



Article Measurement of Forest Ecological Benefits Based on Big Data

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Abstract: Socioeconomic development combined with the development and utilization of forest resources have resulted in the forest ecological environment becoming more and more valuable, and its impact on the national economy has also increased. Firstly, based on a modern statistical model, the dependent variable and independent variable set of standardized forest ecological benefits were determined, and the seemingly unrelated forest ecological benefit model was established. According to the alternative market method and market approximation theory, the first and second monetary models of forest ecological benefit value were constructed using the market approximation coefficient, the effective area coefficient, and the physical quantity conversion coefficient. Next, the concept of "whole diffusion" was introduced into the establishment of the forest ecological benefit model, and the whole diffusion model was established to estimate the physical amount of forest ecological benefit were proposed. Forest management survey data were used to measure forest ecological benefit, and classic ecological benefit and generalized forest benefit were integrated into one system for the first time. The economic value is 94.31 million RMB ¥.

Keywords: big data; forest ecological benefit; measurement; National nature reserve

1. Introduction

Forest ecosystem services are multifaceted, which is first manifested in the utilization of forest biological resources. Forests are the only important resource that can provide wood, which is closely related to human production and life. Alternatively, forests provide significant ecological services. Forests have obvious diversion and blocking effects on surface runoff, therefore, they can greatly delay the duration of surface runoff, effectively reduce the peak value of runoff, regulate the flood and dry season, and reduce flood and river interruption. The canopy can objectively intercept part of the precipitation, reduce the mechanical damage of raindrops to the soil. The root system can hold the soil and litter and increase the field precipitation, resulting in a better forest microclimate, which has a beneficial impact on the surrounding farmland, grassland, and other ecosystems. Forests protect the wild animals and plants in the system, allowing them to grow well, absorb a large amount of carbon dioxide in the air, release oxygen, purify the atmosphere, conserve water sources, reduce flood and drought disasters, restrain wind and sand, and reduce noise.

Internationally, Costanza et al., in the United States conducted a series of studies on ecosystem services. The most influential is the paper published in Nature [1]. This paper classified and evaluated ecosystem services on a global scale and divided ecosystem services into 17 types. Costanza et al. [2] published another paper on the value of ecosystem services. Holzman [3] studied the service value of ecosystems. Calder [4] found that forest and water guarantee forest benefits exceed water charges, Pereira [5] explored the cost



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). support of Amazon Forest environmental services, and Rosser [6] studied the value of a forest as a factor of an eco-economic system. Tiemann and Ring [7] developed biophysical indicators for forest ecosystem services. They also studied the challenges and opportunities of aligning forest function mapping and the ecosystem service concept in Germany [8]. Frélichová et al. [9] integrated an assessment of ecosystem services in the Czech Republic. Barrette et al. [10] performed naturalness assessment using forestry maps to validate forest management sustainability. Sorge et al. [11] built a socio-ecological-technical-analytical framework to understand the dynamics of forest ecosystem services in tribal communities of the Barind region, Eastern India. Maiera et al. [13] had a systematic literature review for securing forest ecosystem service provision in Europe.

To realize sustainable forestry development, except from the economic value of wood, we should assess the ecology-related economic benefits of forests. Frizzle et al. [14] used a spatial Bayesian belief network to quantify trade-offs among forest-related ecosystem services towards achieving sustainable forestry. Dandabathula [15] explored the nexus between Indian forestry and sustainable development goals. Baumgartner [16] studied the complex relationship between sustainable development goals and the forest sector.

