Multi-Time Scale Coordinated Scheduling Strategy with Distributed Power Flow Controllers for Minimizing Wind Power Spillage

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Abstract: The inherent variability and randomness of large-scale wind power integration have brought great challenges to power flow control and dispatch. The distributed power flow controller (DPFC) has the higher flexibility and capacity in power flow control in the system with wind generation. This paper proposes a multi-time scale coordinated scheduling model with DPFC to minimize wind power spillage. Configuration of DPFCs is initially determined by stochastic method. Afterward, two sequential procedures containing day-head and real-time scales are applied for determining maximum schedulable wind sources, optimal outputs of generating units and operation setting of DPFCs. The generating plan is obtained initially in day-ahead scheduling stage and modified in real-time scheduling model, while considering the uncertainty of wind power and fast operation of DPFC. Numerical simulation results in IEEE-RTS79 system illustrate that wind power is maximum scheduled with the optimal deployment and operation of DPFC, which confirms the applicability and effectiveness of the proposed method.

Keywords: distributed power flow controller; wind power spillage; multi-time scales; coordinated scheduling

1. Introduction

In future power systems, the share of wind power in the total generation portfolio is expected to have a substantial increase, due to the energy crisis and excessive CO₂ emission around the world. However, the inherent variability and randomness of large-scale wind power integration have brought great challenges to power flow control and dispatch. High penetration of wind power has the potential to affect the safe and stable operation of power systems in some areas. If appropriate generation scheduling is not formulated, there will be the unnecessary wind power spillage which increases the system operation costs. Therefore, it is urgent to make reasonable scheduling decisions considering network security and minimum wind power curtailment.

In previous studies, there are several studies on limiting the wind spillage under the acceptable level from various viewpoints [1–14]:

(1) High-precision wind power prediction methods: reduce wind power forecast error and alleviate the deviation of generation scheduling.

(2) Multi-energy coordinated scheduling solution: combine other power supplies or storages for optimal scheduling considering their regulatory characteristics.

(3) Demand response: encourage users to participate in power system scheduling and utilize their flexibility potential to cope with the uncertainty of wind power.
An improved wind power prediction error distribution model is proposed by the authors of [1] to quantify the probability of a specific error, which provided important information for short-term economic scheduling. In [2], dynamic spatial correlations between the geographically distributed wind farms is investigated to provide more favorable interval forecasts for the aggregate wind power. The best combination percentage of solar and wind resources is determined to reduce the forecast error based on the portfolio theory by the authors of [3]. In [4–7], the economic scheduling model with wind power is established and the uncertainty of wind power prediction is taken into account. In addition, various power supplies such as energy storage [8–11], solar [12] and pumped storage [13] are utilized for the optimizing scheduled power of wind with forecast data. In [14–17], the residential demand response in the system is considered to match the fluctuation of wind power output to reduce the reserve capacity required by the system. The above studies make contribution to minimizing wind power spillage, but all of them are from the aspects of power sources or loads, that is, the flexibility of power grids is not taken into account, which makes the traditional scheduling strategy conservative.

With the extensive application of power electronic devices in power systems, flexible AC transmission system (FACTS) and distributed flexible AC transmission (D-FACTS) have played important roles in enhancing flexibility of power flow control [18–20]. In the future, the power grids will gradually transfer to source-grid-load systems, in which power generations, power grids and residential loads are all participating in scheduling. Therefore, the combination of FACTS or D-FACTS devices and traditional power system economic scheduling model has a broad application prospect.

In [21], an optimal power flow model with FACTS devices based on a two-stage stochastic programming is proposed to minimize wind curtailment and determine the setting points of devices; however, the optimal locations and capacity of FACTS are not evaluated. In [22], a day-ahead operation planning model with Static Var Compensators (SVCs) and Thyristor Controlled Series Compensators (TCSCs) based on the probabilistic method is investigated for the best utilization of wind power, but the effect of wind power prediction error on optimal results is not taken into account. A long-term economic model for optimal allocation of FACTS devices with the objective to maximize the profit is proposed in [23], but the operation setting points of FACTS are not investigated. Compared with the lumped FACTS devices, little effort has been devoted to the co-scheduling problem with D-FACTS devices. D-FACTS devices have advantages in adjusting the locations according to the change of system operation mode, which makes them more applicable. However, the configuration and operation control of D-FACTS are the problems of optimization in multi-time scale, which include long-term, day-ahead and real-time scales. Hence, disturbances occurring at all time-scales will directly affect the power flow control and wind power spillage. Therefore, it is essential to formulate reasonable configuration and operation control strategy of D-FACTS in multi-time scale.

