

Article



# Evolution of Thermoelectric Properties of Zn<sub>4</sub>Sb<sub>3</sub> Prepared by Mechanical Alloying and Different Consolidation Routes

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Abstract: In this research, a method combining the mechanical alloying with the vacuum sintering or hot pressing was adopted to obtain the compact of  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub>. Pure zinc and antimony powders were used as the starting material for mechanical alloying. These powders were mixed in the stoichiometry ratio of 4 to 3, or more Zn-rich. Single phase Zn<sub>4</sub>Sb<sub>3</sub> was produced using a nominally 0.6 at. % Zn rich powder. Thermoelectric Zn<sub>4</sub>Sb<sub>3</sub> bulk specimens have been fabricated by vacuum sintering or hot pressing of mechanically alloyed powders at various temperatures from 373 to 673 K. For the bulk specimens sintering at high temperature, phase transformation of  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> to ZnSb and Sb was observed due to Zn vaporization. However, single-phase Zn<sub>4</sub>Sb<sub>3</sub> bulk specimens with 97.87% of theoretical density were successfully produced by vacuum hot pressing at 473 K. Electric resistivity, Seebeck coefficient, and thermal conductivity were evaluated for the hot pressed specimens from room temperature to 673 K. The results indicate that the Zn<sub>4</sub>Sb<sub>3</sub> shows an intrinsic p-type behavior. The increase of Zn<sub>4</sub>Sb<sub>3</sub> phase ratio can increase Seebeck coefficient but decrease electric conductivity. The maximum power factor and figure of merit (*ZT*) value were  $1.31 \times 10^{-3}$  W/mK<sup>2</sup> and 0.81 at 600 K, respectively. The ZT value was lower than that reported in the available data for materials prepared by conventional melt growth and hot pressed methods, but higher than the samples fabricated by vacuum melting and heat treatment techniques.

Keywords: Zn<sub>4</sub>Sb<sub>3</sub>; mechanical alloying; vacuum hot pressing; thermoelectric materials; ZT

## 1. Introduction

Thermoelectric (TE) materials that convert electrical energy into heat can be used to manufacture thermoelectric generators or thermoelectric coolers. The former directly convert heat into electrical energy, while the latter use electrical energy to disperse heat and achieve a cooling effect. For practical applications, the conversion efficiency of TE materials is often characterized according to a TE figure of merit, *ZT*, which is a dimensionless parameter and is conventionally defined as Equation (1).

$$ZT = (\alpha^2 \sigma / \kappa)T \tag{1}$$

where *Z* is the figure of merit, *T* represents the absolute temperature,  $\alpha$  is the Seebeck coefficient,  $\sigma$  represents electrical conductivity, and  $\kappa$  is total thermal conductivity with contributions from the lattice ( $\kappa_L$ ) and charge carriers ( $\kappa_e$ ). A larger *ZT* indicates higher energy conversion efficiency in a TE material. Clearly an efficient TE material with high *ZT* requires high  $\alpha$ , high  $\sigma$ , and low  $\kappa$  [1,2]. Using thermoelectric materials in component manufacturing has the following advantages [3]: (1) small size, light weight, and providing localized cooling; (2) precise temperature control up to  $\pm 0.001$  °C; (3) high reliability, and capability to work in any orientation or under vibration; (4) long service life

of up to 200,000 h. Despite these numerous advantages, thermoelectric materials are expensive and their efficiency is smaller than 5%, far less than conventional refrigerators or generators. Therefore, the current applications of thermoelectric materials are limited within some special applications such as military or space flight applications. Improving the efficiency of thermoelectric materials is thus an important research and development issue.

Thermoelectric materials can be classified by its working temperature range: (1) room temperature range, such as Bi-Te alloys; (2) ~400 K, the Pb-Te series; and (3) ~800 K, the Si-Ge series [4–8]. The first type is primarily used as thermoelectric coolers, while the latter two are primarily used as thermoelectric generators. In recent years, many new compounds and alloys have been proposed, including skutterudites, clathrates, half-Heusler alloys,  $Zn_4Sb_3$ , SnSe, GeTe, and AgSbTe<sub>2</sub> and some layer-structured compounds [9–15]. These new materials exhibit higher *ZT* values at high temperature ranges. Generally,  $Zn_4Sb_3$  can be prepared in several ways: consolidation of powders either prepared by crushing ingots made by vacuum melting [16,17] or mechanical alloying methods [18], bulk mechanical alloying (BMA) followed by hot pressing [19]. The high defect densities in mechanically alloyed powders are expected to reduce the material's lattice thermal conductivity, thus improving the efficiency of thermoelectric conversion [20]. Thus, the feasibility to prepare a single  $\beta$ -phase  $Zn_4Sb_3$  alloy was fabricated by combining mechanical alloying with a vacuum sintering or vacuum hot pressing approach.