In China, Zhou [17] evaluated the ecological value of forests in Heilongjiang Province using the hypothetical market method. Lang et al. [18] performed a study entitled "10 forest ecological benefits measurement theories and methods of forestry ecological engineering". Sun and Lang [19] published an overall estimation of the seemingly unrelated model of generalized forest ecological benefits. Thereafter, Meng and Hou [20] discussed the research progress and diachronic development of forest ecosystem service value accounting theory and evaluation methods. Wang et al. [21] measured and evaluated the forest ecosystem service and its value in China. Zhu et al. [22] summarized and studied estimation methods of forest ecological value. Some Chinese scholars have published articles that estimated the ecological value of China's forests [23]. Xiao et al. [24] made a value assessment of the function of the forest ecosystem services in Chongqing. Feng et al. [25] had a case evaluation of forest ecosystem services in China. Li [26] studied the improvement of forest ecological benefit system construction in Tibet. Shi [27] explored the ecological benefit characteristics and value of returning farmland to a forest project in the middle and upper reaches of the Yangtze River and the Yellow River. Huang [28] analyzed the coupling relationship between multi-functional changes and comprehensive benefits of forest ecosystem in Hulunbeier. Pan [29] discussed the diverse compensation methods of forest ecological benefits in Heilongjiang Province based on the perspective of "government incentive". Liu et al. [30] used the method of "whole diffusion model" to construct the diffusion models of canopy interception, water holding capacity of litter, soil capillary pore water storage, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen, restraining wind and sand. Ou et al. [31] expounded on the connotation of trade-offs in forest ecosystem services and clarified the basic characteristics and main steps of trade-off analysis of forest ecosystem services. Then, we sorted the principles, techniques, and main functions of trade-off analysis methods, as well as their scope of application and analyzed the driving roles of natural and human factors in trade-off of the forest ecosystem services. Liu et al. [32] developed a software system for forest ecological benefit evaluation. It was composed of the calculation modules of the forest ecological benefit parameter table, calculation of six classical forest ecological benefit physical quantities, conversion from physical quantity to monetary quantity, calculation of 11 kinds of monetary quantity of generalized forest ecological benefit. Liu et al. [33] constructed a seemingly unrelated model of forest ecological benefit by using stand, meteorological factors, geographical location factors, and other independent variable sets, and taking various ecological benefits of forests as dependent variables. Liu and Shi [34] made an evaluation of water retention services of forest ecosystems in Fujian Province: Comparison between results from the InVEST model and meta-analysis.

Scholars at home and abroad have not yet formed a unified evaluation system, there is a marked deviation in research results, and the values obtained by different scholars vary greatly. However, there is still an opportunity to expand the research on the forest ecological benefits of the National Nature Reserve at home and abroad. This paper aimed to use forest big data for the National Nature Reserve, which spends a lot of human, material, and financial resources to obtain a forest management survey, allowing us to construct a forest seemingly unrelated model based on the modern statistical theory to study the forest ecological benefits of Liangshui National Nature Reserve.

2. Methods

2.1. Forest Ecological Benefits Seemingly Unrelated Model

Tang et al. [35] assumed that the linear statistical relationship between the random variables Y_1, \ldots, Y_q and some factors based on the modern statistical model, that is:

Generally, it can be assumed that the mean value of the error matrix is 0, and its rows are uncorrelated (independent), that is:

$$\mathbf{E}(\mathbf{e}) = \mathbf{0} \tag{2}$$

$$\operatorname{cov}(\mathbf{e}_{i\bullet}) = \sigma^2 \sum_{q \times q}$$
(3)

The following linear model group can be obtained from Equations (1)–(4):

$$\begin{cases} Y \quad j \quad X \quad j \quad \beta \\ n \times 1 = n \times p_j p_j \times 1^{(j)} + \mathbf{e}_{\bullet j} \\ E(\mathbf{e}_{\bullet j}) = 0 \qquad \dots \dots \dots 1 \le i \ne i' \le n \ 1 \le j \le q \\ \operatorname{cov}(\mathbf{e}_{i\bullet}) = \sigma^2 \sum_{q \times q} \\ \operatorname{cov}(\mathbf{e}_{i\bullet}, \ \mathbf{e}_{i'\bullet}) = 0 \\ q \times q \end{cases}$$
(5)

where: $e_{i\bullet} = (e_{i1}, ..., e_{iq}).$

Equation (5) is called seemingly uncorrelated linear model.

This model was proposed by Tang et al., based on modern statistics. It widened the application scope of the usual univariate or multivariate linear model or nonlinear model. At that time, simultaneous equations were established only for water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen, and restraining wind and sand. Based on Tang Shouzheng's seemingly unrelated model, this study will define various classical concepts of forest ecological benefits according to the unique biological characteristics of the forest, adding easily available independent variable sets, such as stand, meteorological factors, and geographical location factors affecting forest growth, and will take various ecological benefits of the forest as dependent variables, to construct a complex seemingly unrelated model of forest ecological benefits.

