

Article



# Numerical Study of Pressure Fluctuation in a Gas- Liquid Two-Phase Mixed-Flow Pump

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**Abstract:** To explore the pressure fluctuation characteristics in a mixed-flow pump handling a gas-liquid two-phase flow, an unsteady simulation was carried out with ANSYS CFX for the whole flow passage when the inlet gas void fraction (*IGVF*) was 0%, 5%, and 10%, respectively. Under pure water conditions (*IGVF* = 0%), the reliability of the simulation was verified by comparing with the experiment in both aspects of external characteristics and fluctuation. Through the implementation of the fast Fourier transform (FFT) algorithm, the characteristics of the pressure fluctuation in the impeller and the guide vane were obtained at different *IGVF* conditions. The results demonstrate that pressure fluctuations exist under different *IGVF* conditions due to the rotor-stator interaction and the gas-liquid phase interaction, and the intensity of the fluctuation is firstly enhanced, and then weakened, along the streamwise direction with the maximum located near the impeller outlet. The relationship between the gas content and the pressure fluctuation was analyzed, and it is shown that the regional pressure fluctuation will be intensified only if the gas content therein reaches a certain level and the local phase interaction is strong. In addition, the pressure fluctuation in both the rotor-stator interaction region and the guide vane may be effectively inhibited under small *IGVF* conditions.

**Keywords:** gas-liquid two-phase flow; mixed-flow pump; pressure fluctuation; rotor-stator interaction; phase interaction

# 1. Introduction

The gas-liquid two-phase transport exists widely in petroleum, chemical engineering, food, urban water supply, nuclear industry, etc. Moreover, the energy performance of multiphase pumps handling gas-liquid two-phase flows will have a significant impact on the economic benefits of the relevant industries [1–4]. Compared with the single-phase pumps, since the gas-liquid two-phase transport process is often accompanied with the polymerization and division of bubbles, the pulsation of phase content, the separation and intermixing of the two phases, the flow in the multiphase pumps will be more complicated. In turn, the complex two-phase flow phenomenon will inevitably affect the pressure fluctuation in the pump.

In recent years, research has been conducted on the pressure fluctuation of the gas-liquid two-phase flow, especially for the two-phase flow in the pipeline. The pressure fluctuation signal is commonly used to identify the regime of the two-phase flow [5,6]. For instance, in order to describe the relationship between the flow pattern and the pressure, Hanafizadeh et al. [7] drew a flow regime map by measuring the pressure fluctuation signal of the gas-liquid two-phase flow in a vertical pipe. In practical applications, the frequency of the slug flow is closely related to the structural damage, the corrosion rate, and the coating protection of the pipeline [8,9], therefore, it is also very important to predict the formation

mechanism of the slug flow, and further understand its characteristics by measuring the pressure fluctuation signal [10–12].

However, studies on gas-liquid multiphase pumps are mainly concentrated on energy performance and flow instability. In the first aspect, a NACA65 axial flow pump handling gas-liquid two-phase flow was simulated by Tremante et al. [13]. It was found that when the attack angle is large, the air mass extends from the blade leading edge to the entire pressure side as the attack angle increases, and the stratified flow is generated in the impeller passage. Trevisan and Prado [14] explored the viscous effect on the two-phase flow pattern and the hydraulic performance of an electrical submersible pump, and found that the increase in equivalent-viscosity will cause the decrease in overall energy performance of the pump. In the analysis of Lu et al., [15] an Eulerian model was performed for the gas-liquid two-phase bubbly flow in a centrifugal pump and it showed that the gas content is high near the impeller shroud. Furthermore, a serious phase separation phenomenon will occur therein when the inlet gas void fraction is 14%. By observing the movement of the bubbles in a pump with high-speed photography technology, Poullikkas [16,17] explored the effect of the gas content on the energy performance of the pump. For flow instability, Yu et al. [18] simulated the internal flow in a gas-liquid two-phase rotodynamic pump and found that, under the condition of high gas content, obvious features of the bubble flow and the wave flow are presented in the leading edge and trailing edge of the impeller passage, respectively. Through the simulation of a multiphase rotodynamic pump under the condition of high gas content, Huang et al. [19] obtained that the static pressure in the gathering area of the liquid phase is generally higher than the gathering area of the gas phase, and the static pressure in the impeller increases gradually along the flow direction.