This paper proposes a two-stage optimal power flow (OPF) model with novel distributed power flow controllers (DPFCs) for the maximum utilization of wind power. The objective of the first stage is to determine the optimal locations of DPFCs in long-term stage based on the stochastic programming. In the second stage, an optimal coordinated scheduling model containing day-ahead and real-time scales is proposed to reduce wind power spillage considering the fast operation of DPFCs.

The rest of this paper is organized as follows. The introduction and mathematical model of DPFC are presented in Section 2. In Section 3, the multi-time scale scheduling problem is formulated. In Section 4, numerical results are used to demonstrate the effectiveness of the proposed method. Conclusions are presented in Section 5.

2. Structure and Mathematic Model of DPFC

2.1. Structure of DPFC

As shown in Figure 1, a DPFC can be directly installed on the conductor, which allows it to overcome many drawbacks of existing lumped FACTS technologies. The remarkable benefits are as follows: (i) ability to match the investment with the actual increase of load demand; (ii) ability to adjust
the locations according to the change of load and wind power; (iii) flexible installation does not require an additional footprint; (iv) avoidance of high voltage insulation, which reduces manufacturing costs.

Figure 1. Distributed power flow controller (DPFC) deployed on transmission line.

Figure 2 shows an electro-mechanical concept diagram for a DPFC and Figure 3 shows the schematic representation of the DPFC containing a single turn transformer (STT), a low-power single-phase inverter, a communication module and a composite switch. The inverter injects a desired quadrature voltage into the transmission line once it is activated. DPFC installed on lines is controlled by the control center deployed in the substation and system commands are received from the energy management system (EMS). Thus, the operation settings of DPFCs are adjusted rapidly by the control center as the change of load or power supply. The inverter and communication module are self-powered by induction from the conductor. The composite switch contains a normally closed electromechanical switch and a thyristor switch. The electromechanical switch is utilized to bypass the DPFC if the transmission line current is relatively small. With this switch closed, only a minimal level of reactance corresponding to the STT leakage reactance is inserted into the line, which has an extremely low impact on the power flow. The thyristor switch is used to ensure that the DPFC is bypassed quickly if a fault is detected by the current feedback signal.
where the unit vector in the direction of line current vector is represented by \( \hat{I} \).

\[
\tilde{V}_q = \pm j|V_q| \frac{\tilde{I}}{|I|},
\]

(1)

where the unit vector in the direction of line current vector is represented by \( \frac{\tilde{I}}{|I|} \).

Figure 4 presents the circuit model of a DPFC deployed on a transmission line without considering the line resistance. \( V_1 \) and \( V_2 \) are the voltage amplitudes of sending and receiving end buses. \( X \) represents the reactance of the transmission line. \( V_q \) represents the voltage injected by a DPFC. Therefore, the relationship of line current and the voltage injected by a DPFC can be described as follow:
The series injected voltage clearly has an impact on controlling line power flow. The real power flow \( P_{12} \) along a transmission line deployed with a DPFC can be described as (2) by assumption that the voltage amplitudes of buses 1 and 2 are equal to \( V \) and the angle difference is equal to \( \delta \).

\[
P_{12} = \frac{V^2}{X} \sin(\delta) \pm \frac{V|V_q|}{X} \cos(\delta/2).
\] (2)

Since a DPFC is utilized to control real power flow and installed in the high voltage level transmission network, the DC power flow model is used in this paper for the mathematic formulation of the DPFC. In the DC model, the voltage amplitudes of all buses are assumed equal to 1 p.u., and voltage phase angle differences are assumed to be extremely small. Therefore, the active power flow given in (2) can be simplified as:

\[
P_{12} = \frac{\delta}{X} \pm \frac{|V_q|}{X}.
\] (3)

Utilizing the linearization model of DPFC in (3), the injected voltage of DPFC can be embedded in the optimization model as a continuous control variable and solved by a linear programming solver.

