





Determination of the Optimal Tilt Angle of Solar Collectors for Different Climates of China

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Abstract: The tilt angle with the horizon (with respect to the ground) of the solar energy system affects the amount of solar radiation received. This paper suggests a simple and universal method to obtain the optimum tilt angles by estimating the monthly mean daily global solar radiation on tilted surfaces facing directly towards the equator, which is based on monthly average daily global solar radiation data produced from Typical Meteorological Year (TMY) data. The monthly, seasonal, and yearly optimum tilt angles for photovoltaic panels are calculated at six stations of different climatic types (Tropical Zone (TZ), Subtropical Zone (SZ), Warm Temperate Zone (WTZ), Mid Temperate Zone (MTZ), Cold Temperate Zone (CTZ) and Tibetan Plateau Zone (TPZ)). The results indicate that changing the monthly, seasonal, and yearly optimum tilt angles causes a significant yearly gain in the solar radiation for the region. In addition, general correlations are generated to estimate the optimum tilt angle of solar collectors at six typical climatic stations of China. The performances of the proposed models are compared using statistical error tests such as the mean absolute bias error (MABE), the root mean square error (RMSE) and the correlation coefficients (R).

Keywords: optimum tilt angle; Typical Meteorological Year; solar radiation; solar energy

1. Introduction

The performance of a photovoltaic panel is highly influenced by its tilt angle with the horizontal surface (with respect to the ground) because the tilt angle changes the solar radiation reaching the surface of the collector [1,2]. The best way to collect the maximum daily energy is to use a tracking system. A tracking system is a mechanical device that tracks the sun on its daily sweep across the sky. However, most photovoltaic (PV) modules are not suited for tracking, as they collect more sunlight and, therefore, produce more electricity if they are always oriented toward the sun. Trackers are expensive, need energy for their operation, and are not always applicable. Therefore, it is often practical to orient the solar collector at an optimum tilt angle and to correct the tilt from time to time.

Some investigators have made different recommendations for the optimum tilt, based on the latitude. Lunde [3] and Garg [4] obtained the optimum tilt angle, β_{opt} , $\varphi \pm 15^{\circ}$. Duffie and Beckman [5] obtained β_{opt} , ($\varphi \pm 15^{\circ}$) $\pm 15^{\circ}$. Ibrahim [6] showed the optimum tilt angles of summer months ($\varphi - 21^{\circ}$) and winter months ($\varphi + 13^{\circ}$) for Cyprus. Asl-Soleimani [7] reported an annual optimum tilt angle of 30° , which is a bit lower than the local latitude (35.7°). Kalogirou [8,9] suggested the optimum tilt angle for collectors in Izmir to be 35.8° , which is approximately the location's latitude. Lave and Kleissl [11] suggested yearly optimum tilt angles for several regions of the United States as β_{opt} , $\varphi - (1^{\circ} - 10^{\circ})$, by calculating the maximum incident solar radiation on the solar collector, where φ is the latitude of the location. Jafarkazemi [12] concluded that the yearly optimum tilt angle ($\beta_{opt} = 22^{\circ}$) is almost close to the latitude of Abu Dhabi ($\varphi = 24.4^{\circ}$).

Some other optimization techniques have also been devoted to this problem in recent years, most of which treat the problem both qualitatively and quantitatively. Abdolzadeh and Mehrabian [13], Bakirci [14,15], and Despotovic [1] estimated the total (global) solar radiation intensity to obtain the optimum slope angle in a specific period for solar collectors. Kaldellis [16,17] and Pourgharibshahi [18] verified the computational optimum tilt angles of a PV module by conducting experiments. The genetic algorithm method [19,20], particle swarm optimization [21,22], and the artificial neural network method [23,24] were also used to estimate the optimum tilt angle of PV modules.

The previous studies on the topic were carried out mostly in the foreign climate and geography. Yang and Lu [25] developed a new mathematical model for calculating the optimum tilt angles and azimuth angles for building-integrated photovoltaic (BIPV) applications in Hong Kong on yearly, seasonal, and monthly bases. Sun [26] investigated the combined energy effect produced by shading-type BIPV claddings and found that the optimum tilt angles of shading-type BIPV claddings at different orientations provide the most desirable energy-saving effect. Tang [27] theoretically investigated the multi-reflection of radiation on both parabolic reflectors of a compound parabolic concentrator (CPC) with a one-sided flat absorber and its effect on energy-collection calculations. Generally, such research in China is still limited. Thus, the present study aims to develop an analytical procedure to obtain formulae which determine β_{opt} for any climatic type in China.