$$\begin{aligned} \ln(y_{i1}) &= a_{11} + b_{11}LF_{i1} + b_{21}LF_{i2} + b_{31}LF_{i3} + c_{11}LZ_{i1} + c_{21}LZ_{i2} + c_{31}LZ_{i3} + d_{11} \times \ln(JY_i) + d_{21}YB_i + e_{i1} \\ y_{i2} &= a_{12} + b_{12}LF_{i1} + b_{22}LF_{i2} + b_{32}LF_{i3} + c_{12}LZ_{i1} + c_{22}LZ_{i2} + c_{32}LZ_{i3} + d_{32}JD_i + d_{42}WD_i + d_{52}HB_i + e_{i2} \\ y_{i3} &= a_{13} + b_{13}LF_{i1} + b_{23}LF_{i2} + b_{33}LF_{i3} + d_{33}JD_i + d_{43}WD_i + d_{53}HB_i + e_{i3} \\ y_{i4} &= a_{14} + c_{14}LZ_{i1} + c_{24}LZ_{i2} + c_{34}LZ_{i3} + d_{14}JY_i + d_{24}YB_i + d_{34}JD_i + d_{44}WD_i + e_{i4} \\ y_{i5} &= a_{15} + c_{15}LZ_{i1} + c_{25}LZ_{i2} + c_{35}LZ_{i3} + d_{15}JY_i + d_{25}YB_i + d_{35}JD_i + d_{45}WD_i + e_{i5} \\ y_{i6} &= a_{16} + c_{16}LZ_{i1} + c_{26}LZ_{i2} + c_{36}LZ_{i3} + d_{16}JY_i + d_{26}YB_i + d_{36}JD_i + d_{46}WD_i + e_{i6} \\ y_{i7} &= a_{17} + c_{17}LZ_{i1} + c_{27}LZ_{i2} + c_{37}LZ_{i3} + d_{17}JY_i + d_{27}YB_i + d_{37}JD_i + d_{47}WD_i + e_{17} \\ y_{i8} &= a_{18} + c_{18}LZ_{i1} + c_{28}LZ_{i2} + c_{38}LZ_{i3} + d_{18}JY_i + d_{28}YB_i + d_{38}JD_i + d_{48}WD_i + e_{i8} \end{aligned}$$

The variables in Equation (6) are:

1. Dependent variable of forest ecological benefit

 Y_{i1} is annual ecological benefit of water intercepted by the forest canopy (hm²·a), Y_{i2} is the water holding capacity of the forest litter (hm²·a), Y_{i3} is the annual ecological benefit of water storage in the non-capillary pores of the forest soil (hm²·a), Y_{i4} is the annual ecological benefit of fixing soil (hm²·a), Y_{i5} is the annual ecological benefit of retaining fertilizer (hm²·a), Y_{i6} is the annual ecological benefit of absorbing carbon dioxide by the forest (m³·a), Y_{i7} is the annual ecological benefit of releasing oxygen by the forest (m³·a), Y_{i8} is the annual ecological benefit of restraining wind and sand by the forest (hm²·a).

2. Independent variable set of forest ecological benefit

LF is a qualitative variable, whose forest type response value is: 1 for a Korean pine forest, 2 for a coniferous forest, 3 for a mixed forest, 4 for a hard broad-leaved forest, 5 for a soft broad-leaved forest and 6 for a sub arbor forest, *LZ* is a qualitative variable, whose age group response value is: 1 for a young forest, 2 for a middle-aged forest and 3 for a mature forest, *JY* is precipitation (mm), *YB* is canopy closure (0, 0.1, 0.2, ..., 1), *JD* is longitude (°), *WD* is latitude (°), and *HB* is altitude (m).

3. Others are constants to be estimated

They could be estimated using observation data.

- 2.2. Monetary Construction Model of Forest Ecological Benefits
- 2.2.1. Classification of the Monetary Quantity Construction Model

There are two alternative market technologies for forest ecological benefits:

- (1) Alternative market technologies for alternative goods. According to various classical definitions of forest ecological benefits, seeking appropriate alternative goods and alternative prices, we built a monetary quantity construction model, which is called the first kind of monetary quantity construction model.
- (2) Direct alternative market technology. According to the field measurement data of the external economy (or external non economy) generated by forest ecological benefits, the monetary quantity construction model of forest ecological benefits was constructed directly, which is called the second type of monetary quantity construction model.
- 2.2.2. First Type of Monetary Construction Model

$$E_i(t) = \sum_{j=1}^n P_j \times R_j \times C_j \times Y(t)_{ij} \times S(t)_{ij} \dots \dots \dots i = 1, 2 \dots 6; j = 1, 2 \dots n$$
(7)

where: E_i is monetary amount of water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen and restraining wind and sand, P_j is effective area coefficient, R_j is the market approximation coefficient, C_j is price of substitute goods, $Y(t)_{ij}$ is dependent variable of forest ecological benefit (physical quantity), $S(t)_{ij}$ is a forest resource vector, and t is time, referring to summing according to stand and subcompartment $_j$ [36].