Usually, the centrifugal and axial types of pumps are used to transport the gas-liquid two-phase flow, thus not much relevant research has been done on mixed-flow pumps. Meanwhile, few studies have been performed on the pressure fluctuation in multiphase pumps. In this study, an unsteady flow simulation was carried out with ANSYS CFX 14.0 (SAS IP, Inc., Pittsburgh, PA, USA) for a mixed-flow pump handling a gas-liquid two-phase flow. Applying the fast Fourier transform (FFT), the characteristic difference of the pressure fluctuation under the conditions of pure liquid flow and gas-liquid two-phase flow with different *IGVF* was explored to obtain a preliminary understanding of pressure fluctuations in such pumps.

#### 2. Configuration and Mesh of the Gas-Liquid Two-Phase Pump

The three-dimensional model of the whole flow passage constructed with UG NX 6.0 (Siemens PLM Inc., Nuremberg, Germany) is shown in Figure 1. It includes four parts: inlet pipe, impeller, guide vane, and outlet pipe. The main parameters of this pump are listed as follows: impeller diameter *D* is 150 mm, impeller blade number  $Z_1$  is 6, guide vane number  $Z_2$  is 8, design flow rate  $Q_d$  is 23.2 kg/s, design speed *n* is 2000 r/min, design head  $H_d$  is 14.6 m, and power *P* is 5.5 kW. The structured mesh of the computational domain was generated with ICEM CFD 14.0 (SAS IP, Inc., Pittsburgh, PA, USA) and TurboGrid 14.0 (SAS IP, Inc., Pittsburgh, PA, USA), and the mesh of the impeller and guide vane passages is displayed in Figure 2. Through the analysis of mesh independence, the selected mesh number for the whole domain is 3,624,513.

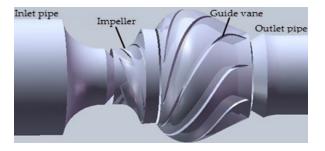
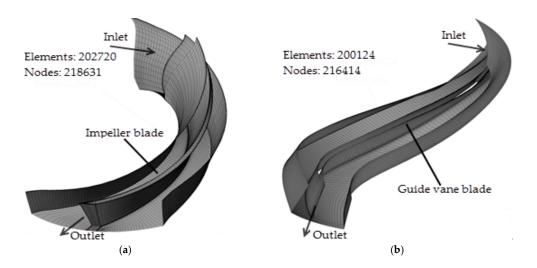


Figure 1. Configuration of the gas-liquid two-phase pump.



**Figure 2.** Structured mesh of the impeller and guide vane passages. (**a**) Impeller passage; and (**b**) guide vane passage.

## 3. Numerical Methods

#### 3.1. Governing Equations

As for the current models applied in the multiphase pumps handling gas-liquid two-phase flow, the two-fluid model has been widely used due to its high computational accuracy [20–22], therefore, it is selected as the numerical model in our study. Additionally, the numerical simulation is based on the following hypotheses: (a) the pattern in this multiphase pump is bubbly flow; (b) clear water and air are taken as the continuous phase and dispersed phase, respectively; and (c) the fluid is regarded as the isothermal flow, so there is no need to consider energy equations. The transport equations without mass transfer can be written as follows:

Continuity equation:

$$\frac{\partial}{\partial t}(\alpha_{k}\rho_{k}) + \nabla \bullet (\alpha_{k}\rho_{k}w_{k}) = 0$$
(1)

Momentum equation:

$$\frac{\partial}{\partial t}(\alpha_{k}\rho_{k}w_{k}) + \nabla \bullet (\alpha_{k}r_{k}w_{k}w_{k} - a_{k}\tau) = -\alpha_{k}\nabla p + M_{k} + a_{k}r_{k}f_{k}$$
(2)

where, subscript k = l or g denotes the liquid or gas phase;  $\rho_k$  is the density;  $\alpha_k$  is the volume fraction and  $\alpha_l + \alpha_g = 1$ ; *p* is the pressure;  $w_k$  is the relative velocity;  $f_k$  is the mass force relevant to the rotation of impeller; and  $M_k$  is the interphase force per unit volume. In the normal running phase of a pump, with the condition of small bubble size or low spin velocity of the bubbles, the Basset effect and the Magnus effect can be neglected [23,24]. In addition, the turbulent dispersion force can also be neglected according to the magnitude analysis by Yu et al. [25]. Therefore, the interphase force herein is associated only with drag, lift, and virtual mass.  $\tau$  denotes the viscous stress tensor concerning molecular viscosity, as well as turbulence viscosity. Its components are written as:

