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Unsteady Flow Numerical Simulations on Internal Energy Dissipation for a Low-Head Centrifugal Pump at Part-Load Operating Conditions

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Abstract: Dredge pumps are usually operated at part-load conditions, in which the low-solidity centrifugal impeller could experience large internal energy dissipation, related to flow separation and vortices. In this study, SST $k-\omega$ and SAS-SST turbulence models were used, in steady and unsteady simulations, for a low-head centrifugal pump with a three-bladed impeller. The main focus of the present work was to investigate the internal energy dissipation in rotating an impeller at part-load operating conditions, related to flow separation and stall. The unsteady nature of these operating conditions was investigated. Performance experiments and transient wall pressure measurements were conducted for validation. A methodology for internal energy dissipation analysis has been proposed; and the unsteady pressure fluctuations were analyzed in the rotating impeller. The internal power losses in the volute and the impeller were mostly found in the centrifugal pump. The rotating stall phenomenon occurred with flow separation and detachment at the part-load operating condition, leading to a dissipation of the internal energy in the impeller. The rotating impeller experienced pressure fluctuations with low frequencies, at part-load operating conditions, while in the design operating condition only experienced rotating frequency.

Keywords: centrifugal pump; internal energy dissipation; vortex flow; rotating stall

1. Introduction

Low-head centrifugal pumps are widely used in small-scale dredging equipment, for delivering slurry. For the slurry transportation, the centrifugal impellers usually feature three to six blades with a large expansion ratio of the flow passages. Most studies on slurry pumps were conducted on pumps with four to six impeller blades [1]. The asymmetric impeller structure with fewer blades had an important influence on the performance and pressure fluctuation of the pumps. For single-bladed sewage pump, Nishi et al. [2] performed numerical simulations and experiments and detected the asymmetric pressure and velocity distribution. Pei et al. [3] investigated the uneven distribution of pressure fluctuation intensity in the single-bladed impeller and volute, using the CFD method. Melzer et al. [4] studied the transient pressure in the volute, numerically and experimentally. The pressure indicated a significant periodicity with the rotation of the impeller. In regards to the three-bladed dredge pumps, current research has mainly focused on the wear characteristics of solid and liquid flow [5,6]. Therefore, it is still necessary to investigate the performance and energy loss of dredge pumps, for geometry and operating parameter modifications in the design and optimization process.

The energy loss in the centrifugal pump could be divided into flow dissipation, disk friction, and discharge leakage loss. Kara Omar et al. [7] calculated the losses through empirical and semi-empirical models, and verified them with experimental results. El-Naggar [8] conducted an experimental one-dimensional flow analysis and predicted the pump performance in a dimensionless form. Klas et al. [9] performed simulations on a centrifugal pump and investigated the energy loss in different flow components, to detect the influence of the component geometry. These studies focused on the whole energy transformation in flow components, without a detailed loss analysis.

The inner flow characteristic was investigated as the energy loss reasons for centrifugal pumps. Posa et al. [10] investigated the streamline distribution on the impeller blade surface and found that a stall phenomenon developed near the impeller shroud. Zhang et al. [11] applied velocity vector distribution to detect the flow pattern near the volute tongue, and to discuss its effects on the efficiency fluctuation of a centrifugal pump. Barrio et al. [12] detected a counter-rotating vortex near the interface between the impeller and the volute, through velocity distribution. Pacot et al. [13] used the pressure distribution to explore the stall propagation mechanism. Asim et al. [14] applied the Q -criterion to illustrate that a secondary flow generated near the volute tongue, with an impact on the pump head. Miorini et al. [15] and Zhou et al. [16] adopted a vorticity study to investigate tip leakage flow and rotating stall, respectively, to describe the development of these unsteady flow phenomena and to prove their effects on pump performance. These methods are able to make apparent specific flow structures inside the centrifugal pump, and could assist the design and optimization of centrifugal pumps [17–19].

The quantity of energy loss related to these particular flow structures, needs to be investigated in details, at different operating conditions. Zheng et al. [20] applied an energy gradient function to describe the energy change rate, along streamlines, and argued that this function represented the turbulence intensity. More researchers were concentrated on the specific turbulent kinetic energy. Keller et al. [21] proposed a method of normalized turbulent kinetic energy, and argued that a high value of normalized turbulent kinetic energy corresponded to the flow detachment. Additionally, turbulent kinetic energy was used to make apparent flow separation [22], reversed flow [23] and impeller wake [24] inside the centrifugal pumps, and was linked directly to the energy loss [25]. Meanwhile, the reduction of specific turbulent kinetic energy has been proposed as a corroborative evidence to prove that the optimized pumps featured a better performance [26,27] and [28]. In fact, the production of specific turbulent kinetic energy has been linked to the energy transfer from the mean flow to the turbulent flow. However, the quantity of specific turbulent kinetic energy cannot directly represent the energy loss [29,30]. Therefore, an accurate method for the quantification of energy dissipation in centrifugal pumps, still needs to be investigated.

The specific speed N_{QE} and the number of blades of the studied centrifugal pumps from the above-mentioned studies are summarized in Table 1. The discharge factor, specific energy factor and specific speed for the design operating condition, are defined by Equations (1)–(3).

$$Q_{nD}^0 = Q_0 n^{-1} D^{-3} \quad (1)$$

$$E_{nD}^0 = (gH_0) n^{-2} D^{-2} \quad (2)$$

$$N_{QE} = (Q_{nD}^0)^{0.5} / (E_{nD}^0)^{0.75} \quad (3)$$

Pei et al. [3] studied a single-bladed pump with a high specific speed. Additionally, References [8,25] investigated the low-solidity centrifugal pump, however, both pumps had a low specific speed. In this study, a high-specific-speed dredge pump with a low-solidity centrifugal impeller was used. In the impeller, the blades were curved with a large ratio between the outlet and the inlet flow section. Low solidity pumps experience a complex unsteady flow phenomena inside the impeller at off-design operating conditions [31,32], such as, flow separation, rotating stall, and secondary flow.

These phenomena have a negative impact on the efficiency and could generate pressure fluctuations and vibrations.

Table 1. Specific speed and number of blades of the study cases in the cited literature.

References	N_{QE}	Number of Blades	References	N_{QE}	Number of Blades
3	0.17	1	21	0.09	6
8	0.09	4	22	0.20	5
9	0.03	7	23	0.02	7
10	0.17	6	25	0.04	4
11	0.13	5	26	0.06	5
12	0.07	7	27	0.08	7
16	0.08	6	28	0.04	6
18	0.07	6	-	-	-

The internal energy dissipation at part-load operating conditions was the focus of this study. The causes for internal energy dissipation at part-load operating conditions were analyzed for their flow separation and stall phenomena in the three-bladed centrifugal impeller. Pressure fluctuation time and dominant frequency were further investigated to establish what comprised the unsteady characteristics of the pump.

This paper has been structured as follows: in Section 2, the case study has been presented; in Section 3, the numerical simulation setup, the experimental setup, as well as the internal energy dissipation methodology have been described; in Section 4, numerical simulating results have been validated with the help of the available experimental data, analysis on internal power loss in the simulating domains have been performed, and the results of the internal energy dissipation and pressure fluctuation have been presented; in Section 5, the analysis on numerical simulating results have been expressed; and finally, in Section 6, the conclusions of the present work have been provided.

2. Case Study

The studied case was an industrial pump and the impeller outlet diameter was 310 mm. The discharge and specific energy factors at the design operating conditions (Q_{nD}^0 and E_{nD}^0) were 0.16 and 4.15, respectively. The specific speed (N_{QE}) of the pump was 0.14. The assembly drawing and computing domains of the centrifugal pump of the dredge pump are shown in Figure 1. The calculation domains included the suction pipe, the centrifugal impeller, front gap, pump-out vanes, the back gap, and the volute.

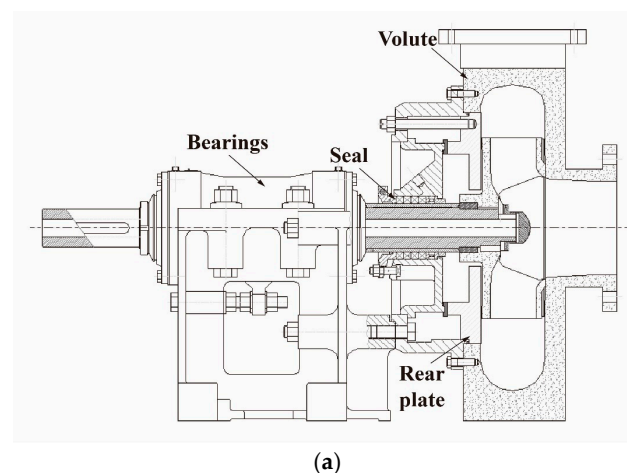


Figure 1. Cont.

