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Sliding Mode and Neural Network Control of Sensorless PMSM Controlled System for Power Consumption and Performance Improvement

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Abstract: This paper deals with the design of sliding mode control and neural network compensation for a sensorless permanent magnet synchronous motor (PMSM) controlled system that is able to improve both power consumption and speed response performance. The position sensor of PMSM is unreliable in harsh environments. Therefore, the sensorless control technique is widely proposed in industry. A sliding mode observer can estimate the rotor angle and has the robustness to load disturbance and parameter variations. However, the sliding mode observer is not conducive to standstill and low speed conditions because the amplitude of the back EMF is almost zero. As a result, this paper combines an iterative sliding mode observer (ISMO) and neural networks (NNs) as an angle compensator to improve the above problems. A dsPIC30F6010A-based PMSM sensorless drive system is implemented to validate the proposed algorithm. The simulation and experimental results prove its effectiveness.

Keywords: sensorless control; sliding mode observer; permanent magnet synchronous motor; neural networks

1. Introduction

It is well-known that electric motors are the single biggest consumer of electricity in modern society and their consumption of industrial and domestic electric motors per year occupy 46.2% of the global electrical demand [1]. In addition, it is estimated that about 20% to 30% of the total global electric motor demand may be saved if the more efficient electric motors and drives are designed and used. The permanent magnet synchronous motor (PMSM) provides some eminent properties, such as high power density/reliability and easy controllability/maintenance, such that it has been widely used in servo motors, robotics, and electric vehicles of industry applications. The excellent performance of PMSM drive systems comes from the information of rotor position that is measured by position sensors (encoders or resolvers) of the motors. However, the disadvantages of shaft sensors result into larger machine volume, expense, and noise problems, and limit the applications because of the harsh environment of high humidity and temperature. As a result, extensive research of sensorless control strategies has been conducted on overcoming these problems [2,3].

For standstill and low speed conditions, signal injection methods [4–7], which inject the high-frequency voltage and current signals to detect or estimate the rotor position, are the popular candidates of sensorless control schemes. Control methods based on carrier signal injection [6] are proposed for sensorless motor control. An innovative self-sensing control scheme based on test current instead of voltage injection [7] is used to deal with problems on sensorless control of PMSM. A two-degree-of-freedom control scheme plays the main role, which needs the information of model dynamics.
At medium- and high-speed ranges, the fundamental excitation methods [3,8–10], which are
based on the motor model and use the fundamental signals of voltages and currents for the rotor
position and speed detection, are adopted by most researchers. An online identification method by
affine projection algorithms in the estimated synchronously rotating frame that is able to estimate its
stator resistance and inductances accurately for the model-based sensorless control of interior PMSMs
is proposed in [3]. An extended Kalman filter (EKF) [8] is usually used to obtain good performance
of sensorless control, however it is complex and difficult to implement. By feeding back stator currents
and voltages, a sixth order nonlinear adaptive controller is designed to address the tracking problem
with unknown constant load torque for the sensorless PMSM system [9]. However, the proposed
control algorithm is just simulated without experimentation. A high-speed sliding-mode observer [9]
for estimating the rotor position and the velocity of PMSM from the back electromotive force (EMF)
is proposed.

Considering the rotor position error during motor starting to lower speeds, this paper proposes
an iterative sliding mode observer (ISMO) [11,12], combined with an artificial neural network (ANN)
to fix the problem. The ISMO will make the sensorless control system robust against disturbance and
parameter variations. Similar to the concept of multi-loop servo control systems, the ISMO internally
estimates the back EMF several times within a speed control cycle to reduce the ripples of the estimated
back EMF, and then externally calculates the position and velocity of the rotor once to obtain accurate
estimations. In order to reduce the chattering effect in the sliding mode behavior, a sigmoid function
replaces a traditional switching function. In addition, because of their good characteristics of having
parallel distributed architecture and the ability to identify nonlinear system dynamics and to learn,
generalize, and adapt to a new environment, ANNs have attracted much attention to more engineering
applications recently [13–16]. Sensorless motor control is one of excellent example.