The main objective of this study is to determine the optimum tilt angle of photovoltaic panels on the basis of maximizing the global solar radiation reaching the collector surface on a monthly, seasonal, and yearly basis and to develop general correlations for estimating the monthly optimum tilt angles at six stations of different climatic zones. The effect of the Earth's reflection on the global solar radiation for a solar collector inclined at the optimum slope angle is investigated. The calculations are based on the data of air-dry bulb temperature, relative humidity, wind velocity, and global solar radiation from China's meteorological stations. These data are collected for a period of 16 years (1994–2009).

2. Different Climates of China and Optimal Angles Designed for the Six Typical Cities

China lies in the northeastern part of East Asia and has a complex climate [28,29]. Various methods for classifying the climatic types of China can be found in References [30–32]. In this paper, we use the method which designated China's temperature strip. Accordingly, China is classified into six climatic types, namely the Tropical Zone (TZ), Subtropical Zone (SZ), Warm Temperate Zone (WTZ), Mid Temperate Zone (MTZ), Cold Temperate Zone (CTZ) and Tibetan Plateau Zone (TPZ). Moreover, the zoning criteria are mainly based on the annual accumulated temperature, which is the sum of the daily mean temperature over 10 degrees within a year. Six stations (Sanya, Shanghai, Zhengzhou, Harbin, Mohe, and Lhasa) in China are investigated and generated based on the measured weather data in this paper. General information about the six selected typical stations is shown in Table 1.

No.	Climate	Location	Latitude (N)	Longitude (E)	Elevation (m)	Period
1	Tropical Zone (TZ)	Sanya	$18^{\circ}14'$	109°31′	5.9	1994-2009
2	Subtropical Zone (SZ)	Shanghai	31°24′	121°29′	6	1994–2009
3	Warm Temperate Zone (WTZ)	Zhengzhou	34°43′	113°39′	110.4	1994–2009
4	Mid Temperate Zone (MTZ)	Harbin	$45^{\circ}45'$	$126^{\circ}46'$	142.3	1994–2009
5	Cold Temperate Zone (CTZ)	Mohe	53°28′	122°31′	433	1994–2009
6	Tibetan Plateau Zone (TPZ)	Lhasa	29°40′	$91^{\circ}08'$	3648.7	1994–2009

 Table 1. Geographical locations and weather database for the present study.

3. Development of Monthly Mean Daily Global Solar Radiation Data

3.1. Data Used

In this work, the measured weather data (including daily maximum, minimum, and mean air-dry bulb temperature; daily minimum and mean relative humidity; daily maximum and mean wind velocity; and daily global solar radiation data) for the six stations are gathered from China's meteorological stations. The missing and invalid measured weather data for the six stations shown in Table 1 are marked and coded as 32,744 or 32,766 in the original document of China's meteorological stations. In addition, the questionable data are replaced by the values of previous or subsequent days using the interpolation method [33].

3.2. Method and Process for Forming Monthly Mean Daily Global Solar Radiation Data

Monthly mean daily global solar radiation data are the basic and key parameters in the following process of forming the optimal tilt angle. Since solar radiation data can vary from year to year, there is a need to generate a customized solar radiation database that can well represent the long-term averaged solar radiation over a year [31,34–37]. In this subsection, the Typical Meteorological Year (TMY) method is recommended and applied. The TMY method is the methodology for combining 12 typical meteorological months (TMMs) from different years of the measured period to form a complete year. The selection procedure of the 12 TMMs consists of two steps:

