



Article Piecewise Linear Power Flow Algorithm of DC Distribution Networks Considering Automatic Adjustment of VSC Control Strategy

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Abstract: Voltage source converter (VSC)-based DC distribution networks (DCDNs) can automatically adjust the control strategy of overloaded VSCs to adapt to the variation in renewable energy power, but it brings difficulties to the steady-state performance analysis of DCDNs. This paper presents a piecewise linear power flow (PLPF) algorithm to estimate the joint effect of power disturbance and VSC control strategy adjustment on steady-state performance. Firstly, according to the VSC power balance, the critical point of the VSC hitting the capacity limit is directly determined, and the power variations in each node before VSC control strategy adjustment are obtained. Then, the linear power flow is revised considering the VSC control strategy adjustment. Inversion of the block Jacobian matrix is used to improve the calculation speed of linear power flow revision. Finally, linear power flow calculation is performed in each stage, and the steady-state performance is obtained by using the superposition method. Simulation results show that the proposed PLPF model can estimate the steady-state performance faster and more simply.

Keywords: DC distribution network; droop control; linear power flow model; piecewise model

1. Introduction

The large-scale integration of renewable energy promotes the progress of high-voltage direct current (HVDC) technology based on the voltage source converter (VSC) [1,2]. The HVDC technologies have been developed through theoretical research and practical verification [3,4]. A series of HVDC projects have been commissioned to connect remote offshore wind farms and regions with large number of electricity customers [5,6].

With the rapid development of distributed photovoltaic (PV) systems as well as electric vehicle (EV) charging piles, a large number of distributed converters lead to significant power losses in distribution network [7]. The VSC-based DC distribution network (DCDN) is a promising way of supplying electricity in areas with a high penetration of PV systems and DC loads [8]. Besides reducing power losses, the advantages of DCDNs include improving power supply reliability and power quality, hosting more PVs and EVs, and so on [9]. The DCDN has become an important research direction in the field of active distribution networks.

In DC networks, the voltage level and power flow distribution are mainly controlled by the VSCs. Constant-voltage controlled VSCs and constant-power controlled VSCs keep converter voltage or converter power constant [10]. Different from the constant-voltage control and the constant-power control, the VSC voltage changes with the VSC power in a droop-controlled VSC. In droop-controlled DC networks, when the load powers or the PV



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). powers change randomly, all the droop-controlled VSCs regulate the DC voltage and share the power imbalance simultaneously [11]. The droop control strategy shows prominent advantages of high reliability and flexibility. The impact of droop control on power flow distribution has been of great interest to researchers in recent years [12].

The steady nodal voltages, VSC powers, and line powers of the entire DC grid can be obtained via accurate power flow calculation (PFC). However, in the conditions with high requirements of calculation speed, the application of a large amount of PFC is limited. Compared with accurate PFC, linear power flow models can directly calculate the steady DC voltage/power variation, which is also the basis for voltage control, optimal operation, and online power flow analysis [13]. A series of linear DC power flow models have been presented by considering different simplified conditions. An effective power flow model is proposed for droop-controlled VSCs, where the equivalent resistance is used to represent the effect of droop control on power flow [14]. Based on the equivalent resistance model, a linear model for estimating the power flow which accounts for DC line voltage drops is presented [15]. Further, a linear sensitivity model of nodal power to voltage is proposed for droop-controlled DC grids, and a quadratic network loss correction term is applied to improve the calculation accuracy with less calculation burden [16]. Ref. [17] proposed a linear power flow calculation method for a bipolar DC distribution network, where the steady-state model of flexible equipment is established based on the Taylor expansion.

The existing linear power flow models mainly concentrate the fixed VSC control strategy. With the high proportion of renewable energies, the operation environment of the DC grid is more complex. Due to the uncertainty of renewable energies, the DC grid must cope with various contingencies, which may lead to VSC outage or overload. In this circumstance, the existing linear power flow models lose efficacy. The power flow algorithms considering the adjustment of converter operation mode have been studied to tackle these issues. An analytical method was derived to address the power sharing problem after a converter outage in a droop-controlled DC system [18]. To obtain the critical point of the VSC hitting the capacity limit, a bisection algorithm-based analytical model is proposed to analyze the steady-state performance of droop-controlled DC systems after a converter hits its limits [19]. In the existing power flow algorithm, the power variations after VSC overload require iterative calculation, which impedes the application of the power flow model in the optimal operation and control of DC systems. There is no effective way to calculate the power flow distribution with the adjustable VSC control strategy. In DCDNs, the random variation in a high penetration of PVs and EVs may easily cause the VSC to reach the capacity limit [20] so that the corresponding VSC outputs constant power with the rated value. The existing linear power flow models cannot accurately estimate the steady-state performance of DCDNs.