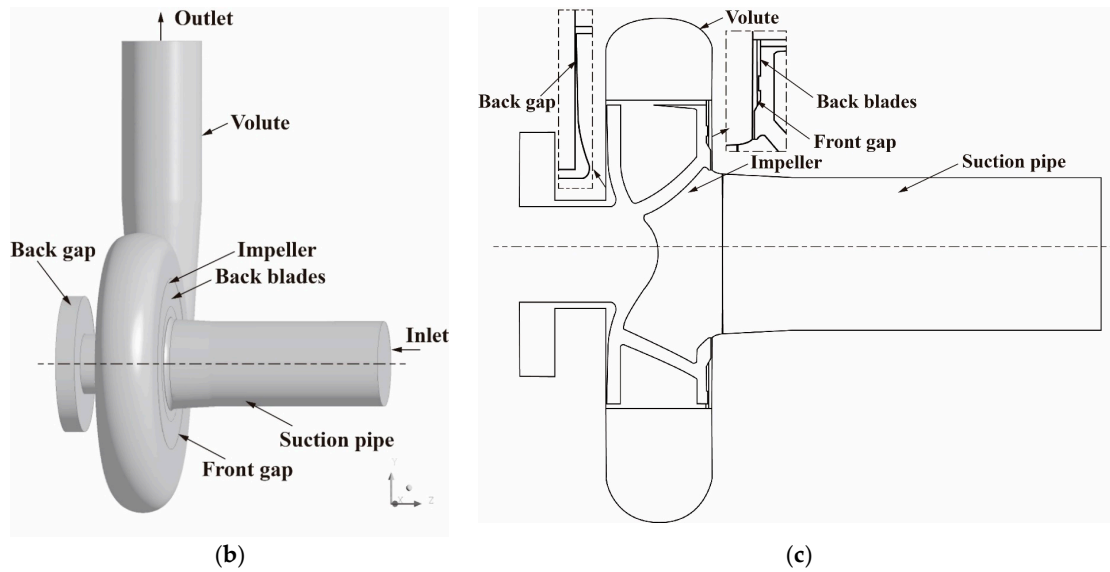


Figure 1. Assembly drawing and computing domains of the centrifugal pump. (a) Cross-sectional assembly drawing of the centrifugal pump; (b) computing domains; and (c) meridional view of the computing domains.

3. Methodology

3.1. Governing Equations and Numerical Setup

The continuity equation:

$$\frac{\partial C_i}{\partial X_i} = 0 \quad (4)$$

The momentum equation:

$$\frac{\partial C_i}{\partial t} + \frac{\partial}{\partial X_j} (C_i C_j) = -\frac{1}{\rho} \frac{\partial p}{\partial X_i} + \frac{1}{\rho} \frac{\partial}{\partial X_j} (2\mu D_{ij} - \rho \overline{c_i c_j}) \quad (5)$$

The specific energy equation:

$$\frac{\partial h_{tot}}{\partial t} - \frac{1}{\rho} \frac{\partial p}{\partial t} + \frac{\partial}{\partial X_j} (C_j h_{tot}) = \frac{\partial}{\partial X_j} \left(\frac{\lambda_t}{\rho} \frac{\partial T}{\partial X_j} - \overline{c_j h} \right) + \frac{1}{\rho} \frac{\partial}{\partial X_j} [C_j (2\mu D_{ij} - \rho \overline{c_i c_j})] \quad (6)$$

In which, C , D_{ij} , h , h_{tot} , p , t , μ , ρ , and λ_t are velocity, strain rate tensor, specific enthalpy, specific total enthalpy, pressure, time, dynamic viscosity, density, and thermal conductivity, respectively. The physical property of water was regarded as a constant in numerical simulations.

The SST turbulence model [33] was used for the steady simulations, in which a switching function was used to combine the k - ω model with the k - ϵ model. The SST turbulence model was widely used in numerical simulations of pumps, with satisfying results [34–36]. The SAS–SST turbulence model [37] was used in the unsteady simulations, which included the von Karman length-scale in the turbulence eddy frequency equation. The SAS–SST model was proved to satisfactorily describe the unsteady flow patterns, especially with the complex flow phenomena at the off-design operating conditions [38–40]. To accommodate the streamline curvature and the rotating feature in the centrifugal impeller, curvature correction [41] was added as an advanced turbulence control [42].

Mesh sensitivity checks were conducted with five different meshes. The influence of the mesh amount on the head and efficiency at the design operating condition is shown in Figure 2.

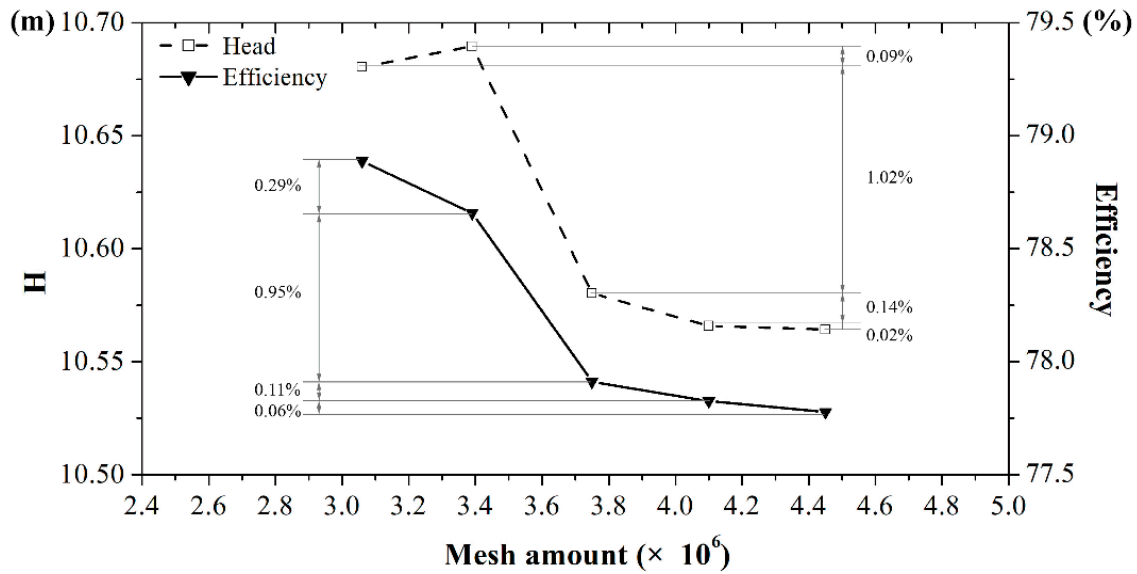


Figure 2. Influence of mesh amount on the head and efficiency.

As the differences in head and efficiency in the last three meshes were less than 1%, the mesh set with 3.75×10^6 elements was utilized in the simulations, considering both the precision and the cost of calculation. The definitions of head H , power P , and efficiency η are as follows:

$$H = \frac{1}{gQ} \int_{A_{out}} \sum \left(\frac{p}{\rho} + \frac{\vec{C}^2}{2} \right) \vec{C} \cdot \vec{n} dA - \frac{1}{gQ} \int_{A_{in}} \sum \left(\frac{p}{\rho} + \frac{\vec{C}^2}{2} \right) \vec{C} \cdot \vec{n} dA \quad (7)$$

$$P = nT_t \quad (8)$$

$$\eta = \frac{\rho g Q H}{P} \quad (9)$$

where Q is the discharge; T_t is the torque; A_{in} and A_{out} represent the inlet and outlet boundary, respectively. All of mesh elements were structural meshes, except for the impeller computing domain. The averaged y^+ value in each domain was less than 130.

The mass flow rate boundary condition was set at the pipe inlet at an initial temperature of 25 °C. The inlet turbulence intensity was set as 5%. The outlet boundary at the volute outlet was set as the static pressure. The domains of the impeller and nine pump-out vanes were set as the rotating parts with the same rotation speed, while others were stationary. The wall boundary was set as smooth wall, no-slip, and adiabatic. The interface between the rotating and stationary domains corresponded to frozen rotor in steady simulations and to transient frozen rotor in unsteady simulations. The steady results were set as the initial flow field of unsteady simulations. The time step in unsteady simulations was 2×10^{-4} s, which was 1/300 of a rotating period.

Pressure signal was recorded in unsteady simulations. Monitor point arrangements in numerical simulations are shown in Table 2. The monitor points in the impeller were distributed at the pressure and suction sides of a flow passage. The cylindrical coordinates of the monitor points are shown in Figure 3.

