## Article

# Magnetic Positioning Technique Integrated with Near-Field Communication for Wireless EV Charging 

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#### Abstract

For wireless electric vehicle charging, the relative position of the primary and secondary coils has significant impacts on the transferred power, efficiency and leakage magnetic flux. In this paper, a magnetic positioning method using simultaneous power and data transmission (SWPDT) is proposed for power coil alignment. Four signal coils are installed on the primary coil to detect the secondary coil position. By measuring the positioning signal amplitudes from the four signal coils, the power coil relative position can be obtained. Moreover, all the communication needed in the positioning process can be satisfied well by SWPDT technology, and no extra radio frequency (RF) communication hardware is needed. The proposed positioning method can work properly both in power transfer online condition and in power transfer offline condition. Thus, a highly integrated wireless charging system is achieved, which features simultaneous power transfer, data transmission and position detection. A positioning experimental setup is built to verify the proposed method. The experimental results demonstrate that the positioning resolution can be maintained no lower than 1 cm in a $1060 \mathrm{~mm} \times 900 \mathrm{~mm}$ elliptical region for a pair of $510 \mathrm{~mm} \times 410 \mathrm{~mm}$ rectangular power coils. The three-dimensional positioning accuracy achieves up to 1 cm .


Keywords: electric vehicle charging; magnetic positioning; online positioning; simultaneous wireless power and data transmission

## 1. Introduction

Wireless electric vehicle charging (WEVC) is gaining worldwide attention and developing very quickly [1-3]. Compared to the conductive charging method, WEVC eliminates the bulky cables, the requirement of a manual connection, and the associated hazards. WEVC exhibits many attractive advantages such as convenience, safety and weatherproofing. Both inductive power transfer (IPT) and capacitive power transfer (CPT) can be used for WEVC [3]. This paper is focused on the IPT system.

For IPT systems, the coil misalignment greatly deteriorates the transferred power, efficiency and leakage of magnetic flux [3,4]. Much research to improve the misalignment tolerance of IPT systems has been conducted [5-12]. The preferred approach is to optimize the coil structure [5-7], which maintains a relatively uniform magnetic field distribution during misalignment. Another approach is to optimize the compensation network, which improves the circuit performance under misalignment conditions [8-12]. However, the improvement of misalignment tolerance is limited, and the charging still needs to take place in a limited charging zone. To confirm the pickup coil being within the charging zone, the position detection of power coils is indispensable for a practical wireless charger, as described by SAE J2954 [13]. On the other hand, if the position detection method is of high accuracy, it can be combined with the autonomous parking technology to align the power coils accurately. This will reduce the need to design an IPT system with large misalignment tolerance.

Accordingly, the extra hardware cost and control cost for the misalignment tolerance improvement can be reduced. Therefore, for a commercialized wireless EV charger, the cost of improving position detection accuracy and the cost of improving misalignment tolerance should be traded off.

Some position detection methods available on the market have been considered for WEVC, such as radio frequency (RF) positioning [14-20], optical positioning [21,22] and acoustical positioning [23]. However, RF positioning and acoustical positioning both suffer signal multipath impairment and non-line-of-sight impairment when they work in a complex environment. The optical positioning methods, including visual image analysis and infrared positioning, are susceptible to obstacles, dust and harsh weather. Meanwhile, all the methods above are limited by their high cost and difficulty in integrating with the power pads. Magnetoresistive (MR) sensors are investigated to be used for coil misalignment detection [24-27], but this method has not achieved precise three-dimensional (3D) coordinate output, and plenty of sensors involved in the sensor matrix greatly increase the system cost and complexity. Moreover, some magnetic positioning methods are proposed in [28-33], which utilize auxiliary coils to measure the magnetic field generated by the primary power coil. The magnetic positioning methods are of high accuracy, low cost, not susceptible to the environment and are easy to integrate with power pads. In [28-33], the primary power coil needs to generate a very weak magnetic field for positioning. Thus, the primary resonant tank is excited by a very low-voltage source during positioning. For this very low-voltage mode, the primary high-power inverter has to switch to a very low direct current (DC) bus voltage [31,32], or to operate with a very large phase-shift angle [33]. However, either the added bus selection switches or the large phase-shift operation will decrease the reliability and safety of the high-power inverter. Moreover, the inverter can only work in the high voltage mode for power transfer, or the low voltage mode for positioning at a time. Thus, position detection and power transfer cannot be simultaneously conducted, i.e., the online position monitoring is impossible.

We have proposed a simultaneous wireless power and data transmission (SWPDT) system in [34], which is based on the frequency division multiplexing (FDM) technique and quadrature phase-shift keying (QPSK) modulation. A high-frequency data carrier is modulated by four discrete phase shifts to represent two binary bits. The data carrier is injected into one side of the IPT system, and then it transfers to the other side through the magnetic coupling between power coils. The data carrier is then extracted and demodulated, so that the near-field communication can be achieved. In this method, the amplitude of the data carrier is not utilized for communication purpose. However, the receiving amplitude of the data carrier is proportional to the mutual inductance between power coils, which means it contains the relative position information of power coils. Unfortunately, the three-dimensional (3D) position cannot be determined exactly by only one mutual inductance. Thus, more independent mutual inductances should be involved to derive the 3D coordinate. This idea has been revealed in our preliminary work [35].

Based on the near-field communication technology in SWPDT, this paper proposes a magnetic positioning method, which has the following features:
(1) Four auxiliary signal coils are added for positioning while other hardware is shared with the SWPDT system.
(2) The positioning signal is transmitted by the signal coils rather than the primary power coil, so the very low voltage mode of the high-power inverter, as mentioned before, is avoided.
(3) The positioning process can be carried out both in the power transfer online condition and in the power transfer offline condition. The proposed amplitude measurement method is immune to the power fundamental interference and ensures online positioning accuracy.
(4) The communication need in the positioning process can be well satisfied by SWPDT technology. A highly integrated IPT system for WEVC is achieved, i.e., simultaneous power transfer, data transmission and position detection.

## 2. Magnetic Positioning Integrated with Near-Field Communication in Simultaneous Wireless Power and Data Transmission (SWPDT) System

### 2.1. Communication Principle of SWPDT System

The original SWPDT system proposed in [34] is shown in Figure 1a, and labelled as "communication setting" in this paper. The subscripts " 1 " and " 2 " stand for the primary side and the secondary side, respectively. The forward communication channel can be expressed as $\mathrm{TX}_{1} \rightarrow L_{\mathrm{TX} 1} \rightarrow L_{1} \rightarrow L_{2} \rightarrow L_{\mathrm{RX} 2} \rightarrow \mathrm{RX} \mathrm{X}_{2}$, where $L_{\mathrm{TX} 1}$ is used to inject the data carrier into the power circuit, and $L_{\mathrm{RX} 2}$ is used to extract the data carrier from the power circuit. Similarly, the backward communication channel is $\mathrm{TX}_{2} \rightarrow L_{\mathrm{TX} 2} \rightarrow L_{2} \rightarrow L_{1} \rightarrow L_{\mathrm{RX} 1} \rightarrow \mathrm{RX}_{1}$. The configurations of the forward communication and the backward communication are fully symmetrical. The only difference is that they use two different data carrier frequencies, i.e., $f_{\mathrm{d} 1}(5 \mathrm{MHz})$ for the forward and $f_{\mathrm{d} 2}(6.25 \mathrm{MHz})$ for the backward. Thus, the forward communication is illustrated as an example in the following.


Figure 1. Simultaneous wireless power and data transmission (SWPDT) system: (a) original communication setting; (b) proposed positioning setting.

For the primary data transmitter $\mathrm{TX}_{1}$, the switching frequency of $Q_{1}$ is equal to the data carrier frequency $f_{\mathrm{d} 1}$. The gate drive signal $v_{\mathrm{G} 1}$ is modulated with four kinds of phase shift $\varphi$, i.e., $0, \pi / 2$, $\pi, 3 \pi / 2$, as shown in Figure 2 [34]. The transmitting signal $v_{\mathrm{TX} 1}$ with each phase shift for a certain duration $T_{\text {symbol }}$ is called a symbol. As shown in the mapping table of Figure 2, the data is represented by the phase change $\Delta \varphi$ between two adjacent symbols, namely differential quadrature phase-shift keying (DQPSK). The transmitting signal $v_{\mathrm{TX} 1}$ and the adjacent phase change $\Delta \varphi$ can be expressed by:

$$
\begin{gather*}
v_{\mathrm{TX} 1}(t)=A_{1} \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)\right), \varphi(n) \in\{0, \pi / 2, \pi, 3 \pi / 2\},  \tag{1}\\
\Delta \varphi(n)=\varphi(n)-\varphi(n-1), \tag{2}
\end{gather*}
$$

where $A_{1}$ is the constant amplitude, and $n$ is the symbol sequence number.


