## Article

# Series-Connected High Frequency Converters in a DC Microgrid System for DC Light Rail Transit 

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#### Abstract

This paper studies and presents a series-connected high frequency DC/DC converter connected to a DC microgrid system to provide auxiliary power for lighting, control and communication in a DC light rail vehicle. Three converters with low voltage and current stresses of power devices are series-connected with single transformers to convert a high voltage input to a low voltage output for a DC light rail vehicle. Thus, Metal-Oxide-Semiconductor Field-Effect Transistors (MOSFETs) with a low voltage rating and a turn-on resistance are adopted in the proposed circuit topology in order to decrease power losses on power switches and copper losses on transformer windings. A duty cycle control with an asymmetric pulse-width modulation is adopted to control the output voltage at the desired voltage level. It is also adopted to reduce switching losses on MOSFETs due to the resonant behavior from a leakage inductor of an isolated transformer and output capacitor of MOSFETs at the turn-on instant. The feasibility and effectiveness of the proposed circuit have been verified by a laboratory prototype with a 760 V input and a $24 \mathrm{~V} / 60 \mathrm{~A}$ output.


Keywords: DC microgrid; zero-voltage switching; half-bridge converter; light rail transit

## 1. Introduction

Direct current (DC) microgrids are studied to combine alternative current (AC) utility power, renewable energy sources, energy storage units and local DC and AC loads in order to reduce global warming and climbing temperature issues. The common DC voltage on DC microgrids can be 1500 V for traction vehicles; 760 V for light rail vehicles and industry applications; 380 V for residential and commercial buildings. For light rail transits, low frequency power transformers are used in conventional light rail vehicles to provide electrical isolation. The main drawback of line frequency transformers [1-3] is bulk volume. To avoid using bulky line frequency transformers, transformerless converter topologies [4-8] with primary-series and secondary-parallel connections have been proposed to lessen the blocking-voltage capability of active devices on the high voltage side and the current stress of power components on the low voltage side. Half-bridge (HB) or full-bridge (FB) converters have been widely adopted for medium power applications to provide a stable and low voltage output. Conventional FB converters and HB converters using high voltage rating devices such as insulated gate bipolar transistors (IGBTs) are widely adopted to convert a high voltage input to a low voltage output. However, the switching frequency of general IGBT devices is less than 50 kHz . To improve the low switching frequency problem of IGBT devices, multilevel converters [9-11] using Metal-Oxide-Semiconductor Field-Effect Transistor (MOSFET) devices have been developed in medium power converters to reduce converter volume. However, the high switching frequency will also increase core losses on magnetic components and switching losses on power MOSFETs. Zero-voltage switching converters [12-15] have been proposed to achieve a low switching loss. Asymmetric pulse-width modulation [16-18], frequency modulation [19-21] and a phase-shift pulse-width modulation (PWM) scheme [22-24] are general PWM control schemes used in DC/DC converters to regulate load voltage
and also realize the mechanism of the zero-voltage turn-on switching. Therefore, the high efficiency converters can be obtained. The asymmetrical PWM scheme can reset the magnetizing flux in every switching cycle. Therefore, the voltage spike on drain-to-source of power MOSFET can decrease the safety operation region and the electromagnetic interference can be reduced.

This paper presents a series-connected soft switching converter using a single transformer for light rail vehicle applications. The adopted circuit topology includes three series-connected HB circuits on the primary side to reduce the blocking-voltage stress of power MOSFETs. Thus, low turn-on resistance and low voltage rating MOSFETs can be adopted to lessen conduction losses on power devices. The input split voltage balance is achieved by two flying capacitors. The asymmetric PWM scheme is employed to control power switches. The output capacitor of power MOSFETs and the leakage inductor of the transformer are resonant at the transition interval. Thus, the mechanism of the zero-voltage turn-on switching is realized and the electromagnetic interference can be reduced. Current doubler rectifier topology is used on the low voltage side to achieve a ripple current cancellation. Therefore, the resultant ripple current at the output capacitor is reduced. Three HB circuits share one transformer on the primary side so that the primary currents of the three HB circuits are reduced to one-third of the primary current in a conventional HB converter. Therefore, the conduction losses on active switches are reduced and the circuit efficiency is improved. The feasibility of the proposed circuit is verified with a 1.44 kW converter. This paper is organized as follows: in Section 2, the circuit configuration and operation principle of the developed converter used in the DC microgrid are presented and discussed in detail. In Section 3, the circuit characteristics of the developed circuit are presented. Experimental results based on a laboratory prototype are shown and discussed in Section 4. Finally, Section 5 presents the conclusions.