Step 1: Selection of five candidate years. The cumulative distribution function (CDF) for each weather index is determined by the following function:

$$S_n(x) = \begin{cases} 0 & \text{for} \quad x < x_1 \\ (i - 0.5)/n & \text{for} \quad x_i \le x < x_{i+1} \\ 1 & \text{for} \quad x \ge x_n \end{cases}$$
(1)

where $S_n(x)$ is the value of the CDF for weather index x; n is the total number of elements; i is the rank order number (i = 1, 2, 3, ..., n - 1). Next, the values of Finkelstein-Schafer (FS) statistics [38] for each weather index are calculated by the equation:

$$FS_{x}(y,m) = \frac{1}{N} \sum_{i=1}^{N} |CDF_{m}(x_{i}) - CDF_{y,m}(x_{i})|$$
(2)

where $FS_x(y, m)$ is the FS statistic for the year y, month m; CDF_m is the long-term and $CDF_{y,m}$ is the short-term (for the year y) cumulative distribution function of the weather index x for month m; N is the number of daily readings of the month.

The weighted sum (WS) of the FS statistics for the above eight meteorological indices is then calculated for each year. In addition, the five years are selected as the candidate years having the smallest WS values. The WS is defined as follows:

$$WS(y,m) = \frac{1}{M} \sum_{x=1}^{M} WF_x \cdot FS_x(y,m)$$
(3)

where WS(y, m) is the average weighted sum for the month m in the year y; WF_x is the weighting factor for the xth weather index (shown in Table 2); M is the number of meteorological parameter indices (eight in this paper).

Pa	arameter Indices	Present Article
Temperature	Max Dry Bulb Temperature	1/24
-	Min Dry Bulb Temperature	1/24
	Mean Dry Bulb Temperature	3/24
Humidity	Min Relative Humidity	1/24
-	Mean Relative Humidity	2/24
Wind	Max Wind Velocity	2/24
	Mean Wind Velocity	2/24
Solar radiation	Global Solar Radiation	12/24
	P. Temperature Humidity Wind Solar radiation	Parameter IndicesTemperatureMax Dry Bulb TemperatureMin Dry Bulb TemperatureMean Dry Bulb TemperatureHumidityMin Relative HumidityHumidityMean Relative HumidityWindMax Wind VelocityMean Wind VelocityMean Wind VelocitySolar radiationGlobal Solar Radiation

Table 2. Meteorological indices and weighting factors (WF_x) for the FS statistic in this study.

Step 2: Final selection of TMM. The final step is to choose TMMs from the five candidate years. The month with the minimum root mean square difference (RMSD) [39] of global solar radiation is chosen as the TMM. The TMM is calculated according to:

$$RMSD = \left[\frac{\sum_{i=1}^{N} (H_{y,m,i} - H_{ma})^2}{N}\right]^{1/2}$$
(4)

where $H_{y,m,i}$ is the daily global solar radiation values of the year y, month m and day i; H_{ma} is the mean values of the long-term global solar radiation for the month m; N is the number of daily readings of the month.

The TMY data and typical global solar radiation data for the six stations listed in Table 1 are investigated and generated based on the above measured weather data and the TMY method. The detailed generation process for the TMY data can be found in our previous research [39]. In addition, the TMY data of the six stations in different climatic zones of China produced in Reference [39] are shown in Table 3.

By applying the daily mean global solar radiation data, the monthly mean daily global solar radiation data of the six stations in six different climatic zones of China are computed and formed based on the corresponding TMY data. The monthly mean daily global solar radiation data of the six stations are given in Table 3.

Climate	Station	Month											
Climate		January	February	March	April	May	June	July	August	September	October	November	December
T7	Santra	2002	2002	2001	2003	1998	2000	2000	2002	2004	1995	2002	2004
IZ	Sallya	14.06	15.28	15.73	19.29	19.96	18.59	17.58	19.42	16.64	16.12	14.71	12.58
SZ Shanghai	Chanabai	1997	1997	2004	2008	1996	1998	1998	2004	2003	1997	1999	1998
	Shanghai	7.41	11.15	12.74	13.80	17.27	15.05	19.60	17.95	15.21	11.66	8.08	7.79
	Thongshou	1996	1998	1995	2006	2000	1997	2002	2002	2001	2008	1998	1998
WIZ	Znengznou	6.81	10.19	13.90	16.06	19.85	17.96	17.30	16.94	13.33	10.69	8.90	7.13
	TT 1.	2003	1998	2004	1996	2001	1995	1998	2009	2004	2004	2009	1996
MIZ	Harbin	5.59	9.31	13.79	16.00	19.87	21.61	19.81	17.09	14.55	10.00	6.27	4.56
	26.1	2003	2000	2006	2003	2004	1999	2006	2006	2007	2005	2005	2004
CIZ	Mohe	3.94	9.27	13.54	16.51	17.05	23.65	20.26	16.92	12.83	7.69	4.49	3.04
TDZ	T 1	2001	1999	2008	2008	1994	2002	1999	2005	2001	2000	2001	2001
TPZ	Lhasa	15.60	17.82	20.35	22.87	25.30	26.19	22.67	21.35	21.20	19.63	17.64	15.03

