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Risk Assessment of Drought, Based on IDM-VFS in the Nanpan River Basin, Yunnan Province, China

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Abstract: A new model for risk assessment of agricultural drought based on information diffusion method and variable fuzzy sets (IDM-VFS) was proposed. In addition, an integrated index system of agricultural drought risk was established. In the proposed model, IDM was employed to calculate the agricultural drought risk level classification standards, and then the VFS was adopted to assess the dangerousness, sensitivity, vulnerability, and comprehensive risk of agricultural droughts. In the present study, Nanpan River Basin was employed to assess the agricultural drought risk with the proposed model. The results showed that KaiYuan, ShiZong, QiuBei, and ZhanYi have higher dangerousness, due to water shortage. GuangNan have higher sensitivity and vulnerability because of lower drought resistance level and higher crop planting proportion. The comprehensive agricultural drought risk shows apparent regional characteristics: the central, western and northwestern counties have lower risk than the eastern counties. Moreover, most areas of the Nanpan River Basin are of moderate agricultural drought risk grade. The results are consistent with the actual situation of Nanpan River Basin and verify the model's effectiveness. The study can provide a scientific reference in drought risk management for local governmental agencies.

Keywords: agricultural drought risk assessment; integrated index system; information diffusion method (IDM); variable fuzzy sets (VFS); Nanpan River Basin

1. Introduction

Drought originates from a deficiency of precipitation over an extended period of time that results in water shortage for some activity, or some group [1]. It is commonly classified into four typologies: meteorological, agricultural, hydrological, and socio-economic. In recent decades, droughts have occurred more frequently and imposed adverse impacts on natural and human systems [2,3]. China is one of the countries that is most prone to drought disaster [4]. For example, from 2009 to 2011, severe droughts swept China from north to south and from east to west, which caused huge economic and societal losses [5–9]. Drought has become an important factor affecting China's agricultural and sustainable development. The Nanpan River Basin (NRB), located in the southeast of Yunnan-Guizhou Plateau slopes is one of the regions that suffer most from serious and frequent droughts [10]. Therefore, it is important to assess the risk of droughts, which can help to improve the prediction ability of droughts and to reduce the losses caused by droughts.

In order to mitigate losses caused by drought, it is necessary to assess this phenomenon adopting scientific methods. Drought index is a quantitative method that can characterize drought levels through assimilating data from one or several indices into a single numerical value [11]. The WMO

(World Meteorological Organization) defines drought index as “an index which is related to some of the cumulative effects of a prolonged and abnormal moisture deficiency” [12]. Over the years, several drought indicators have been developed to characterize droughts [13–19]. Most of these studies have focused on a single drought index, e.g., Palmer Drought Severity Index (PDSI) [13], Surface Water Supply Index (SWSI) [14], SPI Standardized Precipitation Index (SPI) [15], and Standardized Precipitation Evapotranspiration Index (SPEI) [16]. However, agricultural drought disaster is a multivariate phenomenon that contains interactive physical linkages including antecedent moisture conditions, soil type, slope, and the intensity of the precipitation event [20]. Hence, several integrated drought indicators that combine different drought variables have proposed by researchers. For example, Safavi et al. [17] developed an integrated index using multiple factors including land use, slope and soil type, precipitation, surface water storage, environment needs and other factors. Rajsekhar et al. [18] constructed a multivariate drought index (MDI) through combining hydrological and meteorological information with precipitation, evapotranspiration, runoff, and soil moisture factors. Waseem et al. [19] developed the antecedent condition-based multivariate drought index (AMDI) that includes climatic water balance, antecedent moisture conditions and other factors.

According to the natural disaster system theory, the occurrence of drought is due to dangerousness of hazard-formative factors, sensitivity of hazard-inducing environment, and vulnerability of hazard-affected bodies. The dangerousness is used to describe the abnormal degree of nature and society. The sensitivity is adopted to depict the responsiveness to nature hazards [21]. The vulnerability is conceptualized as “The conditions determined by physical, social, economic and environmental factors or processes which increase the susceptibility of an individual, a community, assets or systems to the impacts of hazards” [22]. In order to assess agricultural drought risk effectively, this study established the agricultural drought integrated index system with dangerousness indices, sensitivity indices, and vulnerability indices. Therefore, the comprehensive agricultural drought risk is defined as a composite function of dangerousness, sensitivity, and vulnerability based on the natural disaster system theory.