$$\tau_{ij} = 2\mu_k s_{ij} - \overline{\rho_k w'_{ki} w'_{kj}} \tag{3}$$

where,  $\underline{i}, j = 1, 2, 3$  represent the three directions of the relative coordinate system;  $\mu_k$  is the dynamic viscosity;  $S_{ij}$  denotes the strain tensor; and  $-\overline{\rho_k w'_{ki} w'_{kj}}$  represents the turbulent Reynolds stresses caused by turbulent motion, and it can be derived by:

$$-\overline{r_k w'_{ki} w'_{kj}} = 2\mu_{k,t} s_{ij} - \frac{2}{3}\rho_k d_{ij}$$

$$\tag{4}$$

here, the turbulent viscosity  $\mu_{k,t}$  is formulated based on the shear stress transport (SST) k- $\omega$  model, a combination of the k- $\omega$  model applied in the near-wall region and the k- $\varepsilon$  model employed for the mainstream region. This SST k- $\omega$  model not only has high accuracy in predicting flow separation under an adverse pressure gradient [26], but also has a certain applicability in the numerical description for the trajectory of the leakage vortex [27]. Here, the turbulent viscosity is computed as follows:

$$\mu_{\rm t} = \frac{\rho a_1 k}{\max(a_1 \omega, SF_2)} \tag{5}$$

and:

$$F_2 = tanh(arg_2^2) \tag{6}$$

$$\arg_{2} = \max\left(\frac{2\sqrt{k}}{\beta'\omega y'}, \frac{500\nu}{y^{2}\omega}\right)$$
(7)

where,  $\alpha_1$  and  $\beta'$  are the model constants ( $\alpha_1 = 5/9$ ,  $\beta' = 0.09$ ); *S* is the invariant measure of the strain rate; and k and  $\omega$  are the turbulence kinetic energy and turbulence frequency, respectively.

Additionally, the above descriptions of the governing equations are not only applicable to the gas-liquid two-phase flow, but also suitable for the single phase liquid, which only requires  $\alpha_l = 1$ .

#### 3.2. Boundary Conditions and Numerical Solutions

At the inlet of the computational domain, the mass flow was specified and the turbulence intensity was set as 5%; at the outlet, the free outflow condition was adopted; at all wall boundaries, a non-slip condition of viscous fluid was used, and the logarithmic wall function approach was applied in the near-wall region. A transient rotor-stator method was adopted for data exchange in the rotor-stator interaction region (namely the impeller/inlet pipe interface and the impeller/guide vane interface), through which the transient effect of the flow can be considered reliably, hence, it can improve the numerical accuracy of flow characteristics between the rotors and stators. To facilitate the convergence of the numerical computation, the unsteady simulation begins with the initial field of steady simulation results. The high resolution was applied in the advection scheme as well as turbulence numeric, and second-order backward Euler method was adopted in the transient scheme. The other unsteady solution settings are listed in Table 1.

Parameters	Notations	Values
Time step	$\Delta t$	0.0002 s
Maximum iteration number per time step	Ν	20
Total time	T	0.3 s
Residual	RMS	$<1 \times 10^{-4}$
Total flow rate Inlet gas void fraction	Qt IGVF	23.2 kg/s 0%, 5%, 10%

Table 1. The unsteady solution settings. RMS: root mean square.

#### 3.3. Monitoring Points Settings

In the unsteady simulation, four and five monitoring sections were set in the impeller and guide vane from the inlet to the outlet, respectively, and denoted as *i* (where *i* = 1 to 9), as shown in Figure 3.  $S_i$ ,  $C_i$ , and  $H_i$  (where *i* = 1 to 9) stand for the central point on the section from the shroud to hub, respectively. Due to the technical limitations, it is impossible to know the pressure frequency characteristics in the rotating impeller by arranging sensors. Therefore, the sensors in this study were only deployed on the stationary guide vane. Actually, the monitoring points  $H_5$ – $H_8$  in Figure 3 were the partial trail points on the hub of the guide vane as well.