Table 3. Summary of TMYs selected and the corresponding monthly average daily global solar radiation (MJ/m^2) for the six stations in different climatic zones of China.

4. Estimation of Solar Radiation on the Inclined Surface

The monthly mean daily global solar radiation data on the inclined surface are important and useful for solar energy applications. However, daily global solar radiation data on a tilted surface are generally unmeasured and unavailable. In this paper, a simple and universal method is proposed to estimate the monthly mean daily global solar radiation on tilted surfaces facing directly towards the equator. Moreover, the monthly mean daily global radiation on a tilted surface (H_T) can be estimated by the following relation:

$$H_T = RH \tag{5}$$

where *R* is the ratio of the monthly average daily global radiation on a tilted surface to that on a horizontal surface. The ratio *R*, developed by Liu and Jordan [15,40], can be defined as:

$$R = \left(1 - \frac{H_d}{H}\right)R_b + \frac{H_d}{H}\left(\frac{1 + \cos\beta}{2}\right) + \rho\left(\frac{1 - \cos\beta}{2}\right) \tag{6}$$

where *H* and H_d are the monthly average daily global and diffuse solar radiation on a horizontal surface, respectively; R_b is the ratio of the average daily beam radiation for each calendar month on an inclined surface to that on a horizontal surface; ρ (=0.2) is the ground reflection coefficient; β is the tilt angle of photovoltaic panels. The monthly average daily global solar radiation data produced from the TMY data, proposed in our earlier research [39], are applied in the present study.

The diffuse component recommended in the previous studies [41] is adopted in this work. Accordingly, the monthly average daily diffuse solar radiation data is calculated according to:

$$H_d = H(1.00 - 1.13K_T) \tag{7}$$

where K_T is the clearness index of the sky. K_T can be obtained using the following formula:

$$K_T = H/H_0 \tag{8}$$

Here, H_0 is the monthly mean daily extraterrestrial radiation on a horizontal surface [42], which is computed by

$$H_0 = \frac{24 \times 3600}{\pi} \cdot I_0 \cdot (1 + 0.033 \cos \frac{360n}{365}) \cdot (\cos j \cos \delta \sin \omega_s + \frac{2\pi \omega_s}{360} \sin j \sin \delta)$$
(9)

where I_0 is the solar constant (1367 W/m²); *n* is the number of daily readings of the month and is counted from 1 January (1–365); *j* is the geographic latitude of the location; ω_S is the sunrise (or sunset) angle on a horizontal surface; δ is the declination of the sun. In this paper, the monthly representative day and its corresponding declination are applied and shown in Table 4.

Table 4. Monthly representative day and its corresponding declination (δ).

Month	January	February	March	April	May	June
Day (n)	$\begin{array}{c} 17 \\ -20.92 \end{array}$	47	75	105	135	162
Declination (δ)		-12.95	-2.43	9.41	18.79	23.09
Month	July	August	September	October	November	December
Day (n)	198	228	258	288	318	344
Declination (δ)	21.18	13.46	2.22	-9.60	18.91	-23.05

In the present study, the photovoltaic panels are all in the Northern Hemisphere, and the factor R_b suggested by Liu and Jordan [40] can be written as

$$R_{b} = \frac{\cos(j-\beta)\cos\delta\sin\omega_{s}' + (\pi/180)\omega_{s}'\sin(j-\beta)\sin\delta}{\cos j\cos\delta\sin\omega_{s} + (\pi/180)\omega_{s}\sin j\sin\delta}$$
(10)

where ω_{S}' is the sunrise (or sunset) hour angle for the inclined surface.