## 2. Proposed Converter

The basic circuit structure of a DC microgrid is given in Figure 1. The bidirectional AC/DC converters are used between the AC utility system and the DC microgrid to stabilize the DC bus voltage. Renewable energy sources from solar cell panels and wind power generators provide clear energy to the DC microgrid system through the unidirectional DC/DC converters and the AC/DC converters. Energy storage units are used to store/release energy from/to the DC microgrid through the bidirectional $\mathrm{DC} / \mathrm{DC}$ converters in order to stabilize the DC bus voltage. In order to increase the voltage reliability, the bipolar voltage system $\left(+V_{d c},-V_{d c}\right.$ and neutral line) can be adopted on the DC microgrid. When a fault condition in one of the DC poles occurs, the DC power is still suppled to the local load by the other two wires and an auxiliary converter. It is clear that the reliability of the DC mircogrid system is increased during fault condition. Therefore, three voltage levels $\left(2 V_{d c},+V_{d c}\right.$ and $-V_{d c}$ ) can be used to provide industry and transportation with the $2 V_{d c}$ voltage level and future residential and commercial buildings with the $+V_{d c}$ or $-V_{d c}$ voltage level. To keep two voltage levels $\left(+V_{d c}\right.$ and $\left.-V_{d c}\right)$ balanced during unbalanced loads, a voltage balancing circuit is normally needed to realize this goal. The DC/DC converter can be used to convert a high input voltage to a low output voltage and it does not relate to the bipolar voltage system. For a DC light rail vehicle, the input voltage is normally around 760 V . Power devices such as the 1500 V IGBT can be adopted in two-level power converters to supply auxiliary low voltage power for control units, telecommunication units and lighting systems in the light rail vehicle. The MOSFETs with a 600 V rating can be adopted in the three-level power converter to achieve the same goal but with a much higher switching frequency to reduce converter size. The studied converter is concentrated on power conversion for light rail vehicle applications. Figure 2a shows the basic block diagrams of power distribution in a conventional light rail vehicle. First, $750 V_{d c}$ is converted to the three-phase AC voltage $380 V_{a c}$ by the DC/AC inverter. Second, the AC/DC converter is adopted to convert $380 V_{a c}$ to a low DC voltage in an auxiliary power distribution system to supply a necessary amount of DC voltage for the battery bank, lighting equipment, door equipment, control power units and communication equipment in a light rail vehicle system. The AC/DC/AC converter is also adopted to convert $380 V_{a c}$ to a variable
$A C$ voltage output for the AC motor drive. If the power of the DC light rail vehicle is supplied directly from the DC microgrid, then some power conversion stages can be saved to reduce costs and increase circuit efficiency. The basic power distribution diagrams in the proposed light rail vehicle are illustrated in Figure 2b. The auxiliary power in a light rail vehicle is directly converted from 760 V through a DC/DC converter. The AC motor drive and the air compressor are controlled by the $\mathrm{DC} / \mathrm{AC}$ converters. Therefore, the AC/DC conversion can be saved to reduce costs and increase circuit efficiency and reliability.


Figure 1. Basic circuit structure of a DC microgrid.

(a)

(b)

Figure 2. Light rail transit. (a) Block diagram of the power distribution in a conventional light rail vehicle; (b) block diagram of the power distribution in the studied light rail vehicle.

The studied DC/DC converter is given in Figure 3. It directly converts a 760 V voltage input from the DC microgrid to a low voltage output by using low voltage rating power MOSFETs to provide auxiliary power in a light rail vehicle. The studied converter includes three HB circuits connected in a primary-series secondary-parallel with a single transformer. The primary sides of the HB circuits are connected in a series so that the voltage stress of the power switches $Q_{1} \sim Q_{6}$ is reduced to $V_{\text {in }} / 3$ and
the low turn-on resistance of power MOSFETs is adopted to reduce conduction losses and increase circuit efficiency. Each HB circuit provides $P_{o} / 3$ to the output load. Flying capacitors are widely used in a multilevel inverter to reduce voltage stress and balance input split voltages. Thus, two flying capacitors $C_{f 1}$ and $C_{f 2}$ are used on the high voltage side to achieve an input voltage balance of $V_{C 1} \sim V_{C 3}$. The current doubler rectifier is used on the low voltage side to reduce the output ripple current. The driving signals of each HB circuit use asymmetric pulse-width modulation. Due to the resonant behavior between the output capacitor of the power MOSFETs and the primary leakage inductor at switch on/off instant, the power MOSFETs can be turned on at zero-voltage switching to reduce the switching loss. Figure 4 shows the timing sequence of switches $Q_{1} \sim Q_{6}$ and the main PWM waveforms in the proposed converter. The operation principle and circuit analysis of the studied circuit are assumed under the following conditions: (1) the output capacitor $C_{o}$ is large enough to be treated as a constant voltage $V_{o}$, (2) power devices $Q_{1} \sim Q_{6}, D_{1}$ and $D_{2}$ are ideal, (3) $C_{f 1}=C_{f 2}=C_{f}$, $C_{b 1}=C_{b 2}=C_{b 3}=C_{b}, L_{r 1}=L_{r 2}=L_{r 3}=L_{r}$, and $L_{m 1}=L_{m 2}=L_{m 3}=L_{m}$, (4) $n_{1}=n_{2}=n_{3}=n_{p} / n_{s}$, and (5) $V_{C b 1}=V_{C b 2}=V_{C b 3}=V_{C b}$ and $V_{C 1}=V_{C 2}=V_{C 3}=V_{C f 1}=V_{C f 2}=V_{i n} / 3$. The duty cycles of $Q_{1}, Q_{3}$ and $Q_{5}$ are $d$. Conversely, the duty cycles of $Q_{2}, Q_{4}$ and $Q_{6}$ are $1-d$. The equivalent circuits of the operating steps in the proposed circuit are shown in Figure 5. There are eight operating stages for every switching period.


