



Article Strain Engineering in Ni-Co-Mn-Sn Magnetic Shape Memory Alloys: Influence on the Magnetic Properties and Martensitic Transformation

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Abstract: Ni-Mn-Sn ferromagnetic shape memory alloys, which can be stimulated by an external magnetic field, exhibit a fast response and have aroused wide attention. However, the fixed and restricted working temperature range has become a challenge in practical application. Here, we introduced strain engineering, which is an effective strategy to dynamically tune the broad working temperature region of Ni-Co-Mn-Sn alloys. The influence of biaxial strain on the working temperature range of Ni-Co-Mn-Sn alloy was systematically investigated by the ab initio calculation. These calculation results show a wide working temperature range (200 K) in Ni₁₄Co₂Mn₁₃Sn₃ FSMAs can be achieved with a slight strain from 1.5% to -1.5%, and this wide working temperature range makes Ni₁₄Co₂Mn₁₃Sn₃ meet the application requirements for both low-temperature and high-temperature (151–356 K) simultaneously. Moreover, strain engineering is demonstrated to be an effective method of tuning martensitic transformation. The strain can enhance the stability of the Ni₁₄Co₂Mn₁₃Sn₃ martensitic phase. In addition, the effects of strain on the magnetic properties and the martensitic transformation are explained by the electronic structure in Ni₁₄Co₂Mn₁₃Sn₃ FSMAs.

Keywords: martensitic transformation; ferromagnetic shape memory alloys; first-principal calculations; Ni-Co-Mn-Sn; strain engineering

1. Introduction

Ni-Mn-Sn ferromagnetic shape memory alloys (FSMAs) with various related magnetic effects, including excellent magnetocaloric effect (MCE) [1,2], extraordinary magnetic shape memory effect (MSME) [3–5], and magnetoresistance effect (MR) [6,7]. These multifunctional properties are attributable to the coupling between the magnetic and structural transitions by the magnetic field [8–10], i.e., magnetic field-induced martensitic transformation (MFIMT). It is the magnetic field-driven shape memory behavior that makes ferromagnetic shape memory alloys different from conventional shape memory alloys, which must be actuated through temperature. The application of magnetic fields is fast and easy, and its fast response to magnetic fields makes this alloy more widely used than conventional shape memory alloys. Moreover, Ni-Mn-Sn FSMAs are cheap, non-toxic, and have simple fabrication processes, which highlights their advantages over conventional shape memory alloys. Although Ni-Mn-Sn FAMAs have so many excellent properties, the relatively narrow working temperature range is still a key drawback in extensive practical application [11,12]. Previous studies have pointed out that the narrow working temperature



Citation: Xia, Q.; Tan, C.; Han, B.; Tian, X.; Zhao, L.; Zhao, W.; Ma, T.; Wang, C.; Zhang, K. Strain Engineering in Ni-Co-Mn-Sn Magnetic Shape Memory Alloys: Influence on the Magnetic Properties and Martensitic Transformation. *Materials* **2022**, *15*, 5889. https:// doi.org/10.3390/ma15175889

Academic Editor: Francesco Iacoviello

Received: 16 July 2022 Accepted: 23 August 2022 Published: 26 August 2022

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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). of Ni-Mn-Sn alloys is mainly near room temperature or slightly below it [13–20], which is just more beneficial to magnetic solid-state refrigeration. However, for the automotive, manufacturing, and energy exploration industries, the high working temperature region of the alloys is needed [21,22]. Similarly, a working temperature range lower than 270 K is needed for several space solutions [23]. In addition, the working temperature is very sensitive to constituent elements. That is, the working temperature region with fixed components is also fixed, which also increases the difficulty of widening the working temperature range is an urgent problem to be solved in Ni-Mn-Sn alloys.

Strain engineering is an efficient method to enhance the properties of functional materials [24–27]. Experimentally, Huang et al. found that uniaxial strain will be an effective means to control thermal effects (such as giant MCE and elastocaloric effects). A significant cooling level of about 4 K is measured when the strain is released [28]. Yang et al. observed that the martensitic transformation temperature (T_M) increased with the increase in uniaxial strain in Ni_{43.5}Co_{6.5}Mn₃₉Sn₁₁ [29]. In addition, Zhao et al. also measured that the refrigerating temperature region increased by 6 K to 10 K in Ni₄₃Co₇Mn₃₉Sn₁₁ films with applying strain [30]. It can be seen that stress engineering is a very effective method to improve many properties of the system. However, few studies have been able to draw on any systematic research on the influence of biaxial strain on the working temperature in the Ni-Mn-Sn system.