#### 2. Experimental

In the present study, mechanical alloying (MA) was used to prepare  $Zn_4Sb_3$  alloy powder. The as-milled powder was then subjected to vacuum sintering or vacuum hot pressing. The as-milled powder, sintered, and hot-pressed specimens were examined by X-ray diffraction (XRD), differential scanning calorimetry (DSC), and scanning electron microscopy (SEM).

The mechanical alloying process used zinc (99.9%, <325 mesh) and antimony (99.5%, <325 mesh) pure elemental powder to synthesize the  $Zn_4Sb_3$  alloy. Stoichiometric  $Zn_4Sb_3$  with superfluous Zn powder up to 1.8 at. % was weighed to a total of 4 g. The mixed powder and stainless steel ball (with a powder to ball ratio of 1:5) was then sealed in a glove box under an Ar atmosphere. A SPEX 8000D (SPEX SamplePrep, Metuchen, NJ, USA) shaker ball mill was used to prepare the  $Zn_4Sb_3$  alloy powder. After 5 h of MA treatment, the as-milled powder was pressed into pellets with a preload pressure of 0.098 GPa and then placed in a vacuum furnace for vacuum sintering at a temperature of 373, 473, 573, and 673 K, respectively. Vacuum hot pressing was performed under the same temperature (i.e., 373, 473, 573, and 673 K) with an applied pressure of 0.49, 0.74, and 0.98 GPa for 15, 30, and 60 min. The actual densities of the fabricated bulk samples were measured by Archimedean method. The level of porosity (%) can be estimated from the theoretical and actual densities. The sample codes and processing parameters for vacuum hot pressing were summarized in Table 1.

X-ray diffraction analysis was conducted using a PANalytical X'Pert Pro (Malvern Panalytical, Malvern, UK) diffractometer. A Dupont 2000 (DuPont, Wilmington, DE, USA) differential scanning calorimeter and a Hitachi S-4800 (Hitachi, Tokyo, Japan) scanning electron microscope were used for DSC and SEM characterization, respectively. The thermoelectric properties were conducted using the ULVAC Zem-3 (ULVAC Technologies, Tokyo, Japan) system to measure the Seebeck coefficient and electrical conductivity. Whereas the thermal conductivity was measured by the ULVAC TC9000 (ULVAC Technologies, Tokyo, Japan) laser flash thermal constant analyzer.

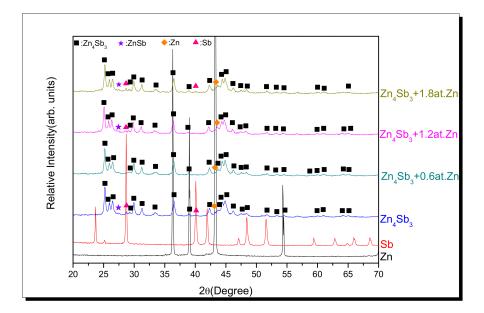
Sample Codes	Pressure (GPa)	Temperature (K)	Time (min)	
A-1	0.98	373	30	
A-2	0.98	473	30	
A-3	0.98	573	30	
B-1	0.49	473	15	
B-2	0.74	473	15	
B-3	0.98	473	15	
C-1	0.49	473	60	
C-2	0.74	473	60	
C-3	0.98	473	60	

Table 1. Sample designations of vacuum hot pressing samples.

#### 3. Results and Discussion

#### 3.1. XRD Diffraction Analysis of MA Powder

Figure 1 shows the X-ray diffraction patterns of the as-milled powder after 5 h of mechanical alloying process. It can be noted that only the  $Zn_4Sb_3$  with 0.6 at. % of excess Zn exhibited nearly a single  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase, thus this composition was used for the subsequent vacuum sintering and hot pressing. There are two more reasons for this selection: (1) this composition can be prepared to a nearly single Zn<sub>4</sub>Sb<sub>3</sub> in a short time by SPEX shaker ball mill; and (2) Zn<sub>4</sub>Sb<sub>3</sub> with superfluous Zn may compensate the loss of Zn evaporation during the sintering heat treatment.