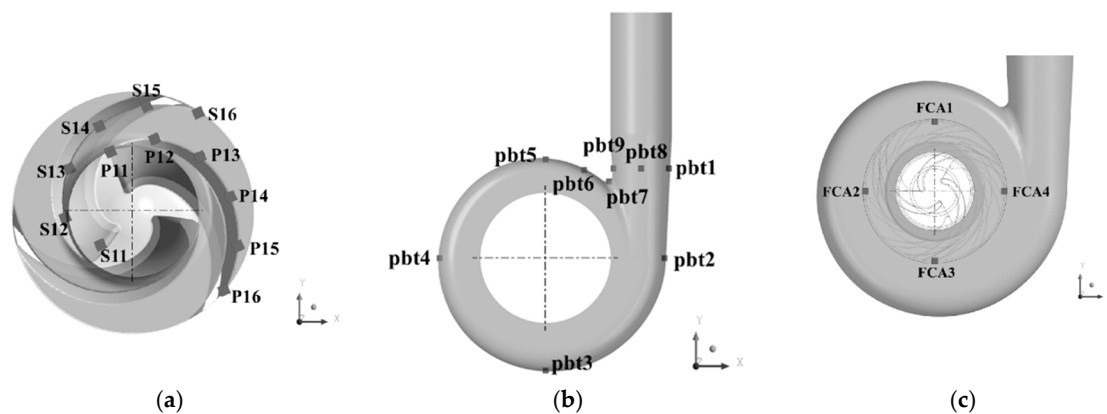


Figure 3. Monitor point arrangements in the numerical simulations. (a) Impeller; (b) volute; and (c) front chamber.

Table 2. Cylindrical coordinates of the monitor points.

Monitor Point	Z (m)	R (m)	θ (°)	Monitor Point	Z (m)	R (m)	θ (°)
S11	0.053	0.060	171.8	pbt1	0.000	0.374	36.1
S12	0.047	0.089	131.7	pbt2	0.000	0.292	0.0
S13	0.035	0.100	92.7	pbt3	0.000	0.277	−90.0
S14	0.035	0.119	58.5	pbt4	0.000	0.260	180.0
S15	0.035	0.137	30.0	pbt5	0.000	0.242	90.0
S16	0.035	0.153	−3.9	pbt6	0.000	0.236	66.3
P11	0.053	0.084	58.2	pbt7	0.000	0.270	52.8
P12	0.037	0.098	20.8	FCA1	0.055	0.155	90.0
P13	0.036	0.112	−13.4	FCA2	0.055	0.155	180.0
P14	0.036	0.127	−44.0	FCA3	0.055	0.155	270.0
P15	0.036	0.142	−71.1	FCA4	0.055	0.155	0.0
P16	0.036	0.154	−93.7	-	-	-	-

3.2. Experimental Setup

The experimental setup for the centrifugal pump is shown in Figure 4. In the test bed, the mass flow rate was measured by a magnetic flowmeter (LDG-500S, Shanghai Guanghua Instrument Co., Ltd., Shanghai, China). The measurement uncertainty of the mass flow rate was $\pm 0.2\%$. The flowmeter was installed between the two tanks, which is not shown in the picture. The torque was measured with a torque meter (JCZL2-500, Powerlink, Instrument Co., Ltd, Changsha, China) and the measurement uncertainty of the torque was $\pm 0.5\%$. The pressure transmitter was V15712-HD1A1D7D (Newsruipu Instrument Co., Ltd, Zhengzhou, China) and the maximum error of the head was 1% of the measurement range. The pressure fluctuation sensor was CGYL-201 (Hefei Dekong Instruments Co., Ltd., Hefei, China) with a sampling frequency 4096 Hz. The monitor point set in the volute and the front gap was the same as that in numerical simulations. The shaft power was calculated by the torque difference between the torque measured by a torque meter and resistance torque from bearings, which was measured when the impeller was not installed on the shaft.

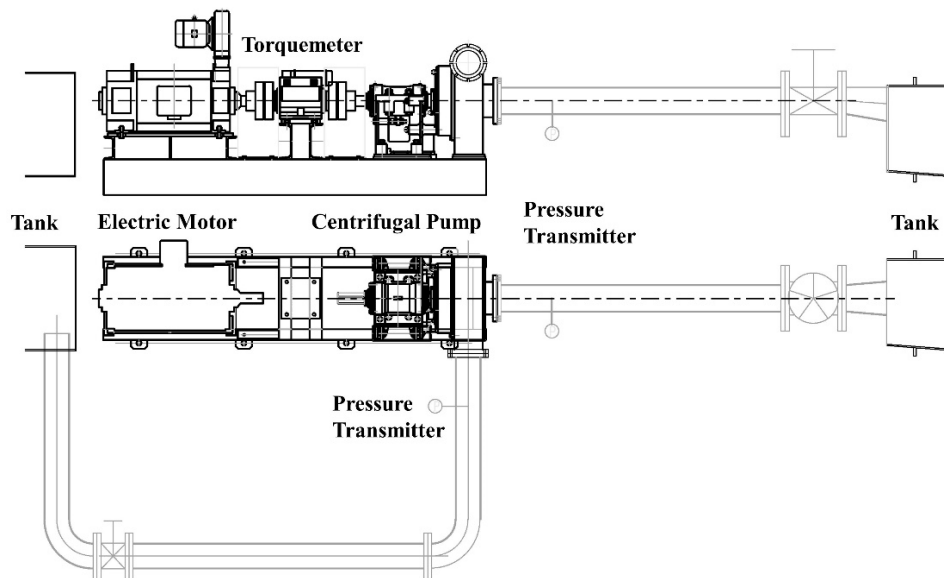


Figure 4. Experimental setup of the centrifugal pump.

3.3. Energy Analysis Method

From the first law of thermodynamics, the total specific energy balance for the pump system yielded Equation (10). The gravitational potential energy change and the thermal radiation were ignored.

$$\frac{D}{Dt} \int_V \rho \left(e + \frac{\vec{C}^2}{2} \right) dV = \int_V \nabla \cdot (P \cdot \vec{C}) dV - \int_V \nabla \cdot \vec{q} dV \quad (10)$$

where e represents the specific internal energy; $\vec{q}$ is the heat flux; and P is the total stress tensor.

$$P = -pI + 2\mu D \quad (11)$$

The local equation of the specific kinetic energy balance for the incompressible fluid could be derived from the momentum balance equation, as:

$$\frac{D}{Dt} \left(\frac{\vec{C}^2}{2} \right) = \frac{1}{\rho} \left[\nabla \cdot (P \cdot \vec{C}) - P : D \right] \quad (12)$$

Substituting Equations (10) and (12), the time change rate of the specific internal energy could be expressed as:

$$\frac{De}{Dt} = \frac{1}{\rho} (P : D) + \left(-\frac{1}{\rho} \nabla \cdot \vec{q} \right) \quad (13)$$

According to the URANS method, time averaging was performed on Equation (13), in which, the time scale was larger than the turbulent time scale, but was much smaller than the time scale of mean flow 37. Equation (13) read as follows:

$$\overline{\frac{De}{Dt}} = \frac{\mu}{\rho} \left[\left(\nabla \vec{C} + \nabla \vec{C}^T \right) : \nabla \vec{C} + \left(\nabla \vec{C} + \nabla \vec{c}^T \right) : \nabla \vec{C} + \overline{\left(\nabla \vec{c} + \nabla \vec{c}^T \right) : \nabla \vec{c}} \right] + \frac{\lambda_t}{\rho T} \left[\Sigma \left(\frac{\partial T}{\partial x_i} \right)^2 + \Sigma \overline{\left(\frac{\partial T'}{\partial x_i} \right)^2} \right] \quad (14)$$

where T is the temperature; and λ_t is the thermal conductivity of the fluid. The items on the right side of Equation (14) describes the viscous dissipation, turbulent production, turbulent dissipation, and dissipation from heat transfer, respectively. Since the turbulent fluctuating flow parameters $\nabla \vec{c}$

and T' could not be obtained directly from the URANS simulations, the internal energy dissipation in the turbulent fluctuating flow needed to be expressed by mean flow components. Expressions and approximations from the previous research, based on the eddy viscosity model [43], were adopted.