Figure 3. Circuit schematic of the studied converter.


Figure 4. Main waveforms during one switching period.

Step $1\left[t_{0} \sim t_{1}\right]$ : Before step 1, power switches $Q_{1}, Q_{3}$ and $Q_{5}$ are conducting and the output current freewheels through $D_{1}$ and $D_{2}$. After time $t_{0}, i_{D 1}$ is decreased to zero and $D_{1}$ becomes reverse biased. $i_{0}$ flows through $D_{2}$. Power is transferred from $V_{i n}$ to $R_{o}$ in this step. In step $1, V_{C f 1}=V_{C 1}$, $V_{C f 2}=V_{C 2}, v_{Q 2, d s}=V_{C 1}, v_{Q 4, d s}=V_{C 2}, v_{Q 6, d s}=V_{C 3}, v_{L m 1} \approx V_{C 1}-v_{C b 1}, v_{L m 2} \approx V_{C 2}-v_{C b 2}, v_{L m 3} \approx V_{C 3}$ $-v_{C b 3}, v_{L o 1} \approx\left[V_{C 1}-v_{C b 1}\right] / n_{1}-V_{o}$ and $v_{L o 2}=-V_{o}$. Thus, $i_{p 1 \sim}^{\sim} i_{p 3}$ and $i_{L o 1}$ increase and $i_{L o 2}$ decreases. Since all circuit components in three HB circuits are identical and $n_{1}=n_{2}=n_{3}=n_{p} / n_{s}$, it can obtain $v_{L m 1}=v_{L m 2}=v_{L m 3}=n v_{n s}$ and $i_{p 1}=i_{p 2}=i_{p 3} \approx i_{s} /\left(3 n_{1}\right)$. Since $i_{L o 1}$ increases and $i_{L o 2}$ decreases in this step, the ripple current of $i_{\text {Lo1 }}+i_{\text {Lo2 }}$ is reduced.

Step 2 [ $t_{1} \sim t_{2}$ ]: When $Q_{1}, Q_{3}$ and $Q_{5}$ are turned off at time $t_{1}$; the positive primary currents $i_{p 1} \sim i_{p 3}$ rapidly discharge $C_{Q 2}, C_{Q 4}$ and $C_{Q 6}$, respectively. On the other hand, $C_{Q 1}, C_{Q 3}$ and $C_{Q 5}$ are charged by $i_{p 1} \sim i_{p 3}$ respectively. The secondary winding voltage $v_{n s}$ is decreased in this step.

Step 3 [ $t_{2} \sim t_{3}$ ]: When $C_{Q 2}, C_{Q 4}$ and $C_{Q 6}$ are discharged to $v_{C b 1}, v_{C b 2}$ and $v_{C b 3}$ respectively, then the secondary winding voltage $v_{n s}=0$. Then the output current $i_{0}$ freewheels through $D_{1}$ and $D_{2}$. In this operation step, $v_{L o 1}=v_{L o 2}=-V_{o}$ and $i_{L o 1}$ and $i_{L o 2}$ decrease.