2.2.3. Second Type of Monetary Construction Model

The second kind of money quantity construction model is constructed from physical quantities that do not exist or for which alternative goods are difficult to find. For example, there are more than ten kinds of benefit physical quantities for a forest to improve its microclimate, but no suitable substitute commodity can be found for each. Forest noise reduction can use the reduced decibel (DB) as its physical quantity, but there is no substitute commodity. There are too many physical quantities of forest protected wildlife to establish its overall diffusion model. Forest recreation itself has direct use value and is a widened forest ecological benefit. It has no physical quantity and does not need to replace commodities [36]. The model parameters of second type monetary construction model of forest ecological benefit are shown in Table 1.

Table 1. Model parameters of second type money of forest ecological benefit.

Forest Ecological Benefit	Pi	Ri	Construction Model of Money (¥/hm ²) *	Number of Samples
Improving microclimate	0.4	0.8	$E_i(t) = \sum P_i \times R_i \times S(t)_{ij} \times 67.99605 \times LZ^{0.4931957}$	60
Reducing flood and drought	1.0	0.9	$E_i(t) = \sum P_i \times R_i \times S(t)_{ii} \times 311.6941 \times LZ^{0.6183988}$	30
Recreation resource	0.6	0.4	$E_{i}(t) = \sum P_{i} \times R_{i} \times S(t)_{ii} \times 12.33866 \times LZ^{0.8235893}$	60
Wild animal protection	1.0	0.9	$E_i(t) = \sum P_i \times R_i \times S(t)_{ij} \times 21.39681 \times LZ^{0.8760093}$	30
Wild plant protection	1.0	0.9	$E_{i}(t) = \sum P_{i} \times R_{i} \times S(t)_{ij} \times 64.11374 \times LZ^{0.82359.8}$	60
Reducing noise	0.1	0.8	$E_{i}(t) = \sum P_{j} \times R_{j} \times S(t) _{ij} \times 62.74023 \times LZ^{0.2500285}$	30

* Where: E_i is the monetary amount of water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen and restraining wind and sand; P_j is the effective area coefficient; R_j is the market approximation coefficient; $S(t)_{ij}$ is a forest resource vector; t is time, referring to summing according to stand and subcompartment $_j$; LZ is the stand age group.

2.3. Overall Diffusion Model

[Definition] According to the characteristics of forest ecological benefits, it is difficult to measure them, so their measurement must be estimated by the sample. This sample cannot be random but often uses the observation value of an ecological positioning station. The sampling ratio is much smaller than that of forest resources. This extension from microobservation data to the whole should be a gradual and layer-by-layer "diffusion". All kinds of forest ecological benefits have a correlation between multiple dependent variables and multiple independent variables. Using this multivariate-to-multivariate linear model to measure forest ecological benefits, the model that meets the overall compatibility and has independent variables was called the overall diffusion model.

The samples of the above parameter estimates are collected from the three North shelter belts, the shelter belts in the middle and upper reaches of the Yangtze River, the coastal shelter belts and the Taihang Mountains. The complexity of some factor measurements mean that many benefits have only 30 samples [30].

2.3.1. Canopy Interception

The overall diffusion model of canopy interception is:

$$I = \alpha \times EXP \Big[a + \sum b_i \times LF + \sum c_i \times LZ + d\ln(JY) + f \times YB \Big]$$
(8)

where: *I* is canopy interception $(t/hm^2 \cdot a)$, *LF* is a qualitative variable, whose forest type response value is: 1 for a Korean pine forest, 2 for a coniferous forest, 3 for a mixed forest, 4 for a hard broad-leaved forest, 5 for a soft broad-leaved forest, and 6 for a sub arbor forest, *LZ* is a qualitative variable, whose age group response value: 1 for a young forest, 2 for a middle-aged forest and 3 for a mature forest, *JY* is precipitation (mm), *YB* is canopy closure (0, 0.1, 0.2, ..., 1), α , a, b_i , c_i , d and f are parameters to be estimated.

The estimated values of the above model parameters were: $\alpha = 6.9$, a = -0.7849, $b_1 = 0.0052$, $b_2 = -0.1834$, $b_3 = 0$, $c_1 = -0.4921$, $c_2 = -0.1919$, $c_3 = 0$, d = 0.7612, f = 1.2388, number of samples = 181.