The main contribution of this study is to present a more straightforward piecewise linear power flow (PLPF) model that can estimate the joint effect of power disturbance and VSC control strategy adjustment on steady-state performance. The advantages of the proposed PLPF algorithm are listed as follows:

- The critical point of the VSC hitting the capacity limit can be directly determined through one linear calculation according to the VSC power balance. Compared with the bisection algorithm, the proposed PLPF algorithm has the same computational accuracy and less calculation time;
- 2. The proposed PLPF algorithm is more straightforward and effective for the situation with multiple overloaded VSCs.

The rest of this paper is organized as follows: Section 2 discusses the influence of VSC control strategy adjustment on power flow distribution. Section 3 introduces the PLPF model. Section 4 discusses the simulation results. Finally, conclusions are presented in Section 5.

2. Linear Power Flow Model

2.1. Control Strategies of DCDNs

The typical control strategies of VSCs include the constant-voltage control, constantpower control, and droop control. Figure 1 shows the main control system of a VSC. For the droop-controlled VSC at node n, the relationship between the VSC voltage U_n and VSC power $P_{n,VSC}$ can be expressed as:

$$U_n = U_{n,\text{ref}} - k_n (P_{n,\text{VSC}} - P_{n,\text{ref}})$$
(1)

where $U_{n,ref}$ and $P_{n,ref}$ are the reference voltage and reference power of the VSC at node n, respectively; k_n is the droop coefficient of the VSC at node n.

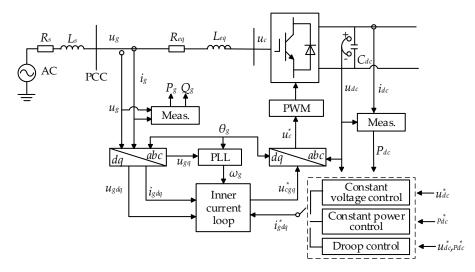


Figure 1. The main diagram and control system of a VSC.

2.2. Generalized Power Flow Model for VSC with Different Control Strategies

As shown in Figure 2, the improved equivalent line model proposed in [21] is used to express the droop node, constant-voltage node, and constant-power node.

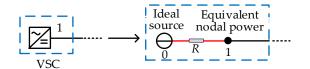


Figure 2. Generalized power flow model for VSC.

The parameters of the equivalent line model for different control modes are expressed in Table 1. The adjustment of the VSC control strategy can be represented by three parameters, including the voltage of the ideal source, line resistance, and equivalent nodal power. When the droop-controlled VSC hits the capacity limit and outputs constant power with the value of its capacity, the line resistance is set to infinite, and the equivalent nodal power is set to its capacity.

Table 1. Parameters of equivalent line for different control strategies.

Control Mode	Voltage of Ideal Source	Line Resistance	Equivalent Nodal Power
Droop control	Reference voltage	Product of droop coefficient and reference voltage	Negative reference power
Constant-voltage control	Reference voltage	0	Negative maximum power
Constant-power control	Reference voltage	∞	Negative reference power

2.3. Linear Power Flow Model for Nodal Voltages

The power flow of DCDNs can be expressed as:

$$P_{i,\text{PV}} - P_{i,\text{L}} + U_i \sum_{j=1}^h g_{ij} U_j = 0 \quad i \in M_{\text{L}}$$

$$-\frac{U_n - U_{n,\text{ref}}}{k_n} + P_{n,\text{ref}} + U_n \sum_{j=1}^h g_{nj} U_j = 0 \quad n \in M_{\text{D}}$$
(2)

where $P_{i,PV}$ and $P_{i,L}$ are the PV output power and load power of node *i*, respectively; g_{ij} is the admittance of the line from node *i* to node *j*; U_i and U_j are the voltage of node *i* and node *j*, respectively; *h* is the number of nodes; M_L is the set of load nodes and M_D is the set of droop nodes.

The nodal voltage variation due to the change in nodal injection power can be expressed as:

$$\Delta U = -J^{-1}\Delta P = S\Delta P \tag{3}$$

where *J* is the Jacobian matrix, *S* is the nodal voltage sensitivity matrix, ΔP represents the change in nodal injection power, and ΔU represents the change in nodal voltage.