Figure 2. Differential quadrature phase-shift keying (DQPSK) modulation of data transmitter.

The transmitting signal $v_{\mathrm{TX} 1}$ is injected into the power circuit by the loose coupling between $L_{\mathrm{TX} 1}$ and the power line, and then transfers to the secondary side through the coupling of power coils $L_{1} L_{2}$. The receiving capacitor $C_{R X 2}$ is resonant with the signal extractor $L_{R X 2}$ at the data carrier frequency $f_{\mathrm{d} 1}$, which forms a narrow passband filter to extract the data carrier $f_{\mathrm{d} 1}$. The data signal received on $C_{\mathrm{RX} 2}$ can be expressed by:

$$
\begin{equation*}
v_{\mathrm{RX} 2}(t)=K_{12} A_{1} \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{12}\right) \tag{3}
\end{equation*}
$$

where $K_{12}$ and $\varphi_{12}$ are the forward transfer gain and phase shift, respectively. $K_{12} A_{1}$ is the receiving signal amplitude, which is denoted as $\left|V_{\mathrm{RX} 2}\right|$.

Through the demodulation circuit in $\mathrm{RX}_{2}$, the adjacent phase change $\Delta \varphi(n)$ can be calculated by (4) [34]. Then the data can be demodulated according to the mapping table in Figure 2, so that the forward communication is achieved.

$$
\begin{equation*}
\Delta \varphi(n)=\varphi_{\mathrm{cal}}(n)-\varphi_{\mathrm{cal}}(n-1) \tag{4}
\end{equation*}
$$

where

$$
\begin{gathered}
\varphi_{\mathrm{cal}}(n)=\left\{\cos ^{-1} \alpha(n), 2 \pi-\cos ^{-1} \alpha(n)\right\} \cap\left\{\sin ^{-1} \beta(n), \pi-\sin ^{-1} \beta(n)\right\} \\
\alpha(n)=\frac{v_{\sin 2}(n)}{\sqrt{v_{\sin 2}^{2}(n)+v_{\cos 2}^{2}(n)}}, \beta(n)=\frac{v_{\cos 2}(n)}{\sqrt{v_{\sin 2}^{2}(n)+v_{\cos 2}^{2}(n)}}
\end{gathered}
$$

### 2.2. Integration of Magnetic Positioning

For the forward communication discussed above, the transmitting signal amplitude $A_{1}$ is a constant. The signal forward transfer gain $K_{12}$ in (3) is proportional to the mutual inductance of the power coils $M_{12}$. Thus, the receiving signal amplitude $\left|V_{\mathrm{RX} 2}\right|$, namely $K_{12} A_{1}$, is also proportional to the mutual inductance $M_{12}$.

$$
\begin{equation*}
\left|V_{\mathrm{RX} 2}\right|=K_{12} A_{1}=\chi_{12} M_{12} \tag{5}
\end{equation*}
$$

where $\chi_{12}$ is the proportionality constant determined by system parameters.
On the other hand, the mutual inductance $M_{12}$ is related to the physical dimensions and relative position of the power coils according to the Neumann formula [32]:

$$
\begin{equation*}
M_{12}=\frac{\mu 0}{4 \pi} \oint_{l 1} \oint_{l 2} \frac{\overrightarrow{d l 1} \cdot \overrightarrow{d l 2}}{r 12} \tag{6}
\end{equation*}
$$

It can be derived from (6) that if the physical dimensions of power coils are fixed, the mutual inductance is only a function of the relative position between two power coils as (7).

$$
\begin{align*}
M_{12} & =F_{12}\left(x_{12}, y_{12}, z_{12}\right)  \tag{7}\\
\left(x_{12}, y_{12}, z_{12}\right) & =\left(x_{2}-x_{1}, y_{2}-y_{1}, z_{2}-z_{1}\right) \tag{8}
\end{align*}
$$

where $\left(x_{12}, y_{12}, z_{12}\right)$ is the relative coordinate of the secondary coil referenced to the primary coil, given that the primary coil coordinate is $\left(x_{1}, y_{1}, z_{1}\right)$ and the secondary coil coordinate is $\left(x_{2}, y_{2}, z_{2}\right)$.

According to (5) and (7), the receiving signal amplitude is a function of the relative position between two power coils.

$$
\begin{equation*}
\left|V_{\mathrm{RX} 2}\right|=\chi_{12} F_{12}\left(x_{12}, y_{12}, z_{12}\right) \tag{9}
\end{equation*}
$$

From (9), it can be seen that for any given relative position of the power coils, there is always a unique receiving amplitude value $\left|V_{\mathrm{RX}}\right|$. However, for a given receiving amplitude $\left|V_{\mathrm{RX} 2}\right|$, the relative coordinate $\left(x_{12}, y_{12}, z_{12}\right)$ cannot be determined uniquely, since the coordinate has three unknown variables. Thus, the original configuration of a SWPDT in Figure 1a is insufficient to determine the 3 D relative position coordinate. In order to obtain the 3D relative position coordinate, at least three independent signal amplitudes are needed. This means at least three independent signal transmitting
coils on the ground side or three independent signal receiving coils on the vehicle side are needed. However, adding the signal receiving coils will increase the hardware volume in the vehicle. Also, the signal receiving coils on the vehicle may suffer the position shift due to the vehicle jolt, which will degrade the positioning accuracy. Thus, adding the signal transmitting coils on the ground side is better.

Based on the analysis above, four identical signal transmitting coils $L_{A}-L_{D}$ are employed for position detection, as shown in Figure 1b. Since the secondary-side setting of positioning system is same as that of communication system in Figure 1a, it is not redrawn in Figure 1b. The signal transmitting coils $L_{A}-L_{D}$ are placed on the primary power coil and connected to the existing data transmitter $\mathrm{TX}_{1}$ through switches $S_{A}-S_{D}$, respectively. All the signal coils $L_{A}-L_{D}$ have the same inductance value as the signal injector $L_{\mathrm{TX} 1}$, so that the compensation capacitor $C_{\mathrm{TX} 1}$ in $\mathrm{TX}_{1}$ can be shared. Compared to the three-coil configuration, the adopted four coils can improve the positioning accuracy by one redundant measurement. Moreover, even if one of the four coils malfunctions, the other three coils can still achieve the 3D positioning. Thus, the four-coil configuration is cost-effective.

In the positioning process, switch $S_{\mathrm{T} 1}$ is always off, so that the signal injector for communication is cut off from the transmitter $\mathrm{TX}_{1}$. Switches $S_{\mathrm{A}}-S_{\mathrm{D}}$ are switched on and off in turns, which means the signal coils $L_{\mathrm{A}}-L_{\mathrm{D}}$ are in turns energized by TX to transmit the positioning signals, i.e., the data carrier $f_{\mathrm{d} 1}$. Thus, only one signal coil can be energized to transmit a signal at a time. The four positioning signals are transferred to the secondary coil in turns, and then received by the secondary receiver $R X_{2}$. According to the amplitudes of the four receiving signals, the relative position between the primary and secondary coils can be determined.

Figure 3 shows the positioning circuit model when $S_{\mathrm{A}}$ is switched on and the signal coil $L_{\mathrm{A}}$ is energized by $\mathrm{TX}_{1}$. The circuit models for the other signal coils during working are the same. In Figure 3, both the power inverter on the primary side and the power rectifier on the secondary side can be seen as a short circuit for data carrier $f_{\mathrm{d} 1}$ due to their large DC bus capacitors. Three mutual inductances are formed between the primary power coil $L_{1}$, the secondary power coil $L_{2}$ and the energized signal coil $L_{\mathrm{A}}$, respectively $M_{12}, M_{\mathrm{A} 1}$ and $M_{\mathrm{A} 2}$. The power resonant tank $L_{1} C_{1}$ and $L_{2} C_{2}$ are both resonant at the power frequency $f_{\mathrm{p}}(85 \mathrm{kHz})$. At the data carrier frequency $f_{\mathrm{d} 1}(5 \mathrm{MHz})$, the parasitic capacitances of the power inductors and the parasitic inductances of the power capacitors should be considered, which are denoted by $C_{L 1 \_p a r a}, C_{L 2 \_p a r a}, L_{C 1 \_p a r a}$ and $L_{C 2 \_p a r a}$, respectively. Thus, the primary impedance $Z_{1}$ and the secondary impedance $Z_{2}$ at the data carrier frequency $f_{\mathrm{d} 1}$ can be derived as:

$$
\begin{gather*}
Z_{1}\left(\omega_{\mathrm{d} 1}\right)=j \omega_{\mathrm{d} 1} L_{1}+\frac{1-\omega_{\mathrm{d} 1}^{2} L_{\mathrm{C} 1 \_ \text {para }} C_{1}}{j \omega_{\mathrm{d} 1}\left(C_{1}+C_{L 1 \_ \text {para }}-\omega_{\mathrm{d} 1}^{2} L_{C 1 \_ \text {para }} C_{1} C_{L 1 \_ \text {para }}\right)}  \tag{10}\\
Z_{2}\left(\omega_{\mathrm{d} 1}\right)=j \omega_{\mathrm{d} 1} L_{2}+\frac{Z_{\mathrm{branch}}}{1+j \omega_{\mathrm{d} 1} C_{L 2 \_ \text {para }} Z_{\mathrm{branch}}} \tag{11}
\end{gather*}
$$

where

$$
Z_{\mathrm{branch}}=\frac{1}{j \omega_{\mathrm{d} 1} C_{2}}+j \omega_{\mathrm{d} 1} L_{\mathrm{C} 2 \_ \text {para }}+j \omega_{\mathrm{d} 1} L_{\mathrm{RX} 2}^{\prime}+\frac{\omega_{\mathrm{d} 1}^{2} M_{\mathrm{RX} 2}^{2}}{R_{L \mathrm{RX} 2 \_ \text {para }}}
$$