The stable MFIMT and the dynamical working temperature are necessary for a tunable broad working temperature region in Ni-Mn-Sn. For a stable MFIMT, the alloys must be ferromagnetic in the austenitic phase (FM) and antiferromagnetic in the martensitic phase (AF) for a stable MFIMT (AFM). For the dynamical working temperature, the alloys need to require two conditions. (1) Both T_M and Curie temperature (T_C) need to be dynamic. (2) Keeping $T_{\rm M}$ lower than $T_{\rm C}$. In addition, from the view of calculations, the large magnetization (ΔM) between the austenitic and martensitic phases is beneficial to the stable MFIMT [5]. The total energy difference (ΔE_{A-M}) between the austenitic phase and martensitic phase and the total energy difference (ΔE_{P-F}) between the ferromagnetic austenitic phase and paramagnetic austenitic phase play important roles in predicting the working temperature in alloys [5,31,32]. The $T_{\rm M}$ and $T_{\rm C}$ are increasing with the increase in the ΔE_{A-M} and ΔE_{P-F} , respectively [31,33]. In light of this, we calculated the ΔM , ΔE_{A-M} . and ΔE_{P-F} with the different strains through first-principles calculations. The results show that the value of ΔM of Ni-Mn-Sn alloys is too small to meet the stable MFIMT. Thus, to improve the value of ΔM and $\Delta E_{P.F}$, we choose the method of doping elements (Co to substitute for Ni atoms) [34,35]. In this way, Ni-Co-Mn-Sn alloys not only have a stable MFIMT but also have a dynamic working temperature. It is a high-quality candidate material for dynamically adjusting the working temperature region.

In the present paper, we aim to propose a strategy to adjust the broad working temperature of Ni-Co-Mn-Sn alloys by strain (from 200 K to 370 K). By using the first-principles calculation, the influences of strain on the magnetic properties, the martensitic phase transformation (MPT), and the working temperature of the alloys have been comprehensively studied. According to the results, a small strain can significantly change the working temperature and maintain the stable MFIMT, and the wide working temperature region of 168 K to 330 K can be predicted under strain from 0% to -1.5% in Ni₁₄Co₂Mn₁₃Sn₃ alloys. In addition, we discussed the physical mechanism of magnetic and martensitic transformation of the Ni₁₄Co₂Mn₁₃Sn₃ alloy through the electronic structure.

2. Calculation Method

The Vienna Ab initio Simulation Package (VASP) code is used to reveal the magnetic properties [36,37], phase structures, and electronic structures of Ni-Co-Mn-Sn FSMAs. All works were performed on the basis of the density functional theory (DFT). As the exchange–correlation functional, we used the Perdew–Burke–Ernzerhof (PBE) method and the generalized gradient approximation (GGA) [38]. For Ni-Mn-Sn FSMAs, a k-mesh of

 $3 \times 6 \times 6$ is used for two phases. The cut-off energy is 500 eV. The $L2_1$ austenite structure (Fm3m) of Ni₁₆Mn₁₃Sn₃ with three inequivalent Wyckoff positions (4a, 4b, 8c) is shown in Figure 1a. The Sb and Mn atoms occupy 4a (0, 0, 0) and 4b (0.50, 0.50, 0.50) positions respectively and Ni atoms occupy the 8c ((0.25, 0.25, 0.25) and (0.75, 0.75, 0.75)) sites. In addition, the calculation method used in the transformation process from austenite to martensite is tetragonal distortion. That is, on the premise of keeping the cell volume unchanged, the optimized austenite structure is subjected to lattice distortion with different tetragonal distortion rates c/a so as to obtain the most stable martensite structure. As seen in Figure 1b, we substituted Co atoms for Ni atoms directly in our study, and Mn_{Sn} is the designation for the excess Mn atoms at the deficient Sn atoms. The Mn atoms that remain at their sites are called Mn_{Mn} in the $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 0, 1, 2) FSMAs. For both the austenitic and martensitic phases, we calculated two situations: the magnetic properties of $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 0, 1, 2) alloys are FM states and AFM states. The FM configuration was set by magnetic moments of all Mn atoms (Mn_{Sn} and Mn_{Mn}) parallel to each other. AFM configuration was decided by magnetic moments of Mn_{Sn}, which are opposite in the direction of the magnetic moments of the Mn_{Mn}. According to the VASP user manual [39], the calculation of spin polarization requires the parameter ISPIN = 2, while the setting of FM and AFM is determined by the parameter MAGMOM. Therefore, the spin polarization of both ferromagnets and antiferromagnets can be achieved by VASP. In first-principles calculations, we simulate biaxial strain by changing lattice vectors directly. That is, fixing the lattice constant in the c-axis while relaxing the lattice constants in the a-axis and b-axis. It is worth mentioning that 0% represents no deformation, positive deformation represents stretching, and negative deformation represents compression.