In (3), ΔP includes the variation in equivalent nodal power, load power, and PV power. The line power P_{ij} of the line l_{ij} can be expressed as:

$$P_{ij} = U_i (U_i - U_j) g_{ij} \tag{4}$$

The line power variation due to the change in nodal injection power is:

$$\Delta P_{\rm L} = G \Delta U = G S \Delta P = T \Delta P \tag{5}$$

where ΔP_L represents the change in line power, *T* represents the sensitivity matrix of nodal injection power to line transmission power, and *G* is the derivative of voltage with respect to line power in (5).

The VSC power variation ΔP_{VSC} is equal to the sum of the power changes in all lines that are connected to the VSC, thereby considering the influence of line loss. The linear power flow model for VSC powers is:

$$\Delta P_{\rm VSC} = \sum \Delta P_{\rm L} = W \Delta P \tag{6}$$

where W represents the sensitivity matrix of nodal injection power to VSC power.

3. Piecewise Linear Power Flow Model to Represent the VSC Control Strategy Adjustment

3.1. Power Flow Analysis Considering VSC Control Strategy Adjustment

The simple two-terminal droop-controlled DCDN in Figure 3 is taken as an example to illustrate the influence of VSC control strategy adjustment on power flow distribution. The variation in VSC power and nodal voltage is briefly depicted in Figure 4.

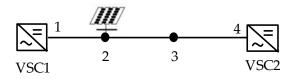


Figure 3. Simple two-terminal DCDN.

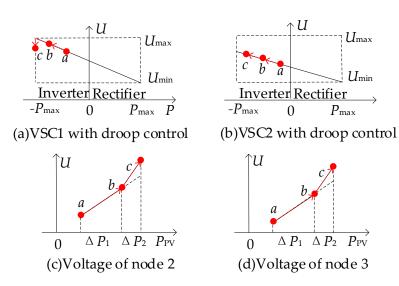


Figure 4. Influence of control strategy adjustment on power flow.

In Figure 4, with the increase in PV power, the operation point changes from a to b to c. As shown in Figure 4, when the PV power begins to increase, the power of the two droopcontrolled VSCs increases to share the PV power. The operation point changes from a to b. The linear model can be used to represent the voltage variation and VSC power variation. With the further increase in PV output power, one VSC reaches the capacity limit and keeps constant-power operation at that limit. The adjustment of the VSC control strategy leads to the change in sensitivity matrix in (3), (5), and (6). The updated linear model corresponding to the current operation point should be used to estimate the variations in voltage and VSC power.

3.2. Piecewise Linear Power Flow Model

For a fixed load level, the final steady-state performance is determined regardless of the transient responses process to the power disturbance. Referring to Figure 4, the voltage and power variation process caused by VSC control mode adjustment can be divided into different stages. In each stage, the linear power flow model can be used to calculate the variations in voltage and VSC power.

The difficulty is to determine the VSC control strategy and calculate the power variations in each stage in a straightforward way. To solve this problem, the nodal power variations in each stage are calculated by the sensitivity matrix in (6) according to the VSC power balance. The main process of PLPF calculation consists of the following steps:

Step 1: Formulate the initial linear power flow model.

Step 2: Calculate the power of each VSC through LPF model.

Step 3: If all the VSC powers are within the limit, calculate the variations in line powers and nodal voltages according to the linear power flow model, and go to step 8; otherwise, go to step 4.

Step 4: Calculate the nodal power variations before and after VSC control strategy adjustment.

Step 5: Update the linear power flow model after VSC control strategy adjustment.

Step 6: Calculate the variations in VSC powers, line powers, and nodal voltages before and after the VSC control strategy adjustment.

Step 7: Calculate the VSC powers, line powers and nodal voltages.

Step 8: Output the calculation results.

The flow chart of the centralized optimal control in DCDNs is shown in Figure 5.

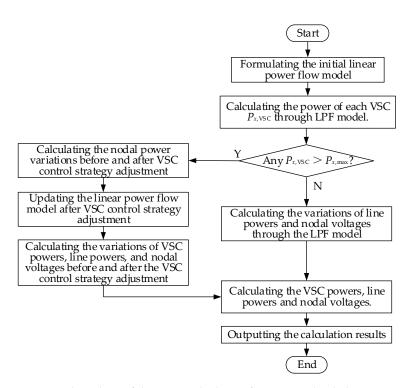


Figure 5. Flow chart of the PLPF calculation for one overloaded VSC.

The detailed explanations for the above steps are shown below:

In Step 1, the power flow calculation (PFC) is performed to obtain the nodal voltages and line powers. The LPF model expressed by (3), (5), and (6) is formulated.