3. Problem Formulation

The uncertainty of wind power brings new challenge to the scheduling of wind power. The accuracy of wind power forecast is closely related to the time scale. The shorter forecast horizons achieve the higher accuracy in wind power forecast error. Therefore, in order to reduce the wind power spillage, this paper designs a stochastic programming model of DPFCs considering many scenarios and establishes a sequential optimization scheduling model with DPFCs for maximum utilization of wind power so that system dispatchers can make reasonable scheduling planning of wind farms and generating units.

Figure 5 shows the two-stage scheduling framework containing multi-time scale for power systems integrating wind power considering DPFCs. Firstly, considering the uncertainty of the scenarios in the planning period, the stochastic programming method is used to determine the comprehensive configuration scheme of DPFCs in the first stage. In the second stage, two sequential scheduling models are considered. Combined with the given configuration scheme of DPFCs, the day-ahead scheduling model with the objective to minimize generation costs according to the forecast value of wind power and demand in day-ahead market. Afterward, the real-time scheduling model is used to eliminate the deviation of power generation plans caused by wind power forecast error. About 1 h prior to power delivery, the real-time scheduling is clear and final values for power consumptions and operation setting points are assigned to each generating unit and DPFC, respectively.
3.1. Stochastic Programming Model of DPFC

3.1.1. Objective Function

The main objective in long-term optimal configuration stage of DPFCs is to minimize wind power spillage and several scenarios are utilized to simulate the uncertainty of demand and wind power. The probability of each scenario represents the frequency of occurrence during the programming period of DPFCs.

Therefore, the objective of DPFCs’ stochastic programming model considering the scenarios is formulated as follows:

$$\min \sum_s \rho_s \left[ \sum_t \left( \sum_w C_w P_{w,t}^s + \sum_g C_g P_{g,t}^s \right) \right],$$

where $\rho_s$ is the probability of scenario $s$; $P_{w,t}^s$ and $P_{g,t}^s$ are real power outputs for wind farm $w$ and generating unit $g$ at period $t$ in scenario $s$, respectively; $C_w$ and $C_g$ are operation costs of wind farm $w$ and unit $g$, respectively.

3.1.2. Constraints

1. Power Balance Constraints for Each Bus:

$$\sum_{k \in \delta^+(n)} L_{kt}^s - \sum_{k \in \delta^-(n)} L_{kt}^s + \sum_{g \in G(n)} P_{g,t}^s + \sum_{w \in W(n)} P_{w,t}^s = D_{nt}^s,$$

where $L_{kt}^s$ is real power flow through line $k$ at period $t$ in scenario $s$; $D_{nt}^s$ is the active power consumption by load $d$ at period $t$.

2. Line Power Flows Equations:

$$L_{kt}^s - B_k (\theta_{nt}^s - \theta_{mt}^s) - B_k V_{qk}^s = 0,$$

where $\theta_{nt}^s$ is voltage angle of bus $n$ at period $t$ in scenario $s$; $V_{qk}^s$ is injected voltage of DPFC in line $k$ at period $t$ in scenario $s$; $B_k$ is susceptibility of line $k$.

3. Generation Units Constraints:

$$0 \leq P_{w,t}^s \leq P_{w,t}^{sf},$$

$$P_{g,t}^s \geq P_{g,t}^{min},$$

$$P_{g,t}^s + RSV_{g,t}^s \leq P_{g,t}^{max},$$

$$|P_{s,t}^{g} - P_{s,t-1}^{g}| \leq R_{g,H},$$

where $P_{w,t}^{sf}$ is forecast value of wind farm $w$ at period $t$ in scenario $s$; $P_{g,t}^{max}$ and $P_{g,t}^{min}$ are upper and lower limits on the active power of generating unit $g$; $RSV_{g,t}^s$ is scheduled spinning reserve for unit $g$ at period $t$ in scenario $s$; $R_{g,H}$ is maximum hourly ramp rate of unit $g$.