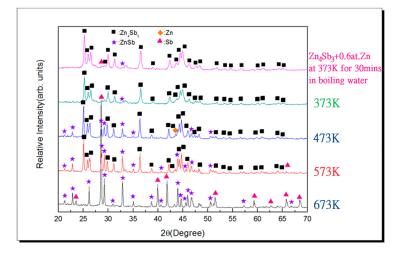
**Figure 1.** X-ray diffraction (XRD) patterns of mechanically alloyed powders with different Zn rich compositions.

### 3.2. Vacuum Sintering and Vacuum Hot Pressing of Bulk Zn<sub>4</sub>Sb<sub>3</sub> Alloy

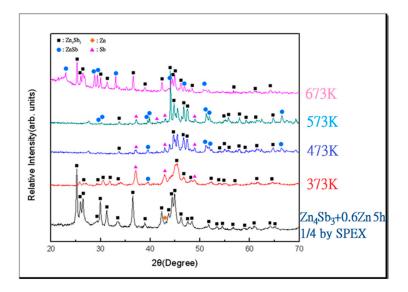
Figure 2 shows the XRD patterns of bulk specimens with 0.6 at. % Zn rich composition vacuum sintered for 30 min at 373, 473, 573, and 673 K, respectively. Impermeable heating of the as-milled powder in 100 °C (i.e., 373 K) boiled water was also shown for comparison with that of 373 K sintered sample. As shown in the top two curves in Figure 2, no significant differences in XRD patterns can be revealed. With increasing sintering temperature, the peaks intensity of ZnSb reflections increased with gradual decrease of corresponding Zn<sub>4</sub>Sb<sub>3</sub> phase. At 673 K, no Zn<sub>4</sub>Sb<sub>3</sub> diffraction peaks can be observed. This can be attributed to the high-temperature sintering where evaporation of Zn occurred

and resulted in the loss of Zn content. It is suggested that the Zn concentration within the 673 K sintered powder was less than 50 at. % and resulted in equilibrium Sb and ZnSb phases.

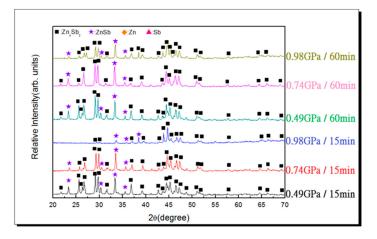
In order to obtain high-density bulk  $Zn_4Sb_3$ , the as-milled powder of  $Zn_4Sb_3$  with 0.6 at. % of excess Zn was vacuum hot pressed into a disc with a diameter of 10 mm and a thickness of 2 mm at different temperatures and pressures for various durations. Figure 3 shows the XRD patterns of selected vacuum hot pressed samples under an applied pressure of 0.98 MPa for 30 min at different temperatures. It can be noted that the vacuum hot pressed samples exhibited different phases compared to that of as-milled powder. After vacuum hot pressing at 373 K and 473 K, the main phase is  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub>. However, detailed analysis revealed a decrease in lattice constant due to the evaporation of Zn during vacuum hot pressing. For 573 and 673 K samples, Sb and ZnSb phases can be observed. This phenomenon is similar to what occurred for the vacuum sintered sample at 673 K. Since major  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase formed at 373 and 473 K, Figure 4 shows the corresponding XRD patterns for those vacuum hot pressed at 473 K but under different applied pressures and durations. It can be noticed that most samples exhibited both Zn<sub>4</sub>Sb<sub>3</sub> and ZnSb phases. The applied pressure and duration do not have a significant effect on the structure.



**Figure 2.** XRD patterns of bulk specimens with 0.6 at. % Zn rich composition vacuum sintered at different temperatures for 30 min.