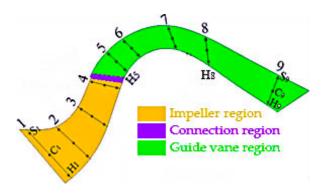
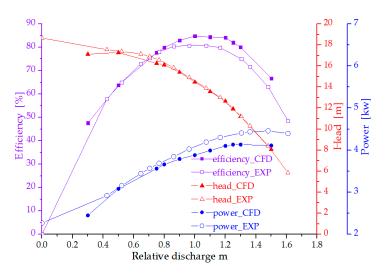


Figure 3. Location of monitoring points.

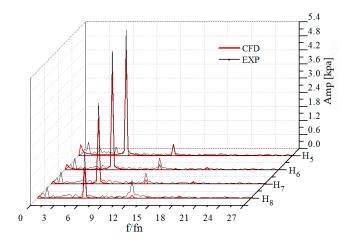
## 4. Results and Discussion

#### 4.1. Validation of Energy Performance and Pressure Fluctuation

To verify the reliability of the numerical model, under eleven pure water flow rate conditions (*IGVF* = 0%), the unsteady internal flow of the two-phase pump was simulated when the tip clearance  $\delta$  is 0.25 mm (0.25 mm is design clearance). The comparison between the simulation and experiment is listed in Figure 4. The efficiency, head, and power curves from the simulation agree well with the experimental results, and the errors of efficiency, head, and power at the design condition are 4.79%, 0.59%, and 4.67%, respectively. Additionally, the frequency domain diagram of points  $H_5$ – $H_8$  (Figure 3) under pure water conditions is presented in Figure 5. Overall, the frequency domains of pressure fluctuation from the simulation are in good agreement with the experimental ones as well, with a dominant frequency of 6 fn and a second dominant frequency of 12 fn occurring in both conditions. The above analysis illustrates that the numerical method used in our study is reasonable. From Figure 5, it can also be seen that more frequencies with small amplitudes appear in the experiment, this may be due to the vibration of the motor and test environment. Meanwhile, the fluctuation amplitude for dominant frequency of points  $H_5$ – $H_8$  gradually decreases under both conditions, which illustrates that the pressure fluctuation at the hub of the guide vane decreases along the streamwise direction, as well as with the rotor-stator interaction.



**Figure 4.** Energy performance curves from the simulation and the experiment under pure water conditions (relative discharge  $m = Q/Q_d$ ). CFD: computational fluid dynamics; EXP: experiment.



**Figure 5.** Frequency domain diagram of points  $H_5$ – $H_8$  at pure water condition ( $Q = Q_d$ ). Amp—the amplitude of pressure fluctuation, kpa; f/fn—the frequency ratio of pressure fluctuation to impeller rotation.

#### 4.2. Pressure Fluctuation in the Impeller Passage at Different IGVF Conditions

The pressure fluctuation coefficients of points  $C_1$ – $C_4$  on the middle of the sections from the impeller inlet to outlet with different *IGVF* at the design condition are presented in Table 2. Here, the pressure fluctuation coefficient is defined as:

$$C_p = \frac{\mathrm{S}}{\mathrm{\rho}\mathrm{g}H_\mathrm{d}} \times 100\% \tag{8}$$

where,  $\rho$  is the fluid density;  $H_d$  is the design head under pure water condition; and *S* is the standard deviation of pressure fluctuation, namely:

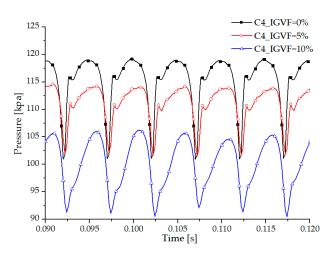
$$S = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left[ P_i(t) - \overline{P_i} \right]^2}$$
(9)

where,  $P_i(t)$  is the pressure at time *t*, while  $\overline{P_i}$  is the average pressure.

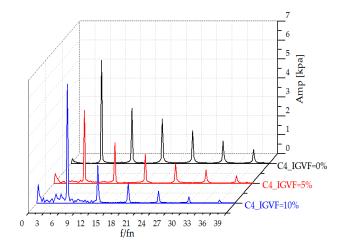
**Table 2.** Pressure fluctuation coefficients of points  $C_1$ – $C_4$  in the impeller (%).