Step $4\left[t_{3} \sim t_{4}\right]$ : At time $t_{3}, C_{Q 2}, C_{Q 4}$ and $C_{Q 6}$ are discharged to zero voltage. Since $i_{p 1}\left(t_{3}\right) \sim i_{p 3}\left(t_{3}\right)$ are all positive, the body diodes $D_{Q 2}, D_{Q 4}$ and $D_{Q 6}$ are forward biased. Therefore, $Q_{2}, Q_{4}$ and $Q_{6}$ can be turned on at this moment to realize a zero-voltage turn-on. Because $i_{0}$ is still freewheeling through $D_{1}$ and $D_{2}$, it can obtain $v_{n s}=0, v_{L o 1}=v_{L o 2}=-V_{o}, v_{L r 1}=-v_{C b 1}, v_{L r 2}=-v_{C b 2}$ and $v_{L r 3}=-v_{C b 3}$. $i_{p 1} \sim i_{p 3}, i_{L o 1}$ and all $i_{L o 2}$ decrease. This step is ended when $i_{D 2}=0$. During this freewheeling interval, the currents $i_{L r 1} \sim i_{L r 3}$ are decreased from $i_{L o 1} /\left(3 n_{1}\right)$ to $-i_{L o 2} /\left(3 n_{1}\right)$ and the current variation on $L_{r 1} \sim L_{r 3}$ is about $I_{o} /\left(3 n_{1}\right)$. The duty loss in step 4 is obtained as (1) shows:

$$
\begin{equation*}
d_{l o s s, 4}=\frac{\Delta t_{34}}{T_{s w}}=\frac{I_{0} L_{r} f_{s w}}{3 n_{1} v_{C b 1}} \tag{1}
\end{equation*}
$$

Step $5\left[t_{4} \sim t_{5}\right]$ : After $t_{4}, i_{D 2}$ is decreased to zero so that $D_{2}$ is reverse biased. $i_{0}$ flows through $D_{1}, L_{o 1}$ and $L_{o 2}$. In step 5, power is transferred from $V_{i n}$ to $R_{0,}, V_{C f 1}=V_{C 2}, V_{C f 2}=V_{C 3}, v_{Q 1, d s}=V_{C 1}, v_{Q 3, d s}=V_{C 2}$, $v_{Q 5, d s}=V_{C 3}, v_{L m 1} \approx-v_{C b 1}, v_{L m 2} \approx-v_{C b 2}, v_{L m 3} \approx-v_{C b 3}, v_{L o 1}=-V_{o}$ and $v_{L o 2} \approx v_{C b 1} / n_{1}-V_{o}$. Thus, $i_{p 1} \sim i_{p 3}$ and $i_{L o 1}$ decrease and $i_{L o 2}$ increases.

Step 6 [ $t_{5} \sim t_{6}$ ]: When $Q_{2}, Q_{4}$ and $Q_{6}$ turn off at time $t_{5}$, the negative primary currents $i_{p 1} \sim i_{p 3}$ rapidly charge $C_{Q 2}, C_{Q 4}$ and $C_{Q 6}$, respectively. On the other hand, $C_{Q 1}, C_{Q 3}$ and $C_{Q 5}$ are discharged by $i_{p 1} \sim i_{p 3}$ respectively. The secondary winding voltage $v_{n s}$ is increased in this step.

Step $7\left[t_{6} \sim t_{7}\right]$ : When $C_{Q 2}, C_{Q 4}$ and $C_{Q 6}$ are charged to $v_{C b 1}, v_{C b 2}$ and $v_{C b 3}$ respectively at $t_{6}$, it can obtain $v_{n s}=0$. Thus, $i_{0}$ freewheels through $D_{1}$ and $D_{2}$ in this step and $v_{L o 1}=v_{L o 2}=-V_{o}$.

Step $8\left[t_{7} \sim t_{0}+T_{s w}\right]$ : When $C_{Q 1}, C_{Q 3}$ and $C_{Q 5}$ are discharged to zero voltage at $t_{7}$, the body diodes $D_{Q 1}, D_{Q 3}$ and $D_{Q 5}$ are forward biased. Power switches $Q_{1}, Q_{3}$ and $Q_{5}$ can be turned on at this moment to realize zero-voltage turn-on. Since $i_{0}$ still freewheels through $D_{1}$ and $D_{2}$, it can obtain $v_{n s}=0, v_{L o 1}=v_{L o 2}=-V_{o}$ and $v_{L r 1}=v_{L r 2}=v_{L r 3}=V_{i n} / 3-v_{C b 1}$. Thus, $i_{p 1} \sim i_{p 3}$ increase and $i_{L o 1}$ and $i_{L o 2}$ decrease. This step is ended when $i_{D 1}=0$. During this freewheeling interval, $i_{L r 1} \sim i_{L r 3}$ increase from $-i_{\text {Lo2 }} /\left(3 n_{1}\right)$ to $i_{\text {Lo1 }} /\left(3 n_{1}\right)$. The duty loss in step 8 is obtained as (2) shows.

$$
\begin{equation*}
d_{l o s s, 8}=\frac{I_{0} L_{r} f_{s w}}{3 n_{1}\left(V_{i n} / 3-v_{C b 1}\right)} \tag{2}
\end{equation*}
$$