Viscous dissipation rate:

$$\Phi = \frac{\mu}{\rho} (\nabla \vec{C} + \nabla \vec{C}^T) : \nabla \vec{C} = \frac{\mu}{\rho} \left[2 \left(\frac{\partial C_i}{\partial X_i} \right)^2 + \left(\frac{\partial C_i}{\partial X_j} + \frac{\partial C_j}{\partial X_i} \right)^2 \right] \quad (15)$$

Turbulent production rate:

$$\Pi = \frac{\mu_t}{\rho} (\nabla \vec{c} + \nabla \vec{c}^T) : \nabla \vec{C} = \frac{\mu_t}{\rho} (\nabla \vec{C} + \nabla \vec{C}^T) : \nabla \vec{C} = \frac{\mu_t}{\rho} \left[2 \left(\frac{\partial C_i}{\partial X_i} \right)^2 + \left(\frac{\partial C_i}{\partial X_j} + \frac{\partial C_j}{\partial X_i} \right)^2 \right] \quad (16)$$

Turbulent dissipation rate:

$$\Theta = \frac{\mu}{\rho} \overline{(\nabla \vec{c} + \nabla \vec{c}^T) : \nabla \vec{c}} = \varepsilon \quad (17)$$

Dissipation rate from heat transfer:

$$\Gamma = \frac{\lambda_t}{\rho T} \left[\sum \left(\frac{\partial T}{\partial X_i} \right)^2 + \sum \overline{\left(\frac{\partial T'}{\partial X_i} \right)^2} \right] = \frac{\lambda_{eff}}{\rho T} \left(\frac{\partial T}{\partial X_i} \right)^2 \quad (18)$$

where μ_t is the eddy viscosity; ε is the turbulence dissipation rate; and λ_{eff} is the effective thermal conductivity.

The internal energy dissipation rate was expressed as follows:

$$\rho \frac{\overline{De}}{Dt} = \Phi + \Pi + \Theta + \Gamma = (\mu + \mu_t) \left[2 \left(\frac{\partial C_i}{\partial X_i} \right)^2 + \left(\frac{\partial C_i}{\partial X_j} + \frac{\partial C_j}{\partial X_i} \right)^2 \right] + \rho \varepsilon + \frac{\lambda_{eff}}{T} \left(\frac{\partial T}{\partial X_i} \right)^2 \quad (19)$$

The distribution of the dissipated internal energy could explain the local energy transformation and could be related to the flow structures. The volumetric integration on the left hand of Equation (19), represents the internal power loss in the whole domain.

Since the internal energy dissipation near the wall could not be calculated accurately from the above-mentioned method, when y^+ value was larger than 50 [44], an approximation for the internal power loss near the wall, was defined as Equation (20).

$$P_{loss,A} = \int_A \sum \tau_i C_i dA \quad (20)$$

where τ_i is the wall shear stress vector component. The internal power loss could be expressed as:

$$P_{loss,i} = \int_V \rho \frac{\overline{De}}{Dt} dV + \int_A \sum \tau_i C_i dA \quad (21)$$

For the purpose of comparing the internal power loss with the hydraulic power loss, the definition of the hydraulic power loss is described as Equation (22).

$$P_{loss,h} = P(1 - \eta) \quad (22)$$

4. Results

4.1. Validation of Numerical Simulating Results

Since the centrifugal impeller was composed of three blades, steady simulations were conducted at three different clocking positions, between the impeller and the volute. The influence of the clocking positions between the three-bladed impeller and the volute on the head and power, varied at different operating conditions, see Figure 5. The result was consistent with the previous research on centrifugal pump [39]. The averaged results were regarded as the final results in the steady simulations. A comparison of the head and efficiency between the steady numerical simulations and the experimental results, are shown in Figure 6. There was a good quantitative agreement for the operating conditions near the design operating condition, while the difference was larger at the part and overload conditions. The maximum relative errors were less than 5% for the 13 operating conditions.

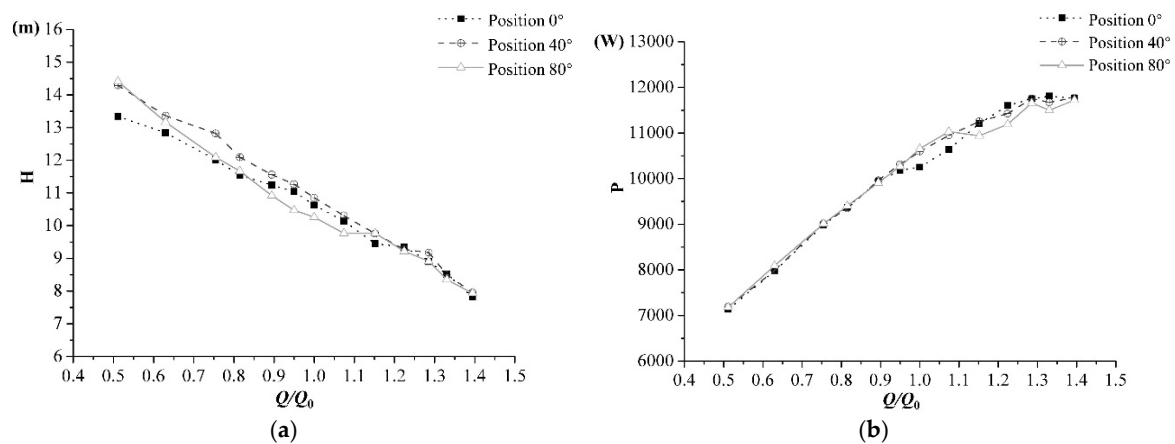


Figure 5. The influence of clocking positions on the head and power at different operating conditions—(a) head; and (b) power.

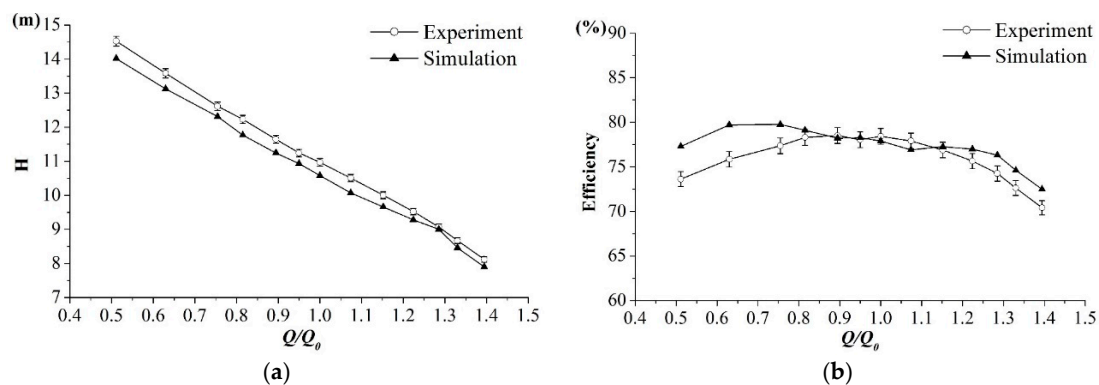


Figure 6. Comparison of the head and efficiency, between the numerical simulations and experimental results—(a) head; and (b) efficiency.

The numerical simulation and experimental results of the pressure signal in the stationary volute and front gap were compared to verify the reliability of the unsteady simulations. The fast Fourier transform (FFT) method was applied to analyze the pressure signals. The pressure normalization c_p was defined as Equation (23), in which the U_2 is the rotating velocity at the impeller outlet [45]. Both, the time history and frequency domain of the monitor points pbt5 and FCA1, from the numerical and experimental results, at $1.0 \times Q_0$ and $0.8 \times Q_0$ operating conditions, are shown in Figure 7, where n represents the rotating frequency. In Figure 7a,c,e,g, it can be seen that there were three oscillations during one impeller revolution. In Figure 7b,d,f,h, the dominant frequency was the blade

passing frequency as $3 \times n$. The pressure analysis from unsteady numerical simulation results can basically describe the periodical change of pressure fluctuations, while there exists differences in the pressure amplitudes.