In step 2, the power P_x of the VSC at node *x* considering the variations in load powers and renewable energy powers is:

$$P_x = P_{x,\text{ini}} + \Delta P_x = P_{x,\text{ini}} + \sum_{i=1}^h W_{i,x} \Delta P_i$$
(7)

where $P_{x,ini}$ is the initial power of the VSC at node x, ΔP_x is the VSC power variation in the VSC at node x, ΔP_i is the nodal power variation at node i, and $W_{i,x}$ is the sensitivity of power variation at node i to the VSC power at node x.

In step 3, the line powers and nodal voltages can be expressed as:

$$P_l = P_{l,\text{ini}} + \sum_{i=1}^h T_{i,l} \Delta P_i \tag{8}$$

$$U_j = U_{j,\text{ini}} + \sum_{i=1}^h S_{i,j} \Delta P_i \tag{9}$$

where P_l is the power of line l; $P_{l,ini}$ is the initial power of line l; $U_{j,ini}$ is the initial voltage of node j; $T_{i,l}$ represents the sensitivity of transmission power of line l to nodal injection power at node i; and $S_{i,j}$ represents the sensitivity of voltage of node j to nodal injection power at node i.

In step 4, it is supposed that the power of the VSC at node *x* is larger than its capacity, and the power variation before the VSC control strategy adjustment is:

$$P_{x,\text{ini}} + \alpha \sum_{i=1}^{h} W_{i,x} \Delta P_i = P_{x,\text{max}}$$
(10)

where α is the proportion of the power variation before the VSC control strategy adjustment, and $P_{x,\max}$ is the capacity of the VSC at node *x*.

From (10), α can be expressed as:

$$\alpha = \begin{cases} 1 & \text{All VSC are within the power limit} \\ \frac{P_{x,\max} - P_{x,\text{ini}}}{\sum\limits_{i=1}^{h} W_{i,x} \Delta P_i} & \text{The VSC } x \text{ is beyond the power limit} \end{cases}$$
(11)

In step 5, the droop coefficient of the VSC that changes from droop control to constantpower control is set to infinite, and the LPF model is updated.

In step 6, the power variations can be divided into different stages. The VSC powers, line powers, and nodal voltages can be expressed as:

$$P_{x} = P_{x,\text{ini}} + \alpha \sum_{i=1}^{h} W_{i,x} \Delta P_{i} + (1 - \alpha) \sum_{i=1, i \neq x}^{h} W_{i,x,s2} \Delta P_{i}$$
(12)

$$P_{l} = P_{l,\text{ini}} + \alpha \sum_{i=1}^{h} T_{i,l} \Delta P_{i} + (1 - \alpha) \sum_{i=1, i \neq x}^{h} T_{i,l,s2} \Delta P_{i}$$
(13)

$$U_{j} = U_{j,\text{ini}} + \alpha \sum_{i=1}^{h} S_{i,j} \Delta P_{i} + (1-\alpha) \sum_{i=1,i\neq x}^{h} S_{i,j,s2} \Delta P_{i}$$
(14)

where ΔP_x is the power variation in VSC x; ΔP_l is the power variation in line l; ΔU_j is the voltage variation in node j; $W_{i,x,s2}$ represents the sensitivity of transmission power of VSC x to nodal injection power at node i after VSC control strategy change; $T_{i,l,s2}$ represents the sensitivity of transmission power of line l to nodal injection power at node i after VSC control strategy change; $T_{i,l,s2}$ represents the sensitivity of voltage of node j to nodal injection power at node i after VSC control strategy change; and $S_{i,j,s2}$ represents the sensitivity of voltage of node j to nodal injection power at node i after VSC control strategy change.

It should be emphasized that when the VSC at node *x* changes from droop control to constant-power control, the power variation $(1 - \alpha) \times \Delta P_x$ of the VSC at node *x* should not be considered in the PFC process of next stage.

In step 7, the power variations can be divided into different stages. The VSC powers, line powers, and nodal voltages can be expressed as:

$$P_x = P_{x,\text{ini}} + \Delta P_x \tag{15}$$

$$P_l = P_{l,\text{ini}} + \Delta P_l \tag{16}$$

$$U_j = U_{j,\text{ini}} + \Delta U_j \tag{17}$$

3.3. Multiple Overloaded Converters

In step 7, when the power of the VSC at node y calculated by (15) is greater than its capacity, it means that multiple VSCs are overloaded. In this circumstance, the power of the VSC at node y should be expressed as:

$$P_{y,\text{ini}} + \alpha \sum_{i=1}^{h} W_{i,y} \Delta P_i + \beta \sum_{i=1, i \neq x}^{h} W_{i,y} \Delta P_i = P_{y,\text{max}}$$
(18)

where β is the proportion of the power variation before the VSC at node *y* control strategy adjustment.