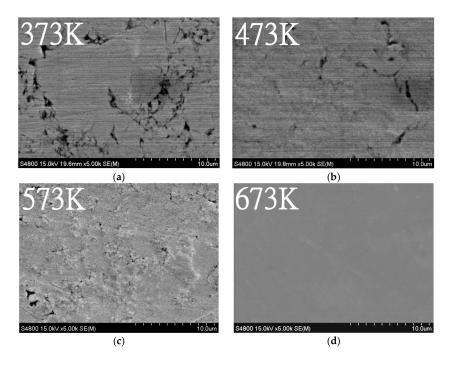


**Figure 3.** XRD patterns of bulk specimens with 0.6 at. % Zn rich composition hot pressed at different temperatures. Pressure: 0.98 GPa, time: 30 min.

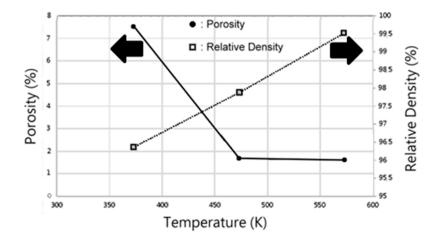


**Figure 4.** XRD patterns of bulk specimens with 0.6 at. % Zn rich composition hot pressed at 473 K under different pressures and times.

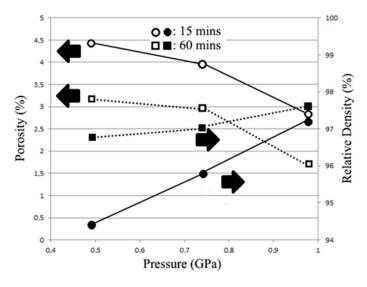
Figure 5 shows the SEM images of vacuum hot pressed samples under an applied pressure of 0.98 GPa for 30 min (i.e., the corresponding samples examined in Figure 3). It can be noted that the porosity decreased with the increase of the hot pressing temperature, hot pressing time, and pressure. The sample hot pressed at 673 K revealed almost pore-free microstructure and exhibited the highest density and smallest porosity among all hot pressed samples. Corresponding density and porosity of vacuum hot pressed samples prepared with different temperatures were shown in Figure 6, where porosity decreases with increasing temperature can be noticed. Figure 7 shows the density and porosity for the samples vacuum hot pressed at 473 K with various applied pressure and duration, i.e., the samples examined in Figure 4. It is noted that, from the perspective of constant pressure, when the duration increases from 15 to 60 min, the porosity decreases by more than 1%. Meanwhile, with the same duration at 473 K, the porosity can be reduced by increasing the applied pressure.



**Figure 5.** Scanning electron microscopy (SEM) micrographs of bulk specimen with 0.6 at. % Zn rich composition hot pressed at different temperatures. Pressure: 0.98 GPa, time: 30 min. (**a**) 373K; (**b**) 473 K; (**c**) 573 K; (**d**) 673 K.



**Figure 6.** Density and porosity of vacuum hot pressed samples prepared with different temperatures. Pressure: 0.98 GPa, time: 30 min.



**Figure 7.** Density and porosity of vacuum hot pressed samples prepared with different time and pressure. Pressure: 0.98 GPa, time: 30 min.

From the XRD results shown in Figures 3 and 4, the hot pressed samples exhibited generally a mixture of  $Zn_4Sb_3$  and ZnSb phases. In calculating the relative density, though the theoretical density of  $Zn_4Sb_3$  (6.20 g/cm<sup>3</sup>) is used as the benchmark [21], the relative density may be overestimated due to the theoretical density of ZnSb (6.38 g/cm<sup>3</sup>) [22]. In fact, the relative density should be lower than the values obtained. For example, as shown in Figure 3, the A-3 hot pressed sample exhibited Sb phase in addition to  $Zn_4Sb_3$  and ZnSb phases. The theoretical density of Sb is 6.69 g/cm<sup>3</sup> [23,24], causing the relative density to be slightly higher than the others. Similar experimental results have been reported by Ueno and Yamamoto [25] who investigated  $Zn_{4.08}Sb_3$  with different oxygen content. They found that the XRD analysis for hot pressed bulk materials with lower oxygen content (0.209%) showed no ZnSb or Zn phase. A relative density of 99.6% was measured. On the other hand, the one with high oxygen content (0.625%) possessed  $Zn_4Sb_3$  and Sb phases and resulted in a relative density of 100.6%. Ueno suggested that, since the sample is pore free, part of the  $Zn_4Sb_3$  may decompose into Sb and led to the calculated density higher than the theoretical density of  $Zn_4Sb_3$ .