$$c_p = \frac{(p - \bar{p})}{0.5\rho U_2^2} \quad (23)$$

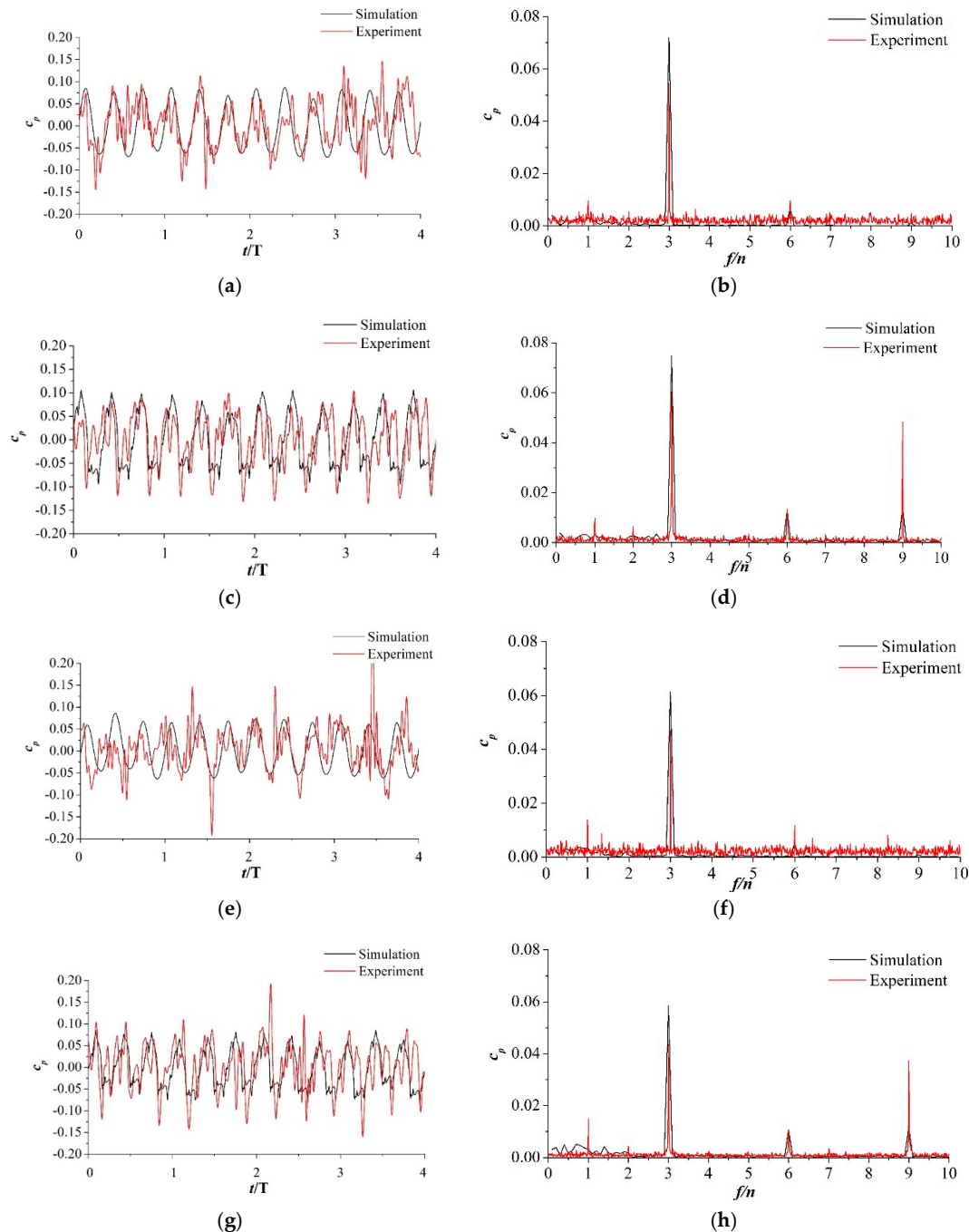


Figure 7. Time history and frequency domain of the monitor points pbt5 and FCA1 from the numerical and experimental results (a) Time history (pbt5, $1.0 \times Q_0$); (b) frequency domain (pbt5, $1.0 \times Q_0$); (c) time history (FCA1, $1.0 \times Q_0$); (d) frequency domain (FCA1, $1.0 \times Q_0$); (e) time history (pbt5, $0.8 \times Q_0$); (f) frequency domain (pbt5, $0.8 \times Q_0$); (g) time history (FCA1, $0.8 \times Q_0$); and (h) frequency domain (FCA1, $0.8 \times Q_0$).

4.2. Internal Power Loss

The influence of the discharge on both the internal and hydraulic power losses, see Equations (21) and (22), are shown in Figure 8. With an increase in discharge, both, internal and hydraulic power losses increased. The internal power loss was in accordance with the hydraulic power loss. Near the design point, the difference between the internal power loss and the hydraulic power loss was small, while the difference was larger at the part and overload operating conditions. In general, the methodology mentioned above could be used to describe the internal energy dissipation inside the centrifugal pump.

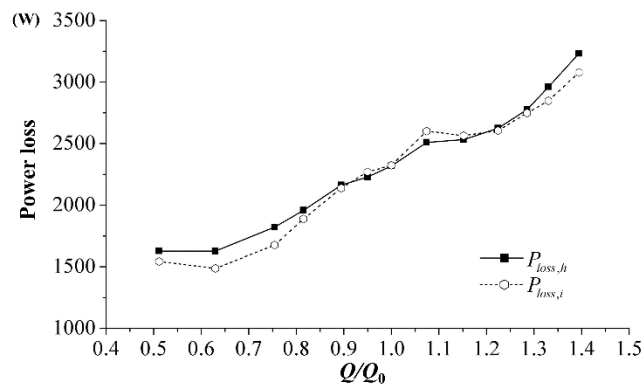


Figure 8. Influence of the discharge on both the internal and hydraulic power losses.

Influence of the discharge on the internal power loss, in each flow component for the centrifugal pump is shown in Figure 9. The pump-out vanes and the impeller were regarded as a whole flow component. The internal power losses inside the volute and the impeller accounted for the most power loss in the pump, at all operating conditions, and increased with discharge. The internal power losses inside the other flow components were similar at different operating conditions.

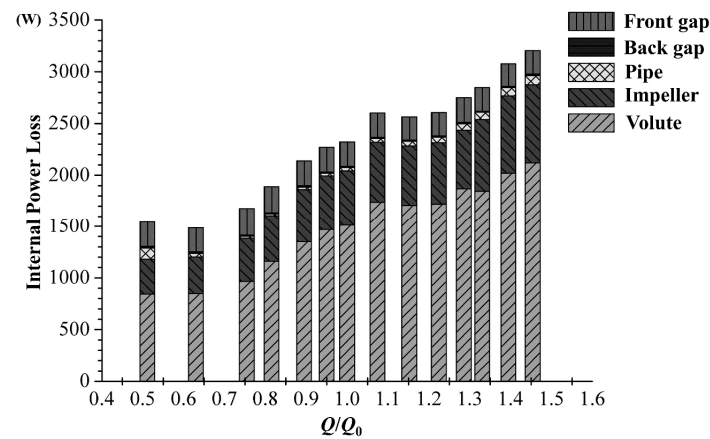


Figure 9. Influence of the discharge on the internal power loss in each component for the centrifugal pump.

4.3. Local Internal Energy Dissipation in the Impeller

Relative flow velocity vectors on the cross-section A, near the impeller shroud ($Z = 0.03$ m) in the impeller, at the design and part-load operating conditions are shown in Figure 10. At the design operating condition, see Figure 10b, the flow in the impeller was smooth, without obvious flow separation or vortices. With a reduction in discharge, the vortex flow developed near the blade suction side. At $0.9 \times Q_0$ operating condition, see Figure 10c, the vortex with low velocity was observed near the trailing edge of the blade suction side, in one flow passage. At $0.8 \times Q_0$ and $0.7 \times Q_0$

operating conditions, see Figure 10d,e, the vortex flow existed in two flow passages. At $0.6 \times Q_0$ and $0.5 \times Q_0$ operating conditions, see Figure 10f,g, the low-velocity vortices were apparent in all the three flow passages.