For instance, the nodal voltage in this circumstance can be expressed as:

$$U_{j} = U_{j,\text{ini}} + \alpha \sum_{i=1}^{h} S_{i,j} \Delta P_{i} + \beta \sum_{i=1, i \neq x}^{h} S_{i,j,s2} \Delta P_{i} + (1 - \alpha - \beta) \sum_{i=1, i \neq x, i \neq y}^{h} S_{i,j,s3} \Delta P_{i}$$
(19)

where $S_{i,j,s3}$ represents the sensitivity of voltage of node *j* to nodal injection power at node *i* after the VSC control strategy is changed.

A DC distribution network with three VSCs is used to illustrate the conditions for different action scenario. Table 2 shows the conditions for each action scenario.

Table 2.	Conditions	for each	action	scenario.
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Scenario	No Overloaded VSCs	Only VSC1 Overload	VSC1 and VSC2 Overload
Conditions	$P_1 < P_{1,\max}, P_2 < P_{2,\max}, P_3 < P_{3,\max}$		$P_1 = P_{1,\max}, P_2 = P_{2,\max}, P_3 < P_{3,\max}$

The general flow chart of the PLPF calculation is shown in Figure 6. Especially, when multiple VSCs are out of the limit in the first calculation in step 4, the proportion of the power variation α for each overloaded VSC is calculated according to (13). The VSC with the minimum α is supposed to be the first overloaded VSC.

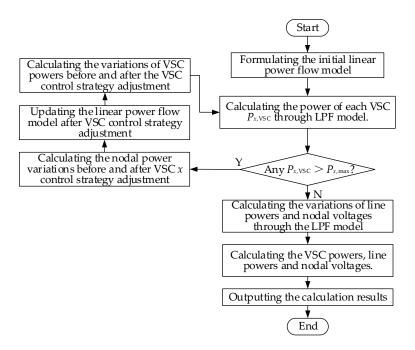


Figure 6. General flow chart of the PLPF calculation.

For the error analysis for the PLPF algorithm, refer to ref. [16].

4. Numerical Examples

4.1. Test System 1

Figure 7 shows the DCDN in Suzhou, China. The VSC capacity was set to 5 MW; for the detailed parameters of the system, refer to [21]. The rated DC voltage was ± 10 kV. The allowable voltage level was $\pm 10\%$ of the rated DC voltage. The VSCs were operated with a droop coefficient of 0.1 kV/MW and an operation reference power of 4 MW. The line parameters are shown in Table A1 of Appendix A. MATLAB 2022b with an Intel(R) Core(TM) i5-8350U CPU was used as the platform to implement the proposed strategy.

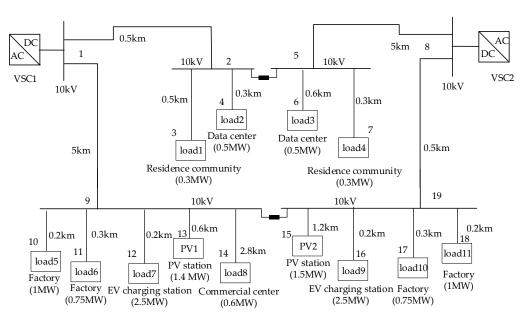


Figure 7. Single diagram of a realistic DCDN in Suzhou, China.

4.2. Accuracy Test of the Improved LPF Model

In the linear PFC (LPFC), the initial voltage was 1.0 p.u., and the initial nodal power variation was equal to the nodal power. The VSC power calculated via LPFC and PFC is shown in Table 3. The VSC1 power is less than the VSC capacity, and the maximum VSC power error of the proposed LPFC is 1.20%. The voltage comparisons are shown in Figure 8, and the maximum voltage error is 0.09%. In the situation with no VSC overload, the LPF model is accurate.

Table 3. Calculation results of VSC power in the situation with no VSC overload.

Alexanthere	VS	C1	VSC2		
Algorithm	Power (MW)	Error (%)	Power (MW)	Error (%)	
PFC	3.3457	-	4.5612	-	
LPFC	3.3065	1.17	4.5005	1.33	

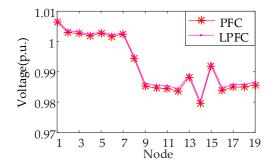


Figure 8. Calculation results of nodal voltages in the situation with no VSC overload.