Drought is a fuzzy phenomenon and is difficult to evaluate mainly because of the lack of sufficient data [23]. Therefore, fuzzy and uncertainty theories have been introduced into the drought risk assessment by some researchers, such as fuzzy comprehensive evaluation [24], information diffusion [25], variable fuzzy sets (VFS) [26], and copula [27,28] et al. However, there are some deficiencies in these approaches. For example, the fuzzy comprehensive evaluation cannot well resolve the duplication information caused by related evaluation indices; the establishment of the relative membership function of the variable fuzzy sets depends on physical analysis and expert experience [29]. Taking into consideration these factors, there is a trend that combines the advantages of different of methods to construct a new approach. For example, Li et al. [30] developed a composite model based on improved information diffusion method and variable fuzzy sets to assess the disaster risk. Ouyang et al. [31] put forward a composite method based on information diffusion method and bootstrap to estimate the drought risk levels of drought-prone areas in Anhui province. Deng et al. [32] put forward a composite model based on projection pursuit and information diffusion to assess the risk of drought in the Qujing city of Yunnan province.

The variable fuzzy sets (VFS) can effectively eliminate the border effect on assessment results and make full use of various index data to obtain comprehensive risk evaluation results. The information diffusion method (IDM) can establish the level classification standards of drought risk assessment indices, and help to determine the relative membership function. Hence, in this paper, VFS was combined with IDM as an integrated model to assess the risk of agricultural drought. In the proposed model IDM was employed to calculate the level classification standards of drought risk assessment indices, and then the VFS was adopted to achieve the comprehensive risk evaluation of droughts. In the support of integrated index system and IDM-VFS model, the Nanpan River Basin in Yunnan province was taken as a case study area. The paper is organized as follows. Section 2 depicts the study

than the non-diffusion estimation [33]. In drought risk assessment, the method can establish the level classification standards of drought assessment risk indices to improve the evaluation accuracy. In this paper IDM was employed to calculate the exceeding probability of every index, then based on the national drought planning and drought data, the level classification standards of drought risk assessment indices were established. There are many types of information diffusion methods, e.g., double exponential jump diffusion, logarithmic diffusion, and the normal information diffusion method. Huang and Wang [34] demonstrated that the normal IDM is better than the logarithmic and exponential diffusion method under the small sample size condition. Therefore, in this paper the normal IDM is adopted. The definition of information diffusion can be shown as follows:

Definition 1. Suppose $X = \{x_1, x_2, \dots, x_n\}$ is a random sample set, V is the universal field, and the information diffusion method is a mapping $\mu : X \times V \rightarrow [0, 1]$ that satisfies the following three conditions [35]:

- (1) $\forall x \in X$, let v^* be the observed value of x , then $\mu(x, v^*) = \max_{v \in V} \mu(x, v)$.
- (2) $\forall x \in X, \forall v', v'' \in V$, if $\|v' - x\| \leq \|v'' - x\|$, then $\mu(x, v') \geq \mu(x, v'')$.
- (3) $\forall x \in X, \int_V \mu(x, v) dv = 1$. If V is discrete, then $\sum_V \mu(x, v) dv = 1$.

The assessment model based on the information diffusion is shown as follows:

Let the index system for drought risk assessment be $X = \{x_1, x_2, \dots, x_n\}$, $x_i (i = 1, 2, \dots, n)$ is the observed value, the level domain for the drought risk is $U = \{u_1, u_2, \dots, u_m\}$, $u_j (j = 1, 2, \dots, m)$ is a value in U . According to the national drought planning of China, the drought risk level is divided into lowest risk, lower risk, moderate risk, higher risk, and highest risk, respectively. The information carried by x_i can be diffused into u_j according to Equation (1).

$$f_i(u_j) = \frac{1}{h\sqrt{2\pi}} \exp\left[-\frac{(x_i - u_j)^2}{2h^2}\right] \cdot i = 1, 2, \dots, n, j = 1, 2, \dots, m \quad (1)$$

Here, h is the diffusion coefficient, can be calculated as follows:

$$h = \begin{cases} 0.8146(b - a), n = 5 \\ 0.5690(b - a), n = 6 \\ 0.4560(b - a), n = 7 \\ 0.3860(b - a), n = 8 \\ 0.3362(b - a), n = 9 \\ 0.2986(b - a), n = 10 \\ 0.6851(b - a)/(n - 1), n \geq 11 \end{cases} \quad (2)$$

where $a = \min_{1 \leq i \leq n} \{x_i\}$; $b = \max_{1 \leq i \leq n} \{x_i\}$.

Suppose:

$$C_i = \sum_{j=1}^m f_i(u_j) \quad (3)$$

Then, the normalized diffusion function $g_i(u_j)$ can be obtained through Equation (4):

$$g_i(u_j) = \frac{f_i(u_j)}{C_i} \quad (4)$$

Furthermore, let $q(u_j) = \sum_{i=1}^n g_i(u_j)$ and $Q = \sum_{j=1}^m q(u_j)$, then the probability of samples falls in u_j can be represented as follows:

$$p(u_i) = q(u_j)/Q \quad (5)$$

The exceeding probability of u_j can be obtained through Equation (6).

$$P(u_j) = \sum_{k=j}^m p(u_k) \tag{6}$$

Finally, according to drought grade probability classification standard, the level classification standards of drought risk assessment indices can be obtained.