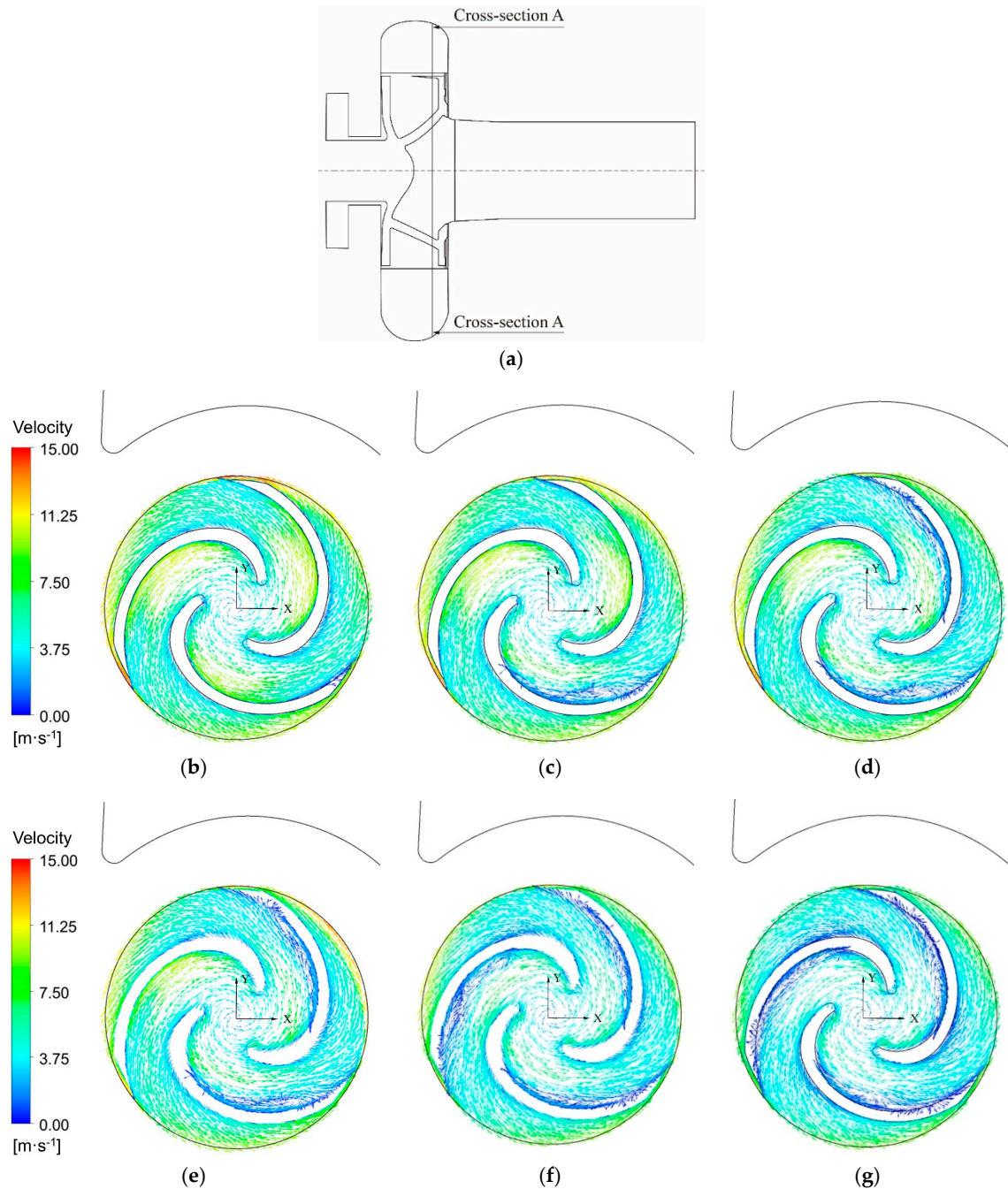


Figure 10. Relative flow velocity vector on the cross-section A at the design and part-load operating conditions, (a) cross-section A; (b) $1.0 \times Q_0$; (c) $0.9 \times Q_0$; (d) $0.8 \times Q_0$; (e) $0.7 \times Q_0$; (f) $0.6 \times Q_0$; and (g) $0.5 \times Q_0$.

Unsteady results at the $1.0 \times Q_0$, $0.8 \times Q_0$, and $0.5 \times Q_0$ operating conditions were applied to analyze the variation of internal energy dissipation rate distribution, in the rotating impeller. The distribution of internal energy dissipation rate on the cross-section A at six different instances of the $0.8 \times Q_0$ operating condition, is shown in Figure 11. In each flow passage, the internal energy dissipation rate near the blade suction side was larger than that near the pressure side. The internal

energy dissipation rate was the most significant near the blade suction side of Blade 2. The large internal energy dissipation region existed with an invariable relative position during the rotating period. However, the strength of the internal energy dissipation rate changed with the impeller rotation. The region with large internal energy dissipation rate also existed near the outlet of impeller, especially at the trailing edge of three impeller blades, as shown with the triangle marked in Figure 11b,d,f.

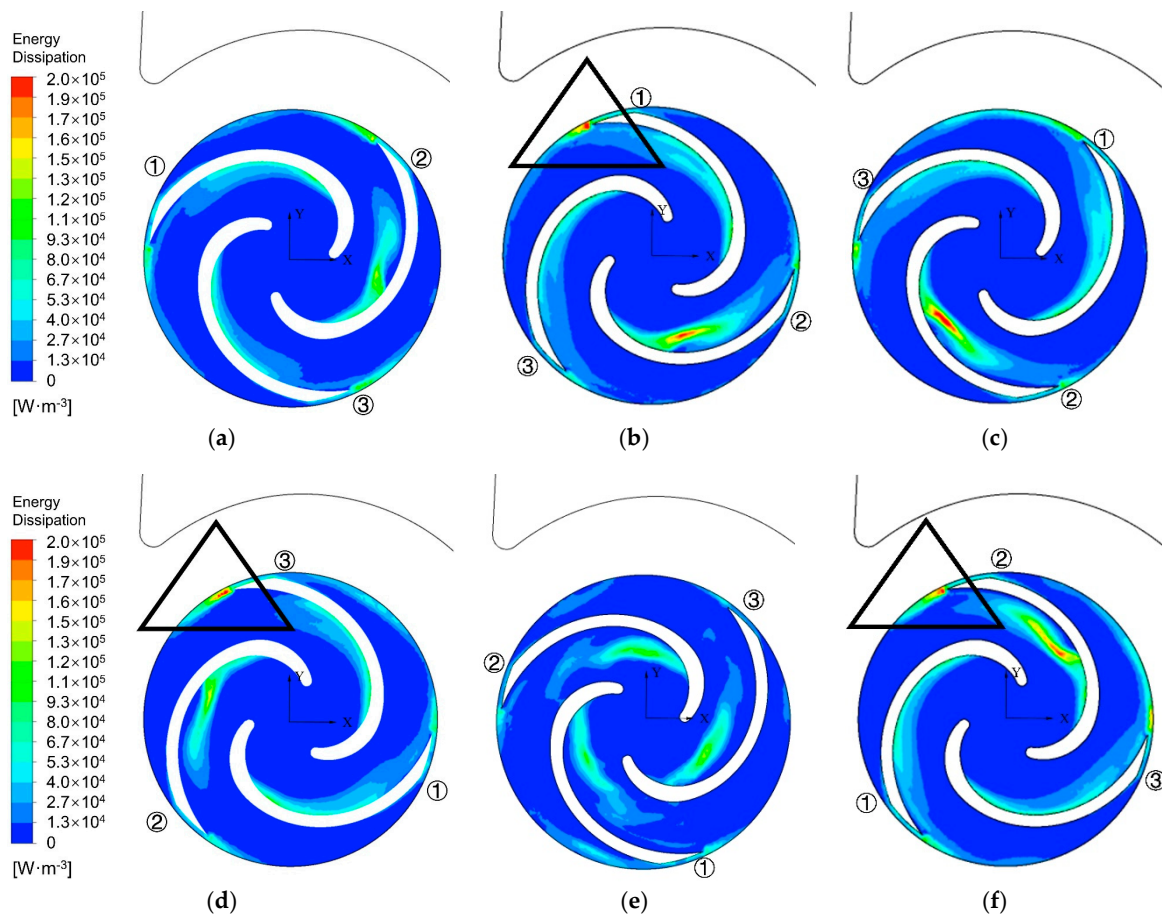


Figure 11. Internal energy dissipation rate on the cross-section A at six different moments at $0.8 \times Q_0$ operating condition (a) $t = 0.84$ s (0°); (b) $t = 0.85$ s (60°); (c) $t = 0.86$ s (120°); (d) $t = 0.87$ s (180°); (e) $t = 0.88$ s (240°); and (f) $t = 0.89$ s (300°).

The internal energy dissipation rate on the cross-section A at six different moments at $0.5 \times Q_0$ operating condition is shown in Figure 12. In all flow passages, there were regions with large internal energy dissipation rate. The strength of the internal energy dissipation rate in each passage, varied with time. It is similar to the flow characteristic at the $0.8 \times Q_0$ operating condition. Taking the flow structure between Blade 1 and Blade 3 as an example, when the impeller rotated from 0° to 60° , the internal energy dissipation strengthened. At the relative position of 120° , the flow separation and detachment developed with a large internal energy dissipation. With the impeller rotating, the detached flow propagated downstream to the trailing edge of the blade suction side and the internal energy dissipation rate decreased. Vortex flow with high internal energy dissipation rate occupied a large area of the flow passage, causing flow blockage. Compared with the $0.8 \times Q_0$ operating condition, the internal energy dissipation near the impeller outlet was not significant.

When analyzing the contour of each source term in the internal energy dissipation rate, it was found that the distribution of each term was similar. The turbulent production and turbulent dissipation were the main causes for internal energy dissipation, in the centrifugal pump. It was in accordance with the characteristic of a high Reynold number flow [46].

