xT[j]
      phi1[i,j]~dnorm(0,tauphi1[j])
      phi2[i,j]~dnorm(0,tauphi2[j])
      phi3[i,j]~dnorm(0,tauphi3[j])
    }#close j loop
#spatial components
    modS1[i]<-v[i]+u1[i]+aS1[1]*xS1[i]+aS1[2]*xS2[i]+aS1[3]*xS3[i]
    modS2[i]<-v[i]+u2[i]+aS2[1]*xS1[i]+aS2[2]*xS2[i]+aS2[3]*xS3[i]
    modS3[i]<-v[i]+u3[i]+aS3[1]*xS1[i]+aS3[2]*xS2[i]+aS3[3]*xS3[i]
    u1[i]~dnorm(0,tauu1)
    u2[i]~dnorm(0,tauu2)
    u3[i]~dnorm(0,tauu3)
    logit(p1[i])<-z1[i]+alp1[i]
    alp1[i]~dnorm(0,taualp1)
    logit(p2[i])<-z2[i]+alp2[i]
    alp2[i]~dnorm(0,taualp2)
    logit(p3[i])<-z3[i]+alp3[i]
    alp3[i]~dnorm(0,taualp3)
  }#close i loop
d1<--2*sum(ll1[,])
d2<--2*sum(ll2[,])
d3<--2*sum(ll3[,])
z1[1:46]~car.normal(adj[,weights[,num[,taup1)
z2[1:46]~car.normal(adj[,weights[,num[,taup2)
z3[1:46]~car.normal(adj[,weights[,num[,taup3)
v[1:46]~car.normal(adj[,weights[,num[,tauv)      #shared CH
for(k in 1:sumNumNeigh){weights[k]<-1}
for(j in 1:14){
  tauphi1[j]<-pow(sdphi1[j],-2)
  tauphi2[j]<-pow(sdphi2[j],-2)
  tauphi3[j]<-pow(sdphi3[j],-2)
  sdphi1[j]~dunif(0,4)
  sdphi2[j]~dunif(0,4)
  sdphi3[j]~dunif(0,4)
  MPLc1[j]<-sum(logppoc1[,j])
  MPLc2[j]<-sum(logppoc2[,j])
  MPLc3[j]<-sum(logppoc3[,j])
}#close j loop
gam1[1]~dnorm(0,taugam1)

```

```

gam2[1]~dnorm(0,taugam2)
gam3[1]~dnorm(0,taugam3)
for (j in 2:14){
    gam1[j]~dnorm(gam1[j-1],taugam1)
    gam2[j]~dnorm(gam2[j-1],taugam2)
    gam3[j]~dnorm(gam3[j-1],taugam3)
}#close j loop
taup1<-pow(sdp1,-2)
sdp1~dunif(0,4)
taup2<-pow(sdp2,-2)
sdp2~dunif(0,4)
taup3<-pow(sdp3,-2)
sdp3~dunif(0,4)
tauv<-pow(sdv,-2)
sdv~dunif(0,4)
taugam1<-pow(sdgam1,-2)
sdgam1~dunif(0,4)
taugam2<-pow(sdgam2,-2)
sdgam2~dunif(0,4)
taugam3<-pow(sdgam3,-2)
sdgam3~dunif(0,4)
a01~dnorm(0,tau01)
tau01<-pow(sd01,-2)
sd01~dunif(0,4)
a02~dnorm(0,tau02)
tau02<-pow(sd02,-2)
sd02~dunif(0,4)
a03~dnorm(0,tau03)
tau03<-pow(sd03,-2)
sd03~dunif(0,4)
tauu1<-pow(sdu1,-2)
sdu1~dunif(0,4)
tauu2<-pow(sdu2,-2)
sdu2~dunif(0,4)
tauu3<-pow(sdu3,-2)
sdu3~dunif(0,4)
taualp1<-pow(sdalp1,-2)
sdalp1~dunif(0,4)
taualp2<-pow(sdalp2,-2)
sdalp2~dunif(0,4)
taualp3<-pow(sdalp3,-2)
sdalp3~dunif(0,4)

```

#separate temporal