The load and PV powers were set to 1.2 times the initial value to perform LPFC. The VSC power calculation results of PLPF calculation (PLPFC) are shown in Table 4. In the first round of PLPFC, the VSC powers of VSC1 and VSC2 are 3.96 MW and 5.40 MW, respectively. The power of VSC2 hits the limit and outputs the constant power with 5 MW. The second round of calculation was then performed under the new working conditions of VSC2, and the final power of VSC1 is 4.36 MW.

Algorithm		VSC1		VSC2	
		Power (MW)	Error (%)	Power (MW)	Error (%)
	PFC	4.5461	-	5.0000	-
LF	PF in [16]	3.9610	12.87	5.4025	8.50
PLPF	First round Second round	3.9610 4.3641	12.87 4.03	5.4025 5.0000	8.50 0

Table 4. Calculation results of VSC power in the situation with one overloaded VSC (1.2 times).

The maximum VSC power error of the proposed PLPF is 4.18%, which is less than the 12.96% of the LPF. The voltage comparisons among the PFC, LPFC, and PLPFC are shown in Figure 9. The maximum voltage errors of PLPF and LPF are 0.22% and 1.14%, respectively. The simulation results show that the proposed PLPF is more accurate than the LPF when the VSC overloads.

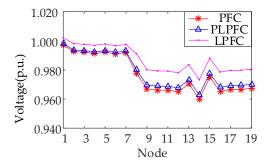


Figure 9. Calculation results of nodal voltages in the situation with one overloaded VSC (1.2 times).

Next, the accuracy of the PLPF in steady-state performance analysis was tested, considering the influence of power disturbances. Accurate PFC was performed based on the initial value of the load power and PV output power. Then, the load power and PV output power were increased by 20%. The results of VSC power obtained by PLPFC, PFC, and LPFC are shown in Table 5. The maximum error of VSC power of the proposed PSPFC is 0.0021%. The voltage comparisons among PFC, LPFC, and PLPFC are shown in Figure 10. The maximum voltage error of PLPF and LPF is 0.14% and 0.73%, respectively. In the steady-state performance analysis of DCDN, when the accurate voltages are provided to the PLPF model, the accuracy of the PLPFC can be further improved.

Algorithm		VSC1		VSC2	
		Power (MW)	Error (%)	Power (MW)	Error (%)
	PFC	4.5461	-	5.0000	-
LI	PF in [16]	3.6687	19.3	5.8391	16.78
PLPF	First round Second round	3.6687 4.5462	19.3 0.0021	5.8391 5.0000	16.78 0

Table 5. Calculation results of VSC power in the situation with one overloaded VSC (increased by 20%).

The accuracy and calculation time comparison of the proposed PLPF and the bisection algorithm in [19] are shown in Table 6. It can be seen that the power variations in each stage calculated by the proposed algorithm are the same as those of [19]. It is because the sensitivity matrix W in (6) is the same in the two models. The calculation time of the proposed PLPF algorithm is less than that of the bisection algorithm because the power variations in each stage are directly calculated according to the VSC power balance.

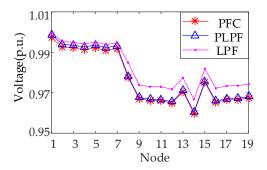


Figure 10. Calculation results of nodal voltages in the situation with one overloaded VSC (increased by 20%).

Table 6. Com	parison of bisec	tion algorithm and	PLPF algorithm	(DCDN in Suzhou).

Algorithm	Proportion of Power Variation in Stage 1	Number of Iterations	Calculation Time	
Proposed PLPF	0.3421	15	0.032 s	
Bisection algorithm in [19]	0.3421	2	0.057 s	

4.3. Test System 2

The proposed algorithm was tested with a large-scale three-terminal DCDN as shown in Figure 11 [22]. The rated DC voltage was ± 10 kV. The allowable voltage level was $\pm 10\%$ of the rated DC voltage. The load and PV output powers were set to 1.2 times the initial value. The parameters of VSCs are shown in Table 7. The line parameters are shown in Table A2 of Appendix A.

 Table 7. Parameters of VSCs.

VSC	Droop Coefficient	Reference Power	VSC Capacity
VSC1	0.1 kV/MW	6 MW	10 MW
VSC2	0.1 kV/MW	6 MW	10 MW
VSC3	0.1 kV/MW	4 MW	10 MW

Suppose that the load power and PV output power are increased by 40%. The obtained results of VSC power are shown in Table 8. The VSC2 hits the power limit and outputs the constant power with 10 MW. The maximum VSC power error of the proposed PLPF is 0.29%, which is less than 1.51% of the LPF.

Table 8. Calculation results of VSC power in the situation with one overloaded VSC (Three-terminal DCDN).