2.3.2. Water Holding Capacity of the Litter

The overall diffusion model of water holding capacity of litter is:

$$K = \alpha + \beta \left[a + \sum b_i \times LF + \sum c_i \times LZ + dJD + fWD + gHB \right]$$
(9)

where: *K* is the water holding capacity of the litter (t/hm². a), *JD* is longitude (°), *WD* is latitude (°), *HB* is altitude (m), α , β , g is the parameters to be estimated. Other symbols are the same as above.

Estimated values of the above model parameters are: $\alpha = 25.374$, $\beta = 16.542$, a = 68.58, $b_1 = 4.83$, $b_2 = -1.81$, $b_3 = 0$, $c_1 = -7.42$, $c_2 = -3.04$, $c_3 = 0$, d = -0.59, f = 0.4415, g = 0.0015, number of samples = 181.

2.3.3. Soil Capillary Pore Water Storage

The overall diffusion model of capillary pore water storage in forest soil is as follows:

$$Q = a + \sum b_i \times LF + cJD + dWD + fHB$$
(10)

where: Q is the water storage in capillary pores of the forest soil (t/hm². a). Other symbols are the same as above.

Estimated values of the above model parameters are: a = -5085.55, $b_1 = -254.8$, $b_2 = -72.462$, $b_3 = 0$, c = 79.80, d = -91.8, f = 0.75, number of samples =181.

2.3.4. Fixing Soil

The overall diffusion model of fixing soil is:

$$Y_1 = \mathbf{a} + \sum \mathbf{b}_i \times LZ + \mathbf{d}JD + \mathbf{C}WD + \mathbf{E}JY + \mathbf{f}YB \tag{11}$$

where: Y_1 is fixing soil (t/hm². a), for sparse forest land $Y_1 = 0$, *JY* is precipitation (mm), *YB* is canopy closure (0, 0.1, 0.2, ..., 1), C, E and f are the parameters to be estimated. Other symbols are the same as above.

Estimated values of the above model parameters are: a = 4, $b_1 = 6$, $b_2 = -2.567$, $b_3 = 0$, d = -0.28445, C = 0.87825, E = 0.01762, f = 17, number of samples = 181.

2.3.5. Retaining Fertilizer

The overall diffusion model of retaining fertilizer is:

$$Y_2 = a + \sum b_i \times LZ + dJD + CWD + EJY + fYB$$
(12)

where: Y_2 is the retaining fertilizer (t/hm². a), for open woodland $Y_2 = 0$. Other symbols are the same as above.

Estimated values of the above model parameters are: a = -1.5, $b_1 = -3.3125$, $b_2 = -0.89391$, $b_3 = 0$, d = 0.05195, C = 0.00039, E = 0.00009, f = 0.5, number of samples = 181.

2.3.6. Absorbing Carbon Dioxide

The overall diffusion model of absorbing carbon dioxide is:

$$Y = a + \sum b_i \times LZ + dJD + CWD + EJY + fYB$$
(13)

where: *Y* is the absorbing carbon dioxide by the forest $(t/m^3 \cdot a)$. Other symbols are the same as above.

Estimated values of the above model parameters are: a = -0.13631, $b_1 = 0.07890$, $b_2 = 0.02197$, $b_3 = 0$, d = 0.00252, C = -0.00293, E = -0.00002, f = 0.00236, number of samples = 30.

2.3.7. Releasing Oxygen

The overall diffusion model of releasing oxygen by forest is:

$$Y = \alpha \left(a + \sum b_i \times LZ + dJD + CWD + EJY + fYB \right)$$
(14)

where: Y is amount of oxygen released by the forest $(t/m^3 \cdot a)$. Other symbols are the same as above.

Estimated values of the above model parameters are: $\alpha = 0.702$, a = -0.13631, $b_1 = 0.07890$, $b_2 = 0.02197$, $b_3 = 0$, d = 0.00252, C = -0.00293, E = -0.00002, f = 0.00236, number of samples = 30.

2.3.8. Restraining Wind and Sand

The overall diffusion model of forest restraining wind and sand is:

$$Y_1 = \mathbf{a} + \sum \mathbf{b}_i \times LZ + \mathbf{d}JD + \mathbf{C}WD + \mathbf{E}JY + \mathbf{f}YB - 1$$
(15)

and

$$Y_2 = \alpha \left(\mathbf{a} + \sum \mathbf{b}_i \times LZ + \mathbf{d}JD + \mathbf{C}WD + \mathbf{E}JY + \mathbf{f}YB - 1 \right)$$
(16)

where: Y_1 is area of restraining wind and sand (hm²/hm²·a), Y_2 is amount of restraining wind and sand (t/hm²·a). Other symbols are the same as above.