```

aT1~dnorm(0,tauaT1)
tauaT1<-pow(sdaT1,-2)
sdaT1~dunif(0,4)
aT2~dnorm(0,tauaT2)
tauaT2<-pow(sdaT2,-2)
sdaT2~dunif(0,4)
aT3~dnorm(0,tauaT3)
tauaT3<-pow(sdaT3,-2)
sdaT3~dunif(0,4)
for (k in 1:3){
  aS1[k]~dnorm(0,tauaS1[k])
  tauaS1[k]<-pow(sdaS1[k],-2)
  sdaS1[k]~dunif(0,4)
  aS2[k]~dnorm(0,tauaS2[k])
  tauaS2[k]<-pow(sdaS2[k],-2)
  sdaS2[k]~dunif(0,4)
  aS3[k]~dnorm(0,tauaS3[k])
  tauaS3[k]<-pow(sdaS3[k],-2)
  sdaS3[k]~dunif(0,4)
  for (j in 1:14){
    aST1[k,j]~dnorm(0,tauaST1[k])
    aST2[k,j]~dnorm(0,tauaST2[k])
    aST3[k,j]~dnorm(0,tauaST3[k])
  }#close j loop
  tauaST1[k]<-pow(sdaST1[k],-2)
  sdaST1[k]~dunif(0,4)
  tauaST2[k]<-pow(sdaST2[k],-2)
  sdaST2[k]~dunif(0,4)
  tauaST3[k]<-pow(sdaST3[k],-2)
  sdaST3[k]~dunif(0,4)

}#close k loop
}#close model loop

```

#Model Alt 2

```

model{
  for (i in 1: 46){
    for (j in 1: 14){
#model set up
      exp1[i,j]<-POPL[i,j]*R1
      Y1[i,j]~dpois(mu1[i,j])
      log(mu1[i,j])<-log(exp1[i,j])+log(theta1[i,j])

```

```

log(theta1[i,j])<-a01+p11[i]*modS1[i]+p12[i]*modT1[j]+p13[i]*modST1[i,j]
ppoc1[i,j] <- exp(-mu1[i,j] + Y1[i,j]*log(mu1[i,j]) -
  logfact(Y1[i,j]) )
# inverse of the conditional predictive ordinate
icpoc1[i,j] <- 1/ppoc1[i,j]
logppoc1[i,j]<-log(ppoc1[i,j])
ll1[i,j]<-Y1[i,j]*log(mu1[i,j])-logfact(Y1[i,j])-mu1[i,j]
exp2[i,j]<-POPL[i,j]*R2
Y2[i,j]~dpois(mu2[i,j])
log(mu2[i,j])<-log(exp2[i,j])+log(theta2[i,j])
log(theta2[i,j])<-a02+p21[i]*modS2[i]+p22[i]*modT2[j]+p23[i]*modST2[i,j]
ppoc2[i,j] <- exp(-mu2[i,j] + Y2[i,j]*log(mu2[i,j]) -
  logfact(Y2[i,j]) )
# inverse of the conditional predictive ordinate
icpoc2[i,j] <- 1/ppoc2[i,j]
logppoc2[i,j]<-log(ppoc2[i,j])
ll2[i,j]<-Y2[i,j]*log(mu2[i,j])-logfact(Y2[i,j])-mu2[i,j]
exp3[i,j]<-POPL[i,j]*R3
Y3[i,j]~dpois(mu3[i,j])
log(mu3[i,j])<-log(exp3[i,j])+log(theta3[i,j])
log(theta3[i,j])<-a03+p31[i]*modS3[i]+p32[i]*modT3[j]+p33[i]*modST3[i,j]
ppoc3[i,j] <- exp(-mu3[i,j] + Y3[i,j]*log(mu3[i,j]) -
  logfact(Y3[i,j]) )
# inverse of the conditional predictive ordinate
icpoc3[i,j] <- 1/ppoc3[i,j]
logppoc3[i,j]<-log(ppoc3[i,j])
ll3[i,j]<-Y3[i,j]*log(mu3[i,j])-logfact(Y3[i,j])-mu3[i,j]
modST1[i,j]<-phi1[i,j]+aST1[1,j]*xST1[i,j]+aST1[2,j]*xST2[i,j]+
  aST1[3,j]*xST3[i,j]
modST2[i,j]<-phi2[i,j]+aST2[1,j]*xST1[i,j]+aST2[2,j]*xST2[i,j]+
  aST2[3,j]*xST3[i,j]
modST3[i,j]<-phi3[i,j]+aST3[1,j]*xST1[i,j]+aST3[2,j]*xST2[i,j]+
  aST3[3,j]*xST3[i,j]

```

#ST RE