Given that the current through $L_{\mathrm{A}}$ is $I_{\mathrm{e}}$, the induced electromotive force (EMF) on the secondary power coil is:

$$
\begin{gather*}
\varepsilon_{2(\mathrm{~A})}\left(\omega_{\mathrm{d} 1}\right)=j \omega_{\mathrm{d} 1} M_{\mathrm{A} 2} I_{\mathrm{e}}+j \omega_{\mathrm{d} 1} M_{12} I_{1} \\
=  \tag{12}\\
=j \omega_{\mathrm{d} 1}\left(M_{\mathrm{A} 2}-M_{12} \frac{\omega_{\mathrm{d} 1}^{2} M_{12} M_{\mathrm{A} 2}+j \omega_{\mathrm{d} 1} M_{\mathrm{A} 1} Z_{2}}{\omega_{\mathrm{d} 1}^{2} M_{12}^{2}+Z_{1} Z_{2}}\right) I_{\mathrm{e}}
\end{gather*}
$$

The term in the parentheses of (12) can be defined as the effective mutual inductance $M_{\text {eff(A) }}$ between the signal coil and the secondary coil, which synthesizes the reflection effect of the primary induced current $I_{1}$. The definition is:

$$
\begin{equation*}
M_{\mathrm{eff}(\mathrm{~A})}=M_{\mathrm{A} 2}-M_{12} \frac{\omega_{\mathrm{d} 1}^{2} M_{12} M_{\mathrm{A} 2}+j \omega_{\mathrm{d} 1} M_{\mathrm{A} 1} Z_{2}}{\omega_{\mathrm{d} 1}^{2} M_{12}^{2}+\mathrm{Z}_{1} Z_{2}} \tag{13}
\end{equation*}
$$



Figure 3. Positioning circuit model when $L_{\mathrm{A}}$ is energized.
Thus, the EMF on the secondary power coil when $L_{\mathrm{A}}$ is energized can be rewritten as:

$$
\begin{equation*}
\varepsilon_{2(\mathrm{~A})}\left(\omega_{\mathrm{d} 1}\right)=j \omega_{\mathrm{d} 1} M_{\mathrm{eff}}(\mathrm{~A}) I_{\mathrm{e}} \tag{14}
\end{equation*}
$$

Since the four signal coils $L_{A}-L_{D}$ are identical, the energized currents through them are same and equal to $I_{\mathrm{e}}$. When $L_{\mathrm{A}}-L_{\mathrm{D}}$ are energized in turns, the secondary induced EMF vector can be obtained as:
where the subscript $A, B, C$ or $D$ represents the coil $L_{A}, L_{B}, L_{C}$ or $L_{D}$ is energized, respectively.
Since the secondary signal extractor $L_{\mathrm{RX} 2}$ is fixed around the power line as shown in Figure 1a, the mutual inductance $M_{R X 2}$ in Figure 3 is a constant. Meanwhile, in Figure 3, $L_{R X 2}$ is resonant with $C_{R X 2}$ at frequency $\omega_{\mathrm{d} 1}$, and $R_{L R X 2}$ para is the parasitic resistance of the signal extractor. Thus, the receiving amplitude $\left|V_{\mathrm{RX} 2}\right|$ is proportional to the EMF on the secondary power coil, which can be derived as:

$$
\left[\begin{array}{l}
\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|  \tag{16}\\
\left|V_{\mathrm{RX} 2(\mathrm{~B})}\right| \\
\left|V_{\mathrm{RX} 2(\mathrm{C})}\right| \\
\left|V_{\mathrm{RX2} \text { (D) }}\right|
\end{array}\right]=\left|\frac{\omega_{\mathrm{d} 1}^{2} M_{\mathrm{RX} 2} L_{\mathrm{RX} 2}}{\left(\omega_{\mathrm{d} 1}^{2} L_{2} C_{L 2 \_ \text {para }} Z_{\mathrm{branch}}-Z_{\mathrm{branch}}-j \omega_{\mathrm{d} 1} L_{2}\right) R_{L \mathrm{RX} 2} \text { _para }}\right|=\left[\begin{array}{c}
\left|\varepsilon_{2(\mathrm{~A})}\right| \\
\left|\varepsilon_{2(\mathrm{~B})}\right| \\
\left|\varepsilon_{2(\mathrm{C})}\right| \\
\left|\varepsilon_{2(\mathrm{D})}\right|
\end{array}\right] .
$$

Since four signal coils are fixed on the primary coil, the effective mutual inductance of each signal coil $M_{\mathrm{eff}(\mathrm{A})}-M_{\mathrm{eff}}(\mathrm{D})$ is a function of the power coils' relative position coordinate ( $x_{12}, y_{12}, z_{12}$ ).

$$
\left[\begin{array}{c}
M_{\operatorname{eff}}(\mathrm{A})  \tag{17}\\
M_{\operatorname{eff}}(\mathrm{B}) \\
M_{\operatorname{eff}(\mathrm{C})} \\
M_{\mathrm{eff}(\mathrm{D})}
\end{array}\right]=\left[\begin{array}{c}
F_{(\mathrm{A})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{B})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{C})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{D})}\left(x_{12}, y_{12}, z_{12}\right)
\end{array}\right]
$$

From (15)-(17), the relationship between the receiving signal amplitudes and the relative coordinate of power coils can be derived as:

$$
\left.\left[\begin{array}{l}
\left|V_{\mathrm{RX} 2(\mathrm{~A})}\right|  \tag{18}\\
\left|V_{\mathrm{RX} 2(\mathrm{~B})}\right| \\
\left|V_{\mathrm{RX} 2(\mathrm{C})}\right| \\
\left|V_{\mathrm{RX} 2(\mathrm{D})}\right|
\end{array}\right]=\left|\frac{j \omega_{\mathrm{d} 1}^{3} M_{\mathrm{RX} 2} L_{\mathrm{RX} 2} I_{\mathrm{e}}}{\left(\omega_{\mathrm{d} 1}^{2} L_{2} C_{L 2 \_ \text {para }} Z_{\text {branch }}-Z_{\text {branch }}-j \omega_{\mathrm{d} 1} L_{2}\right) R_{L R X 2 \_\mathrm{para}} \mid}\right| \begin{array}{l}
F_{(\mathrm{A})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{B})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{C})}\left(x_{12}, y_{12}, z_{12}\right) \\
F_{(\mathrm{D})}\left(x_{12}, y_{12}, z_{12}\right)
\end{array}\right]
$$

The functions $F_{(\mathrm{A})}, F_{(\mathrm{B})}, F_{(\mathrm{C})}$ and $F_{(\mathrm{D})}$ in (18) can be derived from the Neumann formula (6), but they do not have the analytical expressions. Thus, Equation (18) cannot be used to directly calculate the relative coordinate from the receiving amplitudes. However, it confirms the one-to-one correspond-ence between the amplitude vector $V_{\mathrm{RX} 2}\left(\left|V_{\mathrm{RX2} 2(\mathrm{~A})}\right|,\left|V_{\mathrm{RX2} \text { (B) }}\right|,\left|V_{\mathrm{RX2}(\mathrm{C})}\right|,\left|V_{\mathrm{RX2}(\mathrm{D})}\right|\right)$ and the power coils' relative coordinate $\overrightarrow{C_{12}}\left(x_{12}, y_{12}, z_{12}\right)$. Thus, the lookup table method can be used to determine the position coordinate according to the amplitude vector.