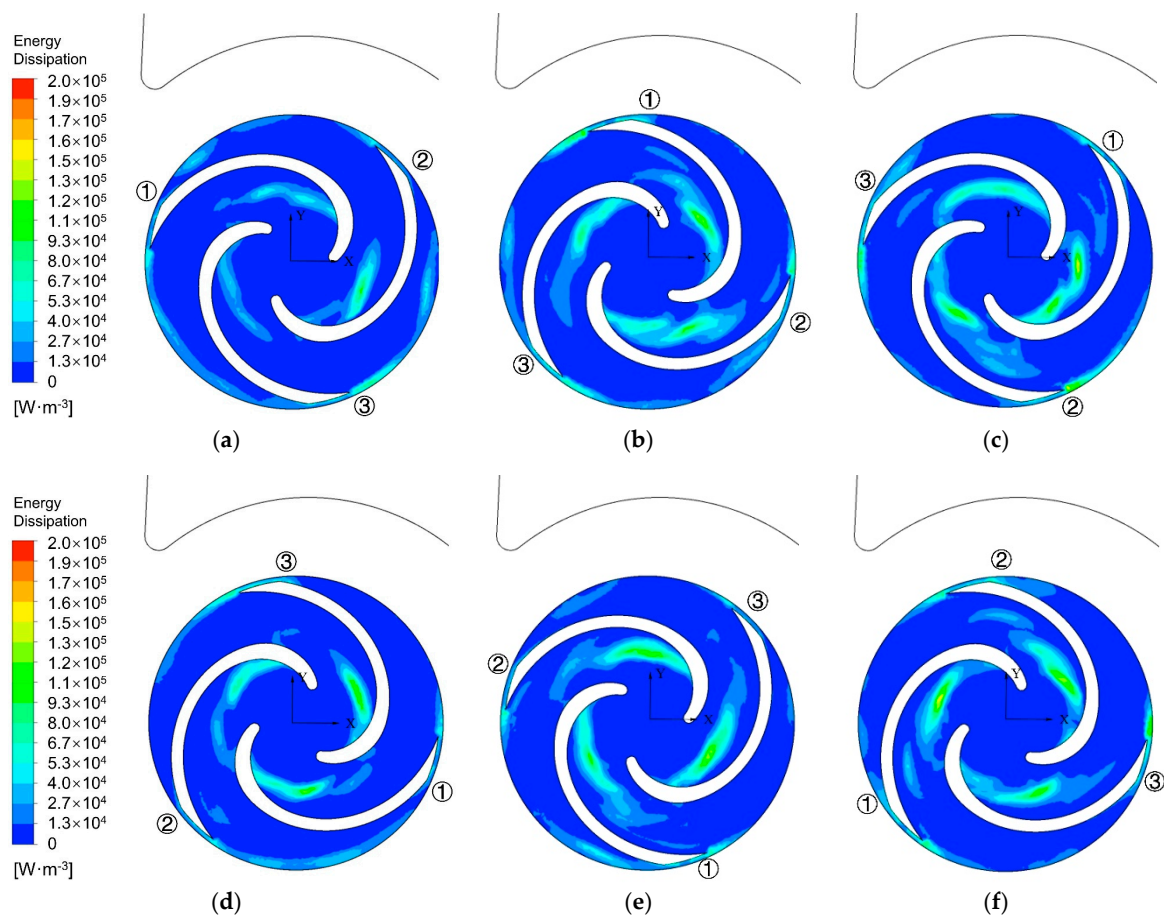


Figure 12. Internal energy dissipation rate on the cross-section A at six different moments at $0.5 \times Q_0$ operating condition. (a) $t = 0.84$ s (0°); (b) $t = 0.85$ s (60°); (c) $t = 0.86$ s (120°); (d) $t = 0.87$ s (180°); (e) $t = 0.88$ s (240°); (f) $t = 0.89$ s (300°).

4.4. Pressure Fluctuations in the Impeller

The pressure fluctuation in the rotating impeller was analyzed by the FFT method. The characteristic frequencies and amplitudes of pressure fluctuations at $1.0 \times Q_0$, $0.8 \times Q_0$, and $0.5 \times Q_0$ operating conditions are listed in Table 3.

Table 3. Characteristic frequencies and amplitudes of pressure fluctuations at $1.0 \times Q_0$, $0.8 \times Q_0$, and $0.5 \times Q_0$ operating conditions.

Discharge	Position	Characteristic Frequency	Maximum $ c_p $	Monitor Point with Maximum $ c_p $
$1.0 \times Q_0$	Pressure Side	n	0.079	P15
$1.0 \times Q_0$	Suction Side	n	0.065	S16
$0.8 \times Q_0$	Pressure Side	n	0.050	P15
$0.8 \times Q_0$	Pressure Side	$0.5 \times n$	0.011	P16
$0.8 \times Q_0$	Suction Side	n	0.043	S16
$0.8 \times Q_0$	Suction Side	$0.5 \times n$	0.008	S14
$0.5 \times Q_0$	Pressure Side	$3 \times n$	0.030	P11
$0.5 \times Q_0$	Pressure Side	$0.7 \times n$	0.012	P11
$0.5 \times Q_0$	Suction Side	$3 \times n$	0.034	S11
$0.5 \times Q_0$	Suction Side	$0.7 \times n$	0.011	S13

The dominant frequency in the rotating impeller was n under $1.0 \times Q_0$ and $0.8 \times Q_0$ operating conditions, and the amplitudes decreased with a smaller discharge. In addition, a low-frequency like $0.5 \times n$ was found with a relatively small amplitude at the $0.8 \times Q_0$ operating condition.

At $0.5 \times Q_0$ operating condition, the dominant frequency was $3 \times n$ with the maximum amplitudes at the blade leading edge. The low-frequency component was more significant with a frequency of $0.7 \times n$. Its amplitude reached 40% of the amplitude of $3 \times n$, at monitor point P11 and was 38% of the amplitude of $3 \times n$ at the monitor point S13.

The inverse fast Fourier transform (IFFT) method was applied to decompose the pressure signal of the monitor points P11 and S13 at the $0.5 \times Q_0$ operating condition. Time history of the pressure signal and pressure components of frequencies, like $3 \times n$ and $0.7 \times n$, at $0.5 \times Q_0$ operating condition is shown in Figure 13. It was found that the pressure signal was mainly affected by the two pressure components of $3 \times n$ and $0.7 \times n$. The pressure signal in monitor point P11 was more complex than the superposition of the two waves.

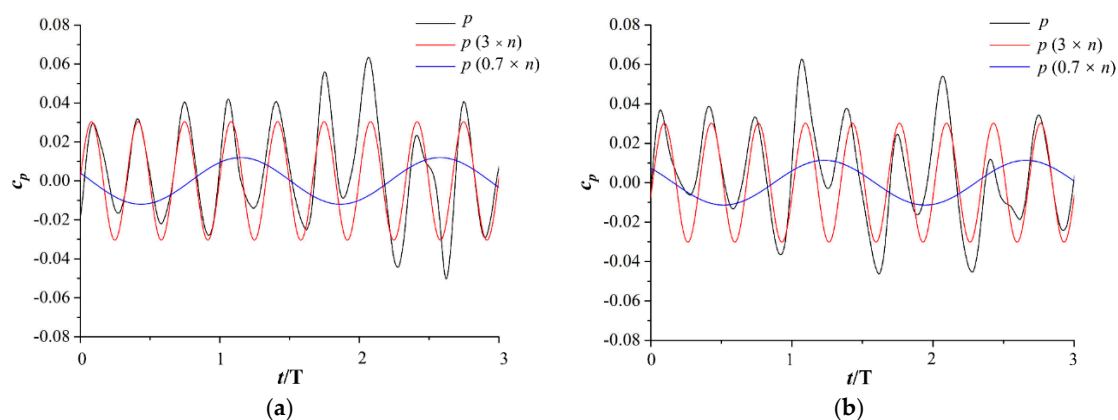


Figure 13. Time history of pressure signal and pressure components of frequencies as $3 \times n$ and $0.7 \times n$ at $0.5 \times Q_0$ operating condition. (a) Monitor point P11; and (b) monitor Point S13.

5. Discussion

In numerical simulations, the disk friction loss between the impeller hub and the back gap was not taken into account, since the back gap was regarded as a stationary flow domain. The wall friction loss and the discharge leaked through the seal were not considered. These factors led to the difference between the numerical and experimental results on performance. In experiments, the recording time of pressure signal was longer and the sampling time was shorter than that in numerical simulations, which had an impact on the difference of unsteady pressure fluctuations, between the numerical and experimental data.