Estimated values of the above model parameters are: $\alpha = 28.7$, a = 1.68262, $b_1 = 0.10423$, $b_2 = 0.06526$, $b_3 = 0$, d = 0.01376, C = -0.03955, E = -0.00067, f = 0.41924, number of samples = 30.

3. Results

3.1. Estimation of the Total Physical Amount of Forest Ecological Benefits

The modeling data for this study are mainly from the database of the third forest management survey in Liangshui National Nature Reserve in 2009. The geographical coordinates are $128^{\circ}47'8''-128^{\circ}57'19''$ E and $47^{\circ}6'49''-47^{\circ}16'10''$ N. The annual average temperature is only $-0.3 \circ$ C, the annual average maximum temperature is 7.5 °C, and the annual average minimum temperature is $-6.6 \circ$ C. The accumulated temperature $\geq 10 \circ$ C is about 1700 °C and that $\geq 5 \circ$ C is about 2000 °C. The annual average precipitation is 676 mm, and the annual average number of precipitation days is 120–150 days. There are 130–150 days of snow, the annual average relative humidity is 78%, and the annual average evaporation is 805 mm. A location map of Liangshui National Nature Reserve is shown in Figure 1.



Figure 1. Location map of Liangshui National Nature Reserve.

Parameters of the forest ecological physical quantity model are shown in Table 2. The collection of total forest ecological benefit physics is shown in Table 3.

3.2. Measurement of Forest Ecological Benefits

In recent years, forest ecological benefits have expanded to the selection value and existence value of forests. For example, forest wildlife protection has value and no physical quantity, the benefit of improving the forest microclimate has an unclear physical quantity, there is no physical quantity for the benefits of forests in reducing floods and drought, and there is no substitute for forest recreation benefits and reducing noise benefits. Therefore, we directly determined the annual forest benefit per unit forest area as its value.

Definition 1. Under the action of atmospheric circulation, forests provide indirect forest selection value and existence value beneficial to human beings for the earth biosphere composed of life and the environment. Generally, they do not have measurable physical quantities for ecological benefits, or there are too many physical quantities to find the characteristics of "substitutes", such as forest benefits of wildlife protection and improving microclimate and other public welfare benefits. Therefore, they are called generalized forest ecological benefits.

The economic value calculated according to the generalized forest ecological benefit is shown in Table 4.

Items	Canopy Interception	Litter Holding Water	Soil Holding Water	Fixing Soil	Retaining Fertilizer	Absorbing CO ₂	Releasing Oxygen	Restraining Wind and Sand hm ²	Restraining Wind and Sand t	General Eco-Benefits
Para. 1	6.9	25.374	-5085.55	4	-1.5	0.95355	0.702	1.68262	28.7	0.4
Para. 2	-0.7849	16.542	-254.8	6	-3.3125	-0.13631	-0.13631	0.10423	1.68262	0.8
Para. 3	0.0052	68.58	-72.46	-2.567	-0.89391	0.0789	0.0789	0.06526	0.10423	122.6
Para. 4	-0.1834	4.83	0	0	0	0.02197	0.00293	0	0.06526	1
Para. 5	0	-1.81	79.8	-0.28445	0.05195	0	0	0.01376	0	0.9
Para. 6	-0.4921	0	-91.8	0.87825	0.00039	0.00252	0.00252	-0.03955	0.01378	91
Para. 7	-0.1919	-7.42	0.75	0.01762	0.00009	-0.00293	-0.00293	-0.00067	-0.03955	0.6
Para. 8	0	-3.04	0	17	0.5	-0.0002	-0.0000	0.41924	-0.00067	0.4
Para. 9	0.7612	0	0	0	0	0.00236	0.00236	0	0.41924	60.1
Para. 10	1.2388	-0.59	0	0	0	0	0	0	0	1
Para. 11	0	0.4415	0	0	0	0	0	0	0	1
Para. 12	0	0.0015	0	0	0	0	0	0	0	129
Effective area coefficient	1	1	1	1	1	1	1	0.5	0	0.1
Market										
approximation	0.8	0.8	0.8	0.9	0.1	1	0.2	0.8	0	1
coefficient										
Price/ha	0.66024	0.66024	0.66024	14.88	843.7	128.33	1269.7	450	0	71

 Table 2. Parameters of the forest ecological physical quantity model.