```

  phi1[i,j]~dnorm(0,tauphi1[j])
  phi2[i,j]~dnorm(0,tauphi2[j])
  phi3[i,j]~dnorm(0,tauphi3[j])
}#close j loop
modS1[i]<-v[i]+u1[i]+aS1[1]*xS1[i]+aS1[2]*xS2[i]+aS1[3]*xS3[i]
modS2[i]<-v[i]+u2[i]+aS2[1]*xS1[i]+aS2[2]*xS2[i]+aS2[3]*xS3[i]
modS3[i]<-v[i]+u3[i]+aS3[1]*xS1[i]+aS3[2]*xS2[i]+aS3[3]*xS3[i]
u1[i]~dnorm(0,tauu1)

```

```

u2[i]~dnorm(0,tauu2)                                #UH RE
u3[i]~dnorm(0,tauu3)
logit(q11[i])<-z11[i]+alp11[i]
alp11[i]~dnorm(0,taualp1)
logit(q12[i])<-z12[i]+alp12[i]
alp12[i]~dnorm(0,taualp1)
logit(q13[i])<-z13[i]+alp13[i]
alp13[i]~dnorm(0,taualp1)
qsum1[i]<-q11[i]+q12[i]+q13[i]
p11[i]<-q11[i]/qsum1[i]
p12[i]<-q12[i]/qsum1[i]
p13[i]<-q13[i]/qsum1[i]
logit(q21[i])<-z21[i]+alp21[i]
alp21[i]~dnorm(0,taualp2)
logit(q22[i])<-z22[i]+alp22[i]
alp22[i]~dnorm(0,taualp2)
logit(q23[i])<-z23[i]+alp23[i]
alp23[i]~dnorm(0,taualp2)
qsum2[i]<-q21[i]+q22[i]+q23[i]
p21[i]<-q21[i]/qsum2[i]
p22[i]<-q22[i]/qsum2[i]
p23[i]<-q23[i]/qsum2[i]
logit(q31[i])<-z31[i]+alp31[i]
alp31[i]~dnorm(0,taualp3)
logit(q32[i])<-z32[i]+alp32[i]
alp32[i]~dnorm(0,taualp3)
logit(q33[i])<-z33[i]+alp33[i]
alp33[i]~dnorm(0,taualp3)
qsum3[i]<-q31[i]+q32[i]+q33[i]
p31[i]<-q31[i]/qsum3[i]
p32[i]<-q32[i]/qsum3[i]
p33[i]<-q33[i]/qsum3[i]
}#close i loop
d1<--2*sum(ll1[,])
d2<--2*sum(ll2[,])
d3<--2*sum(ll3[,])
z11[1:46]~car.normal(adj[],weights[],num[],taup1)
z12[1:46]~car.normal(adj[],weights[],num[],taup1)
z13[1:46]~car.normal(adj[],weights[],num[],taup1)
z21[1:46]~car.normal(adj[],weights[],num[],taup2)
z22[1:46]~car.normal(adj[],weights[],num[],taup2)
z23[1:46]~car.normal(adj[],weights[],num[],taup2)

```