Figure 1. (a) Crystallographic structure in $Ni_{16}Mn_{13}Sn_3$ austenitic phase. (b) Crystallographic structure in $Ni_{15}CoMn_{13}Sn_3$ austenitic phase.

3. Results and Discussion

First, we investigated the two phasic structures, martensitic transition and magnetic properties of the Ni₁₆Mn₁₃Sn₃. Table 1 shows the results of our calculations for the magnetic properties and equilibrium lattice parameters of the Ni₁₆Mn₁₃Sn₃ alloys. For the Ni₁₆Mn₁₃Sn₃ austenitic phase, the AFM state of the alloy is low energy, and the equilibrium lattice parameter is 5.94 Å. The magnetic ground state and lattice constant are in good agreement with other theoretical values [40]. In the Ni₁₆Mn₁₃Sn₃ martensitic phase, the FM state has higher energy and is more unstable than the AFM state at *c/a*~1.35. That is, austenite and martensite phase are AFM states under 0% strain. This is also consistent with the theoretical results [3]. According to the energy corresponding to 0% strain in Figure 2, the energy of AFM austenite is higher than that of AFM martensite, so MPT will occur, which is a prerequisite for shape memory alloys. This is also verified experimentally [41]. The above results confirm the correctness of our calculation, so we can apply biaxial strain based on it, and then we calculated the total energies *E* of the Ni₁₆Mn₁₃Sn₃ austenitic phase

and martensitic phase with strain $(-1.5 \times 1.5\%)$, as shown in Figure 2a,b respectively, to reveal the effect of strain on the phase structures, MPT, and magnetic properties. Figure 2a indicates that the energy of the AFM state is lower than that in the FM state for the austenite phase, and the total energies E of $Ni_{16}Mn_{13}Sn_3$ austenitic phase firstly decrease with strain from 1.5% to 0% and then increase with strain from 0% to -1.5%. For the Ni₁₆Mn₁₃Sn₃ martensitic phase, the total energy *E* of both FM and AFM increases with strain from 1.5% to -1.5%, and the AFM state energies are lower than the FM state energies. Therefore, we can conclude that austenite and martensite of Ni₁₆Mn₁₃Sn₃ alloy are still in AFM state under the application of biaxial strain; that is, the biaxial strain will not affect the magnetic ground state of the system. In addition, the value of ΔE_{A-M} and ΔE_{P-F} in Ni₁₆Mn₁₃Sn₃ alloys under strain $(-1.5 \times 1.5\%)$ are shown in Figure 3 to show the impact of strain on $T_{\rm M}$ and $T_{\rm C}$. It is obvious that the $\Delta E_{\rm A-M}$ increases with strain, while the $\Delta E_{\rm P-F}$ decrease with strain under strain from 1.5% to -1.5%. This shows that $T_{\rm M}$ and $T_{\rm C}$ increase with the increase in ΔE_{A-M} and ΔE_{P-F} , respectively. According to the results, applying strain can tune the working temperature of $Ni_{16}Mn_{13}Sn_3$ alloys. Based on the above results, it can be concluded that the stability of austenite will be reduced no matter whether biaxial compressive strain or biaxial tensile strain is applied. However, the stability of martensite increases with compressive strain and decreases with tensile strain. Moreover, the biaxial strain does not affect the occurrence of MPT and the most stable magnetic configuration of each phase.