At time $t_{0}+T_{s w}, i_{D 1}$ is decreased to zero and this switching period is completed. Since the duty cycle of all switches equals 0.5 , the voltage balance of $C_{1}, C_{2}$ and $C_{3}$ is well achieved with two balance capacitors $C_{f 1}$ and $C_{f 2}$. If $Q_{1}, Q_{3}$ and $Q_{5}$ are in the on-state and $Q_{2}, Q_{4}$ and $Q_{6}$ are in the off-state, it obtains $v_{C f 1}=V_{C 1}$ and $v_{C f 2}=V_{C 2}$. If $V_{C 1}>V_{C 2}$ or $V_{C 1}<V_{C 2}$, then $C_{1}$ charges or discharges $C_{f 1}$ through $Q_{1}$ and $Q_{3}$. When $Q_{1}, Q_{3}$ and $Q_{5}$ are in the off-state and $Q_{2}, Q_{4}$ and $Q_{6}$ are in the on-state, it obtains $v_{C f 1}=V_{C 2}$ and $v_{C f 2}=V_{C 3}$. If $V_{C 1}>V_{C 2}$ or $V_{C 1}<V_{C 2}, C_{f 1}$ charges or discharges $C_{2}$ through $Q_{2}$ and $Q_{4}$. In a similar way, $C_{f 2}$ can be used to balance $V_{C 2}$ and $V_{C 3}$. Therefore, $V_{C 1} \sim V_{C 3}$ are all controlled at $V_{\text {in }} / 3$.


Figure 5. Operation steps of the power converter during one switching cycle (a) step 1 (b) step 2 (c) step 3 (d) step 4 (e) step 5 (f) step 6 (g) step 7 (h) step 8.

## 3. Circuit Characteristics

The asymmetric PWM scheme is adopted to drive $Q_{1} \sim Q_{6}$. Based on the flux balance of primary inductors such as ( $L_{r 1}$ and $\left.L_{m 1}\right),\left(L_{r 2}\right.$ and $\left.L_{m 2}\right)$ and $\left(L_{r 3}\right.$ and $\left.L_{m 3}\right)$, the DC capacitor voltages $V_{C 1} \sim V_{C 3}$ in a steady state can be obtained as $V_{C b 1}=V_{C b 2}=V_{C b 3}=d V_{i n} / 3$, where $d$ is the duty cycle of $Q_{1}, Q_{3}$ and $Q_{5}$. In the same way, the output voltage can be derived from the flux balance of output inductors $L_{01}$ and $L_{o 2}$ in a steady state.

$$
\begin{equation*}
V_{o}=\frac{V_{i n}}{3 n_{1}} d(1-d)-\frac{I_{o} L_{r} f_{s w}}{3 n_{1}^{2}}-V_{f} \tag{3}
\end{equation*}
$$

where $V_{f}$ is the voltage drop on $D_{1}$ and $D_{2}$.

Since the average winding currents $i_{p 1} \sim i_{p 3}$ equal zero and $I_{L o 1}+I_{L o 2}=I_{0}$, the average inductor currents $I_{L o 1}$ and $I_{L o 2}$ are derived as $I_{L o 1}=(1-d) I_{o}$ and $I_{L o 2}=d I_{o}$. The ripple currents on $L_{o 1}$ and $L_{o 2}$ are given in (4) and (5).

$$
\begin{gather*}
\Delta i_{L o 1}=\frac{V_{o}\left(1-d+d_{l o s s, 8}\right) T_{s w}}{L_{o 1}}=\frac{(1-d) V_{o} T_{s w}+\frac{V_{o} L_{r} I_{o}}{n_{1}(1-d) V_{i n}}}{L_{o 1}}  \tag{4}\\
\Delta i_{L o 2}=\frac{V_{o}\left(d+d_{l o s s, 4}\right) T_{s w}}{L_{o 2}}=\frac{d V_{o} T_{s w}+\frac{V_{o} L_{r} I_{o}}{n_{1} d V_{i n}}}{L_{o 2}} \tag{5}
\end{gather*}
$$

The asymmetric PWM is adopted to regulate load voltage. From Figure 4, the turn-on time of $D_{1}$ is related to the duty cycle of $Q_{2}$ and the turn-on time of $D_{2}$ is related to the duty cycle of $Q_{1}$. Therefore, the average diode currents $I_{D 1}$ and $I_{D 2}$ are expressed as $I_{D 1}=(1-d) I_{o}$ and $I_{L o 2}=d I_{o}$. The voltage stress of diodes $D_{1}$ and $D_{2}$ is related to the secondary winding voltage. The secondary winding voltage $v_{n s}$ is dependent on the input voltage $V_{i n}$ and clamped voltage $V_{C b 1}$. Thus, the voltage stress of $D_{1}$ and $D_{2}$ can be given in (6) and (7).

$$
\begin{gather*}
v_{D 1}=(1-d) V_{i n} /\left(3 n_{1}\right)  \tag{6}\\
v_{D 2}=d V_{i n} /\left(3 n_{1}\right) \tag{7}
\end{gather*}
$$