The rest of the paper is organized as follows. Section 2 consists of PMSM modeling, iterative sliding
mode observer, and compensation for rotor angle estimation by neural networks to form
the servo system design. Section 3 is composed of results of simulation by Matlab/Simulink and
experiments. Finally, Section 4 gives conclusions.

2. Servo System Design

The proposed sensorless servo control system design includes PMSM modeling, iterative sliding
mode observer, and rotor angle that is compensated by neural networks.

2.1. PMSM Modeling

The voltage equation of PMSM by Clarke transformation from the three-phase stationary a-b-c
frame to the two-phase fixed $\alpha-\beta$ frame is given as [2–6],

$$
\begin{bmatrix}
  v_\alpha \\
  v_\beta
\end{bmatrix} =
\begin{bmatrix}
  R_s + \frac{d}{dt}L_s & 0 \\
  0 & R_s + \frac{d}{dt}L_s
\end{bmatrix}
\begin{bmatrix}
  i_\alpha \\
  i_\beta
\end{bmatrix} +
\begin{bmatrix}
  e_\alpha \\
  e_\beta
\end{bmatrix}
$$

(1)

where $v_\alpha, v_\beta, i_\alpha, i_\beta$ are $\alpha$- and $\beta$-axis voltages and currents respectively; $R_s$ and $L_s$ are the resistance
and inductance; and the back EMFs are given as:

$$
e_\alpha = -\lambda_f \omega_r \sin \theta$$

(2)

$$
e_\beta = \lambda_f \omega_r \cos \theta$$

(3)

where $\lambda_f$ is flux linkage by the permanent magnets, $\omega_r$ is the electric speed and $\theta$ is rotor angle.
The actual rotor position is absent in a sensorless application and will be estimated by methods.
The block diagram of the proposed sensorless PMSM control system is shown in Figure 1. We will first
conduct simulation by Matlab/Simulink and experiments to verify the design.
2.2. Iterative Sliding Mode Observer

From (1), we have the stator current differential equation,

\[
\frac{di_a}{dt} = -\frac{R_s}{L_s} i_a - \frac{1}{L_s} v_a + \frac{1}{L_s} v_q
\]
\[
\frac{di_\beta}{dt} = -\frac{R_s}{L_s} i_\beta - \frac{1}{L_s} v_\beta + \frac{1}{L_s} v_d
\]

(4)

A sliding-mode observer (SMO) has not only better performance of sliding-mode control (SMC), like robustness to disturbances and parameter variations [17–29], but also provides estimation information of rotor position and speed for the sensorless control system. The dynamic equations of SMO are given based on (4),

\[
\frac{d\hat{i}_a}{dt} = -\frac{R_s}{L_s} \hat{i}_a + \frac{1}{L_s} v_a - \frac{1}{L_s} k \cdot H(\hat{i}_a - i_a)
\]
\[
\frac{d\hat{i}_\beta}{dt} = -\frac{R_s}{L_s} \hat{i}_\beta + \frac{1}{L_s} v_\beta - \frac{1}{L_s} k \cdot H(\hat{i}_\beta - i_\beta)
\]

(5)

where "∧" stands for estimation, \(k\) is observer gain, and the sigmoid function:

\[
\begin{bmatrix}
H(\hat{i}_a - i_a) \\
H(\hat{i}_\beta - i_\beta)
\end{bmatrix} = \begin{bmatrix}
\frac{2}{1+\exp(-a(|\hat{i}_a - i_a|))} - 1 \\
\frac{2}{1+\exp(-a(|\hat{i}_\beta - i_\beta|))} - 1
\end{bmatrix}
\]

(6)

is used to improve the chattering phenomenon in the sliding mode operation and \(a\) is a positive constant, shown in Figure 2 [11,12].