The thermoelectric properties of selected samples, i.e., A-2, C-2, and cold-pressed (pressed at 298 K under 0.49GPa), was shown in Figures 8–12. Within the test temperature range, the Seebeck coefficients ( $\alpha$ ) for all the samples are positive, indicating the p-type semiconductor behavior with

holes as carriers. The Seebeck coefficient generally increases with temperature and the highest  $\alpha$  value (215.8 µV/K) exhibits in A-2 at 603 K. Figure 9 shows the temperature dependence of electrical conductivity ( $\sigma$ ) that slowly rises with increasing temperature, the semiconductor transport behavior might be responsible for such phenomenon. Similar behavior also has been reported in Zn-Sb based alloys by several research groups [17,22,26,27]. Using the data from Figures 8 and 9, we can obtain the power factor  $\theta$  ( $\alpha^2 \sigma$ ) that shows in Figure 10, where the A-2 sample exhibits the highest power factor (1.31 × 10<sup>-3</sup> W/mK<sup>2</sup>) at 600 K. Figure 11 shows the correlation between thermal conductivity ( $\kappa$ ) and temperature, with the A-2 sample at 600 K obtaining the lowest  $\kappa$  value (0.98 W/mK). Finally, with the data obtained from Figures 8–11, we can calculate the *ZT* values according to the formula  $\alpha^2 \sigma T/\kappa$  and the results are shown in Figure 12. Because the A-2 sample possesses a higher power factor and lower thermal conductivity than those from either cold-pressed or C-2 specimens, it has the highest *ZT* value of 0.81 at 600 K.

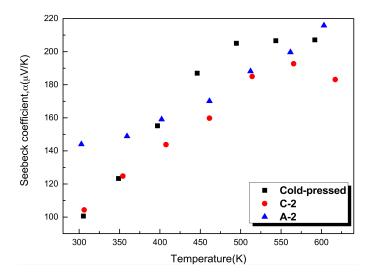
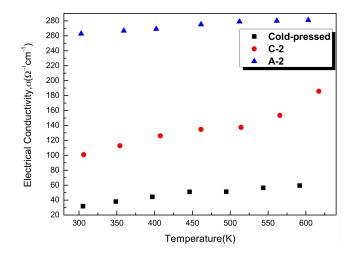


Figure 8. Variation of the Seebeck coefficient as a function of temperature for the hot pressed  $Zn_4Sb_3$  specimens.



**Figure 9.** Variation of the electrical conductivity as a function of temperature for the hot pressed Zn<sub>4</sub>Sb<sub>3</sub> specimens.

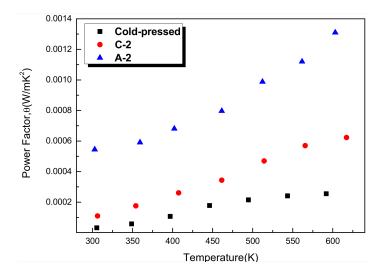
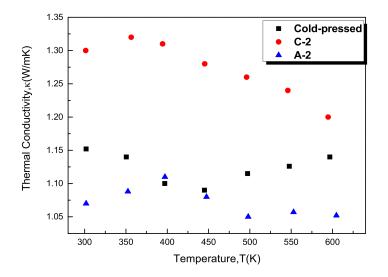


Figure 10. Variation of the power factor as a function of temperature for the hot pressed  $Zn_4Sb_3$  specimens.



**Figure 11.** Variation of the thermal conductivity as a function of temperature for the hot pressed  $Zn_4Sb_3$  specimens.

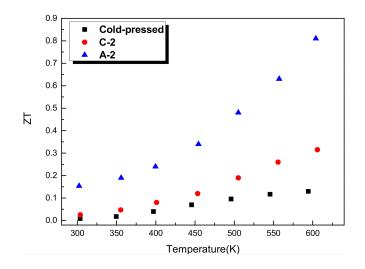


Figure 12. Variation of the ZT values as a function of temperature for the hot pressed Zn<sub>4</sub>Sb<sub>3</sub> specimens.