4. Reserve Constraints:

$$RSV_{t}^{req} \leq \sum_g RSV_{g,t}^s,$$

$$RSV_{g,t}^s \leq \eta R_{g,H},$$

where $RSV_{t}^{req}$ is the required level of spinning reserve at period $t$; $\eta$ is ratio of hourly ramp rate and short-time ramp rate.

5. Network Security Constraints:

$$|L_{kt}^s| \leq L_{klimi},$$
\[ -\pi \leq \theta_{nt}^s \leq \pi, \]  

(14)

where \( L_{k_{\text{lim}}} \) is the thermal limit of transmission line \( k \).

(6) DPFC's Constraints,

(a) installation number constraints of DPFC:

\[ N_k^\text{min} \times u_k \leq N_k \leq N_k^\text{max} \times u_k, \]  

(15)

\[ 3 \times \sum_{k \in \Omega} N_k \leq N_T, \]  

(16)

where \( N_k \) is the number of DPFC installed on line \( k \); \( u_k \) is a binary parameter that specifies whether it is feasible to install DPFCs on line \( k \); \( N_T \) is the maximum total number of DPFCs available to be installed in the system; \( N_k^\text{max} \) and \( N_k^\text{min} \) are the maximum and minimum number of DPFCs installed on the line \( k \). Since DPFCs are directly installed on the transmission lines, \( N_k^\text{max} \) is affected by the length of the line, the bearing capacity of the tower and the weight of the DPFC.

(b) operation constraints of DPFC:

\[ N_k V_{qk}^\text{min} \leq V_{qk} \leq N_k V_{qk}^\text{max}, \]  

(17)

\[ V_{qk}^\text{max} \] and \( V_{qk}^\text{min} \) are upper and lower limits on voltage injected by DPFC installed on the line \( k \) which can be calculated using the following equations:

\[ V_{qk,\text{max}} = \frac{S_{\text{DPFC}}}{I_{k,\text{max}}}, \]  

(18)

\[ V_{qk,\text{min}} = -\frac{S_{\text{DPFC}}}{I_{k,\text{max}}}, \]  

(19)

where \( S_{\text{DPFC}} \) is the capacity of each DPFC; \( I_{k,\text{max}} \) is the thermal limit of line \( k \).

This stochastic programming method determines the optimal configuration of DPFC that appropriates for any plausible scenarios. Therefore, the output variables delivered to the second stage are \( N_k \).

3.2. Day-Ahead Scheduling Model

3.2.1. Objective Function

According to the forecast data of demand and wind power, day-ahead scheduling model is proposed with the objective to minimize the total operation costs in the day-ahead market. Therefore, the objective is formulated as:

\[ \min \sum_T \left( \sum_w C_w P_{w,kt} + \sum_g C_g P_{g,kt} \right), \]  

(20)

3.2.2. Constraints

Constraints in day-ahead scheduling model also consist of power equations, generation unit constraints, reserve constraints and security constraints which are formulated as follows:

\[ \sum_{k \in \delta^+(n)} L_{kt} - \sum_{k \in \delta^-(n)} L_{kt} + \sum_{g \in G(n)} P_{gt} + \sum_{w \in W(n)} P_{wt} = D_{nt}, \]  

(21)

\[ L_{kt} - B_k (\theta_{nt} - \theta_{nt}) - B_k V_{qlt} = 0, \]  

(22)

\[ 0 \leq P_{wt} \leq P_{w,\text{f}}, \]  

(23)
\[ P_{gt} \geq P_{g}^{\text{min}}, \quad (24) \]
\[ P_{gt} + RSV_{gt} \leq P_{g}^{\text{max}}, \quad (25) \]
\[ |P_{gt} - P_{gt-1}| \leq R_{g}^{H}, \quad (26) \]
\[ RSV_{t}^{\text{req}} \leq \sum_{g} RSV_{gt}, \quad (27) \]
\[ RSV_{gt} \leq \eta R_{g}^{H}. \quad (28) \]

As mentioned before, the configuration of DPFCs containing location and number has been determined, hence DPFCs can only alter their injected voltages in this stage. Therefore, the constraint of DPFCs is formulated as follows:
\[ N_{k}^{\text{fix}} V_{qk}^{\text{min}} \leq V_{qkt} \leq N_{k}^{\text{fix}} V_{qk}^{\text{max}}, \quad (29) \]

where \( N_{k}^{\text{fix}} \) represents installed number of DPFCs on line \( k \) determined before.