## 3. Optimal Number and Locations for Auxiliary Signal Coils

According to (17) and (18), the change of the secondary coil position leads to the change of effective mutual inductances, and further leads to the change of receiving signal amplitudes. For the same position change, the more the effective mutual inductances change, the higher position resolution will be obtained, i.e., the higher positioning accuracy. Thus, the optimal locations for the signal coils are the places where the gradient of effective mutual inductance $\nabla M_{\text {eff }}$ is maximized.

$$
\begin{equation*}
\nabla M_{\mathrm{eff}}=\frac{\partial M_{\mathrm{eff}}}{\partial x} \vec{x}+\frac{\partial M_{\mathrm{eff}}}{\partial y} \vec{y}+\frac{\partial M_{\mathrm{eff}}}{\partial z} \vec{z} \tag{19}
\end{equation*}
$$

Simulations were conducted in ANSYS Electromagnetics Suite to find the optimal locations. The Cartesian coordinate system for positioning is built in Figure 4, of which the origin is set to the three-dimensional geometric center of the primary coil. The dimensions of the power coils and signal coils are listed in Table 1. The position of each coil is represented by the coordinate of its three-dimensional geometric center. In the normal alignment condition, the primary coil coordinate $\left(x_{1}, y_{1}, z_{1}\right)$ is $(0,0,0)$, and the secondary coil coordinate $\left(x_{2}, y_{2}, z_{2}\right)$ is $(0,0,160 \mathrm{~mm})$.


Figure 4. Coordinate system for positioning.

Table 1. Coil dimensions.

| Power Coils |  |
| :--- | :--- |
| Primary coil outer dimension $l_{1} \times w_{1} \times h_{1}$ | $510 \mathrm{~mm} \times 410 \mathrm{~mm} \times 2.5 \mathrm{~mm}$ |
| Primary coil copper width $w_{\mathrm{c} 1}$ | 52.5 mm |
| Secondary coil outer dimension $l_{2} \times w_{2} \times h_{2}$ | $510 \mathrm{~mm} \times 410 \mathrm{~mm} \times 2.5 \mathrm{~mm}$ |
| Secondary coil copper width $w_{\mathrm{c} 2}$ | 52.5 mm |
| Normal air gap $g$ | 160 mm |
| Auxiliary Signal Coils |  |
| Signal coil outer diameter $d_{\mathrm{o}}$ | 63 mm |
| Signal coil inner diameter $d_{\mathrm{i}}$ | 58 mm |
| Signal coil height $h_{\mathrm{s}}$ | 10 mm |

To minimize the installation space of the signal coils in practice, it is better to place the signal coils in parallel with the primary coil, i.e., in parallel with the XOY plane. In this condition, only the z-component of flux density through the signal coil will contribute to the effective mutual inductance with the secondary coil. Thus, we can energize the secondary coil and find the places where the gradient of flux density z-component $\nabla B_{z}$ is maximized. These places also have the maximized gradient of effective mutual inductance $\nabla M_{\text {eff }}$. The gradient of flux density z-component $\nabla B_{z}$ is defined as:

$$
\begin{equation*}
\nabla B_{\mathrm{z}}=\frac{\partial B_{\mathrm{z}}}{\partial x} \vec{x}+\frac{\partial B_{\mathrm{z}}}{\partial y} \vec{y}+\frac{\partial B_{\mathrm{z}}}{\partial z} \vec{z} \tag{20}
\end{equation*}
$$

In the simulation, the secondary coil is energized with a 1-A current. Since the thickness of the signal coil is 10 mm , the gradient magnitude $\left|\nabla B_{z}\right|$ on the plane 10 mm above the primary coil is depicted in Figure 5. It can be seen that the highest gradient magnitude appears at the four inner corners. This means the mutual inductance at these places will change to the greatest extent when the secondary coil position changes. Thus, the position resolution can be maximized when the signal coils are placed at the inner corners above the primary coil.


Figure 5. Distribution of the gradient magnitude $\left|\nabla B_{z}\right|$ on the plane 10 mm above the primary coil.
To verify the optimal locations for the signal coils, three kinds of signal coils placement are simulated and compared, as shown in Figure 6. The primary coil is colored by green, and the signal coils are colored by pink. Their coordinates are also given in Figure 6.


Figure 6. Three placements of auxiliary signal coils: (a) placed above four inner corners of the primary coil; (b) placed above four sides' midpoints of the primary coil; (c) placed above the primary coil interior.

In the simulation, the primary coil coordinate $\left(x_{1}, y_{1}, z_{1}\right)$ is always fixed at $(0,0,0)$. In the initial condition, i.e., the normal alignment condition, the secondary coil coordinate $\left(x_{2}, y_{2}, z_{2}\right)$ is $(0,0$, 160 mm ), which is also denoted by $\left(x_{20}, y_{20}, z_{20}\right)$. Then the secondary coil moves along three axes, and its position change along three axes are denoted by $\Delta x_{2}, \Delta y_{2}$ and $\Delta z_{2}$, respectively.

$$
\begin{equation*}
\left(\Delta x_{2}, \Delta y_{2}, \Delta z_{2}\right)=\left(x_{2}-x_{20}, y_{2}-y_{20}, z_{2}-z_{20}\right) \tag{21}
\end{equation*}
$$

The total change of effective mutual inductances $\Delta M_{\text {total }}$ is used to evaluate the performance of coil placement, which is defined as:

$$
\begin{align*}
\Delta M_{\text {total }} & =\left|M_{\text {eff(A) }}-M_{\operatorname{eff}(\mathrm{A})}^{\prime}\right|+\left|M_{\mathrm{eff}(\mathrm{~B})}-M_{\mathrm{eff}(\mathrm{~B})}^{\prime}\right| \\
& +\left|M_{\mathrm{eff}(\mathrm{C})}-M_{\mathrm{eff}(\mathrm{C})}^{\prime}\right|+\left|M_{\mathrm{eff}(\mathrm{D})}-M_{\mathrm{eff}(\mathrm{D})}^{\prime}\right| \tag{22}
\end{align*}
$$

where $M_{\text {eff(A) }}^{\prime}, M_{\text {eff(B) }}^{\prime}, M_{e f f(C)}^{\prime}, M_{e f f(D)}^{\prime}$ are the effective mutual inductances in the initial condition, i.e., when $\left(x_{2}, y_{2}, z_{2}\right)$ is equal to $\left(x_{20}, y_{20}, z_{20}\right)$, and $M_{\text {eff(A) }}, M_{\text {eff( }}$ ) $, M_{\text {eff(C) }}, M_{\text {eff(D) }}$ are the effective mutual inductances when the secondary coil is moved. Thus, $\Delta M_{\text {total }}$ describes the total change of four effective mutual inductances relative to those of the initial position $\left(x_{20}, y_{20}, z_{20}\right)$.

When the secondary coil moves along three axes, $\Delta M_{\text {total }}$ in the three placement conditions are depicted in Figure 7a-c. It can be seen that the Placement I always has the maximum $\Delta M_{\text {total }}$ for the same position change along $\mathrm{x}, \mathrm{y}$ and z axes. The results are consistent with the gradient analysis in Figure 5. This means the Placement I will produce the maximum change of the receiving signal amplitude vector $\left(\left|V_{\mathrm{RX2}}(\mathrm{~A})\right|,\left|V_{\mathrm{RX2}(\mathrm{~B})}\right|,\left|V_{\mathrm{RX2}(\mathrm{C})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{D})}\right|\right)$. As a result, the highest positioning resolution can be obtained from Placement I.


Figure 7. Cont.

(c)

Figure 7. Total change of effective mutual inductances $\Delta M_{\text {total }}$ when the secondary coil moves along: (a) $x$ axis; (b) y axis; and (c) $z$ axis.

To find out the optimal number of signal coils, placements with different numbers of signal coils are analyzed. To achieve 3D positioning, at least three signal coils are needed. Thus, the placements with three coils, four coils and five coils are simulated, as shown in Figure 8. The placement with three coils occupies three inner corners to maximize the sensitivity, as shown in Figure 8a. The placement with four coils in Figure 8b is same as the Placement I in Figure 6a, which has been proved the best placement for the four-coil structure. The placement with five coils adds a central coil, as shown in Figure 8c. The results of $\Delta M_{\text {total }}$ for different numbers of coils are depicted in Figure 9a-c. Compared to three coils, four coils can significantly improve the position sensitivity in all three directions. These improvements are indicated by the shadow areas in Figure 9a-c. Specifically, $\Delta M_{\text {total }}$ is increased $42 \%$ at $\Delta x=100 \mathrm{~mm}$, increased $51 \%$ at $\Delta y=100 \mathrm{~mm}$, and increased $35 \%$ at $\Delta z=-50 \mathrm{~mm}$. However, from four coils to five coils, the further improvement is very limited. There are nearly no improvements in $\Delta M_{\text {total }}$ when moving along $x$ and $y$ axes. In the $z$ direction, $\Delta M_{\text {total }}$ is increased only $25 \%$ at $\Delta z=-50 \mathrm{~mm}$. Thus, four coils are the most cost-effective with regard to accuracy and complexity. More than four coils bring little improvement in positioning accuracy but increase complexity and costs.