```

z31[1:46]~car.normal(adj[],weights[],num[],taup3)
z32[1:46]~car.normal(adj[],weights[],num[],taup3)
z33[1:46]~car.normal(adj[],weights[],num[],taup3)
v[1:46]~car.normal(adj[],weights[],num[],tauv)           #shared spatial
for(k in 1:sumNumNeigh){weights[k]<-1}
for(j in 1:14){
  modT1[j]<-gam[j]+aT1*xT[j]
  modT2[j]<-gam[j]+aT2*xT[j]           #temporal component
  modT3[j]<-gam[j]+aT3*xT[j]
  tauphi1[j]<-pow(sdphi1[j],-2)
  tauphi2[j]<-pow(sdphi2[j],-2)
  tauphi3[j]<-pow(sdphi3[j],-2)
  sdphi1[j]~dunif(0,4)
  sdphi2[j]~dunif(0,4)
  sdphi3[j]~dunif(0,4)
  MPLc1[j]<-sum(logppoc1[,j])
  MPLc2[j]<-sum(logppoc2[,j])
  MPLc3[j]<-sum(logppoc3[,j])
}#close j loop
gam[1]~dnorm(0,taugam)
for (j in 2:14){
  gam[j]~dnorm(gam[j-1],taugam)           #shared temporal RE
}#close j loop
taup1<-pow(sdp1,-2)
sdp1~dunif(0,4)
taup2<-pow(sdp2,-2)
sdp2~dunif(0,4)
taup3<-pow(sdp3,-2)
sdp3~dunif(0,4)
tauv<-pow(sdv,-2)
sdv~dunif(0,4)
taugam<-pow(sdgam,-2)
sdgam~dunif(0,4)
a01~dnorm(0,tau01)
tau01<-pow(sd01,-2)
sd01~dunif(0,4)
a02~dnorm(0,tau02)
tau02<-pow(sd02,-2)
sd02~dunif(0,4)
a03~dnorm(0,tau03)
tau03<-pow(sd03,-2)
sd03~dunif(0,4)

```

```

tauu1<-pow(sdu1,-2)
sdu1~dunif(0,4)
tauu2<-pow(sdu2,-2)
sdu2~dunif(0,4)
tauu3<-pow(sdu3,-2)
sdu3~dunif(0,4)
taualp1<-pow(sdalp1,-2)
sdalp1~dunif(0,4)
taualp2<-pow(sdalp2,-2)
sdalp2~dunif(0,4)
taualp3<-pow(sdalp3,-2)
sdalp3~dunif(0,4)
aT1~dnorm(0,tauaT1)
tauaT1<-pow(sdaT1,-2)
sdaT1~dunif(0,4)
aT2~dnorm(0,tauaT2)
tauaT2<-pow(sdaT2,-2)
sdaT2~dunif(0,4)
aT3~dnorm(0,tauaT3)
tauaT3<-pow(sdaT3,-2)
sdaT3~dunif(0,4)
for (k in 1:3){
  aS1[k]~dnorm(0,tauaS1[k])
  tauaS1[k]<-pow(sdaS1[k],-2)
  sdaS1[k]~dunif(0,4)
  aS2[k]~dnorm(0,tauaS2[k])
  tauaS2[k]<-pow(sdaS2[k],-2)
  sdaS2[k]~dunif(0,4)
  aS3[k]~dnorm(0,tauaS3[k])
  tauaS3[k]<-pow(sdaS3[k],-2)
  sdaS3[k]~dunif(0,4)
  for (j in 1:14){
    aST1[k,j]~dnorm(0,tauaST1[k])
    aST2[k,j]~dnorm(0,tauaST2[k])
    aST3[k,j]~dnorm(0,tauaST3[k])
  }#close j loop
  tauaST1[k]<-pow(sdaST1[k],-2)
  sdaST1[k]~dunif(0,4)
  tauaST2[k]<-pow(sdaST2[k],-2)
  sdaST2[k]~dunif(0,4)
  tauaST3[k]<-pow(sdaST3[k],-2)
  sdaST3[k]~dunif(0,4)
}

```