It is interesting to note the high electrical conductivity of the A-2 samples suggests there might be significant electron contribution to the thermal conductivity reported in Figure 11. To improve this argument, the electronic thermal conductivity ( $\kappa_e$ ) is calculated by the Wiedemann-Franz relation,  $\kappa_e = L\sigma T$  (where  $L = 2.0 \times 10^{-8} \text{ V}^2/\text{K}^2$  is Lorenz number,  $\sigma$  is electrical conductivity, and T is absolute temperature) [28]. The results indicate the estimate electronic thermal conductivity is much larger than the estimate lattice thermal conductivity ( $\kappa_L$ ). The high electrical conductivity also suggests a stronger phonon-electron coupling might be observed due to quite high carrier concentration in A-2 samples. The effect of phonon-electron (p-e) scattering on  $\kappa_L$  has been investigated in Cu, Ag, Au, Al, Pt, Ni, and Si by first principle calculation [29,30]. The results indicate the  $\kappa_L$  of Pt, Ni, and Si can be reduced by p-e scattering. Specifically, a significant reduction of  $\kappa_L$  reaches up to 45% in p-type Si was obtained when the carrier concentration is around  $10^{21}$  cm<sup>-3</sup>.

Table 2 summarizes the thermoelectric properties of the cold-pressed, C-2, and A-2 samples measured at 600 K. The Seebeck coefficients ( $\alpha$ ) are positive, indicating that these three bulks are p-type semiconductors. In 2003, Ur [31] et al. mentioned that  $\alpha$  increases with the proportion of Zn<sub>4</sub>Sb<sub>3</sub>. The present results show the similar trend. Cold-pressed and A-2 possessed primarily Zn<sub>4</sub>Sb<sub>3</sub> phase, thus the Seebeck coefficient was slightly higher than that of C-2 which contained ZnSb phase.

Table 2. Thermoelectric properties of Zn<sub>4</sub>Sb<sub>3</sub> bulk specimens measured at 600 K.

Code	α (μV/K)	$\sigma$ ( $\Omega^{-1}$ cm <sup>-1</sup> )	$\theta$ (W/mK <sup>2</sup> )	κ (W/mK)	ZT	Relative Density (%)	Phases
cold-pressed	207.1	59.5	0.00026	1.14	0.13	81.05	$Zn_4Sb_3 + Zn$
C-2	183.2	185.8	0.00062	1.2	0.31	97.02	$Zn_4Sb_3 + ZnSb$
A-2	215.8	281.1	0.00131	0.982	0.81	97.87	$Zn_4Sb_3$

Table 3 summarizes the ZT values measured at 600 K by various researchers. Itoh's [27] thermoelectric data showed that the phase formation is the key factor affecting the ZT value. Zn<sub>4</sub>Sb<sub>3</sub> exhibits better thermoelectric properties (including electrical conductivity, Seebeck coefficient, and thermal conductivity) compared to those containing ZnSb and Zn phase. Caillat et al. [16] used the specimen's density, heat capacity, and thermal diffusion coefficient to calculate the thermoelectric conductivity of Zn<sub>4</sub>Sb<sub>3</sub> that was about 0.7~0.9 W/mK within 300~650 K. Since limited fluctuation of the thermal conductivities were observed from above Caillat's calculation, Zhu [17] and Ur [32] separately referred to Caillat's data to estimate the ZT values of their Zn<sub>4</sub>Sb<sub>3</sub> specimens prepared by either vacuum melting or hot pressing method. Zhu's result indicated that, due to the large number of cracks caused by quenching after melting, the electrical conductivity and the ZT value are too low. Ur used hot pressing to prepare  $Zn_4Sb_3$  bulk materials. Similar Seebeck coefficient and electrical conductivity were noticed when compared to those of A-2 specimen investigated in the present study. A high ZT value of 1.2, however, was obtained and this was attributed mainly to low thermal conductivity estimated by Ur. A similar behavior was also reported by Ueno [25]. On the other hand, Cui et al. [33,34] introduced Cu and Al pure elements into Zn-Sb system expecting that doping these elements could induce lattice distortions and lower the thermal conductivity. Their results showed that, in contrast to the expectation that Cu can completely substituted some of Zn or Sb atoms, the formation of  $Cu_2Sb$  phase was observed and increased the thermal conductivity. Its Seebeck coefficient, however, was almost twice that of  $Zn_4Sb_3$ . It has been reported that the Seebeck coefficient is primarily affected by the scatter factor and carrier concentration. The addition of Cu makes the structure more complicate, thus increasing the scatter factor and carrier concentration, leading to the final ZT value being slightly higher than that of  $Zn_4Sb_3$  phase. In terms of doping Al element, the Seebeck coefficient shows a similar trend as that of doping Cu. The thermal conductivity is also lower than that of  $Zn_4Sb_3$  as expected by Cui et al. Ruan et al. [35] reported that for  $Zn_4Sb_3$  coated with a layer of SiO<sub>2</sub> film, the results showed that the coating does not induce phase transformation, but  $SiO_2$  film can effectively reduce thermal conductivity and increase the *ZT* value.