Figure 8. Placement with different coil number: (a) three signal coils; (b) four signal coils; (c) five signal coils.


Figure 9. $\Delta M_{\text {total }}$ obtained by different numbers of signal coils when the secondary coil moves along: (a) x axis; (b) y axis; and (c) z axis.

## 4. Amplitude Measurement of Positioning Signal

In Figure 3, the receiving positioning signal $v_{R X 2}$ is a high-frequency sine wave ( 5 MHz ). The conventional method to measure the amplitude is to rectify the high-frequency wave and sample the DC voltage by analog-to-digital converter (ADC) [33], i.e., the envelope detection. However, in the power transfer online condition, the envelope detector will be severely interfered by the power fundamental component, which is also received by signal extractor $L_{\mathrm{TX} 2}$. Thus, it is unsuitable for online positioning.

In [34], the data receiver circuit $R X_{2}$ has been proved immune to the power fundamental component when it works as data demodulator. Also, it is not hard to see that the data receiver output also contains the amplitude information of the receiving signal $v_{\mathrm{RX} 2}$, which is just neglected in the communication process in [34]. Thus, we can reuse the data receiver $R X_{2}$ to measure the positioning signal amplitude. No extra hardware is needed and the measurement is immune to the power fundamental interference.

The amplitude measurement circuit is separated from Figure 1a and redrawn in Figure 10a. Similar to (1) and (3), the transmitting signals $v_{L A}-v_{L D}$ and the receiving signals $v_{R X 2(A)}-v_{R X 2(D)}$ in positioning can be expressed as:

$$
\begin{gather*}
v_{L i}(t)=\left|V_{L i}\right| \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)\right)  \tag{23}\\
v_{\mathrm{RX} 2(i)}(t)=\left|V_{\mathrm{RX} 2(i)}\right| \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{t(i)}\right), \tag{24}
\end{gather*}
$$

where $i=\mathrm{A}, \mathrm{B}, \mathrm{C}$ or D , which indicates the transmitting coil. $\left|V_{L i}\right|$ is the transmitting amplitude on $L_{\mathrm{A}}-L_{\mathrm{D}},\left|V_{\mathrm{RX2}(i)}\right|$ is the receiving amplitude from $L_{\mathrm{A}}-L_{\mathrm{D}}$, and $\varphi_{\mathrm{t}(i)}$ is the phase shift of the transfer channel. $\varphi(n)$ is the transmitting phase shift containing data bits, as illustrated in Section 2.1.

Since the receiving signals $v_{\mathrm{RX2}(\mathrm{~A})}-v_{\mathrm{RX2}}(\mathrm{D})$ are equivalent for the amplitude measurement circuit, the subscript $i(i=A, B, C$ or $D)$ is omitted in the following analysis for simplification. In Figure 10a, the receiving signal $v_{\mathrm{RX} 2}$ is divided by two identical resistors $R_{\mathrm{RX} 2}$ which are grounded at the center to produce a pair of differential outputs $v_{\mathrm{RX} 2+}$ and $v_{\mathrm{RX} 2-}$.

$$
\begin{align*}
& v_{\mathrm{RX} 2+}=+\frac{v_{\mathrm{RX} 2}}{2}=\frac{1}{2}\left|V_{\mathrm{RX} 2}\right| \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{t}\right)  \tag{25}\\
& v_{\mathrm{RX} 2-}=-\frac{v_{\mathrm{RX} 2}}{2}=-\frac{1}{2}\left|V_{\mathrm{RX} 2}\right| \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{t}\right) \tag{26}
\end{align*}
$$

The differential signals $v_{\mathrm{RX} 2+}$ and $v_{\mathrm{RX} 2-}$ are respectively connected to the two inputs, $a$ and $b$, of the single-pole double-throw analog switches, $S_{\cos 2}$ and $S_{\sin 2}$. The output table of the analog switch is shown in Table 2.

Table 2. Output table of analog switch.

| Control Pin $c$ | Output Pin $\boldsymbol{o}$ |
| :--- | :--- |
| High | Connected to input $a$ |
| Low | Connected to input $b$ |

The control signals of two switches $v_{\mathrm{c}_{2} \sin 2}$ and $v_{\mathrm{c}_{\mathrm{L}} \cos 2}$ are square waves with frequency $f_{\mathrm{d} 1}{ }^{\prime}$, and they are shifted by $\pi / 2$ with each other, as shown in Figure 10 b. Thus, each analog switch output $v_{\mathrm{o}_{-} \sin 2}$ or $v_{\mathrm{o}_{-} \cos 2}$ is equal to $v_{\mathrm{RX} 2+}$ multiplied by the respective square wave as:

$$
\begin{align*}
& v_{\mathrm{O}_{-} \sin 2}=v_{\mathrm{RX} 2+} \times \frac{4}{\pi} \sum_{k} \frac{\sin \left(k \cdot 2 \pi f^{\prime}{ }_{\mathrm{d} 1} t+k \cdot \varphi_{\mathrm{c}}\right)}{k} \\
& =\frac{2\left|V_{\mathrm{RX} 2}\right|}{\pi} \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{t}\right) \times \sum_{k} \frac{\sin \left(k \cdot 2 \pi f^{\prime}{ }_{\mathrm{d} 1} t+k \cdot \varphi_{\mathrm{c}}\right)}{k}  \tag{27}\\
& v_{\mathrm{O}_{-} \cos 2}=v_{\mathrm{RX} 2+} \times \frac{4}{\pi} \sum_{k} \frac{\cos \left(k \cdot 2 \pi f^{\prime}{ }_{\mathrm{d} 1} t+k \cdot \varphi_{\mathrm{c}}\right)}{k} \\
& =\frac{2\left|V_{\mathrm{RX} 2}\right|}{\pi} \sin \left(2 \pi f_{\mathrm{d} 1} t+\varphi(n)+\varphi_{t}\right) \times \sum_{k} \frac{\cos \left(k \cdot 2 \pi f^{\prime}{ }_{\mathrm{d} 1} t+k \cdot \varphi_{\mathrm{c}}\right)}{k} \tag{28}
\end{align*}
$$

where $k=1,3,5 \ldots ; \varphi_{\mathrm{c}}$ is the phase shift between the receiver control signal and the transmitter reference phase. In Figure $10 b, \varphi_{c}$ and $\varphi_{\mathrm{t}}$ are both set to zero for clarity.

(a)

Figure 10. Cont.


Figure 10. Amplitude measurement: (a) circuit; (b) waveforms.
Applying the trigonometric product-to-sum formula to (27) and (28), it can be derived that $v_{\mathrm{o}_{-} \sin 2}$ and $v_{\mathrm{o}_{-} \cos 2}$ are composed of $f_{\mathrm{d} 1} \pm k f_{\mathrm{d} 1}{ }^{\prime}(k$ is odd) frequency components. If we set the control frequency $f_{\mathrm{d} 1}{ }^{\prime}$ equal to the data carrier frequency $f_{\mathrm{d} 1}, v_{\mathrm{o}_{-} \sin 2}$ and $v_{\mathrm{o}_{-} \cos 2}$ will have a DC component (i.e., $f_{\mathrm{d} 1}-f_{\mathrm{d} 1}$ ) and all the other components are higher than $2 f_{\mathrm{d} 1}$, as shown in Figure 10b. Since $2 f_{\mathrm{d} 1} \gg 0$, the DC components in $v_{\mathrm{o}_{-} \sin 2}$ and $v_{\mathrm{o}_{-} \cos 2}$ are easy to be obtained through low-pass filters (LPF), which are:

$$
\begin{align*}
& v_{\sin 2}(n)=\frac{\left|V_{\mathrm{RX} 2}\right|}{\pi} \cos \left(2 \pi\left(f_{\mathrm{d} 1}-f_{\mathrm{d} 1}^{\prime}\right) t+\varphi(n)+\varphi_{t}-\varphi_{\mathrm{c}}\right),  \tag{29}\\
& v_{\cos 2}(n)=\frac{\left|V_{\mathrm{RX} 2}\right|}{\pi} \sin \left(2 \pi\left(f_{\mathrm{d} 1}-f_{\mathrm{d} 1}^{\prime}\right) t+\varphi(n)+\varphi_{t}-\varphi_{\mathrm{c}}\right) . \tag{30}
\end{align*}
$$

The DC voltages $v_{\sin 2}(n)$ and $v_{\cos 2}(n)$ are sampled by the digital signal processor (DSP). Then the amplitude of $v_{\mathrm{RX} 2}$ can be calculated by:

$$
\begin{equation*}
\left|V_{\mathrm{RX} 2}\right|=\pi \cdot \sqrt{v_{\sin 2}^{2}(n)+v_{\cos 2}^{2}(n)} \tag{31}
\end{equation*}
$$

It should be noted that if there is no PLL (phase-locked loop) in the receiver to synchronize the control signal frequency $f_{\mathrm{d} 1}{ }^{\prime}$ with the receiving positioning signal frequency $f_{\mathrm{d} 1}$, these two frequencies cannot be exactly equal. The results of (29) and (30) will be two very low-frequency ( $f_{\mathrm{d} 1}-f_{\mathrm{d} 1}$ ) sine waves rather than two DC voltages, which is determined by the small deviation between $f_{\mathrm{d} 1}$ and $f_{\mathrm{d} 1}$. However, this deviation will not affect the amplitude calculation, since (31) will eliminate the deviation frequency item $2 \pi\left(f_{\mathrm{d} 1}-f_{\mathrm{d} 1}{ }^{\prime}\right) t$. Thus, the amplitude of high-frequency signal $v_{\mathrm{RX} 2}$ still can be determined by measuring these two very low-frequency sine waves. On the other hand, the receiving amplitude $\left|V_{\mathrm{RX} 2}\right|$ is independent of the transmitting phase shift $\varphi(n)$ which is related to data transmission. This means the position detection and the data transmission can work simultaneously through auxiliary coils $L_{A}-L_{D}$.