The day-ahead scheduling model identifies variables \( P_{gt} \) which are delivered to the next stage as constraints.

### 3.3. Real-Time Scheduling Model

In the real-time scheduling stage, final outputs of power generations would adjust for delivery of reserve needed for particular wind power forecast error. Therefore, considering the consecutiveness of multi-time scales, outputs of power generations should be modified based on the results given in day-ahead market solution. References [24,25] indicate that wind power forecast error is close to Laplace distribution whose probability density function is:
\[ \Delta P_{wt}^{f} = \frac{1}{2} \lambda \exp(-\lambda |P_{wt}^{f}|), \quad (30) \]

where \( \Delta P_{wt}^{f} \) is wind power forecast error at period \( t \). The parameter \( \lambda \) fitting the Laplace distribution of wind power forecast error is 38.22 in [24]. Hence, the actual schedulable power of wind farm \( k \) is expressed by \( \Delta P_{wt}^{f} + P_{wt}^{f} \).

#### 3.3.1. Objective Function

Real-time scheduling model is proposed with the objective to minimize the total operation costs hourly. Therefore, the objective is formulated as:
\[ \min(\sum_{w} C_{w} P_{wkt} + \sum_{g} C_{g} P_{gkt}). \quad (31) \]

#### 3.3.2. Constraints

Constraints in real-time scheduling model are presented as follow:
\[ \sum_{k \in \delta^{+}(n)} L_{kt} - \sum_{k \in \delta^{-}(n)} L_{kt} + \sum_{g \in G(n)} P_{gt} + \sum_{w \in W(n)} P_{wt} + \sum_{w \in W(n)} \Delta P_{wt} = D_{nt}, \quad (32) \]
\[ L_{kt} - B_{k}(\theta_{nt} - \theta_{mt}) - B_{k} V_{qkt} = 0, \quad (33) \]
\[ 0 \leq P_{wt} \leq P_{wt}^{f} + \Delta P_{wt}^{f}, \quad (34) \]
\[ \frac{P_{g}^{\text{min}}}{g} \leq P_{gt} \leq P_{g}^{\text{max}} \quad (35) \]
\[ -R_{g}^{H} \leq P_{gt} - P_{gt}^{*} \leq R_{g}^{H}, \quad (36) \]
\[ |L_{kt}| \leq L_{\text{lim}}, \quad (37) \]
\[-\pi \leq \theta_{nt} \leq \pi, \quad (38)\]
\[ N_{k}^{\text{fix}} V_{qk}^{\text{min}} \leq V_{qkt} \leq N_{k}^{\text{fix}} V_{qk}^{\text{max}}, \quad (39)\]

where \( P^*_g \) is scheduled power of generating unit \( g \) at period \( t \) in day-ahead market. Constraints (32) and (34) limit the power for each bus and outputs of wind farm considering the wind power forecast error, respectively. Constraint (36) limits the rescheduled outputs of generating units.

Final optimization results pertaining to the real-time scheduling stage are:

1. the final scheduled power of generating units;
2. the final scheduled power of wind farms;
3. the real-time operation control strategy of DPFCs.

4. Simulation Results

4.1. Data

This section presents numerical results for case study based on the IEEE-RTS79 system and the complete data of this test system can be obtained from [26]. To analyze the effect of DPFCs on the wind power spillage and verify the correctness and validity of the proposed method, a wind farm is considered and located at bus 19. The generation capacity of wind power is 800 MWA and its power factor is assumed to be equal to one. System daily load data can be obtained from [27]. For the maximum utilization of wind power, the values for operation costs of wind farm in objective function (4), (20) and (31) are assumed equal to 0. In order to better illustrate the effects of the proposed method, the transmission limits of all lines in the system are reduced by 50%. Besides, since the capacity of a DPFC is set to 70 kVA, the injected voltages of DPFCs installed on different transmission lines are shown in Table 1.