The conduction losses on rectifier diodes $D_{1}$ and $D_{2}$ are approximately equal to $I_{o} V_{f}$. If the transformer is constructed, then the magnetizing inductances $L_{m 1} \sim L_{m 3}$ are given. Thus, the ripple currents $i_{L m 1} \sim i_{L m 3}$ are obtained in (8).

$$
\begin{equation*}
\Delta i_{L m 1}=\Delta i_{L m 2}=\Delta i_{L m 3} \approx \frac{\left(V_{i n} / 3-v_{C b 1}\right)\left(d-d_{l o s s, 8}\right) T_{s w}}{L_{m 1}}=\frac{d(1-d) V_{i n} T_{s w}}{3 L_{m 1}}-\frac{I_{0} L_{r}}{3 n_{1} L_{m 1}} \tag{8}
\end{equation*}
$$

Three HB circuits are connected in a series on the high voltage side to reduce the voltage stress of active switches. Therefore, it is able to obtain the voltage stress of each active switch clamped at $V_{i n} / 3$. If the ripple currents on magnetizing inductors and output inductors are neglected, the root-mean-square (rms) currents $i_{Q 1, r m s} \sim i_{Q 1, r m s}$ can be derived as (9) and (10) show.

$$
\begin{gather*}
i_{Q 1, r m s}=i_{Q 3, r m s}=i_{Q 5, r m s} \approx \frac{(1-d) I_{o} \sqrt{d}}{3 n_{1}}  \tag{9}\\
i_{Q 2, r m s}=i_{Q 4, r m s}=i_{Q 6, r m s} \approx \frac{d I_{o} \sqrt{1-d}}{3 n_{1}} \tag{10}
\end{gather*}
$$

The conduction losses on $Q_{1} \sim Q_{6}$ are approximately equal to $d(1-d) I_{o}^{2} R_{o n} /\left(3 n_{1}^{2}\right)$, where $R_{o n}$ is turn-on resistance of $Q_{1} \sim Q_{6}$. The positive peak currents of $i_{p 1} \sim i_{p 3}$ at time $t_{1}$ are given in (11).

$$
\begin{array}{r}
i_{p 1}\left(t_{1}\right)=i_{p 2}\left(t_{1}\right)=i_{p 3}\left(t_{1}\right) \approx i_{L m 1, \text { max }}+\frac{i_{L o 1, \text { max }}}{3 n_{1}} \approx \frac{d(1-d) V_{i n} T_{s w}}{6 L_{m 1}}-\frac{I_{o} L_{r}}{6 n_{1} L_{m 1}} \\
+\frac{(1-d) I_{o}}{3 n_{1}}+\frac{(1-d) V_{o} T_{s w}+\frac{V_{o L} I_{o}}{n_{1}(1-d) V_{i n}}}{6 n_{1} L_{o 1}} \tag{11}
\end{array}
$$

Likewise, the negative peak currents of $i_{p 1} \sim i_{p 3}$ at time $t_{5}$ are given in (12).

$$
\begin{equation*}
i_{p 1}\left(t_{5}\right)=i_{p 2}\left(t_{5}\right)=i_{p 3}\left(t_{5}\right) \approx i_{L m 1, \max }+\frac{i_{L o 1, \text { max }}}{3 n_{1}} \approx-\frac{d(1-d) V_{i n} T_{s w}}{6 L_{m 1}}+\frac{I_{o} L_{r}}{6 n_{1} L_{m 1}}-\frac{d I_{o}}{3 n_{1}}-\frac{d V_{o} T_{s w}+\frac{V_{0 L} L_{0} I_{o}}{n_{1} V_{\text {in }}}}{6 n_{1} L_{o 2}} \tag{12}
\end{equation*}
$$

The minimum primary current to realize zero-voltage turn-on switching of $Q_{1}, Q_{3}$ and $Q_{5}$ is given in (13).

$$
\begin{equation*}
i_{p 1}\left(t_{5}\right) \geq \frac{V_{i n}}{3} \sqrt{\frac{2 C_{Q}}{L_{r 1}}} \tag{13}
\end{equation*}
$$

Similarly, the minimum primary current to realize zero-voltage turn-on switching of $Q_{2}, Q_{4}$ and $Q_{6}$ is given in (14).

$$
\begin{equation*}
i_{p 1}\left(t_{1}\right) \geq \frac{V_{i n}}{3} \sqrt{\frac{2 C_{Q}}{L_{r 1}}} \tag{14}
\end{equation*}
$$

where $C_{Q}=C_{Q 1}=C_{Q 2}=C_{Q 3}=C_{Q 4}=C_{Q 5}=C_{Q 6}$.