In the power transfer online condition, the power fundamental component interference $f_{\mathrm{p}}$ received on $C_{\mathrm{RX} 2}$ will be transformed to $f_{\mathrm{p}} \pm k f_{\mathrm{d} 1}{ }^{\prime}$ ( $k$ is odd) components at the outputs of analog switches according to (27) and (28). Since $f_{\mathrm{p}} \ll f_{\mathrm{d} 1}{ }^{\prime}$, all the transformed components can be easily filtered out by LPF. Thus, the amplitude measurement is immune to the power fundamental component interference.

As discussed in Section 2, Equation (18) confirms the one-to-one correspondence between the amplitude vector $\overrightarrow{V_{\mathrm{RX} 2}}\left(\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|,\left|V_{\mathrm{RX2}(\mathrm{~B})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{C})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{D})}\right|\right)$ and the power coils' relative coordinate $\overrightarrow{C_{12}}\left(x_{12}, y_{12}, z_{12}\right)$. Thus, the lookup table method can be used to determine the position coordinate $\overrightarrow{C_{12}}\left(x_{12}, y_{12}, z_{12}\right)$ according to the measured amplitude vector $\overrightarrow{V_{R X 2}}\left(\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|,\left|V_{\mathrm{RX2}(\mathrm{~B})}\right|,\left|V_{\mathrm{RX2}(\mathrm{C})}\right|\right.$,
$\left.\left|V_{\mathrm{RX2}(\mathrm{D})}\right|\right)$. The procedure of deriving the 3D position coordinate is illustrated by the flowchart in Figure 11.


Figure 11. Procedure for deriving 3D position coordinate.

## 5. Experimental Results

To verify the proposed magnetic positioning method, an experimental setup was built, as shown in Figure 12. The adopted data transceiver hardware is same as that proposed in [34]. Four auxiliary signal coils $L_{\mathrm{A}}-L_{\mathrm{D}}$ are connected to the primary data transmitter $\mathrm{TX}_{1}$ output through switches $S_{\mathrm{A}}-S_{\mathrm{D}}$, respectively. The positioning signal is extracted by $L_{\mathrm{RX} 2}$ and further processed by the secondary data receiver $\mathrm{RX}_{2}$. The system parameters are listed in Table 3.


Figure 12. Experimental setup of proposed magnetic positioning method.
Table 3. System parameters.

| Power Transfer Circuit |  |
| :--- | :--- |
| Power carrier frequency $f_{\mathrm{p}}$ | 85 kHz |
| Power Coils $L_{1}$ and $L_{2}(\mathrm{uH})$ | 85 and 85 |
| Compensation capacitors $C_{1}$ and $C_{2}(\mathrm{nF})$ | 45 and 42 |
| Load resistor $R_{\mathrm{L}}(\Omega)$ | 10 |
| Primary Data Transmitter TX $\mathbf{1}_{1}$ |  |
| Forward data carrier frequency $f_{\mathrm{d} 1}$ |  |
| Input voltage $V_{\mathrm{d} 1}$ | 5 MHz |
| Auxiliary signal coils $L_{\mathrm{A}}, L_{\mathrm{B}}, L_{\mathrm{C}}$ and $L_{\mathrm{D}}$ | 12 V |
| $C_{\mathrm{TX} 1}$ | 1.3 uH |
| $C_{\mathrm{s} 1}$ | 800 pF |
| DC chokes $L_{\mathrm{f} 1}$ | 1000 pF |
| MOSFET $Q_{1}$ | 33 uH |
| Power consumption | TPH 3206 LD |
| Secondary Data Receiver $\mathrm{RX} \mathbf{X}_{\mathbf{2}}$ |  |
| Signal extractors $L_{\mathrm{RX} 2}$ | 1.5 W |
| $C_{\mathrm{RX} 2}$ | 1.4 uH |
| $R_{\mathrm{RX} 2}$ | 700 pF |
| Analog switches $S_{\mathrm{sin} 2}$ and $S_{\text {cos2 }}$ | $15.1 \mathrm{k} \Omega$ |
| Corner frequency of LPF $f_{\mathrm{c}}$ | TS 5 A 23159 |

The transmitting waveforms of four auxiliary signal coils are shown in Figure 13a, where $v_{L A}-v_{L D}$ are the voltages on auxiliary signal coils $L_{A}-L_{D}$, respectively. It can be seen that $L_{A}-L_{D}$ are enabled in turns to transmit positioning signals, and the enabled time is 1 s for each coil. The transmitting amplitudes of the four signal coils are equal, and keep constant during the power coils' misalignment. There is a 20 ms dead time between two adjacent signal coils. Each signal coil sends its unique identity (ID) at 100 ms after being enabled, to tell the receiver which coil is sending the signal. The zoom-in waveforms in Figure 13b show the positioning signal is 5 MHz sine wave.


Figure 13. (a) Transmitting waveforms of auxiliary signal coils; (b) zoom-in waveforms when $L_{\mathrm{C}}$ is enabled.

The receiving waveforms of secondary signal extractor $L_{R X 2}$ is shown in Figure 14a. The signal extractor receives the positioning signal sent by $L_{A}-L_{D}$ in turns. Since Figure 14a is measured without power coils' misalignment, the voltage amplitudes received from $L_{A}-L_{D}$ are nearly the same. The output of the amplitude measurement circuit is shown in Figure 14b. Since PLL is not adopted in the receiver, it can be seen that the waveforms of $v_{\sin 2}$ and $v_{\cos 2}$ are two very low-frequency sine waves $(41 \mathrm{~Hz})$ rather than two $D C$ voltages due to the small deviation between $f_{\mathrm{d} 1}$ and $f_{\mathrm{d} 1}{ }^{\prime}$, as analyzed in Section 4 . DSP samples these two very low-frequency sine waves, and the voltage amplitude received from each auxiliary signal coil $\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|-\left|V_{\mathrm{RX2}(\mathrm{D})}\right|$ can be calculated according to (31).


Figure 14. (a) Receiving waveforms of secondary signal extractor $L_{R X 2} ;$ (b) amplitude measurement waveforms when $L_{\mathrm{A}}$ is enabled.

The ID detection waveforms are shown in Figure 15. The DQPSK communication method is adopted, which has been illustrated in Section 2.1. The IDs for $L_{A}-L_{D}$ are " $A$ " - " $D$ " in ASCII code, respectively. According to the data mapping table in Figure 2, the data transmitter $\mathrm{TX}_{1}$ changes the signal phase to modulate the coil ID into the signal. In Figure 15, the phase change will result in the transient responses in both transmitter and receiver, which accounts for the voltage spikes in $v_{L A}-v_{L D}$ and $v_{\mathrm{RX} 2}$ waveforms. The duration for each data symbol $T_{\text {symbol }}$ is 31.25 us , and the bit rate is 64 kbps . On the receiver side, the phase changes are demodulated back to data, which are displayed by the high-bit pin and low-bit pin of DSP, as shown in Figure 15. The demodulation delay is 16 us.


Figure 15. Identity (ID) detection waveforms of auxiliary signal coils: (a) $L_{A} ;$ (b) $L_{B}$; (c) $L_{C}$; and (d) $L_{D}$.
When the secondary power coil position was changed, the receiving voltage waveforms $v_{\mathrm{RX}}$ were measured, as shown in Figure 16. In Figure 16a, the voltage amplitudes received from $L_{A}-L_{D}$ are nearly equal when the secondary coil is aligned with the primary coil. This is because four signal coils are symmetric with respect to the secondary coil in this condition. In Figure 16b, the secondary coil was moved 100 mm along the x axis. The voltage amplitudes received from $L_{\mathrm{B}}$ and $L_{\mathrm{C}}$ are increased while the voltage amplitudes received from $L_{A}$ and $L_{D}$ are decreased. In Figure 16 c , the secondary coil was moved 100 mm along the y axis. The voltage amplitudes received from $L_{\mathrm{A}}$ and $L_{\mathrm{B}}$ are increased while the voltage amplitudes received from $L_{C}$ and $L_{D}$ are decreased. In Figure 16d, the secondary coil was moved 50 mm along z axis. The voltage amplitudes received from $L_{\mathrm{A}}-L_{\mathrm{D}}$ are nearly equal once again due to the symmetry. However, the receiving amplitudes in Figure 16d are smaller than those in Figure 16a because the effective mutual inductances between the auxiliary signal coils and the secondary power coil are reduced.