Table 1. Equilibrium lattice parameters, total spin moments and magnetic state of the cubic austenite (Cub.) and tetragonal non-modulated martensite (Tet.) for $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 0, 1, 2) alloys with strain ($-1.5 \sim 1.5\%$).

Alloys	Strain %	Phase	a Å	с Å	M _t μB	Δ <i>M</i> μΒ	Magnetic State FM/AFM
Ni ₁₆ Mn ₁₃ Sn ₃	-1.5	Cub.	5.85	5.94	1.36	0.06	AFM
		Tet.	5.30	7.26	1.42		AFM
	-1.0	Cub.	5.88	5.94	1.37	0.05	AFM
		Tet.	5.33	7.26	1.42		AFM
	-0.5	Cub.	5.91	5.94	1.38	0.04	AFM
		Tet.	5.35	7.26	1.42		AFM
	0	Cub.	5.94	5.94	1.39	0.04	AFM
		Tet.	5.38	7.26	1.43		AFM
	0.5	Cub.	5.97	5.94	1.40	0.03	AFM
		Tet.	5.41	7.26	1.43		AFM
	1.0	Cub.	6.00	5.94	1.41	0.02	AFM
		Tet.	5.43	7.26	1.43		AFM
	1.5	Cub.	6.03	5.94	1.42	0.01	AFM
		Tet.	5.46	7.26	1.43		AFM
	-1.5	Cub.	5.83	5.92	1.42	0.02	AFM
		Tet.	5.35	7.06	1.44		AFM
Ni ₁₅ CoMn ₁₃ Sn ₃	-1.0	Cub.	5.86	5.92	1.44	0.01	AFM
		Tet.	5.37	7.06	1.45		AFM
	-0.5	Cub.	5.89	5.92	1.44	0.01	AFM
		Tet.	5.40	7.06	1.45		AFM
	0	Cub.	5.92	5.92	1.46	0	AFM
		Tet.	5.43	7.06	1.46		AFM
	0.5	Cub.	5.95	5.92	1.47	0	AFM
		Tet.	5.46	7.06	1.47		AFM
	1.0	Cub.	5.98	5.92	1.49	0.01	AFM
		Tet.	5.48	7.06	1.48		AFM
	1.5	Cub.	6.01	5.92	1.50	0.01	AFM
		Tet.	5.51	7.06	1.49		AFM

Alloys	Strain %	Phase	a Å	с Å	M _t μB	Δ <i>M</i> μΒ	Magnetic State FM/AFM
Ni ₁₄ Co ₂ Mn ₁₃ Sn ₃	-1.5	Cub.	5.84	5.93	6.98	5.48	FM
		Tet.	5.32	7.15	1.50		AFM
	-1.0	Cub.	5.87	5.93	7.00	5.50	FM
		Tet.	5.35	7.15	1.50		AFM
	-0.5	Cub.	5.90	5.93	7.03	5.51	FM
		Tet.	5.37	7.15	1.52		AFM
	0	Cub.	5.93	5.93	7.06	5.54	FM
		Tet.	5.40	7.15	1.52		AFM
	0.5	Cub.	5.96	5.93	7.08	5.56	FM
		Tet.	5.43	7.15	1.52		AFM
	1.0	Cub.	5.99	5.93	7.10	5.58	FM
		Tet.	5.45	7.15	1.52		AFM
	1.5	Cub.	6.02	5.93	7.13	5.58	FM
		Tet.	5.48	7.15	1.55		AFM



Figure 2. Strain change $(-1.5 \sim 1.5\%)$ of the total energies of Ni₁₆Mn₁₃Sn₃ alloys. (**a**) the austenitic phase. (**b**) the martensitic phase.

Table 1. Cont.



Figure 3. Strain change (-1.5-1.5%) of ΔE_{A-M} and ΔE_{P-F} for Ni₁₆Mn₁₃Sn₃.