		VSC1		VSC2		VSC3	
A	lgorithm	Power (MW)	Error (%)	Power (MW)	Error (%)	Power (MW)	Error (%)
	PFC	8.6128	-	10.0000	-	7.1297	-
	LPF	8.5060	1.24%	10.0273	5.46	7.0220	1.51
DI DE	First round	8.5060	1.24%	10.0273	5.46	7.0220	1.51
PLPF	Second round	8.6335	0.24	10.0000	0	7.1508	0.29

The voltage comparisons are shown in Figure 12. The maximum voltage error of PLPF is 0.02%, which is less than the 0.21% of the LPF.

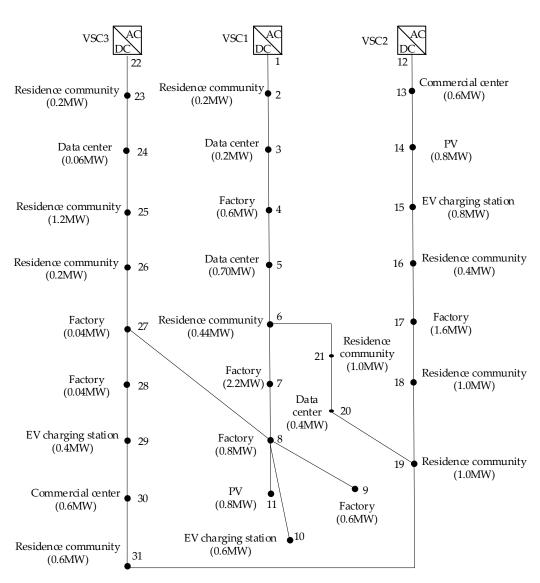


Figure 11. Three-terminal DCDN.

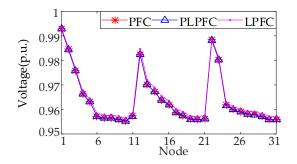


Figure 12. Calculation results of nodal voltages in the situation with two overloaded VSCs.

Next, the load power and PV output power were increased by 55% to analyze the circumstances with multiple overloaded VSCs. The VSC power calculation results are shown in Table 9. The VSC2 hits the capacity limit in the first round of calculations, and the VSC1 hits the capacity limit in the second round of calculations. The steady-state performance analysis was accomplished after three instances of LPFC. The maximum VSC power error of the proposed PLPF is 0.43%, which is less than 14.08% of the LPF. The voltage comparisons are shown in Figure 13, and the maximum voltage errors of PLPF and

LPF are 0.04% and 1.27%, respectively. The simulation results prove the accuracy of the proposed PLPF when VSCs are overloaded.

Table 9. Calculation results of VSC power in the situation with two overloaded VSCs.

		VSC1		VSC2		VSC3	
A	lgorithm	Power (MW)	Error (%)	Power (MW)	Error (%)	Power (MW)	Error (%)
	PFC	10.0000	-	10.0000	-	8.6450	-
	LPF	9.6087	3.91%	11.5966	15.97%	7.4282	14.07
	First round	9.6087	3.91%	11.5966	15.97%	7.4282	14.07
PLPF	Second round	10.1031	0	10.0000	0	8.5972	0.55
	Third round	10.0000	0	10.0000	0	8.6820	0.42

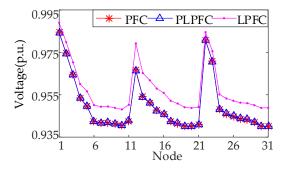


Figure 13. Calculation results of nodal voltages in the situation with two overloaded VSCs (increased by 55%).

The accuracy and calculation time comparison of the proposed PLPF and the bisection algorithm in [19] are shown in Table 10. The simulation results show that the proposed PLPF algorithm obtains the same results with fewer iterations and less calculation time compared with the bisection algorithm.

Algorithm	Proportion of Power Variation in Stage 1	Proportion of Power Variation in Stage 2	Number of Iterations	Calculation Time
PLPF	0.6211	0.3588	3	0.143 s
Bisection algorithm in [19]	0.6211	0.3588	27	0.293 s

Table 10. Comparison of bisection algorithm and PLPF algorithm (Three-terminal DCDN).

5. Conclusions

In this paper, a PLPF algorithm is presented to estimate the joint effect of power disturbance and VSC control strategy adjustment on the steady-state performance. In the proposed PLPF algorithm, the power variations before and after VSC overload can be directly calculated by the power sensitivity. The proposed PLPF algorithm is accurate enough for the situation with multiple overloaded VSCs, and the Maximum error of VSC power is less than 4%. Compared with the bisection algorithm, the proposed PLPF algorithm has the same computational accuracy only with half the calculation time of the bisection algorithm. The proposed PLPF algorithm provides a more accurate and straightforward way to estimate the steady-state performance.