Points IGVF	<i>C</i> <sub>1</sub>	<i>C</i> <sub>2</sub>	<i>C</i> <sub>3</sub>	<i>C</i> <sub>4</sub>
0%	0.20	0.26	0.36	3.52
5%	0.52	0.53	0.58	2.46
10%	2.13	1.86	1.48	3.44

As shown in Table 2, the pressure fluctuation coefficients at corresponding points  $C_1-C_3$  increase as *IGVF* increases. On the one hand, this is because their locations are relatively far away from the rotor-stator interaction region, thus the influence of the rotor-stator interaction is weak; on the other hand, taking into account the rotation effect of impeller, the interaction mode between the gas and liquid is more complicated as *IGVF* increases [25] and this will lead to the appearance of complex flow patterns and the enlargement of pressure fluctuation. The maximum values of pressure fluctuation coefficients of the points  $C_1-C_4$  are located near the impeller outlet under different *IGVF* conditions, which are closely related to the rotor-stator interaction and the complicated gas-liquid flow therein. Meanwhile, the pressure fluctuation coefficients of point  $C_4$  under conditions of *IGVF* = 0%, 10% are 1.43 and 1.40 times the condition of *IGVF* = 5%, respectively, which indicates that the pressure fluctuation near the impeller outlet may be effectively inhibited under small *IGVF* conditions. The pressure fluctuation of point  $C_4$  at the design condition with different *IGVF* values in one period is demonstrated in Figure 6. It can be seen that the average pressure of point  $C_4$  decreases as *IGVF* increases. Meanwhile, six peaks and valleys occur in one cycle under different *IGVF* conditions and this coincides with the number of the impeller blades. Through the FFT, the corresponding frequency domain diagram is shown in Figure 7. The dominant frequency of pressure fluctuation of point  $C_4$  is 6 fn under different *IGVF* conditions (corresponding to Figure 6), and the fluctuation amplitude for dominant frequency at *IGVF* = 5% is smaller than for the conditions of *IGVF* = 0%, 10%. There are also  $N \times 6$  fn frequencies (where N is a positive integer) at all of these conditions, which is the result of the periodically-rotating impeller blades ( $Z_1 = 6$ ) [28]. Moreover, there are other frequencies with small amplitudes arising when *IGVF* is 5% and 10%, which are closely related to the more disordered flow caused by the complex phase interaction between the gas and the liquid.



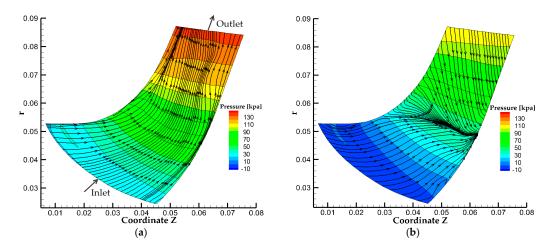
**Figure 6.** Time domain characteristics of point  $C_4$  under different *IGVF* conditions ( $Q = Q_d$ ).



**Figure 7.** Frequency domain diagram of point  $C_4$  under different *IGVF* conditions ( $Q = Q_d$ ).

Figure 8 shows the pressure and liquid phase streamlines distributions of the central hub-to-shroud surface of the impeller passage when *IGVF* is 0% and 10%. It can be seen that, compared with the condition of *IGVF* = 0%, a larger range low pressure zone appears in the impeller inlet region at the condition of *IGVF* = 10%, which manifests that the cavitation performance of this pump is worse under the gas-liquid two-phase condition. Moreover, under the gas-liquid two-phase condition, the flow in the impeller passage is more disordered, and backflow phenomenon occurs in the impeller hub (Figure 8b). This is caused by the rotating effect of the impeller, as the liquid phase is subjected to a larger centrifugal force than for the gas phase, resulting in the gathering of the gas in the impeller hub [29]. In turn, the

cumulative gas will block the impeller passage, and considering the effect of the complex interphase forces between the gas and the liquid, the flow in the impeller passage is more disordered. This is also the reason why points  $C_1$ – $C_3$  have large pressure fluctuations when IGVF = 10%.



**Figure 8.** Pressure and liquid phase streamlines distribution of the central hub-to-shroud surface at different *IGVF* conditions ( $Q = Q_d$ ). (a) *IGVF* = 0%; and (b) *IGVF* = 10%.