In this paper, Equations (5)–(10) are applied to calculate the monthly mean daily global solar radiation on the south-facing inclined surface for six different stations in China. The tilt angle is changed from -20° to 90° in steps of 0.1° and the corresponding value of maximum global solar radiation for a specific period is defined as the optimal tilt angle.

5. Results and Discussions

By applying the above procedure and the data from the six stations listed in Table 1, the monthly, seasonal, and yearly optimum tilt angles and total radiation on the inclined panel are calculated using Equations (5)–(10).

Table 5 shows the monthly optimum tilt angle of the six stations. The monthly optimum angles range from -14.7° (June) to 43.3° (December) for Sanya, from -5.2° (June) to 53.2° (December) for Shanghai, from -3.9° (June) to 57° (December) for Zhengzhou, from 2.6° (June) to 69.4° (December) for Harbin, from 9.3° (June) to 78.4° (December) for Mohe, and from -8.5° (June) to 60.5° (December) for Lhasa. Obviously, negative values appear in the determination of optimum tilt angles, such as for June in Lhasa. A negative value of the optimum tilt angle indicates that the photovoltaic panels face North.

Taking Harbin as an example, the calculated data generated by the above method are given in Table 6, including the monthly mean daily extraterrestrial radiation on a horizontal surface (H_0), the clearness index of the sky (K_T), diffuse solar radiation on a horizontal surface (H_d), the optimum tilt angle (β_{opt}), the monthly mean daily global solar radiation on an optimum tilt surface (H_T), and the comparison of H and H_T . Clearly, the maximum and minimum H_T values occur in June and December, respectively. Meanwhile, it can be seen from Table 6 (the last column) that the efficiency of the solar panel at the monthly optimum tilt angle is obviously increased compared to that with a horizontal surface. Within a year, the comparison of H and H_T has a maximum value of 120.95% (December).

Station	Period							Month					
0	i ciiou	January	February	March	April	May	June	July	August	September	October	November	December
	Monthly	42.9	32.5	17.4	2.7	-9.7	-14.7	-11.6	-2.8	11.9	27.8	39.9	43.3
Sanya (TZ)	Seasonal	39.6	39.6	3.5	3.5	3.5	-9.7	-9.7	-9.7	26.5	26.5	26.5	39.6
	Yearly	15.0	15.0	15.0	15.0	15.0	15.0	15.0	15.0	15.0	15.0	15.0	15.0
	Monthly	49.1	43.1	27.4	11.6	-0.3	-5.2	-3.5	7.4	23	37.6	46.6	53.2
Shanghai (SZ)	Seasonal	48.6	48.6	12.9	12.9	12.9	-0.4	-0.4	-0.4	35.7	35.7	35.7	48.6
-	Yearly	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2	24.2
	Monthly	53.1	46	32.3	15.6	2.2	-3.9	-1.3	9.8	24.6	40.3	53.3	57
Zhengzhou (WTZ)	Seasonal	52.0	52.0	16.7	16.7	16.7	1.5	1.5	1.5	39.4	39.4	39.4	52.0
, i i i i i i i i i i i i i i i i i i i	Yearly	27.4	27.4	27.4	27.4	27.4	27.4	27.4	27.4	27.4	27.4	27.4	27.4
	Monthly	68.2	60.5	45.9	26	11	2.6	6.3	19.2	38.2	54.8	65.4	69.4
Harbin (MTZ)	Seasonal	66.0	66.0	27.6	27.6	27.6	9.4	9.4	9.4	52.8	52.8	52.8	66.0
	Yearly	39.0	39.0	39.0	39.0	39.0	39.0	39.0	39.0	39.0	39.0	39.0	39.0
	Monthly	76.9	71.2	56.2	35	15.9	9.3	12.4	26.5	46.1	62.8	74.3	78.4
Mohe (MTZ)	Seasonal	75.5	75.5	35.7	35.7	35.7	16.1	16.1	16.1	61.1	61.1	61.1	75.5
	Yearly	47.1	47.1	47.1	47.1	47.1	47.1	47.1	47.1	47.1	47.1	47.1	47.1
	Monthly	58.5	48.3	32.2	13.9	-1.7	-8.5	-5	6.8	25.2	43.7	56.5	60.5
Lhasa (TPZ)	Seasonal	55.8	55.8	14.8	14.8	14.8	-2.2	-2.2	-2.2	41.8	41.8	41.8	55.8
(Yearly	27.5	27.5	27.5	27.5	27.5	27.5	27.5	27.5	27.5	27.5	27.5	27.5

 Table 5. Monthly, seasonal, and yearly optimum tilt angles for six selected stations.