Age Group	Stand	Total Area hm ²	Total Volume m ³	Total Physics	Water Source Cultivation y	Water Source Cultivation Total	Fixing Soil y	Fixing Soil Total	Retaining Fertilizer y	Retaining Fertilizer Total	Absorbing CO ₂ y	Absorbing CO ₂ Total	Releasing Oxygen y	Releasing Oxygen Total	Restraining Wind and Sand Y	Restraining Wind and Sand Total
		6334	1,820,433	14,516,716	2215.8	14,034,662	33.2	210,462	4.7	29,972	15	94,913	8.8	55,794	0.003	3167.9
Young		748	120,026	1,441,877	1838.5	1,375,208	40.1	29,961	2.3	1724	17.7	13,235	13	9743	0.854	418.4
	Korean pine	35	6778	67,724	1839.2	64,373	40.2	1407	2.3	81	21.4	748	15.7	551	15	19.7
	Coniferous	312	63,908	598,553	1820.2	567,912	40.4	12,595	2.3	722	22.6	7054	16.6	5193	0.567	176.9
	Mixed	203	33,853	412,405	1941.7	394,158	39.8	8080	2.3	466	18.4	3731	13.5	2747	0.941	112.3
	Hard broad- leaved	15	585	27,137	1745.5	26,183	38.7	581	2.3	34	4.3	64	3.1	47	7.467	8
	Soft broad- leaved	182	14,852	334,685	1765.1	321,248	39.9	7268	2.3	419	9	1638	6.6	1206	2.159	101.3
	Sub arbor	1	50	1374	1335	1335	29	29	2	2					14	0.3
Middle		2418	796,924	5,427,877	2165.9	5,237,228	31.5	76,219	4.7	11,424	18.5	44,632	9.2	22,206	0.003	1260.2
	Korean pine	720	402,608	1,622,049	2155.2	1,551,730	31.3	22,524	4.7	3397	31.3	22,539	15.6	11,212	0.14	371
	Coniferous	999	276,356	2,240,161	2167.7	2,165,508	31.7	31,666	4.7	4725	15.5	15,487	7.7	7708	0.137	525
	Mixed	366	71,227	862,443	2288.9	837,720	31.5	11,540	4.7	1729	10.9	3991	5.4	1986	0.437	190.8
	Hard broad- leaved	26	3172	56,855	2124.9	55,247	31.8	826	4.7	123	6.8	178	3.4	88		13.7
	Soft broad- leaved	307	43,562	646,369	2042.4	627,023	31.5	9664	4.7	1450	7.9	2437	3.9	1212		159.7
Mature		3168	903,483	7,646,962	2342.9	7,422,227	32.9	104,283	5.3	16,824	11.7	37,047	7.5	23,845		1489.1
	Korean pine	668	224,243	1,636,089	2374.1	1,585,905	33.5	22,405	5.4	3586	13.6	9092	8.9	5914		320
	Coniferous	1368	392,493	3,299,191	2340.8	3,202,150	33.3	45,524	5.4	7383	11.3	15,491	7.5	10,306		638.9
	Mixed	838	232,454	2,084,974	2417.7	2,026,065	32.3	27,084	5.2	4364	12	10,017	7.4	6174		392.7
	Soft broad- leaved	294	54,294	626,709	2068.4	608,108	31.5	9270	5.1	1491	8.3	2448	4.9	1450		137.4

 Table 3. Collection of total forest ecological benefit physics.

Age Group	Stand	Total Area hm ²	Total Volume m ³	Total Money	Water Source Cultivation	Fixing Soil	Retaining Fertilizer	Absorbing CO ₂	Releasing Oxygen	Restraining Wind and Sand	Improving Micro Climate	Reducing Water Disaster	Recreation	Living Things Protection	Reducing Noise
		6334	1,820,433	9431	2402	761	455	2850	2550	103	45	93	16	147	8
Young		748	120,026	1263	235	108	26	397	445	14	5	11	2	17	1
0	Korean pine	35	6778	67	11	5	1	22	25	1		1		1	
	Coniferous	312	63,908	624	97	46	11	212	237	6	2	5	1	7	
	Mixed	203	33,853	355	67	29	7	112	126	4	1	3	1	5	
	Hard broad- leaved	15	585	12	4	2	1	2	2						
	Soft broad- leaved	182	14,852	204	55	26	6	49	55	3	1	3		4	
	Sub arbor	1	50												
Middle		2418	796,924	3860	896	276	173	1340	1015	41	17	36	6	56	3
	Korean pine	720	402,608	1635	266	81	52	677	512	12	5	11	2	17	1
	Coniferous	999	276,356	1440	371	114	72	465	352	17	7	15	3	23	1
	Mixed	366	71,227	446	143	42	26	120	91	6	3	5	1	8	
	Precious														
	hard broad- leaved	26	3172	25	9	3	2	5	4					1	
	Soft broad- leaved	307	43,562	313	107	35	22	73	55	5	2	5	1	7	
Mature		3168	903,483	4308	1270	377	255	1112	1090	48	22	47	8	74	4
	Korean pine	668	224,243	993	271	81	54	273	270	10	5	10	2	16	1
	Coniferous	1368	392,493	1849	548	165	112	465	471	21	10	20	4	32	2
	Mixed	838	232,454	1148	347	98	66	301	282	13	6	12	2	19	1
	Soft broad- leaved	294	54,294	319	104	34	23	74	66	4	2	4	1	7	