<table>
<thead>
<tr>
<th>Maximum Injected Voltage</th>
<th>Minimum Injected Voltage</th>
<th>Line</th>
</tr>
</thead>
<tbody>
<tr>
<td>V pu</td>
<td>V pu</td>
<td>Voltage (kV)</td>
</tr>
<tr>
<td>191.22 ( \times 10^{-3} )</td>
<td>-191.22 ( \times 10^{-3} )</td>
<td>138</td>
</tr>
<tr>
<td>111.54 ( \times 10^{-4} )</td>
<td>-111.54 ( \times 10^{-4} )</td>
<td>230</td>
</tr>
</tbody>
</table>

The maximum and minimum numbers of DPFCs allowed to be installed on a conductor of a transmission line must be specified. Since DPFCs can only be attached to the lines closely connected to the strain tower and there is approximately one strain tower per mile of a transmission line, the maximum number of DPFC installed on a transmission line is assumed equal to one per mile per conductor by considering the weight of DPFCs and the distribution of strain towers. The minimum number of DPFCs on each line is assumed equal to zero.

The following cases are considered for the verification purpose:

Case A: 150 DPFCs are installed by the proposed method.
Case B: No DPFCs in the system.

These cases are copied with the optimization model proposed previously and the results are presented in the following.

4.2. Optimal Configuration of DPFC

As depicted in Section 2.1, the locations of DPFCs can be adjusted according to the change of load and wind power. In fact, the locations of DPFCs are changed only once a quarter considering
the transportation cost. Therefore, transmission system operators (TSOs) should make “configuration
decisions” appropriate for any plausible load and wind power forecasted in the next quarter through a
set of scenarios. For the sake of simplicity, TSOs usually select several scenarios occurring frequently
as typical scenarios representing the operation state of system. Hence the scenarios are determined
by TSOs based on historical operational data and forecasts of economy and meteorology. However,
the computation time may become intractable if too many scenarios are considered. In order to
simplify the calculation, four typical scenarios are utilized to determine the optimal configuration of
DPFCs in this paper. The probability of each scenario may be distinguishing in different power grids.
Without losing the generality, the duration of each selected scenario is assumed to be identical and the
probabilities of these scenarios are equal to 0.25.

Figure 6 shows the optimal power flows in IEEE-RTS79 system. The expected average load rates
of lines are calculated based on (40):\

\[ L^R_k = \sum_s \sum_t \rho_s \frac{L^s_{kt}}{L^\text{lim}} \]  
(40)

The average load rates of lines 14–16 and 16–19 are 96.31% and 56.35%, respectively. The
scheduling periods that load rates of these lines exceed 80% are 23 and 8, respectively. Therefore,
the insufficient capacity of these two lines has significantly affected the wind power consumption.
Table 2 shows the specific configuration of DPFCs. From Table 2 and Figure 6 it can be seen that
99 DPFCs are installed on lines 14–16 and 11–14. This configuration result is consistent with the
engineering experience, i.e., FACTS devices are installed around the lines that are more heavily utilized.

Table 2. Optimal configuration of DPFC.

<table>
<thead>
<tr>
<th>Line Number of DPFC</th>
<th>From Bus</th>
<th>To Bus</th>
<th>Length/Mile</th>
<th>Number of DPFC</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>6</td>
<td>50</td>
<td></td>
<td>51</td>
</tr>
<tr>
<td>11</td>
<td>14</td>
<td>29</td>
<td></td>
<td>87</td>
</tr>
<tr>
<td>14</td>
<td>16</td>
<td>27</td>
<td></td>
<td>12</td>
</tr>
<tr>
<td>Sum</td>
<td></td>
<td></td>
<td></td>
<td>150</td>
</tr>
</tbody>
</table>

Figure 6. Power flows in IEEE-RTS79 system, (a) without DPFCs, and (b) with DPFCs.
4.3. Results of Day-Ahead Scheduling

Figure 7 shows the daily load curve and wind power forecast error calculated by (30). It can be seen from Figure 7 that there exists apparent difference between load and wind power.