Month	H_0 (MJ/m ²)	K _T	H_d (MJ/m ²)	βopt (°)	H_T (MJ/m ²)	The Comparison H_T with H (%)
January	11.13	0.50	2.42	68.2	12.06	115.69
February	16.40	0.57	3.34	60.5	16.22	74.21
March	24.57	0.56	5.04	45.9	18.12	31.42
April	32.09	0.50	6.98	26	17.18	7.39
May	40.47	0.49	8.84	11	20.08	1.04
June	41.78	0.52	8.98	2.6	21.62	0.05
July	42.91	0.46	9.48	6.3	19.87	0.30
August	36.43	0.47	8.03	19.2	17.70	3.58
September	26.95	0.54	5.67	38.2	17.33	19.13
Ôctober	19.37	0.52	4.16	54.8	15.08	50.80
November	13.02	0.48	2.86	65.4	12.18	94.23
December	10.25	0.45	2.27	69.4	10.27	120.95

Table 6. H_0 , K_T , H_d , β_{opt} , H_T , and comparison with H of Harbin.

The monthly total global solar radiation, when the tilt angle changes from -20° to 90° , is given in Figure 1. The figure indicates that for each month, there is a great difference among the monthly total global solar radiation values due to different tilt angles. In addition, the maximum value of the monthly total global solar radiation corresponds to a specific tilt angle, i.e., the monthly optimum tilt angle. For October, the maximum value of the monthly total global solar radiation for Harbin (MTZ) is 467.48 MJ/m², corresponding to 54.8° (the monthly optimum tilt angle).



Figure 1. Monthly total global solar radiation data (Harbin) when the tilt angle changes from -20° to 90° , (**a**) January–June and (**b**) July–December.

Figure 2 shows the total global solar radiation for the determined tilt angles when the solar collector is tilted at the monthly optimum tilt angle, the latitude, and the latitude ± 15 . Results reveal that the optimum angles give higher values of the optimum angle for the whole year as compared with the latitude and the latitude ± 15 . It is noted that in March, there is little difference in the radiation values determined by these methods.



Figure 2. Total global solar radiation (Harbin) for determined tilt angles.

The seasonal and yearly optimum tilt angles for six stations in different climatic zones are also given in Table 5. The seasonal optimum tilt angles are the mean of the monthly optimum tilt angles in a season, while the yearly optimum tilt angles are the average of the monthly optimum tilt angles in a year. Figure 3 shows the mean daily global solar radiation collected fixed at zero and at optimum monthly, optimum seasonal, and optimum yearly tilt angles for each month at six stations. As shown in the figure, the mean daily global solar radiation on a solar collector fixed at the monthly optimum tilt angle shows a significant increase compared to the horizontal and yearly collectors. Moreover, the mean daily global solar radiation at the optimum tilt angle is generally more than that for the horizontal collector, especially in the spring and winter at the Zhengzhou (WTZ), Harbin (MTZ), Mohe (CTZ), and Lhasa (TPZ) stations.





Figure 3. Cont.



Figure 3. Comparison between the monthly mean daily solar radiation on a solar collector fixed at zero and at optimum monthly, optimum seasonal, and optimum yearly tilt angles at six different climatic stations. (a) Sanya (TZ); (b) Shanghai (SZ); (c) Zhengzhou (WTZ); (d) Harbin (MTZ); (e) Mohe (CTZ); (f) Lhasa (TPZ).

