



Article Disturbance Elimination for Partial Discharge Detection in the Spacer of Gas-Insulated Switchgears

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Abstract: With the increasing demand for precise condition monitoring and diagnosis of gas-insulated switchgears (GISs), it has become a challenge to improve the detection sensitivity of partial discharge (PD) induced in the GIS spacer. This paper deals with the elimination of the capacitive component from the phase-resolved partial discharge (PRPD) signal generated in GIS spacers based on discrete wavelet transform (WT). Three types of typical insulation defects were simulated using PD cells. The single PD pulses were detected and were further used to determine the optimal mother wavelet. As a result, the bior6.8 was selected to decompose the PD signal into 8 levels and the signal energy at each level was calculated. The decomposed components related with capacitive disturbance were discarded, whereas those associated with PD were de-noised by a threshold and a thresholding function. Finally, the PRPD signals were reconstructed using the de-noised components.

Keywords: partial discharge (PD); gas-insulated switchgears (GISs); spacer; capacitive component; wavelet transform (WT); multi-resolution analysis (MRA)

1. Introduction

Detection and analysis of partial discharge (PD) in insulation structures for gas-insulated switchgears (GISs), transformers, cables, and rotating machines are important to ensure their stable and reliable operation [1–6]. Among the components of GISs, the epoxy spacer is a critical part and can result in the eventual failure of GISs. It is usually examined by AC withstand voltage tests with high electrical stress and by PD tests [7,8]. It is specified that the maximum permissible PD level for GISs should not exceed 5 picocoulombs (pC) [9]. It is also indicated that the spacer should be replaced if the PD induced in spacer is greater than 1 pC [7]. However, the sensitivity of PD measurement is influenced by the capacitive current flowing in the GIS test section, especially in the spacer.

Figure 1 shows a PD signal detected within a cycle of the applied voltage, accumulation of such signals forms the phase-resolved partial discharge (PRPD) pattern. It can be seen that the disturbance due to the capacitive component is so high that the PD signal is seriously overlapped. Since the PRPD pattern is extracted using the peak detection technique, such distortion lowers the sensitivity of PD measurement and invalidates the specific feature of a defect, consequently making defect identification inaccurate. This problem has been dealt with by applying a high pass filter (HPF); however, it is difficult to determine the exact cutoff frequency of the filter since an improper filter attenuates the magnitude of PD. In addition, the filter cannot remove the disturbance completely.



Figure 1. Partial discharge (PD) signal detected within a cycle of applied voltage in gas-insulated switchgear (GIS) spacer.

The wavelet transform (WT) is an effective signal processing method and has achieved its application in the field of condition monitoring and diagnosis. It has been used for de-noising of the ultra-high frequency signal and eliminating the corona from PD signal [10–16]. In addition, parameters derived from wavelet decomposition are implemented in the feature extraction for defect classification [17,18]. Satish and Nazneen studied the de-noising of PD signals buried in excessive discrete spectral, stochastic, and random interferences using the WT method. The simulated signals and pulses detected from a point-plane gap were analyzed. The results revealed that the wavelet method was successful in rejecting all the three types of interference [11]. Ma et al. proposed the automatic level-dependent thresholding criterion for de-noising the damped exponential and damped oscillatory pulses immersed in noise when the narrow-band and the ultra-band detection circuit were used [12]. Zhou et al. introduced the filter pairs for wavelet decomposition and analyzed the frequency bands of the wavelet coefficients. By investigating the energy distribution at each decomposition level, the de-noising effect was significantly improved [13]. Zhang et al. implemented a WT technique to reject noise in on-site PD measurement in cables. The continuous sinusoidal noise, pulse-like noise, and white noise were successfully rejected [14,15]. Chang et al. presented a separation of corona from the PD signal by wavelet packet transform and a neural network method. The parameters including node energy, kurtosis, and skewness were calculated and used for characterizing PD signal and corona [16].

However, few works have been carried out to deal with the capacitive current for PD detection in GIS spacers using the WT method. This paper discusses the elimination of the capacitive component based on the WT technique for the purpose of improving the PD detection sensitivity in GIS spacers.