### 4.3. Pressure Fluctuation in the Guide Vane Passage at Different IGVF Conditions

The pressure fluctuation coefficients of points  $C_5$ – $C_9$  on the middle of the sections from inlet to outlet of the guide vane passage with different *IGVF* at the design condition are presented in Table 3. Pressure fluctuation coefficients of points  $C_5$ – $C_9$  decrease gradually from inlet to outlet of the guide vane under different *IGVF* conditions, which illustrates that the rotor-stator interaction is attenuated. Meanwhile, the pressure fluctuation of corresponding points at *IGVF* = 5% is generally less than the conditions of *IGVF* = 0%, 10%, which demonstrates that the pressure fluctuation in the guide vane can also be inhibited under small *IGVF* conditions.

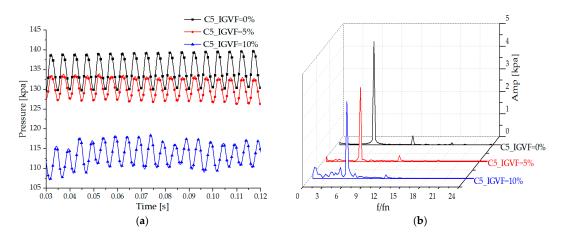
**Table 3.** Pressure fluctuation coefficients of points  $C_5$ – $C_9$  in the guide vane (%).

Points IGVF	<i>C</i> <sub>5</sub>	<i>C</i> <sub>6</sub>	<i>C</i> <sub>7</sub>	<i>C</i> <sub>8</sub>	C9
0%	2.29	2.12	1.48	0.73	0.20
5%	1.68	1.43	0.94	0.48	0.21
10%	2.03	1.16	1.11	0.46	0.43

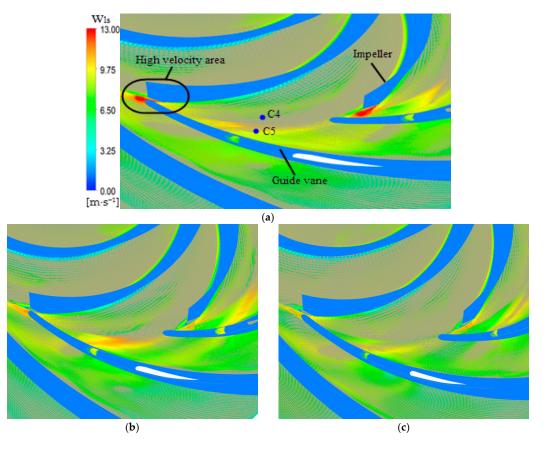
The time domain and frequency domain characteristics of point  $C_5$  at different *IGVF* conditions in three periods are demonstrated in Figure 9 ( $Q = Q_d$ ). With the increase of *IGVF*, the average pressure of point  $C_5$  decreases, while the turbulence of periodicity increases; the amplitude of the dominant frequency under the condition of *IGVF* = 5% is smaller than for the conditions of *IGVF* = 0%, 10%. From Figure 9b, it can also be seen that there are other frequencies with small amplitudes at the gas-liquid two-phase conditions.

Through the above analysis of pressure fluctuation in both the impeller and guide vane, it can be found that the pressure fluctuation in the rotor-stator region (points  $C_4$ ,  $C_5$ ) is somewhat large at different *IGVF* conditions. The vector distributions of both the liquid superficial velocity ( $W_{ls}$ ) and the gas superficial velocity ( $W_{gs}$ ) from the impeller outlet region to the guide vane inlet region at the span of 0.5, when t is 0.24 s, are displayed in Figures 10 and 11, respectively. Figure 10a shows that the liquid superfical velocity in the vicinity will increase significantly when the impeller blades are close to the guide vane blades under the condition of *IGVF* = 0%, this is because there is a larger water discharge under the condition of *IGVF* = 0% than under the gas-liquid two-phase conditions.