```

}#close k loop
}#close model loop

#Model Alt 3a
model{
for (i in 1: 46){
  for (j in 1: 14){
    exp1[i,j]<-POPL[i,j]*R1
    Y1[i,j]~dpois(mu1[i,j])
    log(mu1[i,j])<-log(exp1[i,j])+log(theta1[i,j])
    log(theta1[i,j])<-a01+p1[i]*modS1[i]+(1-p1[i])*modST1[i,j]
    ppoc1[i,j] <- exp(-mu1[i,j] + Y1[i,j]*log(mu1[i,j]) -
      logfact(Y1[i,j]) )
    # inverse of the conditional predictive ordinate
    icpoc1[i,j] <- 1/ppoc1[i,j]
    logppoc1[i,j]<-log(ppoc1[i,j])
    ll1[i,j]<-Y1[i,j]*log(mu1[i,j])-logfact(Y1[i,j])-mu1[i,j]
    exp2[i,j]<-POPL[i,j]*R2
    Y2[i,j]~dpois(mu2[i,j])
    log(mu2[i,j])<-log(exp2[i,j])+log(theta2[i,j])
    log(theta2[i,j])<-a02+p2[i]*modS2[i]+(1-p2[i])*modST2[i,j]
    ppoc2[i,j] <- exp(-mu2[i,j] + Y2[i,j]*log(mu2[i,j]) -
      logfact(Y2[i,j]) )
    # inverse of the conditional predictive ordinate
    icpoc2[i,j] <- 1/ppoc2[i,j]
    logppoc2[i,j]<-log(ppoc2[i,j])
    ll2[i,j]<-Y2[i,j]*log(mu2[i,j])-logfact(Y2[i,j])-mu2[i,j]
    exp3[i,j]<-POPL[i,j]*R3
    Y3[i,j]~dpois(mu3[i,j])
    log(mu3[i,j])<-log(exp3[i,j])+log(theta3[i,j])
    log(theta3[i,j])<-a03+p3[i]*modS3[i]+(1-p3[i])*modST3[i,j]
    ppoc3[i,j] <- exp(-mu3[i,j] + Y3[i,j]*log(mu3[i,j]) -
      logfact(Y3[i,j]) )
    # inverse of the conditional predictive ordinate
    icpoc3[i,j] <- 1/ppoc3[i,j]
    logppoc3[i,j]<-log(ppoc3[i,j])
    ll3[i,j]<-Y3[i,j]*log(mu3[i,j])-logfact(Y3[i,j])-mu3[i,j]
    modST1[i,j]<-rho[1]*gam[j]+phi1[i,j]+aST1[1,j]*xST1[i,j]+aST1[2,j]*xST2[i,j]+
      aST1[3,j]*xST3[i,j]+aT1*xT[j]
    modST2[i,j]<-rho[2]*gam[j]+phi2[i,j]+aST2[1,j]*xST1[i,j]+aST2[2,j]*xST2[i,j]+
      aST2[3,j]*xST3[i,j]+aT2*xT[j]
    modST3[i,j]<-rho[3]*gam[j]+phi3[i,j]+aST3[1,j]*xST1[i,j]+aST3[2,j]*xST2[i,j]+

```

```

      aST3[3,j]*xST3[i,j]+aT3*xT[j]
      phi1[i,j]~dnorm(0,tauphi1[j])
      phi2[i,j]~dnorm(0,tauphi2[j])
      phi3[i,j]~dnorm(0,tauphi3[j])
    }#close j loop
    modS1[i]<-v[i]+u1[i]+aS1[1]*xS1[i]+aS1[2]*xS2[i]+aS1[3]*xS3[i]
    modS2[i]<-v[i]+u2[i]+aS2[1]*xS1[i]+aS2[2]*xS2[i]+aS2[3]*xS3[i]
    modS3[i]<-v[i]+u3[i]+aS3[1]*xS1[i]+aS3[2]*xS2[i]+aS3[3]*xS3[i]
    u1[i]~dnorm(0,tauu1)
    u2[i]~dnorm(0,tauu2)
    u3[i]~dnorm(0,tauu3)
    logit(p1[i])<-z1[i]+alp1[i]
    alp1[i]~dnorm(0,taualp1)
    logit(p2[i])<-z2[i]+alp2[i]
    alp2[i]~dnorm(0,taualp2)
    logit(p3[i])<-z3[i]+alp3[i]
    alp3[i]~dnorm(0,taualp3)
  }#close i loop
  d1<--2*sum(ll1[,])
  d2<--2*sum(ll2[,])
  d3<--2*sum(ll3[,])
  z1[1:46]~car.normal(adj[,weights[,num[,taup1)
  z2[1:46]~car.normal(adj[,weights[,num[,taup2)
  z3[1:46]~car.normal(adj[,weights[,num[,taup3)
  v[1:46]~car.normal(adj[,weights[,num[,tauv)
  for(k in 1:sumNumNeigh){weights[k]<-1}
  for(j in 1:14){
    tauphi1[j]<-pow(sdphi1[j],-2)
    tauphi2[j]<-pow(sdphi2[j],-2)
    tauphi3[j]<-pow(sdphi3[j],-2)
    sdphi1[j]~dunif(0,4)
    sdphi2[j]~dunif(0,4)
    sdphi3[j]~dunif(0,4)
    MPLc1[j]<-sum(logppoc1[,j])
    MPLc2[j]<-sum(logppoc2[,j])
    MPLc3[j]<-sum(logppoc3[,j])
  }#close j loop
  gam[1]~dnorm(0,taugam)
  for (j in 2:14){
    gam[j]~dnorm(gam[j-1],taugam)
  }#close j loop
  taup1<-pow(sdp1,-2)

```