2. Insulation Defects in Spacer

Although various types of insulation defects have been introduced and evaluated, the ones existing in an epoxy spacer are regarded as the most critical and initiate the failure of GISs. Such defects are usually minute imperfections that are difficult to be detected, including a void inside spacer (VIS), a particle on spacer (POS), and a crack [6,19,20]. The VIS is the result from air bubbles produced during the manufacturing process of solid spacers, such as high temperature casting and curing of epoxy. The POS is a conductive contaminant or particle that adheres to the surface of insulating materials. Cracks are one of the most common defects in GISs, which are formed due to mechanical impacts from the outside, operations of the circuit breaker, and strains generated by heat shock [7,8,21]. These three types of defects were simulated using artificial PD cells, and the epoxy resin insulator for GIS spacer was used. The PD cells were filled with SF₆ gas with a pressure of 0.5 MPa. Figure 2 shows a PD cell for POS. The plane electrodes were made of tungsten–copper alloy with a diameter of 80 mm and a thickness of 20 mm. Their edges were rounded to prevent the concentration of the electric field [22]. An epoxy insulator with a height of 30 mm, and a length as well as a width of 10 mm was placed

between the high-voltage electrode (upper) and the grounding electrode (lower). The metallic particle was attached to the insulator by a very small amount of epoxy compound. For VIS and crack cells, epoxy plates with a diameter of 80 mm and a thickness of 20 mm were used, and both of them were collected from a GIS manufacturer.



Figure 2. PD cell for a particle on spacer (POS).

3. Experimental Setup

Figure 3 illustrates the experimental setup. A 220 V/50 kV PD-free dry-type transformer was used to apply high voltage to the PD cell. The transformer was immersed in insulation oil to ensure that there is no PD occurring adjacent to the transformer at high voltage. The applied voltage was tested using a high-voltage divider with a ratio of 10,000:1. The artificial PD cell was filled with SF₆ gas with a pressure of 0.5 MPa. For accurate measurement, PD signals were detected by a 50 Ω non-inductive resistor. A digital storage oscilloscope (DSO) with a sampling rate of 5 GS/s and an NI PXI (National Instruments, Austin, TX, USA) with a sampling rate of 250 MS/s were used for signal acquisition and analysis. The input impedance of DSO and PXI were set as 50 Ω for impedance matching.



Figure 3. Experimental setup.

4. Wavelet Transform

4.1. Selection of Mother Wavelet

The WT analyzes a signal in both time and frequency domains simultaneously using the scaled and shifted versions of the mother wavelet [23]. Therefore, a proper mother wavelet is of great importance to characterize a given signal. The mother wavelet can be categorized into the orthogonal wavelets (Daubechies (dbX), Coiflets (coifX), Symmlets (symX)) that are suitable for signal de-noising and compression, and the bi-orthogonal wavelets (biorX) that are fit for signal de-noising and feature extraction, where X is the order of the wavelet. The higher the order, the smoother the wavelet [12,24,25]. Two kinds of mother wavelets were considered in this section.

Since the PRPD pattern is the accumulation of single pulses within a certain period of time, the single PD pulses rather than the PD signal detected in a cycle of the applied voltage used to determine the optimal mother wavelet. Single PD pulses were extracted from three types of artificial PD cells. Figure 4 shows the typical detected pulses. The apparent charge values of PD pulses in the VIS, POS, and crack were 17.5 pC, 13.9 pC, and 20.4 pC, respectively [26].



Figure 4. Typical detected PD pulses. (a) In the void inside spacer (VIS); (b) in the POS; (c) in the crack.

Such pulses were compared with the mother wavelets by calculating their correlation coefficient that is given by

$$\gamma = \frac{\sum_{i=1}^{N-1} \left[X(i) - \overline{X} \right] \left[Y(i) - \overline{Y} \right]}{\sqrt{\sum_{i=1}^{N-1} \left[X(i) - \overline{X} \right]^2 \cdot \sum_{i=1}^{N-1} \left[Y(i) - \overline{Y} \right]^2}}$$
(1)

where X(i) and Y(i) are the single PD pulse and the mother wavelet, respectively, and \overline{X} and \overline{Y} are their mean values. A larger value of correlation coefficient indicates a higher similarity between these two signals. The calculation results of correlation coefficient are shown in Figure 5.

The results show that bior6.8 has the highest similarity with PD pulses occurring in the VIS and crack. In the POS, the mother wavelet that has the highest γ value of 0.421 with discharge pulses was bior2.8, and γ value of bior6.8 with pulses was 0.419. According to the average correlation coefficient value, bior6.8 was selected as the optimal mother wavelet for further investigation.