Additionally, the correlation equations of the optimum tilt angle (β_{opt}) based on the declination factor (δ) are generated and investigated for six stations in different climatic zones of China. These correlation equations are given below, where *a*, *b*, *c*, *d* are the regression coefficients of δ from degree 0 (constant term) to degree 3, respectively.

$$\beta_{opt} = a - b \cdot (\delta) \tag{11}$$

$$\beta_{opt} = a - b \cdot (\delta) - c \cdot (\delta)^2 \tag{12}$$

$$\beta_{ovt} = a - b \cdot (\delta) - c \cdot (\delta)^2 - (d) \cdot \delta^3$$
(13)

The accuracy and suitability of the models is checked by the mean absolute bias error (MABE), the root mean square error (RMSE) and the correlation coefficient (R) [43–45]. The values of β_{opt} calculated from the above equations obtained for each station are presented in Table 7. The regression coefficients and the statistical errors of the proposed equations for the six stations in different climates of China are shown in Table 8. The MABE lies between 0.2221 MJ/m² and 2.5413 MJ/m², the maximum of RMSE is 2.8892 MJ/m² and the minimum of RMSE is 0.2697 MJ/m². Also, the mean value of the correlation coefficients R for all the six stations is as high as 0.9983. The results indicate that the monthly optimum tilt angle data obtained from the proposed models are sufficiently reliable. According to the results of the statistical indicators, Equation (13) generally has the best performance when compared with Equations (11) and (12).

Station	Equation	tion Month											
Station	-1	January	February	March	April	May	June	July	August	September	October	November	December
Camua	(11)	42.0	31.7	18.1	2.8	-9.3	-14.8	-12.4	-2.4	12.1	27.4	39.4	44.8
Sanya	(12)	42.1	31.7	18.1	2.8	-9.3	-14.8	-12.3	-2.4	12.1	27.4	39.5	44.8
(1Z)	(13)	41.9	32.3	18.2	2.3	-9.4	-14.2	-12.2	-2.9	11.9	27.9	39.6	44.3
Shanahai	(11)	50.8	40.7	27.3	12.2	0.3	-5.1	-2.7	7.1	21.4	36.4	48.2	53.5
Shanghai	(12)	50.2	41.0	28.2	12.9	0.0	-6.1	-3.3	7.4	22.3	37.0	47.9	52.5
(52)	(13)	50.0	41.6	28.4	12.3	-0.2	-5.5	-3.2	6.8	22.1	37.6	48.0	52.0
	(11)	55.2	44.6	30.7	15.0	2.5	-3.2	-0.6	9.6	24.5	40.2	52.5	58.0
Znengznou	(12)	54.5	45.0	31.6	15.6	2.2	-4.1	-1.3	9.9	25.5	40.8	52.2	57.0
(VV1Z)	(13)	54.4	45.3	31.7	15.3	2.1	-3.8	-1.2	9.6	25.4	41.1	52.3	56.7
Uarbin	(11)	69.7	58.0	42.5	25.2	11.4	5.1	7.8	19.2	35.7	53.1	66.8	72.9
(MTZ)	(12)	68.0	59.0	45.2	27.0	10.5	2.3	6.0	20.1	38.4	54.9	65.8	70.1
(IVI I Z.)	(13)	67.8	59.7	45.4	26.3	10.3	3.0	6.2	19.5	38.2	55.6	66.0	69.5
Maha	(11)	79.3	67.1	50.8	32.6	18.2	11.6	14.5	26.4	43.7	61.9	76.3	82.6
(MTZ)	(12)	77.0	68.4	54.4	35.1	17.0	8.0	12.1	27.6	47.3	64.3	75.0	79.0
(M1Z)	(13)	76.8	69.3	54.7	34.2	16.8	8.8	12.3	26.7	47.0	65.1	75.2	78.1
Lhasa	(11)	59.4	47.3	31.3	13.2	-1.0	-7.6	-4.7	7.1	24.2	42.2	56.4	62.7
(TDZ)	(12)	58.6	47.7	32.5	14.1	-1.4	-8.8	-5.5	7.5	25.4	43.0	55.9	61.4
(TPZ)	(13)	58.4	48.3	32.7	13.5	-1.6	-8.2	-5.3	6.9	25.3	43.6	56.1	60.8

Table 7. The values of the monthly optimum tilt angle (in degrees) calculated from correlations obtained for each station.