Figure 16. Cont.


Figure 16. Receiving voltage waveforms when the position change of secondary power coil ( $\Delta x_{2}, \Delta y_{2}$, $\Delta z_{2}$ ) is equal to: (a) $(0,0,0) \mathrm{mm}$; (b) $(100,0,0) \mathrm{mm}$; (c) $(0,100,0) \mathrm{mm}$; and (d) $(0,0,50) \mathrm{mm}$.

In the condition of 3.3 kW power transfer, the power interference to the positioning amplitude measurement was tested, as shown in Figure 17. In Figure 17a, the power inverter output voltage $v_{p}$ and current $i_{\mathrm{p}}$ are shown in CH 1 and CH 2 , respectively. The positioning transmitting waveform $v_{L A}$ and receiving waveform $v_{\mathrm{RX} 2}$ are both superimposed with a 85 kHz component. Since the 85 kHz component received by $L_{\mathrm{RX} 2}$ is much larger than the 5 MHz component, the 5 MHz component nearly cannot be identified in the receiving waveform $v_{\mathrm{RX} 2}$ in Figure 17a. However, in Figure 17b, it can be seen that the small 5 MHz component can still be extracted through the analog switches and LPF, and transformed to 41 Hz sine wave, i.e., $v_{\sin 2}$ and $v_{\cos 2}$. Meanwhile, the large 85 kHz power fundamental component has no effect on the waveforms of $v_{\sin 2}$ and $v_{\cos 2}$, which are sampled by DSP for amplitude calculation. Thus, the amplitude measurement is immune to the power fundamental interference, as analyzed in Section 4. The online positioning is achieved. It should be noted that the power losses caused by the signal coils during online positioning can be neglected, since the signal coils are resonant with the compensation capacitor $C_{T X 1}$ at 5 MHz , which forms a bandpass filter to greatly suppress the power carrier of 85 kHz .


Figure 17. Online positioning under 3.3 kW power transfer: (a) transmitting waveform $v_{L A}$ and receiving waveform $v_{\mathrm{RX} 2} ;(\mathbf{b})$ amplitude measurement waveforms $v_{\sin 2}$ and $v_{\cos 2}$.

The measured voltage amplitudes when the secondary coil moves along x axis, y axis, z axis and the linear track $y=x$ are shown in Figure 18a-d, respectively. The measurement is taken every $1-\mathrm{cm}$ position change along x axis, y axis or z axis. The voltage amplitudes of $\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|-\left|V_{\mathrm{RX2}(\mathrm{D})}\right|$ are represented by the digital values in DSP, which are calculated according to (31). The amplitude value at each position shown in Figure 18 is the average value of 20 repeated measurements. In the measurement, the maximum amplitude variation due to the background noise is 9 in digital value. Thus, the digital amplitude change less than 9 will be deemed as noise, and cannot be used to distinguish position.

In Figure 18a, when $\Delta x_{2} \geq 530 \mathrm{~mm}$, the amplitude changes of $\left|V_{\mathrm{RX2}(\mathrm{~B})}\right|$ and $\left|V_{\mathrm{RX2}(\mathrm{C})}\right|$ due to a 1-cm position change will be less than 9 . When $\Delta x_{2} \leq-530 \mathrm{~mm}$, the amplitude changes of $\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|$ and $\left|V_{\mathrm{RX2}(\mathrm{D})}\right|$ due to $1-\mathrm{cm}$ position change will be less than 9. In Figure 18 b , when $\Delta y_{2} \geq 450 \mathrm{~mm}$, the amplitude changes of $\left|V_{\mathrm{RX2}(\mathrm{~A})}\right|$ and $\left|V_{\mathrm{RX2}(\mathrm{~B})}\right|$ due to a $1-\mathrm{cm}$ position change will be less than 9 . When $\Delta y_{2} \leq-450 \mathrm{~mm}$, the amplitude changes of $\left|V_{\mathrm{RX2}(\mathrm{C})}\right|$ and $\left|V_{\mathrm{RX2}}(\mathrm{D})\right|$ due to a 1-cm position change will be less than 9. According to the amplitude change rule mentioned above, a conservative positioning region in the normal air gap condition ( $\mathrm{g}=160 \mathrm{~mm}$ ) can be derived as a $1060 \mathrm{~mm} \times 900 \mathrm{~mm}$ elliptical region. Inside this region, the positioning resolution can keep no lower than 1 cm . The results of air gap changing conditions are shown in Figure 18c. The variation range of air gap is $\pm 100 \mathrm{~mm}$. It can be seen that the positioning resolution along $z$ axis can also keep no lower than 1 cm . Figure 18 d shows the results when the secondary coil moves along the linear track $y=x$ in the normal air gap condition. Since $\Delta y_{2}$ is always equal to $\Delta x_{2}$ on the line $y=x$, Figure 18d can be drawn in a two-dimensional plot, and $\Delta x_{2}$ is set as the horizontal axis. It can be seen that in the range $\left|\Delta x_{2}\right| \leq 350 \mathrm{~mm}$, every 1-cm position change also can be distinguished.


Figure 18. Measured receiving voltage amplitude when the position of secondary power coil changes along: (a) x axis; (b) y axis; (c) z axis; and (d) the line $y=x$ in the normal air gap condition.

In the positioning experiment, the lookup table method was used to derive the real-time position coordinate according to the measured amplitude vector. The lookup table that links the amplitude vector $\overrightarrow{V_{\mathrm{RX} 2}}\left(\left|V_{\mathrm{RX} 2(\mathrm{~A})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{~B})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{C})}\right|,\left|V_{\mathrm{RX} 2(\mathrm{D})}\right|\right)$ to the power coils' relative coordinate $\overrightarrow{C_{12}}\left(x_{12}\right.$, $y_{12}, z_{12}$ ) was established by the initial calibration. In the calibration, the amplitude vector $\overrightarrow{V_{\mathrm{RX} 2}}$ was measured every $1-\mathrm{cm}$ step along $\mathrm{x}, \mathrm{y}$ and z axes in the whole positioning region, and then recorded together with the current coordinate $\overrightarrow{C_{12}}$. After calibration, 227 horizontal positions under three air gap conditions, respectively $110 \mathrm{~mm}, 160 \mathrm{~mm}$ and 210 mm , were tested to verify the positioning accuracy. The 227 horizontal positions are marked by red points in Figure 19, which include the positions on the outline of the quarter elliptical region and the positions on $y=x$. The minimum interval between
these test points is 1 cm . Finally, all the coordinates of the total 681 test points were output accurately without error. The results show that the positioning accuracy of 1 cm is achieved.


Figure 19. Horizontal positions for positioning accuracy verification.

## 6. Conclusions

In this paper, a magnetic positioning method based on the SWPDT system is proposed. A high integration of simultaneous power transfer, data transmission and position detection is achieved. The three-dimensional positioning accuracy achieves up to 1 cm . Compared to the conventional methods, the proposed positioning signal is transmitted by the auxiliary signal coils rather than the primary power coil. Thus, the operation of the primary high-power inverter will not be affected in the positioning process, and the online positioning can be achieved. The optimal locations for the auxiliary signal coils have been analyzed by finite element method (FEM) simulation, which are found to be the inner corners of the primary rectangular power coil. Since the signal coils for positioning are installed on the ground side, it can save the in-vehicle space and avoid the accuracy degrading due to the vehicle jolt. The amplitude measurement of the positioning signal is achieved by the data receiver circuit, which is immune to the power fundamental interference and ensures the online positioning accuracy. Moreover, all the communication needs in the positioning process can be satisfied well by SWPDT technology, and no extra RF communication hardware is needed.