In order to tune the working temperature of alloys, alloys must have stable MFIMT. The ΔM is larger, and the MFIMT is more stable [41,42]. Therefore, we calculated the ΔM of Ni₁₆Mn₁₃Sn₃ alloys with strain in Table 1. Table 1 further accurately shows that the ΔM of Ni₁₆Mn₁₃Sn₃ is very small, and the strain has a weak effect on the value of ΔM (0.06–0.01 µB). The low ΔM cannot satisfy the stable MFIMT. Therefore, the biaxial strain alone cannot satisfy the stable MFIMT, which is a necessary condition for an adjusted wide working temperature region. Fortunately, the Co element enhances ferromagnetism in the austenitic phase and $T_{\rm C}$ of Ni₁₆Mn₁₃Sn₃ alloys. Thus, the strain may be an efficacious strategy to adjust the wide working temperature of Ni-Co-Mn-Sn.

The impact of Co doping on the physical properties of the Ni-Co-Mn-Sn system, particularly on the operating temperature, must also be taken into account. We first evaluate the equilibrium lattice parameters and magnetic properties of the $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 1, 2) and present them in Table 1 to show the change in phase structures, MPT, and magnetic properties of the Ni₁₆Mn₁₃Sn₃ with Co doping. The findings demonstrate that as Co increases, the equilibrium lattice parameters of the $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 1, 2) austenitic phases increase from 5.91 Å to 5.93 Å. The change of Ni_{16-x}Co_xMn₁₃Sn₃ (x = 1, 2) lattice constant can be attributed to the fact that the atomic radius of the substitution elements is slightly larger than that of the substituted element, and the lattice parameters are close to the value of the experiment (5.987 Å) and theory (5.973 Å) [43,44]. The origin of the experimental error is the slight difference between the actual compound and the nominal compound, and then the DFT calculation is carried out at T = 0 K, while the equilibrium lattice constant measured by XRD is carried out at room temperature. The theoretical error may be caused by the error between different calculation software. The austenitic $Ni_{14}Co_2Mn_{13}Sn_3$ phase is the FM state, whereas the martensitic phase is the AFM state, and there is a large ΔM (5.48 µB) between these two phases as shown in Table 1. This is also consistent with the experimental facts (6.68 μ B) [45]. In short, the Ni₁₄Co₂Mn₁₃Sn₃ alloys meet the stable MFIMT, and the strain method may be an efficient strategy to tune the wide working temperature of Ni₁₄Co₂Mn₁₃Sn₃ alloys.

Subsequently, we calculated the total energies of $Ni_{14}Co_2Mn_{13}Sn_3$ alloys with strain (-1.5~1.5%) and shown in Figure 4 to show the impact of the magnetic properties and working temperature on this alloy. It is obvious that the total energies of austenitic phases firstly decrease with strain (-1.5~0%) and then increase with strain (0–1.5%), and FM states are the most stable magnetic configuration for austenitic phases. The total energies of martensitic phases increase with strain (-1.5~1.5%), as shown in Figure 4b. Moreover,

the most stable magnetic configuration of martensitic phases is AFM states. Combined with (a) and (b) of Figure 4, it can be seen that the energy of AFM martensite is always less than that of FM austenite under the action of biaxial strain. It shows that the alloy will undergo magnetic structure coupling transformation, which further confirms that there is a large magnetic moment difference in the system. To show the change of $T_{\rm M}$ and $T_{\rm C}$ of Ni₁₄Co₂Mn₁₃Sn₃ alloys with strain, we listed the $\Delta E_{\rm A-M}$ and $\Delta E_{\rm P-F}$ in Table 2. The value of ΔE_{A-M} increase with strain from 1.5% to -1.5%, while the value of ΔE_{P-F} decrease with strain from 1.5% to -1.5%. The results show the strain can increase $T_{\rm M}$ and decrease $T_{\rm C}$. In consideration of the wide working temperature of Ni₁₄Co₂Mn₁₃Sn₃ alloys, one of the conditions is that $T_{\rm C}$ must be higher than $T_{\rm M}$. Therefore, we need to evaluate the value of $T_{\rm M}$ and $T_{\rm C}$. Generally, the $T_{\rm M}$ and $T_{\rm C}$ increase linearly with $\Delta E_{\rm A-M}$ and ΔE_{P-F} in Ni-Mn-based Heusler alloys. To further explore the relationship between T_M and $\Delta E_{\text{A-M}}$, as depicted in Figure 5, we made the T_{M} and $\Delta E_{\text{A-M}}$ fitting curves [1,10,34,35,46–51]. According to the Heisenberg model and Stoner theory [52], the relationship of $T_{\rm M}$ and $\Delta E_{\text{A-M}}$ is represented by $\Delta E_{\text{P-F}} = -k_B T c M/M_0$, where *M* is the magnetic moment at $T \neq 0$ K, and M_0 is the equilibrium magnetic moment at T = 0 K [53]. Based on it, we calculated the $T_{\rm M}$ and $T_{\rm C}$ of Ni₁₄Co₂Mn₁₃Sn₃ alloys with strain in Figure 6. It shows that the $T_{\rm M}$ and $T_{\rm C}$ increase with strain, and the $T_{\rm M}$ is lower than $T_{\rm C}$ with strain (-1.5~1.5%), which indicates that the alloy has been fully qualified to dynamically adjust the wide working temperature range. In addition, the changing trend of $T_{\rm M}$ is consistent with the experiment in other Ni-Mn based [54]; that is, the working temperature moves to a high temperature under the compressive strain. Then, with strain from 0% to -1.5%, the Ni₁₄Co₂Mn₁₃Sn₃ FSMAs show a tunable wide working temperature (from 168 K to 330 K), which meets the application in different temperatures. The operating temperature range of Ni₁₄Co₂Mn₁₃Sn₃ is 160 K; the wide range may be overestimated compared to experimental values. In short, the strain method is an effective way to tune effectively by using the strain approach for Ni₁₄Co₂Mn₁₃Sn₃ alloys.