Limited by the article space, only the principle of the PLPF algorithm was studied in this work. The application of the PLPF model in the optimization and planning of DC distribution networks can be studied in future work.

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Nomenclature

$U_{n,\mathrm{ref}}$	Reference voltage of the VSC at node n	W	Sensitivity matrix of nodal injection power to VSC power
$P_{n,\mathrm{ref}}$	Reference power of the VSC at node <i>n</i>	$P_{x,ini}$	Initial power of the VSC at node <i>x</i>
k _n	Droop coefficient of the VSC at node <i>n</i>	ΔP_x	VSC power variation in the VSC at node <i>x</i>
$P_{i,\mathrm{PV}}$	PV output power of node <i>i</i>	ΔP_i	Nodal power variation at node <i>i</i>
$P_{i,L}$	Load power of node <i>i</i>	$W_{i,x}$	Sensitivity of power variation at node <i>i</i> to the VSC power at node <i>x</i>
8ij	Admittance of the line from node <i>i</i> to node <i>j</i>	$T_{i,l}$	Sensitivity of transmission power of line <i>l</i> to nodal injection power at node <i>i</i>
U_i	Voltage of node <i>i</i>	S _{i,j}	Sensitivity of voltage of node <i>j</i> to nodal injection power at node <i>i</i>
$M_{\rm L}$	Set of load nodes	α	Proportion of the power variation before the VSC control strategy adjustment
$M_{\rm D}$	Set of droop nodes	$P_{x,\max}$	Capacity of the VSC at node <i>x</i>
S	Nodal voltage sensitivity matrix	P _{l,ini}	Initial power of line <i>l</i>
ΔP	Change in nodal injection power	U _{j,ini}	Initial voltage of node <i>j</i>
ΔU	Change in nodal injection power		Sensitivity of transmission power of
	_	$W_{i,x,s2}$	VSC <i>x</i> to nodal injection power at node <i>i</i> after VSC control strategy change
$\Delta P_{\rm L}$	Change in line power	$T_{i,l,s2}$	Sensitivity of transmission power of line <i>l</i> to nodal injection power at node <i>i</i> after VSC control strategy change
	Sensitivity matrix of nodal injection		Sensitivity of voltage of node <i>j</i> to nodal
Т	power to line transmission power	S _{i,j,s2}	injection power at node <i>i</i> after VSC control strategy change
G	Derivative of voltage with respect to		Proportion of the power variation
-	line power	β	before the VSC at node <i>y</i> control strategy adjustment
	Sensitivity of voltage of node <i>j</i> to nodal	$P_{x,\max}$	Capacity of the VSC at node <i>x</i>
S _{i,j,s3}	injection power at node <i>i</i> after the VSC control strategy is changed	x jiiux	1 5
VSC	Voltage source converter	PV	Photovoltaic
	DC distribution network	EV	Electric vehicle
PLPF	Piecewise linear power flow	PFC	Power flow calculation
HVDC	High-voltage direct current		

Appendix A

Table A1. Line parameter of the test system 1.

Head Node	End Node	Line Resistance (Ω)	Head Node	End Node	Line Resistance (Ω)
1	2	0.1708	9	12	0.0683
2	3	0.1025	9	13	0.2050
2	4	0.2050	9	14	0.9567
2	5	0.0170	9	15	0.0170
5	6	0.2050	19	15	0.4100
5	7	0.1025	19	16	0.0683
5	8	1.7080	19	17	0.1025
1	9	1.7080	19	18	0.0683
9	10	0.0680	19	8	0.1708
9	11	0.1025			

Table A2. Line parameter of the test system 2.

Head Node	End Node	Line Resistance (Ω)	Head Node	End Node	Line Resistance (Ω)
1	2	0.1944	17	18	0.0786
2	3	0.2096	18	19	0.0393
3	4	0.2358	19	20	0.0786
4	5	0.0917	20	21	0.0524
5	6	0.2096	22	23	0.2268
6	7	0.0393	24	25	0.5371
7	8	0.0405	25	26	0.0524
8	9	0.1048	26	27	0.0405
8	10	0.2358	27	28	0.0393
8	11	0.1048	28	29	0.0262
12	13	0.2430	29	30	0.1048
13	14	0.0655	30	31	0.2358
14	15	0.0655	6	21	0.1310
15	16	0.0655	19	31	0.0393
16	17	0.0393	8	27	0.1310

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