3.3. Entropy Combination Weighted Method

The integrated index system of drought risk assessment includes a lot of indices. Each index plays a different role in the integrated system. The index weight reflects the relative importance of each index in the integrated index system. The entropy weight method is an objective method that determines the importance of index based on the information carried by the given data. The more concentrated information that one index provides, the less important the index is. The less concentrated information that one index provides, the more important the index is. The ANP (Analytic Network Process) is a subjective method to determine the weight of indices based on experts' experience [36]. The Super Decisions software can be adopted to determine the ANP weight of an index. Those two methods have their own advantages and disadvantages. Therefore, in this paper, we use a combined method to improve the reliability as follows:

$$\omega = \alpha\omega_1 + (1 - \alpha)\omega_2 \tag{7}$$

where ω is the combined weight, ω_1 is the subjective weight calculated by ANP, ω_2 is the objective weight calculated by entropy weight method, α ($0 < \alpha < 1$) is the coefficient, in this paper we set $\alpha = 0.5$. Then the combined weight vector ω can be calculated as follows:

$$\omega = (\omega_1, \omega_2, \dots, \omega_m) \tag{8}$$

where m is the number of sample indicators.

3.4. Variable Fuzzy Set Theory (VFS)

Chen proposed the Variable fuzzy sets (VFS) based on engineering fuzzy sets and the relative membership degrees [37]. It extends the static fuzzy set proposed by Zadeh [38] and establishes the dynamic variable fuzzy sets theory. The model can deal well with the variable fuzzy phenomena, such as flood, drought, and so on. Therefore, in this paper after the calculations of the level classification standards of drought risk assessment indices and the weight of each index, the VFS was adopted to obtain the comprehensive risk values. The VFS model is shown as follows:

Assume A is a fuzzy concept in the domain of $U(u \in U)$, \tilde{A} and \tilde{A}^c are the attract ability of U and the repellency of U , respectively. The relative membership degree (RMD) of \tilde{A} ($\forall u \in U$) is $\mu_{\tilde{A}}(u)$, which ranges from 0 to 1. The RMD of \tilde{A}^c ($\forall u \in U$) is $\mu_{\tilde{A}^c}(u)$, which ranges from 1 to 0. RMD satisfies $\mu_{\tilde{A}}(u) + \mu_{\tilde{A}^c}(u) = 1$. The relationship between $\mu_{\tilde{A}}(u)$ and $\mu_{\tilde{A}^c}(u)$ is shown in Figure 2.

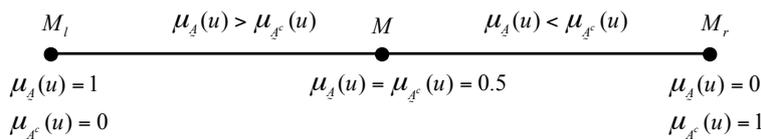


Figure 2. The relation of the relative membership degree function $\mu_{\tilde{A}}(u)$ and $\mu_{\tilde{A}^c}(u)$.

Let $D_{\tilde{A}}(u) = \mu_{\tilde{A}}(u) - \mu_{\tilde{A}^c}(u)$, where $D_{\tilde{A}}(u)$ is defined as the relative difference degree function of u to \tilde{A} that satisfy the mapping $D : u \rightarrow D_{\tilde{A}}(u) \in [-1, 1]$. Due to $\mu_{\tilde{A}}(u) + \mu_{\tilde{A}^c}(u) = 1$, then

$$D_{\tilde{A}}(u) = 2\mu_{\tilde{A}}(u) - 1 \tag{9}$$

$$\mu_{\tilde{A}}(u) = (1 + D_{\tilde{A}}(u))/2 \tag{10}$$

where $0 \leq \mu_{\tilde{A}}(u) \leq 1, 0 \leq \mu_{\tilde{A}^c}(u) \leq 1$.

Let $V_0 = \left\{ (u, D) \mid u \in U, D_{\tilde{A}}(u) = \mu_{\tilde{A}}(u) - \mu_{\tilde{A}^c}(u), D \in [-1, 1] \right\}$, $A_+ = \left\{ u \mid u \in U, 0 < D_{\tilde{A}}(u) < 1 \right\}$, $A_- = \left\{ u \mid u \in U, -1 < D_{\tilde{A}}(u) < 0 \right\}$ and $A_0 = \left\{ u \mid u \in U, D_{\tilde{A}}(u) = 0 \right\}$. A_+, A_- and A_0 are defined as the attracting sets, repelling sets and balance boundary of VFS V_0 , respectively. For any element u in the set V_0 is defined as VFS.