Preparation Methods *	κ (W/mK)	ZT	Relative Density (%)	Phases	References	
	0.7	0.24	>95	ZnSb + Zn	Itoh [27]	
MA→HT (723 K)	0.45	1.0	>95	$Zn_4Sb_3$		
Melting $\stackrel{\text{crushing}}{\rightarrow}$ HP $\rightarrow$ HT	0.7	1.0	96–98	$Zn_4Sb_3$	Caillat [16]	
Vacuum melting	0.7 <sup>a</sup>	0.32	-	$Zn_4Sb_3$	Zhu [17]	
HP	0.7 <sup>a</sup>	1.2	98.5	$Zn_4Sb_3$	Ur [32]	
HP	0.83	0.9	99.6	$Zn_4Sb_3$	Ueno [23]	
$Melting {\rightarrow} MA {\rightarrow} HT$	1.0	0.61	-	$Zn_4Sb_3 + ZnSb + Cu_2Sb + Zn$	Cui [33]	
	0.9	0.47	-	$Zn_4Sb_3$		
Melting $\rightarrow$ MA $\rightarrow$ HT	0.62	0.5	-	$Zn_4Sb_3 + ZnSb + AlSb$	Cui [34]	
Melting to MA, the ingot were	0.6	0.7	-	$Zn_4Sb_3 + SiO_2$	Ruan [35]	
coated by SiO2, then HT	0.84	0.56	-	$Zn_4Sb_3$	Kuan [55]	

**Table 3.** Thermoelectric properties at 600 K for Zn<sub>4</sub>Sb<sub>3</sub> bulk specimens prepared by different methods.

\* HP: hot pressing, HT: heat treatment, MA: mechanical alloying. <sup>a</sup> Denotes that  $\kappa$  was estimated from the graph of thermal conductivity as a function of temperature in [4].

# 4. Conclusions

- 1. The formation of complete Zn<sub>4</sub>Sb<sub>3</sub> compound phase by mechanical alloying of pure zinc and antimony elemental powders with Zn<sub>4</sub>Sb<sub>3</sub> composition is unsuccessful due to the partial volatility of the zinc during milling process.
- 2. A nearly single  $Zn_4Sb_3$  compound phase can be obtained in mechanically alloyed  $\beta$ - $Zn_4Sb_3$  alloy powder with superfluous 0.6 at. % of Zn.
- 3. The  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase was found to be the main phase in vacuum-sintered specimens after sintering around 373–473 K. As the sintering temperature increased to 573 K, ZnSb phase gradually emerges and the amount of  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase gradually decreases. The evaporation of Zn during high-temperature sintering at 673 K can cause the complete disappearance of  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase, leading to the formation of an Sb and ZnSb equilibrium phase.
- 4. Under an applied pressure of 0.98 GPa at 473 K for a duration of 30 min,  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> powder can be vacuum hot pressed into a single  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> bulk with a density of 97.87%. Raising the applied pressure, duration, and temperature can moderately increase the relative density of the hot pressed bulk materials. However, excessive hot pressing temperature will reduce the proportion of the  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase.
- 5. The  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> bulk exhibits p-type semiconducting properties. As the proportion of Zn<sub>4</sub>Sb<sub>3</sub> increases, the Seebeck coefficient increases but the electrical conductivity decreases. The bulk specimen with single  $\beta$ -Zn<sub>4</sub>Sb<sub>3</sub> phase exhibits the best thermoelectric properties with the power factor and ZT value is  $1.31 \times 10^{-3}$  W/mK<sup>2</sup> and 0.81, respectively.

Author Contributions: P.-H.L. carried out the sample preparation and data analysis. P.-Y.L. designed the experimental procedure and prepared the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

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