![Figure 7. Wind power curve and forecast error.](image)

Based on the configuration of DPFCs showed in Table 2, scheduled power of wind farm and generating units are optimized by day-ahead scheduling model. Figure 8 shows the comparison of scheduled wind power in two cases. The intermittent characteristics of wind power make the wind power spillage occurring in the period of peak load or sufficient wind energy, such as 1–4 h and 11–14 h. With the deployment of DPFCs, the wind power consumption has been increased from 96.85% to 98.97%.

![Figure 8. Scheduled power in day-ahead scheduling stage.](image)

From the optimized results of the power flow, it can be found that the load rates of double lines 19–20 are lower than 30% when the lines 16–19 and 14–16 are overload. Figure 9 shows the
compassion of power flows in two cases. In case A with DPFCs deployed, the total expected value of wind power consumption is increased from 101.82 MW to 120.39 MW during the 1–4 h and 11–14 h that wind power spillage occurs. This implies that more transmission capacity has been utilized in reducing wind power spillage.

4.4. Results of Real-Time Scheduling

Figure 10 depicts the final scheduled power curve of wind farm. Accordingly, wind power spillage has occurred in two case and the amount of Case A is comparatively lower than Case B. Table 3 shows the final optimization results of cases. With the deployment of DPFCs to regulate power flows, the total consumption of wind power is increased from 8692.01 MWh to 8839.48 MWh and the final consumption rate is increased from 95.83% to 97.45%. Besides, compared with the day-ahead scheduling solutions, the wind power consumption is reduced slightly. This implies that wind power forecast error is not conducive to the consumption of wind power. Moreover, the periods that wind power occurred in have changed considering the forecast error. All the wind power has been scheduled in 18 h and total periods of wind power spillage are reduced from 8 to 5. Therefore, the total operation cost in Case A is lower than Case B.
Table 3. Numerical results for cases considered.

<table>
<thead>
<tr>
<th>Cases</th>
<th>Wind Power Consumption (MWh)</th>
<th>Wind Power Consumption Percentage (%)</th>
<th>Total Periods of Wind Power Spillage</th>
<th>Operation Cost (Dollar)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case A</td>
<td>8839.48</td>
<td>97.45</td>
<td>5</td>
<td>26,774.72</td>
</tr>
<tr>
<td>Case B</td>
<td>8692.01</td>
<td>95.83</td>
<td>8</td>
<td>27,114.59</td>
</tr>
</tbody>
</table>

If DPFCs are utilized to reduce wind power spillage, their optimal control strategy needs to be determined. Figure 11 illustrates the optimal injected voltage setting of DPFCs. Note that, the optimal setting of DPFC across periods often equal to their bounds for maximum capability in controlling power flows and injected voltage of DPFCs adjusts along with the change of wind power and loads. As shown in Figure 6, lines 16–19 and 19–20 constitute the transmission interface of wind power deployed in bus 19. During the periods that wind spillage occurs, DPFCs operating in capacitive compensation on lines 14–16 and 11–14 can effectively control the power flows within thermal limits which makes the power flows in line 19-20 increase if wind power is abundant. Therefore, the flexibility in power flow control can utilize the total transfer capacity of transmission interface which is conducive to the consumption of wind power.

![Figure 11. Optimal control strategy of DPFCs in real-time scheduling stage.](image)

5. Conclusions

This paper proposes a multi-time scale scheduling methodology with DPFCs in system with high penetration of wind power. The optimal configuration of DPFCs is determined considering several plausible scenarios in the long-term scale. In the short-term scheduling stage consists of day-ahead and real-time scale, economic scheduling plans containing control strategy of DPFCs and scheduled power of several energies are obtained while considering uncertainty of wind power and physical and operating limitations on DPFCs. The case studies for the IEEE-RTS79 system illustrate the effectiveness of the proposed method, which can offer more economically scheduling plan and maximum utilization of wind power when DPFCs are optimal deployed and controlled. The proposed methodology could be applied for other sorts of FACTS or D-FACTS devices to promote the utilization of wind energy in power systems.

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