Station	Equation	а	b	С	d	MABE (MJ/m ²)	RMSE (MJ/m ²)	R
	(11)	14.9988	1.2923	-	-	0.5665	0.6751	0.9995
Sanya (TZ)	(12)	14.9353	1.2924	-0.0002	-	0.5491	0.6736	0.9995
	(13)	14.9307	1.3636	-0.0002	-0.0002	0.4429	0.5489	0.9997
	(11)	24.1982	1.2704	-	-	0.9491	1.1931	0.9995
Shanghai (SZ)	(12)	25.1463	1.2699	0.0036	-	0.8186	0.9829	0.9989
Ŭ	(13)	25.1413	1.3460	0.0036	-0.0002	0.7523	0.8901	0.9991
	(11)	27.4496	1.3257	_	-	0.8056	1.0048	0.9995
Zhengzhou (WTZ)	(12)	28.4550	1.3252	0.0038	_	0.5101	0.7036	0.9989
-	(13)	28.4522	1.3683	0.0038	-0.0001	0.5256	0.6628	0.9990
	(11)	38.9948	1.4703	_	_	1.8021	2.0810	0.9995
Harbin (MTZ)	(12)	41.7488	1.4689	0.0103	_	0.5701	0.6860	0.9960
	(13)	41.7430	1.5579	0.0103	-0.0002	0.4097	0.4830	0.9962
	(11)	47.1216	1.5402	_	_	2.5413	2.8892	0.9995
Mohe (CTZ)	(12)	50.7494	1.5385	0.0136	_	1.0451	1.2842	0.9940
	(13)	50.7418	1.6551	0.0136	-0.0003	0.8702	1.1139	0.9942
	(11)	27.5711	1.5222	-	-	0.8796	1.0273	0.9995
Lhasa (TPZ)	(12)	28.8263	1.5216	0.0047	_	0.4431	0.5035	0.9988
	(13)	28.8212	1.5993	0.0047	-0.0002	0.2221	0.2697	0.9989

Table 8. Regression coefficients and statistical indicators (MABE, RMSE, R) of Equations (11)–(13) at six different climatic stations.

6. Conclusions

The optimum tilt angle plays an important role in enhancing the energy collection of solar collectors. In the present research, the monthly, seasonal, and yearly optimum tilt angles for solar collectors in six different climatic zones of China are computed using the measured weather data from China's meteorological stations over a 16-year period from 1994 to 2009, including air-dry bulb temperature, relative humidity, wind velocity, and global solar radiation data. The results show that the calculated maximum and minimum monthly optimum tilt angles are -9.7° (June, Sanya) and 78.4° (December, Mohe) at six typical stations. The monthly optimum tilt angles, with Harbin as an example, are studied and analyzed. The yearly average optimum tilt angles for a south-facing solar collector are 15°, 24.2°, 27.4°, 39.0°, 47.1°, and 27.5° in Sanya, Shanghai, Zhengzhou, Harbin, Mohe, and Lhasa, respectively. We have found that the yearly average of the optimum tilt angle is equal to the latitude of the site. This, in general, is in agreement with the results of many other researchers [13,46]. It is observed that six cities have the highest gain in solar radiation intensity when a collector is fixed at the monthly optimum tilt angle. It can be concluded that a yearly average fixed tilt angle can be used in many general applications in order to keep the manufacturing and installation costs of collectors low. For higher efficiency, the collector should be designed such that the tilt angle can easily be changed at least on a seasonal basis, if not monthly. Moreover, the general correlation equations for estimating the monthly optimum angles are developed for six stations at different climatic zones. The three proposed models are investigated using statistical indicators (including MABE, RMSE and R). The results of the statistical analysis indicate that the models in Equations (11)–(13) obtained in the paper can be used to estimate the optimum tilt angle with a high accuracy in China. These correlations can be used elsewhere with similar climatic conditions.

It is expected that the monthly, seasonal, and yearly optimum tilt angles and the general correlation equations giving optimum tilt angles generated in this paper will exert positive effects on pertinent energy-related scientific research and engineering applications in China. Future research will focus on optimum tilt angles and the general correlations on a larger regional scale; we hope to report on such works in the near future.

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