**Figure 1.** The block diagram of the proposed sensorless permanent magnet synchronous motor (PMSM) control system.
The sliding vector for the system is:

\[ S_n = [s_a \ s_\beta]^T = [\tilde{i}_a - i_a \ \tilde{i}_\beta - i_\beta]^T = [\tilde{i}_a \ \tilde{i}_\beta]^T \]  

(7)

and the defined Lyapunov function is:

\[ V = \frac{1}{2} S_n^T S_n = \frac{1}{2} (s_a^2 + s_\beta^2) \]  

(8)

By Lyapunov’s stability theorem, \( k \) will be designed to satisfy the inequality, \( \dot{V} < 0 \), when the system trajectory approaches to the sliding surface, \( S_n = 0 \). The error equations of estimated currents are:

\[ \dot{\tilde{i}}_a = \tilde{i}_a - i_a = -\frac{R_e}{L_a} \tilde{i}_a + \frac{1}{L_a} e_a - \frac{1}{L_a} k \cdot H(\tilde{i}_a) \]
\[ \dot{\tilde{i}}_\beta = \tilde{i}_\beta - i_\beta = -\frac{R_e}{L_\beta} \tilde{i}_\beta + \frac{1}{L_\beta} e_\beta - \frac{1}{L_\beta} k \cdot H(\tilde{i}_\beta) \]  

(9)

For \( \dot{V} = S_n^T \dot{S}_n < 0 \), we have:

\[ S_n^T \dot{S}_n = -\frac{R_e}{L_a} (\tilde{i}_a^2 + \tilde{i}_a^2) + \frac{1}{L_a} (e_a \tilde{i}_a - k \tilde{i}_a H(\tilde{i}_a)) + \frac{1}{L_a} (e_\beta \tilde{i}_\beta - k \tilde{i}_\beta H(\tilde{i}_\beta)) < 0 \]  

(10)

Rearranging (10), we have:

\[ S_n^T \dot{S}_n = -\frac{R_e}{L_a} (\tilde{i}_a^2 + \tilde{i}_\beta^2) + \frac{1}{L_a} [(e_a - k) \tilde{i}_a H(\tilde{i}_a) + (e_\beta - k) \tilde{i}_\beta H(\tilde{i}_\beta)] < 0 \]

The product of \( \tilde{i}_a H(\tilde{i}_a) \) (and \( \tilde{i}_\beta H(\tilde{i}_\beta) \)) is always positive. As a result, if

\[ k \geq \max(|e_a|, |e_\beta|) \]  

(11)

the inequality of (10) will be satisfied. The sliding mode may then exist on the sliding surface as follows:

\[ [\dot{s}_a \ \dot{s}_\beta]^T = [s_a \ s_\beta]^T \approx [0 \ 0] \]  

(12)

With (11) to satisfy (10), the following conditions are obtained:

\[ \dot{\tilde{e}}_a = k \cdot H(\tilde{i}_a) = -\lambda \tilde{\omega}_r \sin \hat{\theta} \]
\[ \dot{\tilde{e}}_\beta = k \cdot H(\tilde{i}_\beta) = \lambda \tilde{\omega}_r \cos \hat{\theta} \]  

(13)

As a result, and the estimated rotor angle and motor speed are given as:

\[ \hat{\theta} = -\tan^{-1}(\dot{\tilde{e}}_a/\dot{\tilde{e}}_\beta) \]  

(14)
\[ \hat{\omega} = \frac{d}{dt} \hat{\theta} \]  

(15)

The designed SMO (5) will internally estimate the back EMF (13) several times within a speed control cycle to reduce the ripples of the estimated back EMF, and then externally calculate the position and the velocity of the rotor (14) and (15) once to obtain accurate estimations.

2.3. Neural Networks Compensation

As the problem mentioned previously, a neural network (NN) with error back propagation structure, as shown in Figure 3, is adopted to compensate the rotor position estimation error, which consists of input layer with two inputs, hidden layer with two neurons, and output layer. In Figure 3, \( \theta \), \( \hat{\theta} \), and \( \ddot{\theta} \) are input variables, \( w^n_{ij} \) is the weight between the jth neuron of the n\textsuperscript{th} layer and the ith neuron of the \((n-1)\textsuperscript{th} \) layer, \( b^n_j \) is the bias of the jth neuron of the nth layer, \( v^n_i \) is sum of the product sum of outputs and weights and biases of the \((n-1)\textsuperscript{th} \) layer, \( y^n_i \) is output value of jth neuron of the nth layer, \( y_k \) is sum of the NN, \( f^n \) is activation function of the nth layer, and \( d_k \) is the reference rotor angle from the speed command, respectively. The relationships are described in the following two equations:

\[ y'^n_i = f^n(v^n_i) \]  