```

sdp1~dunif(0,4)
taup2<-pow(sdp2,-2)
sdp2~dunif(0,4)
taup3<-pow(sdp3,-2)
sdp3~dunif(0,4)
tauv<-pow(sdv,-2)
sdv~dunif(0,4)
taugam<-pow(sdgam,-2)
sdgam~dunif(0,4)
a01~dnorm(0,tau01)
tau01<-pow(sd01,-2)
sd01~dunif(0,4)
a02~dnorm(0,tau02)
tau02<-pow(sd02,-2)
sd02~dunif(0,4)
a03~dnorm(0,tau03)
tau03<-pow(sd03,-2)
sd03~dunif(0,4)
tauu1<-pow(sdu1,-2)
sdu1~dunif(0,4)
tauu2<-pow(sdu2,-2)
sdu2~dunif(0,4)
tauu3<-pow(sdu3,-2)
sdu3~dunif(0,4)
taualp1<-pow(sdalp1,-2)
sdalp1~dunif(0,4)
taualp2<-pow(sdalp2,-2)
sdalp2~dunif(0,4)
taualp3<-pow(sdalp3,-2)
sdalp3~dunif(0,4)
aT1~dnorm(0,tauaT1)
tauaT1<-pow(sdaT1,-2)
sdaT1~dunif(0,4)
aT2~dnorm(0,tauaT2)
tauaT2<-pow(sdaT2,-2)
sdaT2~dunif(0,4)
aT3~dnorm(0,tauaT3)
tauaT3<-pow(sdaT3,-2)
sdaT3~dunif(0,4)
for (k in 1:3){
  aS1[k]~dnorm(0,tauaS1[k])
  tauaS1[k]<-pow(sdaS1[k],-2)
}

```



```

sdaS1[k]~dunif(0,4)
aS2[k]~dnorm(0,tauaS2[k])
tauaS2[k]<-pow(sdaS2[k],-2)
sdaS2[k]~dunif(0,4)
aS3[k]~dnorm(0,tauaS3[k])
tauaS3[k]<-pow(sdaS3[k],-2)
sdaS3[k]~dunif(0,4)
rho[k]~dnorm(0,taurho[k])
taurho[k]<-pow(sdrho[k],-2)
sdrho[k]~dunif(0,10)
for (j in 1:14){
  aST1[k,j]~dnorm(0,tauaST1[k])
  aST2[k,j]~dnorm(0,tauaST2[k])
  aST3[k,j]~dnorm(0,tauaST3[k])
}#close j loop
  tauaST1[k]<-pow(sdaST1[k],-2)
  sdaST1[k]~dunif(0,4)
  tauaST2[k]<-pow(sdaST2[k],-2)
  sdaST2[k]~dunif(0,4)
  tauaST3[k]<-pow(sdaST3[k],-2)
  sdaST3[k]~dunif(0,4)