## 4. Experimental Results

A laboratory prototype with 1.44 kW rated power was constructed and tested in order to verify the feasibility of the studied converter to supply the auxiliary power in a light rail vehicle from the DC microgrid system. The experimental circuit diagram of the developed converter is provided in Figure 6. The TL431 voltage regulator and photocoupler PC817 are used to regulate load voltage. The PWM UCC2893 is used to achieve asymmetric pulse-width modulation (APWM) generation. Pulse transformers are adopted to achieve electrical isolation and gate drive. The specifications of the experimental prototype are given in Table 1. The power rating of the magnetic transformer is the same as the transformer in the three-level converter and the two-level full-bridge converter. The turns-ratio of the transformer in the developed converter is one-third of the turns-ratio in the two-level full-bridge converter. The magnetizing voltage and primary turns of the transformer in the studied converter are only one-third of the magnetizing voltage and primary turns in the two-level full-bridge converter. The PC40 EER-42 magnetic core is used with 15 primary turns and 8 secondary turns to build the isolated transformer. The experimental results of the proposed converter while it supplies 1.44 kW to the output load under a 760 V input are shown in Figures $7-12$. Based on the test results, the measured waveforms agree well with the theoretical waveforms as given in Figure 4. Figure 7 shows the gate voltages of $Q_{1} \sim Q_{6}$ at $20 \%$ and $100 \%$ loads. It is clear that $Q_{1}, Q_{3}$ and $Q_{5}$ have the same PWM waveforms. In the same manner, $Q_{2}, Q_{4}$ and $Q_{6}$ have the same PWM waveforms. The input split voltages and balance capacitor voltages at a full load are shown in Figure 8. From the experimental results, the input split voltages and two flying voltages are balanced well. The primary side currents of three HB circuits are illustrated in Figure 9. It is observed that the three primary currents are balanced well. Figure 10 gives the measured waveforms of three DC block capacitor voltages. It can be observed that the three voltages are balanced and the capacitor voltages are related to the duty cycle of $Q_{1}$, $Q_{3}$ and $Q_{5}$. Figure 11 shows the experimental waveforms of the secondary side currents. The ripple currents on $L_{01}$ and $L_{02}$ partially cancel each other so that the resultant ripple current on the load side is reduced. Figure 12 shows the test results of $Q_{1}$ and $Q_{2}$ at $20 \%$ and $100 \%$ loads. Before the switch is turned on, the switch current is negative to discharge the output capacitor $C_{Q}$ to zero voltage. Thus, the mechanism of the zero-voltage turn-on switching is clearly achieved for both $Q_{1}$ and $Q_{2}$ from a $20 \%$ load. It can also be observed that all drain voltages of $Q_{1}$ and $Q_{2}$ are clamped at $V_{\text {in }} / 3$. Since the PWM signals of the three HB circuits are identical and the input split voltages are also balanced, $Q_{3} \sim Q_{6}$ can also be turned on at zero-voltage from a $20 \%$ load. Figure 13 shows the circuit efficiency of the studied converter under different load cases. The measured maximum efficiency is about $93.6 \%$. The main advantage of the studied converter is the lower voltage rating of power switches compared to the conventional three-level converter with eight MOSFETs and the two-level full-bridge converter with four IGBTs. Considering the turns-ratio of the transformer, the root-mean-square current of the studied converter is the same as the three-level and two-level converters. However, the lower conduction resistance of MOSFETs with lower voltage rating is used in the developed converter. Therefore, the total conduction losses (six MOSFETs) in the studied converter can be reduced compared to the three-level converter with eight MOSFETs and the full-bridge converter with four IGBTs.

Table 1. Prototype Specifications.

| Items | Symbol | Parameter |
| :---: | :---: | :---: |
| Input voltage | $V_{i n}$ | 760 V |
| Output voltage | $V_{o}$ | 24 V |
| Output current | $I_{o}$ | 60 A |
| Switching frequency | $f_{s w}$ | 100 kHz |
| Power switches | $Q_{1} \sim Q_{6}$ | IRFP460 |
| Rectifier diodes | $D_{1}, D_{2}$ | MBR40100T |
| Split capacitors | $C_{1}, C_{2}, C_{3}$ | $330 \mu \mathrm{~F} / 400 \mathrm{~V}$ |
| Flying capacitors | $C_{f 1}, C_{f 2}$ | $2.2 \mu \mathrm{~F} / 630 \mathrm{~V}$ |
| Block capacitors | $C_{b 1}, C_{b 2}, C_{b 3}$ | $750 \mathrm{nF} / 630 \mathrm{~V}$ |
| Turns ratio of $T$ | $n_{p}: n_{p}: n_{p}: n_{s}$ | $15: 15: 15: 8$ |
| Primary inductances | $L_{r 1}, L_{r 2}, L_{r 3}$ | $30 \mu \mathrm{H}$ |
| Magnetizing inductances | $L_{m 1}, L_{m 2}, L_{m 3}$ | 0.8 mH |
| Output filter inductances | $L_{o 1}, L_{o 2}$ | $32 \mu \mathrm{H}$ |
| Output filter capacitance | $C_{o}$ | $4400 \mu \mathrm{~F} / 50 \mathrm{~V}$ |



Figure 6. The experimental circuit diagram of the developed converter.