(16)

\[ v^n_i = \sum_{i=1} w^n_{ij} y'^{i-1}_j + b^n_j \]  

(17)

The error function is defined as:

\[ e(k) = \frac{1}{2} \sum_{k=1} (d_k - y_k)^2 \]  

(18)

and the reference angle is given as:

\[ d_k = \theta_m(k + 1) = \sum_{i=1}^k T_s \omega^*(i) + \theta_0 \]  

(19)

where \( \omega^*(k) \) is the reference speed, \( T_s \) is the sampling period, and \( \theta_0 \) is the initial rotor angle. The gradient method is adopted to search the minimum value of (18) by the following equations:

\[ \Delta w^n_{ij}(k) = -u \frac{\partial e(k)}{\partial v^n_i} = -u \frac{\partial e(k)}{\partial v^n_j} \frac{\partial v^n_j}{\partial w^n_{ij}} \]  

(20)
\[
\Delta b^n_{ij}(k) = -u \frac{\partial e(k)}{\partial b^n_{ij}} = -u \frac{\partial e(k)}{\partial v^n_{ij}} \frac{\partial v^n_{ij}}{\partial b^n_{ij}}
\]

\[
w^n_{ij}(k + 1) = w^n_{ij}(k) + \Delta w^n_{ij}(k)
\]

\[
b^n_{ij}(k + 1) = b^n_{ij}(k) + \Delta b^n_{ij}(k)
\]

where \(u\) is the learning rate.

3. Simulation and Experimental Results

The simulation system with the parameters of PMSM 8CB75 listed in Table 1 is programmed by Matlab/Simulink. The activation functions with hyperbolic tangent sigmoid type in the hidden layers and linear transfer function in the output layer of the neural network are used. The neural network is trained by 100 rpm speed response and an encoder attached on the motor shaft. The values of these weights and biases are depicted as,

\[
\{ w^1_{11}, w^1_{12}, w^1_{21}, w^1_{22}, w^2_{11}, w^2_{12}, w^2_{21}, w^2_{22} \} = \{ 0.840252, 0.690252, 0.0799998, 0.200000, 0.042868, 0.19287, 0.040042, -0.029958 \}
\]

\[
\{ b^1_1, b^1_2, b^2_1, b^2_2 \} = \{ -1.049934, -1.054758, 0.033902, 0.033902 \}
\]

The final absolute error of \(1 \times 10^{-3}\) is reached after 125 training epochs with learning rate of 0.5 for the neural network. The popular proportional-integral (PI) control is used in the speed and current control loops,

\[
G_x(s) = K_{xp}(1 + \frac{K_{xi}}{s}),
\]

where the index \(x\) is \(s\) for speed or \(i\) for current loop. Based on the rule of thumb [30], the gains of speed control loop are \(K_{sp} = 0.03\) and \(K_{si} = 3\), and those for current control loop are \(K_{ip} = 150\) and \(K_{ii} = 200\), respectively. These parameters are used in the simulations and experiments.

### Table 1. Parameters of PMSM Sinano 8CB75.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Unit</th>
<th>Value</th>
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</thead>
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<tr>
<td>P</td>
<td>W</td>
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</tr>
<tr>
<td>V</td>
<td>V</td>
<td>149.4</td>
</tr>
<tr>
<td>T</td>
<td>N·m</td>
<td>2.931</td>
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<tr>
<td>I</td>
<td>A</td>
<td>3.4</td>
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<tr>
<td>N</td>
<td>Rpm</td>
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<tr>
<td>K</td>
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<tr>
<td>J</td>
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<tr>
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</tr>
<tr>
<td>Ls</td>
<td>mH</td>
<td>10.2</td>
</tr>
</tbody>
</table>