}#close k loop
}#close model loop

#Model Alt 3b
model{
for (i in 1: 46){
  for (j in 1: 14){
    exp1[i,j]<-POPL[i,j]*R1
    Y1[i,j]~dpois(mu1[i,j])
    log(mu1[i,j])<-log(exp1[i,j])+log(theta1[i,j])
    log(theta1[i,j])<-a01+p1[i]*modS1[i]+(1-p1[i])*modST1[i,j]
    ppoc1[i,j] <- exp(-mu1[i,j] + Y1[i,j]*log(mu1[i,j]) -
      logfact(Y1[i,j]) )
    # inverse of the conditional predictive ordinate
    icpoc1[i,j] <- 1/ppoc1[i,j]
    logppoc1[i,j]<-log(ppoc1[i,j])
    ll1[i,j]<-Y1[i,j]*log(mu1[i,j])-logfact(Y1[i,j])-mu1[i,j]
    exp2[i,j]<-POPL[i,j]*R2
    Y2[i,j]~dpois(mu2[i,j])
    log(mu2[i,j])<-log(exp2[i,j])+log(theta2[i,j])

```

```

log(theta2[i,j])<-a02+p2[i]*modS2[i]+(1-p2[i])*modST2[i,j]
ppoc2[i,j] <- exp(-mu2[i,j] + Y2[i,j]*log(mu2[i,j]) -
  logfact(Y2[i,j]) )
# inverse of the conditional predictive ordinate
icpoc2[i,j] <- 1/ppoc2[i,j]
logppoc2[i,j]<-log(ppoc2[i,j])
ll2[i,j]<-Y2[i,j]*log(mu2[i,j])-logfact(Y2[i,j])-mu2[i,j]
exp3[i,j]<-POPL[i,j]*R3
Y3[i,j]~dpois(mu3[i,j])
log(mu3[i,j])<-log(exp3[i,j])+log(theta3[i,j])
log(theta3[i,j])<-a03+p3[i]*modS3[i]+(1-p3[i])*modST3[i,j]
ppoc3[i,j] <- exp(-mu3[i,j] + Y3[i,j]*log(mu3[i,j]) -
  logfact(Y3[i,j]) )
# inverse of the conditional predictive ordinate
icpoc3[i,j] <- 1/ppoc3[i,j]
logppoc3[i,j]<-log(ppoc3[i,j])
ll3[i,j]<-Y3[i,j]*log(mu3[i,j])-logfact(Y3[i,j])-mu3[i,j]
modST1[i,j]<-pow(gam[j]*step(gam[j]),rho[1])+
  pow(gam[j]*(step(gam[j])-1),rho[1])*(-1)+
  phi1[i,j]+aST1[1,j]*xST1[i,j]+aST1[2,j]*xST2[i,j]+
  aST1[3,j]*xST3[i,j]+aT1*xT[j]
modST2[i,j]<-pow(gam[j]*step(gam[j]),rho[2])+
  pow(gam[j]*(step(gam[j])-1),rho[2])*(-1)+
  phi2[i,j]+aST2[1,j]*xST1[i,j]+aST2[2,j]*xST2[i,j]+
  aST2[3,j]*xST3[i,j]+aT2*xT[j]
modST3[i,j]<-pow(gam[j]*step(gam[j]),rho[3])+
  pow(gam[j]*(step(gam[j])-1),rho[3])*(-1)+
  phi3[i,j]+aST3[1,j]*xST1[i,j]+aST3[2,j]*xST2[i,j]+
  aST3[3,j]*xST3[i,j]+aT3*xT[j]
phi1[i,j]~dnorm(0,tauphi1[j])
phi2[i,j]~dnorm(0,tauphi2[j])
phi3[i,j]~dnorm(0,tauphi3[j])
}#close j loop
modS1[i]<-v[i]+u1[i]+aS1[1]*xS1[i]+aS1[2]*xS2[i]+aS1[3]*xS3[i]
modS2[i]<-v[i]+u2[i]+aS2[1]*xS1[i]+aS2[2]*xS2[i]+aS2[3]*xS3[i]
modS3[i]<-v[i]+u3[i]+aS3[1]*xS1[i]+aS3[2]*xS2[i]+aS3[3]*xS3[i]
u1[i]~dnorm(0,tauu1)
u2[i]~dnorm(0,tauu2)
u3[i]~dnorm(0,tauu3)
logit(p1[i])<-z1[i]+alp1[i]
alp1[i]~dnorm(0,taualp1)
logit(p2[i])<-z2[i]+alp2[i]

```