Figure 7. PWM signals of $Q 1 \sim Q 6$ under (a) $20 \%$ load; (b) full load [ $v_{Q 1} \sim v_{Q 6}: 10 \mathrm{~V} /$ div; time: $\left.2 \mu \mathrm{~s}\right]$.


Figure 8. Measured input capacitor voltages under full load [ $V_{C 1} \sim V_{C f 2}: 200 \mathrm{~V} /$ div; time: $\left.2 \mu \mathrm{~s}\right]$.


Figure 9. Test results of the primary side currents under (a) $20 \%$ load $\left[i_{p 1} \sim i_{p 3}: 2 \mathrm{~A} /\right.$ div; time: $\left.2 \mu \mathrm{~s}\right]$; (b) full load [ $i_{p 1} \sim i_{p 3}: 5 \mathrm{~A} /$ div; time: $2 \mu \mathrm{~s}$ ].


Figure 10. Test results of the primary capacitor voltages under (a) $20 \%$ load $\left[V_{C b 1} \sim V_{C b 3}: 100 \mathrm{~V} /\right.$ div; time: $2 \mu \mathrm{~s}$ ]; (b) full load [ $V_{C b 1} \sim V_{C b 3}: 100 \mathrm{~V} /$ div; time: $2 \mu \mathrm{~s}$ ].


Figure 11. Measured secondary side currents at (a) $20 \%$ load $\left[i_{D 1}, i_{D 2}, i_{L o 1}, i_{L o 2}, i_{L o 1}+i_{L o 2}: 10 \mathrm{~A} / \mathrm{div}\right.$; time: $2 \mu \mathrm{~s}]$; (b) $100 \%$ load [ $i_{D 1}, i_{D 2}, i_{L o 1}+i_{L o 2}: 50 \mathrm{~A} /$ div; $i_{L o 1}, i_{L o 2}: 20 \mathrm{~A} /$ div; time: $\left.2 \mu \mathrm{~s}\right]$.


Figure 12. Measured switch voltages and current (a) $Q_{1}$ at $20 \%$ load [ $v_{Q 1, g}: 10 \mathrm{~V} /$ div; $v_{Q 1, d}: 200 \mathrm{~V} /$ div; $i_{Q 1}: 2 \mathrm{~A} /$ div; time: $\left.1 \mu \mathrm{~s}\right]$; (b) $Q_{1}$ at full load [ $v_{Q 1, g}: 10 \mathrm{~V} / \mathrm{div} ; v_{Q 1, d}: 200 \mathrm{~V} /$ div; $i_{Q 1}: 10 \mathrm{~A} / \mathrm{div}$; time: $1 \mu \mathrm{~s}]$; (c) $Q_{2}$ at $20 \%$ load $\left[v_{Q 2, g}: 10 \mathrm{~V} /\right.$ div; $v_{Q 2, d}: 200 \mathrm{~V} / \mathrm{div} ; i_{Q 2}: 2 \mathrm{~A} /$ div; time: $\left.1 \mu \mathrm{~s}\right] ;$ (d) $Q_{2}$ at full load [ $v_{Q 2, g}: 10 \mathrm{~V} /$ div; $v_{Q 2, d}: 200 \mathrm{~V} /$ div; $i_{Q 2}: 10 \mathrm{~A} /$ div; time: $1 \mu \mathrm{~s}$ ].


Figure 13. Test results of circuit efficiency.

## 5. Conclusions

In this paper, a series-connected HB converter with a single transformer is proposed for light rail transit applications. The proposed circuit's main benefits are the low voltage rating of power semiconductors, low switching losses, high circuit efficiency and balance split voltages compared to conventional converter topologies used in light rail vehicles. The asymmetric PWM scheme is used to control power switches, regulate output voltage and achieve the mechanism of the zero-voltage
turn-on switching. The circuit analysis, operation principle and design example of the proposed circuit are presented and discussed in detail. Finally, the feasibility of the studied circuit is verified by experimental results with a 1.44 kW laboratory prototype. The current harmonics on the input side is dependent on the switching frequency and the load current. The large current harmonics will result in unstable voltage on the input DC voltage bus. Therefore, in a future study, the interleaved DC/DC converter of the studied circuit will be developed to reduce the input current harmonics.

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