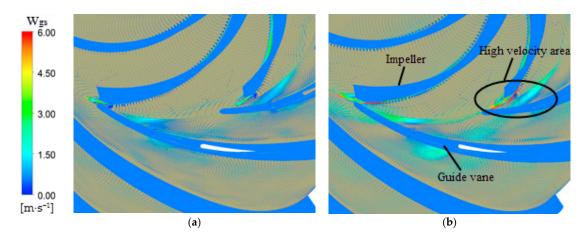
larger liquid superfical velocity will result in a stronger impact loss in the inlet region of the guide vane passage, this is the reason why the pressure fluctuation in the rotor-stator region (points  $C_4$ ,  $C_5$ ) at this condition is larger. From Figure 11, it can be observed that the gas superficial velocity at condition of IGVF = 10% is larger than for the condition of IGVF = 5%, taking into account the rotating effect of the impeller, this results in larger pressure fluctuation at corresponding points under the condition of IGVF = 10%. Actually, the above analyses are also the reasons that larger pressure fluctuations occur in the guide vane passage under the conditions of IGVF = 0%, 10%.



**Figure 9.** Time domain and frequency domain characteristics of point  $C_5$  under different *IGVF* conditions ( $Q = Q_d$ ). (a) Time domain characteristics; and (b) frequency domain characteristics.



**Figure 10.** Vector distributions of the liquid superficial velocity ( $W_{ls}$ ) in the interaction region (Span = 0.5,  $Q = Q_d$ ). (a) *IGVF* = 0%; (b) *IGVF* = 5%; and (c) *IGVF* = 10%.

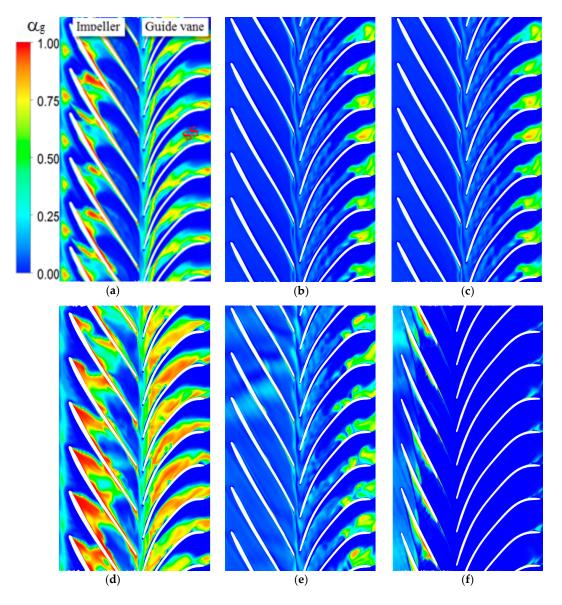


**Figure 11.** Vector distributions of the gas superficial velocity ( $W_{gs}$ ) in the interaction region (Span = 0.5,  $Q = Q_d$ ). (a) *IGVF* = 5%; and (b) *IGVF* = 10%.

From the above analysis, it is found that, under the design condition with different *IGVF*, the fluctuation intensity of points  $C_1$ – $C_9$  on the middle of the sections is firstly enhanced and then weakened along the streamwise direction with the maximum located near the impeller outlet (point  $C_4$ ). The pressure fluctuation in both the rotor-stator interaction region and the guide vane may be effectively inhibited under small *IGVF* conditions, and more frequencies with small amplitudes appear under the gas-liquid two-phase conditions than under the pure water condition.

#### 4.4. Relationship between the Gas Content and the Pressure Fluctuation in the Impeller/Guide Vane

The distribution of the gas content from hub to shroud of both the impeller and guide vane under conditons of IGVF = 5%, 10% is shown in Figure 12. The gas content in the impeller passage is mainly accumulated near the hub in these two conditions (Figure 12a,d). On the one hand, this is caused by the rotating effect of the impeller; on the other hand, the liquid phase with a larger density is subjected to a larger centrifugal force than for the gas phase. These two resons result that the liquid moving to the shroud while the gas gathers in the hub and, hence, the flow in the impeller hub is more disordered (Figure 8b). The gas content decreases from the hub to the shroud of the guide vane and the gas content in the hub accumulates near the back surface (namely the "SS" surface in Figure 12a). This is due to the gas entering guide vane passage is affected by the pressure difference between the working surface and the back surface, and the gas moves to the back surface and gathers therein. Meanwhile, the gas content is also high on the back surface of the guide vane outlet under the conditions of IGVF = 5%, 10% (span = 0.5), while the pressure fluctuation is small therein (point  $C_9$ ). This is because the corresponding area is relatively far away from the rotor-stator interaction region, the rotor-stator interaction and the gas-liquid phase interaction are weak, resulting in a small acceleration existing in the gas phase, and the distribution of the gas content is relatively stable therein. Then, compared with Tables 2 and 3, the pressure fluctuation in the rotor-stator interaction region (points  $C_4$ ,  $C_5$ ) at the span of 0.5 is far greater than that in the guide vane outlet region (point  $C_9$ ), which is ascribed to the larger gas-liquid phase interaction caused by rotor-stator interaction. According to the above analysis, it is found that, for the flow in the gas-liquid two-phase mixed-flow pump, the regional pressure fluctuation will be intensified only if the gas content therein reaches a certain level and the gas-liquid phase interaction is strong.