Table 2. Calculated energy difference ΔE_{A-M} in meV/atom between the austenite and martensite phases, ΔE_{P-F} in meV/atom between the paramagnetic and ferromagnetic state, martensite transition temperature T_M and Curie temperature T_C in Ni_{16-x}Co_xMn₁₃Sn₃ (x = 0, 1, 2) alloys with strain (-1.5~1.5%).

Alloys	Strain %	ΔE_{A-M} (meV/atom)	ΔE_{P-F} (meV/atom)	<i>Т</i> _М (К)	Т _С (К)
	-1.5	31.7	385.7	405	397
	-1.0	29.6	387.8	378	399
	-0.5	27.6	390.0	353	401
Ni ₁₆ Mn ₁₃ Sn ₃	0	24.6	393.3	314	405
	0.5	22.3	395.2	285	407
	1.0	19.4	397.6	248	409
	1.5	18.5	400.7	236	412
	-1.5	30.8	392.6	394	404
	-1.0	28.1	395.9	359	407
	-0.5	26.8	397.7	343	409
Ni ₁₅ CoMn ₁₃ Sn ₃	0	23.4	398.2	299	410
	0.5	21.6	403.4	276	415
	1.0	18.7	407.3	239	419
	1.5	17.8	410.4	227	422
	-1.5	25.8	399.6	330	411
	-1.0	22.9	402.1	293	414
	-0.5	19.0	404.8	243	416
Ni ₁₄ Co ₂ Mn ₁₃ Sn ₃	0	13.2	406.9	168	419
	0.5	12.7	410.7	162	423
	1.0	9.8	413.8	125	426
	1.5	7.2	415.7	92	428



Figure 4. Strain change $(-1.5 \sim 1.5\%)$ of the total energies of Ni₁₄Co₂Mn₁₃Sn₃ alloys. (a) The austenitic phase. (b) the martensitic phase.



Figure 5. Relationship of ΔE_{A-M} and experimental T_M of alloys.



Figure 6. Strain change ($-1.5 \sim 1.5\%$) of the T_M and the T_C in Ni₁₄Co₂Mn₁₃Sn₃.

The total density of states (TDOS) of austenite and martensite in Ni₁₄Co₂Mn₁₃Sn₃ and the partial density of states (PDOS) of Mn_{Mn} and Mn_{Sn} of austenite and martensite in Ni₁₄Co₂Mn₁₃Sn₃ are shown in Figures 7–9 respectively to further illuminate the physical mechanism of the MPT and magnetic properties [55,56]. In addition, the phase stability is strongly dependent upon the TDOS at the Fermi level plays (E_F) [57,58]. Usually, the low TDOS indicates the stable phase in Ni₁₄Co₂Mn₁₃Sn₃ FSMAs. Figure 7a shows that the TDOS at E_F of strain (-1.5%, 1.5%) is similar in Ni₁₄Co₂Mn₁₃Sn₃ austenitic phases. The strain has a weak effect on austenitic phase stability. Moreover, for martensitic phases, the TDOS of -1.5% strain is lower than the TDOS of 1.5% strain at E_F, as shown in Figure 7b. The -1.5% strain decreases the instability of the Ni₁₄Co₂Mn₁₃Sn₃ martensitic phases. Then, the instability of the martensitic phase decreases, and the stability of austenitic phases show a few changes. In addition, austenite is a peak at E_F, while martensite is a pseudopotential valley. It shows that the stability of austenite is lower than that of martensite, which leads to the MPT according to the Jahn teller splitting effect. The results show that strain can tune the $T_{\rm M}$ of Ni₁₄Co₂Mn₁₃Sn₃ FSMAs.