```

        alp2[i]~dnorm(0,taualp2)
        logit(p3[i])<-z3[i]+alp3[i]
        alp3[i]~dnorm(0,taualp3)
    }close i loop
    d1<--2*sum(l1[,])
    d2<--2*sum(l2[,])
    d3<--2*sum(l3[,])
    z1[1:46]~car.normal(adj[,weights[,num[,taup1)
    z2[1:46]~car.normal(adj[,weights[,num[,taup2)
    z3[1:46]~car.normal(adj[,weights[,num[,taup3)
    v[1:46]~car.normal(adj[,weights[,num[,tauv)
    for(k in 1:sumNumNeigh){weights[k]<-1}
    for(j in 1:14){
        tauphi1[j]<-pow(sdphi1[j],-2)
        tauphi2[j]<-pow(sdphi2[j],-2)
        tauphi3[j]<-pow(sdphi3[j],-2)
        sdphi1[j]~dunif(0,4)
        sdphi2[j]~dunif(0,4)
        sdphi3[j]~dunif(0,4)
        MPLc1[j]<-sum(logppoc1[,j])
        MPLc2[j]<-sum(logppoc2[,j])
        MPLc3[j]<-sum(logppoc3[,j])
    }#close j loop
    gam[1]~dnorm(0,taugam)
    for (j in 2:14){
        gam[j]~dnorm(gam[j-1],taugam)
    }#close j loop
    taup1<-pow(sdp1,-2)
    sdp1~dunif(0,4)
    taup2<-pow(sdp2,-2)
    sdp2~dunif(0,4)
    taup3<-pow(sdp3,-2)
    sdp3~dunif(0,4)
    tauv<-pow(sdv,-2)
    sdv~dunif(0,4)
    taugam<-pow(sdgam,-2)
    sdgam~dunif(0,4)
    a01~dnorm(0,tau01)
    tau01<-pow(sd01,-2)
    sd01~dunif(0,4)
    a02~dnorm(0,tau02)
    tau02<-pow(sd02,-2)

```

```

sd02~dunif(0,4)
a03~dnorm(0,tau03)
tau03<-pow(sd03,-2)
sd03~dunif(0,4)
tauu1<-pow(sdu1,-2)
sdu1~dunif(0,4)
tauu2<-pow(sdu2,-2)
sdu2~dunif(0,4)
tauu3<-pow(sdu3,-2)
sdu3~dunif(0,4)
taualp1<-pow(sdalp1,-2)
sdalp1~dunif(0,4)
taualp2<-pow(sdalp2,-2)
sdalp2~dunif(0,4)
taualp3<-pow(sdalp3,-2)
sdalp3~dunif(0,4)
aT1~dnorm(0,tauaT1)
tauaT1<-pow(sdaT1,-2)
sdaT1~dunif(0,4)
aT2~dnorm(0,tauaT2)
tauaT2<-pow(sdaT2,-2)
sdaT2~dunif(0,4)
aT3~dnorm(0,tauaT3)
tauaT3<-pow(sdaT3,-2)
sdaT3~dunif(0,4)
for (k in 1:3){
  aS1[k]~dnorm(0,tauaS1[k])
  tauaS1[k]<-pow(sdaS1[k],-2)
  sdaS1[k]~dunif(0,4)
  aS2[k]~dnorm(0,tauaS2[k])
  tauaS2[k]<-pow(sdaS2[k],-2)
  sdaS2[k]~dunif(0,4)
  aS3[k]~dnorm(0,tauaS3[k])
  tauaS3[k]<-pow(sdaS3[k],-2)
  sdaS3[k]~dunif(0,4)
  rho[k]~dgamma(2,1)
  for (j in 1:14){
    aST1[k,j]~dnorm(0,tauaST1[k])
    aST2[k,j]~dnorm(0,tauaST2[k])
    aST3[k,j]~dnorm(0,tauaST3[k])
  }#close j loop
  tauaST1[k]<-pow(sdaST1[k],-2)

```

```
sdaST1[k]~dunif(0,4)
tauaST2[k]<-pow(sdaST2[k],-2)
sdaST2[k]~dunif(0,4)
tauaST3[k]<-pow(sdaST3[k],-2)
sdaST3[k]~dunif(0,4)
}#close k loop
}#close model loop
```