Figure 5. Correlation coefficient between the single PD pulses and the mother wavelets.

4.2. The Determination of Decomposition Level

A desirable decomposition level should avoid being redundant and have sufficient resolution to decompose a signal. According to Equation (2), the maximum number of decomposition level J_{max} depends on the record length (L_R) of signals, which is given by

$$J_{max} = fix(log_2 L_R) \tag{2}$$

where *fix* specifies the level to be the largest integer no greater than log_2L_R [24]. In this paper, the record length of the PRPD signal was 125 k bit, thus the maximum decomposition level was 16. This value was too high to cause a large amount of computation and a waste of time. The decomposition level can be also determined by

$$J_{max} = fix \left(log_2 \frac{L_R}{L_W - 1} \right) \tag{3}$$

where L_W is the length of the octave band filter associated with the corresponding mother wavelet [13,27]. The length of the selected wavelet bior6.8 is 17, so the maximum decomposition level was 12. In this paper, the decomposition level was selected as 8, which could characterize the PRPD signal with a sufficient resolution.

4.3. Decomposition of PRPD and Signal Energy

After selecting the optimal mother wavelet and determining the decomposition level, the PRPD signals were decomposed by discrete wavelet transform (DWT), using filter banks to calculate the wavelet coefficients. The signal was first down-sampled by an HPF and a low pass filter (LPF), generating the detail (D) and approximation (A) coefficient, respectively. The approximation component was then fed through another filter pair and down-sampled to the maximum decomposition level. This process is also known as multi-resolution analysis (MRA) [2,12,28–30]. Therefore, the result of MRA is the detail component at each level and an approximation component at the highest level.

Figure 6 demonstrates the decomposition of the PRPD signal in the VIS into 8 levels, generating the detail components D1–D8 at Levels 1–8 and the approximation component A8 at the 8th level. It can be seen that the detail components D1–D5, which are in the high frequency range, are associated with the PD signal, whereas the components D6–D8 that are in the low frequency range do not contain any PD information since they are related to the background noise. In addition, the approximate component A8 is regarded as a capacitive component.



Figure 6. Decomposition of the phase-resolved partial discharge (PRPD) signal in the VIS into 8 levels.

The signal energy of the detail component at each level was calculated by

Signal energy =
$$\sum_{i=1}^{N} x_i^2$$
 (4)

where x_i is the signal at each level and N is the signal length. The result is shown in Figure 7. In the detail components, 95.6% of signal energy was distributed in D1–D5, which were expected to be used for signal reconstruction. However, as indicated in Figure 6, there is still background noise interfering with the decomposed components. Therefore, a threshold and a thresholding function were implemented for de-noising the signals in D1–D5.



Figure 7. Signal energies distribution of detail components in the VIS.

4.4. Threshold and Thresholding Function

The automatic scale-dependent threshold was used, which is given by

$$\lambda = \frac{m_j}{0.6745\sqrt{2\log(N)}}\tag{5}$$

where m_i are the median values of detail components at each level [13,25].

The intermediate thresholding function is defined as

$$\eta(x) = \begin{cases} sign(x)(|x| - \frac{\lambda}{\exp\left[\frac{|x| - \lambda}{\delta}\right]}) \ |x| \ge \lambda \\ 0 \ |x| < \lambda \end{cases}$$
(6)

where δ is a positive integer [31]. The intermediate thresholding function is between the hard and the soft function and provides good continuity at $\pm \lambda$. Figure 8 shows the result of de-noising D1.



Figure 8. De-noising of detail component D1.

4.5. Signal Reconstruction

The decomposed signals were reconstructed using inverse DWT. Based on the above analysis, the de-noised detail components D1–D5 were used for signal reconstruction. The result is illustrated in Figure 9, which led a reduction in noise level of 16.83 dB compared with the original detected signal and of -11.43 dB relative to the noised D1–D5.



Figure 9. Reconstruction of PRPD signal in the VIS using D1–D5.

5. Results and Discussions

From the above analysis, the optimal mother wavelet for analyzing PD pulses in spacer was bior6.8, and the decomposition level of 8 was implemented to decompose the PRPD signal. After applying the MRA, it was investigated that the PD events in the VIS were associated with components of D1–D5, which were then de-noised using the automatic scale-dependent threshold and the intermediate thresholding to eliminate the background noise and capacitive disturbance. Finally, the PRPD signal was reconstructed with the de-noised D1–D5.