On simulation results, Figure 4a,b display the encoder output (\(\theta\)) and rotor angle estimation (\(\hat{\theta}\)) by ISMO, and the estimation error at the motor speed of 100 rpm, respectively. It is easy to find that the estimation lags encoder signal by almost 180 degrees. Similarly, Figure 5a,b display the encoder output and rotor angle estimation (\(\hat{\theta}'\)) by proposed ISMO and neural network (NN-ISMO), and the estimation error at the motor speed of 100 rpm, respectively. The maximum error is 0.007 radians and there is almost no lagging. The step speed responses of 100 rpm by ISMO and NN-ISMO are shown in Figure 6. Even with small overshoot and ringing, the response by NN-ISMO depicts the better performance.
The maximum error is 0.007 radians and there is almost no lagging. The step speed responses of 100 rpm by ISMO and NN-ISMO are shown in Figure 6. Even with small overshoot and ringing, the response by NN-ISMO depicts the better performance.

Figure 4. The rotor angle at the motor speed of 100 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}$) by iterative sliding mode observer (ISMO), and (b) the estimation error.

Figure 5. The rotor angle at the motor speed of 100 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}'$) by NN-ISMO, and (b) the estimation error.
The experimental setup is shown in Figures 7 and 8. The setup in Figure 7 consists of the microcontroller dsPIC30F6010A and its programmer ICD3, PMSM, drive, current sensing circuit, and encoder signals for comparison. The dynamometer is shown in Figure 8. Figures 9–12 display the results corresponding to simulations at speeds of 100 and 500 rpm and show the similar results. Figure 13 depicts the speed step responses of 500 rpm without loading by encoder (upper), ISMO, and NN-ISMO (bottom), respectively. With load of 2 Nm, slightly worse step responses of 500 rpm by encoder (upper), ISMO, and NN-ISMO (bottom), respectively, in Figure 14 are compared with those of Figure 13. Figure 15 shows the 0-100-300-500-300-100 step responses by encoder (upper), ISMO, and NN-ISMO (bottom), respectively. From the figures, it is easily proven that the proposed control algorithm show its validation and effectiveness.

Figure 6. The step speed responses of 100 rpm by (a) ISMO and (b) NN-ISMO.

Figure 7. The experimental setup.
Figure 8. Dynamometer.

Figure 9. The rotor angle at the motor speed of 100 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}$) by ISMO, and (b) the estimation error.

Figure 10. The rotor angle at the motor speed of 100 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}'$) by NN-ISMO, and (b) the estimation error.
Figure 11. The rotor angle at the motor speed of 500 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}$) by ISMO, and (b) the estimation error.

Figure 12. The rotor angle at the motor speed of 500 rpm (a) encoder output ($\theta$) and rotor angle estimation ($\hat{\theta}'$) by NN-ismo, and (b) the estimation error.
Figure 13. The step speed responses of 500 rpm without loading by (a) encoder, (b) ISMO, and (c) NN-ismo, respectively.
Figure 14. The step speed responses of 500 rpm with loading of 2 Nm by (a) encoder, (b) ISMO, and (c) NN-ISMO, respectively.

Figure 15. Cont.
Ming-Shyan Wang conceived and designed the experiments; Tse-Ming Tsai performed the experiments; Ming-Shyan Wang wrote the paper.

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Author Contributions: Ming-Shyan Wang conceived and designed the experiments; Tse-Ming Tsai performed the experiments; Ming-Shyan Wang and Tse-Ming Tsai analyzed the data; Ming-Shyan Wang contributed reagents, materials, and analytical tools; Ming-Shyan Wang wrote the paper.

Conflicts of Interest: The authors declare that there is no conflict of interests regarding the publication of this article.

References


Figure 15. The speed step responses of 0-100-300-500-300-100 rpm with loading of 2 Nm by (a) encoder, (b) ISMO, and (c) NN-ISO, respectively.

4. Conclusions

This paper proposes an approach based on ISMO to first estimate the rotor position and neural networks to compensate the estimated position error due to small amplitudes of estimated back EMF for a sensorless PMSM control system that is able to improve both power consumption and speed response performance. The suggested ISMO adopts the concept of a multi-loop servo control system, and is applicable to many fields. The results of simulations and experiments show that the proposed control system is capable of estimating rotor angle to synchronize the original sensor outputs within acceptable limits and to improve motor speed responses for many applications.


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