Table 4. Generalized forest ecological money benefits. Unit: 10 thousand RMB ¥.

It can be seen from Table 4 that the benefits of water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen and restraining wind and sand of Liangshui National Nature Reserve are 24.02 million, 7.61 million, 4.55 million, 28.5 million, 25.5 million, and 1.03 million RMB ¥, respectively. The generalized ecological benefits include the benefits of improving the microclimate, reducing flood and drought, recreation, wildlife protection, and reducing noise and are valued at 930,000, 160,000, 1,470,000, and 80,000 RMB ¥, respectively, and the total annual forest ecological benefit is 94.31 million RMB ¥.

The authors also calculated the forest ecological benefits of Maoershan National Forest Park and the state-owned forest of Songhuajiang Forest Administration Bureau of Heilongjiang Province. The area of Maoershan National Forest Park is 22,720 hm², and the monetary value of forest ecological benefits is 188.27 million RMB ¥ per year. The area of the state-owned forest of Songhuajiang Forest Administration Bureau is 2,056,544 hm², and the monetary value of forest ecological benefits is 10,211.83 million RMB ¥ per year, while the area of Liangshui National Nature Reserve is only 6334 hm², and the total annual forest ecological benefits are 94.31 million RMB ¥. Calculated by unit area, the annual forest ecological benefits per hectare are Liangshui National Nature Reserve (14,889 RMB ¥) > Maoershan National Forest Park (8286 RMB ¥) > Songhuajiang Forest Administration Bureau (4965 RMB ¥). These data also show that the size of forest ecological benefits is closely related to forest quality.

4. Discussion

Many scholars only give the total monetary value of forest ecological benefits. We used forest management survey data to calculate and accumulate forest ecological benefits from subcompartment to subcompartment. In this way, our estimate of the amount of forest ecological benefits should be more reliable.

The concept of "overall diffusion" in the establishment of the forest ecological benefit model and the unification of various forest ecological benefits into one system was used. The first and second types of monetary models were constructed by using the market approximation coefficient, the effective area coefficient, and the physical quantity conversion coefficient, respectively, followed by estimation, which greatly reduced the controversy of overestimating the value of forest ecological benefit at home and abroad.

5. Conclusions

This paper proposes the concepts of classical forest ecological benefit and generalized forest ecological benefit. The forest ecological benefits with clear physical quantities such as water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen, and restraining wind and sand are called classic forest ecological benefits. The forest benefits without clear physical quantities or market alternative products, such as improving the microclimate, reducing flood and drought, recreation, wildlife protection, and reducing noise, are called generalized forest ecological benefits.

The six forest ecological benefits of water source cultivation, fixing soil, retaining fertilizer, absorbing carbon dioxide, releasing oxygen, and restraining wind and sand must be linear models. The theory of ecological benefit is not too deep. Therefore, it can only be described by a linear model, that is, individual exponential values and the logarithm can be transformed into a linear model. The development of these six forest ecological benefits occurred in order, thus these six forest ecological benefit models have a certain independence in that they have their own independent variable system, which is different from the multivariate linear model. These six forest ecological benefits are interrelated, so they are both independent and related, which we termed the seemingly uncorrelated linear model.

Forest management survey data were used to measure the forest ecological benefits for the first time. Firstly, the coefficient of forest ecological benefits was determined, and then the physical quantities of the forest ecological benefits were calculated by subcompartments. Then, the classical forest ecological benefits were obtained using the physical quantity conversion coefficient, and then the generalized forest ecological benefits were estimated using the second type of monetary model. Finally, forest ecological benefits of each subcompartment were accumulated.

Technically, based on the seemingly uncorrelated model of modern statistics, we deduced the seemingly uncorrelated model of forest ecological benefits, introduced the concept of "overall diffusion", and finally estimated the monetary value of forest ecological benefits.

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