To verify the validity of the proposed method, a simulated PRPD signal and the signals detected in the POS and crack were analyzed.

5.1. Simulated PRPD

Figure 10a shows the simulated PD pulse sequences with different magnitudes and phase distributions. They were mixed with the applied voltage detected at 0.8 time of the discharge inception voltage in the VIS, resulting in a signal–noise ratio (SNR) of -43.08 dB. The simulated PRPD signal is demonstrated in Figure 10b. Its disturbance was eliminated by the proposed wavelet de-noising method and by the HPF with cutoff frequencies of 1 kHz, 9 kHz, and 100 kHz. The results evaluated in terms of correlation coefficient and SNR are shown in Table 1.

Method	Correlation Coefficient	SNR	Reduction in Amplitude [%]
1 kHz filter	0.063	-23.91	2.69
9 kHz filter	0.135	-17.35	3.02
100 kHz filter	0.134	-16.77	5.51
Wavelet, noisy D1–D5	0.141	-16.76	0.19
Wavelet, de-noised D1–D5	0.814	4.17	2.30
Wavelet, de-noised D1–D8	0.813	4.09	1.70

Table 1. Results of disturbance elimination. SNR: signal-noise ratio.

Figure 10c,d shows the signals de-noised by the filters with the cutoff frequencies of 1 kHz and 100 kHz, respectively. It is indicated that the filter with a low cutoff frequency could not completely eliminate the disturbance and even that with a high cutoff frequency still could not completely eliminate the background noise. As a result, the correlated coefficients as well as the SNRs between the simulated signal and de-noised signal were very low.

Figure 10e,f illustrates the signals reconstructed using the noisy and de-noised components D1–D5, respectively. Both the capacitive disturbance and background noise were well eliminated after applying the threshold and thresholding function. The signal reconstructed by noisy D1–D5 resulted in a correlation coefficient of 0.141 and an SNR of -16.76 dB, whereas that processed by the de-noised D1–D5 led to a correlation coefficient of 0.814 and an SNR of 4.17 dB, achieving an improvement

in SNR of 47.25 dB. Table 1 also gives the results of extraction of PRPD using all of the de-noised detail components. However, an increase in the reconstruction level could not improve the correlation coefficient or SNR, but causes the computational complexity. From Table 1, the application of the WT method may cause reduction in pulse amplitude, but the reduction is much lower compared with using filters. In addition, the implementation of filters resulted in a lower SNR.



Figure 10. Disturbance elimination for simulated PRPD signal. (a) Simulated PD pulse sequences; (b) simulated PRPD; (c) with a 1 kHz filter; (d) with a 100 kHz filter; (e) via noisy D1–D5; (f) via de-noised D1–D5.

5.2. PRPD in the POS and the Crack

Figures 11 and 12 demonstrate the results of disturbance elimination for PRPD in the POS and crack, respectively. In the POS, 95.4% of the signal energy was distributed in the components of D1–D5, and the disturbance elimination resulted in a reduction in a noise level of 0.46 dB. D1–D5 occupied 96.0% of the energy of PRPD signal in the crack, and a reduction in noise level of 17.18 dB was achieved.



Figure 11. Disturbance elimination for PRPD in the POS. (a) Signal energy distribution; (b) extraction of PRPD.



Figure 12. Disturbance elimination for PRPD in the crack. (a) Signal energy distribution; (b) extraction of PRPD.

6. Conclusions

In this paper, the WT was used to eliminate the capacitive disturbance from PD signals induced by typical defects in GIS spacers. The optimal mother wavelet was determined as bior6.8 by calculating the correlation coefficients with single PD pulses. The PRPD signals were decomposed into 8 levels using the MRA method. It was revealed that more than 95% of signal energy was distributed in the detail components of D1–D5, whereas the components of D6–D8 and A8, which were related to background noise and capacitive component, respectively, were discarded. Furthermore, components of D1–D5 were de-noised by the automatic scale-dependent threshold and the intermediate thresholding function. The PRPD signals were reconstructed using the de-noised D1–D5. Compared to dealing with filters, the proposed method extracted the PRPD signals with a higher correlation coefficient and SNR, resulting in a high sensitivity for PD detection in GISs.

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