**Figure 12.** Distribution of the gas content from the hub to the shroud of both the impeller and the guide vane at conditions of IGVF = 5%, 10% ( $Q = Q_d$ ). (a) Span = 0.01, IGVF = 5%; (b) Span = 0.5, IGVF = 5%; (c) Span = 0.99, IGVF = 5%; (d) Span = 0.01, IGVF = 10%; (e) Span = 0. 5, IGVF = 10%; and (f) Span = 0.99, IGVF = 10%.

# 5. Conclusions

Through the unsteady numerical calculation, the characteristics of pressure fluctuation in a mixed-flow pump handling a gas-liquid two-phase flow were explored under different *IGVF* conditions. The results can be summarized as follows:

- (1) Influenced by the rotor-stator interaction and the gas-liquid phase interaction, pressure fluctuations occur in three *IGVF* conditions and the dominant frequency of the pressure fluctuation of point  $C_4$  is 6 fn (the impeller blade number is 6). Meanwhile, more frequencies with small amplitudes appear under the gas-liquid two-phase condition the than pure water condition.
- (2) At different *IGVF* conditions, the intensity of the fluctuation is firstly enhanced, and then weakened, along the streamwise direction with the maximum located near the impeller outlet (point  $C_4$ ). Additionally, the pressure fluctuations in both the rotor-stator interaction region and the guide vane may be effectively inhibited under small *IGVF* conditions.

(3) Due to the rotating effect of the impeller, the liquid phase is subjected to a larger centrifugal force than for the gas phase, as the gas gathers in the hub of both the impeller and the guide vane. The relationship between the gas content and the pressure fluctuation was analyzed, and it is shown that the regional pressure fluctuation will be intensified only if the gas content therein reaches a certain level and the local phase interaction is strong.

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**Author Contributions:** Baoshan Zhu conceived, designed and performed the experiments; Wenwu Zhang and Zhiyi Yu analyzed the data and wrote the paper.

Conflicts of Interest: The authors declare no conflict of interest.

### Nomenclature

D	Impeller diameter, m	
$Q_{\rm d}$	Design flow rate, kg/s	
$n^{\sim u}$	Rotational speed, r/min	
Р	Shaft power, kW	
$H_{d}$	Head, m	
Z	Blade number	
$F_2$	Blending function in SST-k-ω model	
р	Static pressure, kpa	
, w	Relative velocity, m/s	
n <sub>s</sub>	Specific speed, $m^{3/4} s^{-3/2}$	
$\Delta t$	Time step, s	
Т	Total time, s	
Qt	Total flow rate, kg/s	
$a_1$	Model constant, dimensionless	
Cp	Pressure coefficient, dimensionless	
r	Radial coordinate, dimensionless	
fn	Frequency of the impeller rotation, 1/s	
k	Turbulent kinetic energy, $m^2/s^2$	
$W_{\rm ls}$	Water superficial velocity, m/s	
$W_{\rm gs}$	Air superficial velocity, m/s	
Amp	Amplitude of the fluctuation, kpa	
IGVF	Inlet gas void fraction, dimensionless	
f	Mass force relevant to the rotation of the impeller, $m/s^2$	
S	Standard deviation of the fluctuation, dimensionless	
$M_{ m k}$	Total interphase force per unit volume, N/m <sup>3</sup>	
Ν	Maximum iteration number per time step, dimensionless	
Greek sy	mbols	
α	Void fraction, dimensionless	
ρ	Density of phase k, kg/m <sup>3</sup>	
τ	Viscous stress tensor, pa	
$\mu_t$	Turbulent viscosity, pa·s	
ω	Rotational frequency of the impeller, 1/s	
Subscripts		
k	Phase	

- g Gas phase
- l Liquid phase

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