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## References

1. ta Galigekere, V.P.; Pries, J.; Onar, O.C.; Su, G.J.; Anwar, S.; Wiles, R.; Seiber, L.; Wilkins, J. Design and implementation of an optimized 100 kW stationary wireless charging system for EV battery recharging. In Proceedings of the 2018 IEEE Energy Conversion Congress and Exposition (ECCE), Portland, OR, USA, 23-27 September 2018.
2. Li, W.; Zhao, H.; Deng, J.; Li, S.; Mi, C.C. Comparison study on SS and double-sided LCC compensation topologies for EV/PHEV wireless chargers. IEEE Trans. Veh. Technol. 2016, 65, 4429-4439. [CrossRef]
3. Zhang, Z.; Pang, H.; Georgiadis, A.; Cecati, C. Wireless power transfer-an overview. IEEE Trans. Ind. Electron. 2019, 66, 1044-1058. [CrossRef]
4. Budhia, M.; Covic, G.A.; Boys, J.T. Design and optimization of circular magnetic structures for lumped inductive power transfer systems. IEEE Trans. Power Electron. 2011, 26, 3096-3108. [CrossRef]
5. Budhia, M.; Boys, J.T.; Covic, G.A.; Huang, C. Development of a single-sided flux magnetic coupler for electric vehicle IPT charging systems. IEEE Trans. Ind. Electron. 2013, 60, 318-328. [CrossRef]
6. Zaheer, A.; Hao, H.; Covic, G.A.; Kacprzak, D. Investigation of multiple decoupled coil primary pad topologies in lumped IPT systems for interoperable electric vehicle charging. IEEE Trans. Power Electron. 2015, 30, 1937-1955. [CrossRef]
7. Kim, S.; Covic, G.A.; Boys, J.T. Comparison of tripolar and circular pads for IPT charging systems. IEEE Trans. Power Electron. 2018, 33, 6093-6103. [CrossRef]
8. Villa, J.L.; Sallan, J.; Sanz Osorio, J.F.; Llombart, A. High-misalignment tolerant compensation topology for ICPT systems. IEEE Trans. Ind. Electron. 2012, 59, 945-951. [CrossRef]
9. Lu, F.; Zhang, H.; Hofmann,H.; Mi, C. A dual-coupled LCC-compensated IPT system to improve misalignment performance. In Proceedings of the IEEE PELS Workshop Emerging Technologies: Wireless Power Transfer (WoW), Chongqing, China, 20-22 May 2017.
10. Zhao, L.; Thrimawithana, D.J.; Madawala, U.K. Hybrid bidirectional wireless EV charging system tolerant to pad misalignment. IEEE Trans. Ind. Electron. 2017, 64, 7079-7086. [CrossRef]
11. Zhao, L.; Thrimawithana, D.J.; Madawala, U.K.; Hu, A.P.; Mi, C.C. A misalignment-tolerant series-hybrid wireless EV charging system with integrated magnetics. IEEE Trans. Power Electron. 2019, 34, 1276-1285. [CrossRef]
12. Zhang, Z.; Krein, P.T.; Ma, H.; Tang, Y.; Zhou, J.; Xu, D. An inductive power transfer system design with large misalignment tolerance for EV charging. In Proceedings of the IEEE 27th International Symposium on Industrial Electronics, Cairns, Australia, 13-15 June 2018.
13. Wireless Power Transfer for Light-Duty Plug-in/Electric Vehicles and Alignment Methodology, SAE J2954 Recommended Practice. 2017. Available online: https://www.sae.org/standards/content/j2954_201605/ (accessed on 26 February 2020).
14. Chen, S.; Liao, C.; Wang, L. Research on positioning technique of wireless power transfer system for electric vehicles. In Proceedings of the IEEE Conference and Expo Transportation Electrification Asia-Pacific (ITEC Asia-Pacific), Beijing, China, 31 August-3 September 2014.
15. Tiemann, J.; Pillmann, J.; Bocker, S.; Wietfeld, C. Ultra-wideband aided precision parking for wireless power transfer to electric vehicles in real life scenarios. In Proceedings of the IEEE 84th Vehicular Technology Conference (VTC-Fall), Montreal, QC, Canada, 18-21 September 2016.
16. Ni, L.M.; Liu, Y.; Lau, Y.C.; Patil, A.P. LANDMARC: Indoor location sensing using active RFID. In Proceedings of the First IEEE International Conference on Pervasive Computing and Communications 2003 (PerCom 2003), Fort Worth, TX, USA, 26 March 2003.
17. Bouet, M.; dos Santos, A.L. RFID tags: Positioning principles and localization techniques. In Proceedings of the 2008 1st IFIP Wireless Days, Dubai, UAE, 24-27 November 2008.
18. Xu, H.; Ding, Y.; Li, P.; Wang, R.; Li, Y. An RFID indoor positioning algorithm based on Bayesian probability and K-Nearest Neighbor. Sensors 2017, 17, 1806. [CrossRef]
19. Xu, H.; Wu, M.; Li, P.; Zhu, F.; Wang, R. An RFID indoor positioning algorithm based on support vector regression. Sensors 2018, 18, 1504. [CrossRef] [PubMed]
20. Lee, K.; Kim, J.; Cha, C. Microwave-based wireless power transfer using beam scanning for wireless sensors. In Proceedings of the IEEE EUROCON 2019-18th International Conference on Smart Technologies, Novi Sad, Serbia, 1-4 July 2019.
21. Liu, L.; Niu, P.; Luo, D.; Guo, Y.; Sun, Y. A method for aligning of transmitting and receiving coils of electric vehicle wireless charging based on binocular vision. In Proceedings of the 2017 IEEE Conference on Energy Internet and Energy System Integration (EI2), Beijing, China, 26-28 November 2017.
22. Shieh, W.; Hsu, C.J.; Wang, T. Vehicle positioning and trajectory tracking by infrared signal-direction discrimination for short-range vehicle-to-infrastructure communication systems. IEEE Trans. Intell. Transp. Syst. 2018, 19, 368-379. [CrossRef]
23. Langer, D.; Thorpe, C. Sonar based outdoor vehicle navigation and collision avoidance. In Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems, Raleigh, NC, USA, 7-10 July 1992.
24. Han, W.; Chau, K.T.; Jiang, C.; Liu, W. Accurate position detection in wireless power transfer using magnetoresistive sensors for implant applications. IEEE Trans. Magn. 2018, 54, 4001205. [CrossRef]
25. Liu, X.; Han, W.; Liu, C.; Pong, P.W.T. Marker-free coil-misalignment detection approach using TMR sensor array for dynamic wireless charging of electric vehicles. IEEE Trans. Magn. 2018, 54, 4002305. [CrossRef]
26. Liu, X.; Liu, C.; Han, W.; Pong, P.W.T. Design and implementation of a multi-purpose TMR sensor matrix for wireless electric vehicle charging. IEEE Sens. J. 2019, 19, 1683-1692. [CrossRef]
27. Liu, X.; Liu, C.; Pong, P.W.T. TMR-sensor-array-based misalignment-tolerant wireless charging technique for roadway electric vehicles. IEEE Trans. Magn. 2019, 55, 4003107. [CrossRef]
28. Hwang, K.; Park, J.; Kim, D.; Park, H.H.; Kwon, J.H.; Kwak, S.I.; Ahn, S. Autonomous coil alignment system using fuzzy steering control for electric vehicles with dynamic wireless charging. Math. Probl. Eng. 2015, 2015, 205285. [CrossRef]
29. Hwang, K.; Cho, J.; Kim, D.; Park, J.; Kwon, J.H.; Kwak, S.I.; Park, H.H.; Ahn, S. An autonomous coil alignment system for the dynamic wireless charging of electric vehicles to minimize lateral misalignment. Energies 2017, 10, 315. [CrossRef]
30. Cortes, I.; Kim, W. Lateral position error reduction using misalignment-sensing coils in inductive power transfer systems. IEEE ASME Trans. Mechatron. 2018, 23, 875-882. [CrossRef]
31. Moghaddami, M.; Sundararajan, A.; Sarwat, A.I. Sensorless electric vehicle detection in inductive charging stations using self-tuning controllers. In Proceedings of the IEEE Transportation Electrification Conference (ITEC-India), Pune, India, 13-15 December 2017.
32. Gao, Y.; Duan, C.; Oliveira, A.A.; Ginart, A.; Farley, K.B.; Tse, Z.T.H. 3-D coil positioning based on magnetic sensing for wireless EV charging. IEEE Trans. Transp. Electrif. 2017, 3, 578-588. [CrossRef]
33. Jeong, S.Y.; Kwak, H.G.; Jang, G.C.; Choi, S.Y.; Rim, C.T. Dual-purpose nonoverlapping coil sets as metal object and vehicle position detections for wireless stationary EV chargers. IEEE Trans. Power Electron. 2018, 33, 7387-7397. [CrossRef]
34. Qian, Z.; Yan, R.; Wu, J.; He, X. Full-duplex high-speed simultaneous communication technology for wireless EV charging. IEEE Trans. Power Electron. 2019, 34, 9369-9373. [CrossRef]
35. Yan, R.; Qian, Z.; Wu, J.; He, X. Magnetic coupling positioning using simultaneous power and data transfer. In Proceedings of the 44th Annual Conference of IEEE Industrial Electronics Society, Washington, DC, USA, 21-23 October 2018.
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