When analyzing the integral internal energy dissipation, the flow irregularity at the off-design operating conditions had an influence on the error between the internal and hydraulic power losses, since the approximation was applied in the near-wall region. The internal energy dissipation inside the volute accounted for the most among the flow components. The section area in the volute of the centrifugal dredge pump was designed to be larger than that of other centrifugal pumps, to reduce the impact and friction from the slurry to the volute wall. There could be non-uniform flow structures inside the volute, causing internal energy dissipation.

With the discharge decreasing, the angle between the relative velocity and tangential velocity decreased and the angle of attack increased at the impeller inlet. The impeller experienced flow separation, near the blade suction. The vortices were more evident at the part-load operating conditions, with smaller discharge.

At $0.8 \times Q_0$ operating condition, the internal energy dissipation rate of the vortex inside one flow passage changed with the rotating impeller. The vortex flow was related to the internal energy dissipation in the impeller and had an unsteady feature. This flow structure brought about a pressure

fluctuation with a low-frequency, which is 50% of the rotating frequency. The amplitude was not obvious because the separating vortex flow only existed in one impeller passage and occupied a small part of the passage.

In addition, the internal energy dissipation was obvious near the trailing edge of the impeller blades. It was due to the rotor–stator interaction between the impeller and the volute. The wake flow of the rotating blades impacted the flow field downstream and led to an energy loss involving the viscous effect [47,48]. The rotor–stator interaction caused a pressure fluctuation with the rotating frequency n and the maximum amplitudes were found at the blade trailing edge.

At $0.5 \times Q_0$ operating condition, the vortex detachment and propagation generated the internal energy dissipation and enhanced the unsteady characteristic. The periodical change of internal energy dissipation strength showed that the vortex structure was a form of rotating stall. The periodical separation and detachment made the low-frequency components more complicated, with higher amplitudes. The characteristic frequency was 70% of the rotating frequency, which corresponded with the feature of the rotating stall phenomenon, inside the impeller [49–52].

The stall blocked the impeller passage and reduced the flow interference downstream. The internal energy dissipation near the blade trailing edge was not evident. The rotating frequency was not significant in the pressure fluctuation spectra. The dominant frequency was the blade passing frequency, with the maximum amplitudes at the blade leading edge, which was caused by the rotor–stator interaction between the suction pipe and the impeller. Flow pattern on the midsection of the suction pipe at $0.5 \times Q_0$ operating condition is shown in Figure 14. The reverse flow developed at the suction pipe outlet, which had an influence on the flow and the pressure fluctuations, downstream of the impeller. Therefore, the pressure fluctuation at the blade leading edge contained more complex frequency components.

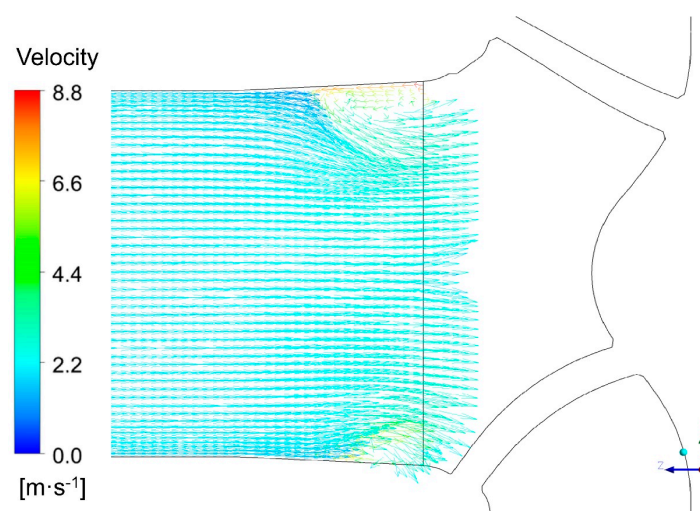


Figure 14. Flow pattern on the midsection of the suction pipe at $0.5 \times Q_0$ operating condition.

6. Conclusions

In this study, an investigation of the internal energy dissipation at part-load operating conditions has been presented for a low-head pump. This pump was a high-specific-speed dredge pump, with a low-solidity centrifugal impeller.

The numerical simulation domains included a suction pipe, a three-bladed centrifugal impeller, pump-out vanes, a volute, as well as the front and back side gaps. The flow was solved by steady and unsteady numerical simulations with consideration of the total energy balance equation. SST $k-\omega$ and SAS–SST turbulence models with curvature correction, were applied.

The performance and pressure fluctuations were compared between the numerical simulation results and the experimental results, to validate the simulations. The internal power losses were in

accordance with the hydraulic power loss, at the design and off-design operating conditions. The internal power losses in the impeller and the volute account for the most among all flow components. For the volute, the large section area of the volute in the dredge pump, weakened the control of the volute on the flow.

The causes for the internal energy dissipation inside the impeller at the part-load operating conditions were the flow separation and the rotating stall. When discharge decreased from the design operating condition, flow separation generated near the impeller shroud and led to a periodical change of internal energy dissipation rate. At $0.5 \times Q_0$ operating condition, the impeller experienced an unsteady rotating stall. The pressure fluctuation analysis made the unsteady characteristic of these flow phenomena apparent. At the $0.5 \times Q_0$ operating condition, there was an obvious low-frequency of pressure fluctuation, like $0.7 \times n$ in the impeller, which was related to the rotating stall phenomenon. The reverse flow near the interface between the suction pipe and the impeller had an influence on the flow patterns, downstream. The cause for the complicated pressure components at the blade leading edge was explained as the reverse flow at the pipe outlet.

Rotor–stator interaction between the impeller and the volute tongue caused internal energy dissipation rate near the blade trailing edge and brings about pressure fluctuation with rotating frequency. Since the stall occupied a large area in the flow passage at $0.5 \times Q_0$ operating condition, the internal energy dissipation due to the rotor–stator interaction and pressure amplitudes of rotating frequency were not obvious. The blade passing frequency was the dominant frequency at the impeller inlet, due to the flow interaction between the pipe and the impeller.

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Nomenclature

A	Area (m^2)
A_{in}	Inlet boundary area (m^2)
A_{out}	Outlet boundary area (m^2)
c_p	Pressure normalization (-)
$\vec{C}$	Flow velocity ($\text{m}\cdot\text{s}^{-1}$)
D	Impeller diameter (m)
D	Strain rate tensor (s^{-1})
e	Specific internal energy ($\text{J}\cdot\text{kg}^{-1}$)
E_{nD}^0	Specific energy factor at design operating condition (-)
g	Gravitational acceleration ($\text{m}\cdot\text{s}^{-2}$)
h	Specific enthalpy ($\text{J}\cdot\text{kg}^{-1}$)
h_{tot}	Specific total enthalpy ($\text{J}\cdot\text{kg}^{-1}$)
H	Head (m)
H_0	Rated head (m)
I	Unit tensor (-)

n	Rotating speed (s^{-1})
N_{QE}	Specific speed (-)
p	Pressure (Pa)
P	Power (W)
$\mathbf{P}$	Total stress tensor (Pa)
$P_{loss,A}$	Internal power loss near wall (W)
$P_{loss,h}$	Hydraulic power loss (W)
$P_{loss,i}$	Internal power loss (W)
$\vec{q}$	Heat flux ($\text{W}\cdot\text{m}^{-2}$)
Q	Discharge ($\text{m}^3\cdot\text{s}^{-1}$)
Q_0	Design discharge ($\text{m}^3\cdot\text{s}^{-1}$)
Q_{nD}^0	Discharge factor at design operating condition (-)
R	Radial coordinate (m)
t	Time (s)
T	Temperature (K)
T_t	Torque ($\text{N}\cdot\text{m}$)
U_2	Circumferential velocity at the impeller outlet ($\text{m}\cdot\text{s}^{-1}$)
V	Volume (m^3)
y^+	Dimensionless wall distance (-)
Z	Height coordinate (m)
ε	Turbulence dissipation rate ($\text{m}^2\cdot\text{s}^{-3}$)
λ_{eff}	Effective thermal conductivity ($\text{W}\cdot\text{K}^{-1}\cdot\text{m}^{-1}$)
λ_t	Thermal conductivity ($\text{W}\cdot\text{K}^{-1}\cdot\text{m}^{-1}$)
η	Efficiency (-)
μ	Dynamic viscosity ($\text{kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$)
μ_t	Eddy viscosity ($\text{kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$)
ρ	Density ($\text{kg}\cdot\text{m}^{-3}$)
τ	Wall shear stress (Pa)
θ	Angular coordinate ($^\circ$)

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