Figure 7. Strain change (-1.5%, 1.5%) of the TDOS of Ni₁₄Co₂Mn₁₃Sn₃ alloys. (**a**) the austenitic phase. (**b**) the martensitic phase.



Figure 8. Strain change (-1.5%, 0%, 1.5%) of the PDOS of Ni₁₄Co₂Mn₁₃Sn₃ austenitic phase. (a) -1.5% strain, (b) 0% strain, (c) 1.5% strain.



Figure 9. Strain change (-1.5%, 0%, 1.5%) of the PDOS of $Ni_{14}Co_2Mn_{13}Sn_3$ martensitic phase. (a) -1.5% strain, (b) 0% strain, (c) 1.5% strain.

For the magnetic properties of Ni₁₄Co₂Mn₁₃Sn₃ austenitic phases, as can be seen in Figure 8b, the PDOS of Mn_{Mn} and Mn_{Sn} are similar and mostly up-spin states under the E_F. With applying strain, for Figure 8a,c, the PDOS of Mn_{Mn} and Mn_{Sn} has almost no change. This is indicated that the most stable magnetic configuration of austenitic phases is always FM, and this configuration is unaffected by strain. For martensite, in Figure 9b, the Mn_{Mn} is in up-states while the Mn_{Sn} is in down-states. With applying strain, the distribution of the PDOS of Mn_{Mn} and Mn_{Sn} is still different, the Mn_{Sn} is down-state, but the Mn_{Mn} is up-state, as shown in Figure 9a,c. The most stable magnetic configuration of austenite and martensite phases is AFM. In addition, the difference in the distribution of austenite and martensite also explains the existence of large ΔM . In conclusion, the strain cannot change the magnetic properties of Ni₁₄Co₂Mn₁₃Sn₃ FSMAs. The Ni₁₄Co₂Mn₁₃Sn₃ FSMAs meet the condition of the stable MFIMT.

4. Conclusions

To summarize, to achieve the tunable broad working temperature region of Ni-Mn-Sn alloys, we have systematically studied the influence of strain on the structures, MPT, and magnetic properties $Ni_{16-x}Co_xMn_{13}Sn_3$ (x = 0, 1, 2) by first-principles calculation. The value of ΔE_{A-M} increases with the strain from 1.5% to -1.5%, bringing about T_M enhancement. According to the results, the strain method can reveal the ability of the tunable wide working temperature range in Ni₁₄Co₂Mn₁₃Sn₃ FSMAs. Particularly, with a slight strain (0~1.5%), Ni₁₄Co₂Mn₁₃Sn₃ with a large working temperature region of ~160 K and the working temperature (168–330 K) of Ni₁₄Co₂Mn₁₃Sn₃ satisfy the application from low-temperature to high-temperature. This work predicts an adjusted broad working temperature region of Ni-Mn-Sn alloys, which shows a great application range of Ni-Mn-Sn FSMAs. Therefore, the strain method provides the reference for designing the tunable wide working temperature FSMAs and makes it possible for the wide application of FSMAs.

Author Contributions: Conceptualization, K.Z.; Data curation, B.H.; Software, L.Z., W.Z., T.M. and C.W.; Writing—original draft, Q.X.; Writing—review & editing, C.T., X.T. and K.Z. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by the National Natural Science Foundation of China (Grant No. 51971085, 51871083, 52001101) and the China Postdoctoral Science Foundation (Grant No. 2021M693229).

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: The data that support the findings of this study are available from the corresponding author upon reasonable request.

Conflicts of Interest: The authors declare no conflict of interest.

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