Suppose $X_0 = [a, b]$ is attracting sets of VFS V_0 . $X = [c, d]$ is a certain internal containing $X_0 (X_0 \subset X)$. $[c, a]$ and $[b, d]$ are the repelling sets of VFS. M is a point value which satisfies $D_{\tilde{A}}(u) = 1$ in attracting sets $[a, b]$, and M can be determined by actual problem or selected as the midpoint value of interval $[a, b]$ (see Figure 3).



Figure 3. Location relationships among points x, M and internals $[a, b], [c, d]$.

Suppose x is a random point in interval X . Then when x lies in the left side of M :

$$\begin{cases} D_{\tilde{A}}(u) = \left(\frac{x-a}{M-a}\right)^\beta; x \in [a, M] \\ D_{\tilde{A}}(u) = -\left(\frac{x-a}{c-a}\right)^\beta; x \in [c, a] \end{cases} \tag{11}$$

When x lies in the right side of M :

$$\begin{cases} D_{\tilde{A}}(u) = \left(\frac{x-b}{M-b}\right)^\beta; x \in [M, b] \\ D_{\tilde{A}}(u) = -\left(\frac{x-b}{d-b}\right)^\beta; x \in [b, d] \end{cases} \tag{12}$$

In which $\beta \geq 0$, generally, setting $\beta = 1$.

Suppose $X = \{x_1, x_2, \dots, x_n\}$ is the sample set of drought risk evaluation. The index eigenvalue of the sample j can be expressed as $x_j = (x_{1j}, x_{2j}, \dots, x_{mj})$ where m is the number of sample indices. Then the sample set can be express as $X = (x_{ij})_{m \times n}$, where $i = 1, 2, \dots, m, j = 1, 2, \dots, n$. h is the total grade number. Then the relative membership degree matrix U_h and the integrated relative membership degree ${}_i u'_h$ can be obtained as follows:

$$[U_h] = (\mu_{\tilde{A}}(u))_{ih}, i = 1, 2, \dots, m, h = 1, 2, \dots, c \tag{13}$$

$${}_i u'_h = \left(1 + \left[\frac{\sum_{i=1}^m [\omega_i (1 - \mu_{\tilde{A}}(u)_{ih})]^p}{\sum_{i=1}^m (\omega_i \mu_{\tilde{A}}(u)_{ih})^p} \right]^{\frac{\alpha}{p}} \right)^{-1}, i = 1, 2, \dots, m, h = 1, 2, \dots, c \tag{14}$$

where, ω_i is the weight of index that can be calculated by Equation (8); α is the optimal rule parameter, $\alpha = 1$ is the least single method and $\alpha = 2$ is the least square method; p is the distance parameter, $p = 1$ is Hamming distance and $p = 2$ is Euclidean distance. ${}_i u'_h$ is the non-normalized relative membership degree; Let the matrix of ${}_i u'_h$ is $U' = ({}_i u'_h)$. Then the normalized relative membership degree ${}_i u_h$ can be obtained through Equation (15), and the matrix of ${}_i u_h$ is $U = ({}_i u_h)$.

$${}_i u_h = {}_i u'_h / \sum_{h=1}^c {}_i u'_h \quad (15)$$

Finally, by adopting ranking feature value method, drought risk grade values of samples can be obtained through Equation (16).

$$H = (1, 2, \dots, c) \cdot U \quad (16)$$

3.5. Assessment Steps Based on IDM-VFS Model

- (1) The combination weight of each drought index can be calculated by Equations (7) and (8).
- (2) Based on the IDM model, the level classification standards of drought risk assessment indices can be calculated.
- (3) According to the matrix of drought risk indices level classification standard, the interval matrix $I_{ab} = ([a, b]_{ih})$, the bound matrix $I_{cd} = ([c, d]_{ih})$, and the point value matrix $M = (M_{ih})$ of index i and grade h can be obtained, where $i = 1, 2, \dots, m$, $h = 1, 2, \dots, c$. Then based on Equations (10)–(15), the relative membership degree matrix U_h and the integrated relative membership degree ${}_i u_h$ can be obtained. Finally, based on the equation of (16), the grade characteristic values (H) of the samples can be calculated.
- (4) The grade of drought risk can be obtained through Equation (17)

$$R = W \times H \quad (17)$$

where, R is the comprehensive risk of each region; W is the combinations weight.

4. Results and Analysis

4.1. Agricultural Drought Index System

The reasonable indices of agricultural drought risk assessment should be able to accurately describe the drought extent, and contain a clearly physical mechanism such as precipitation, evapotranspiration, soil, and so on. According to the natural disaster system theory and the actual situation of Nanpan River Basin, an integrated risk assessment indicator system of agricultural drought was established (see Figure 4). The entire index system is divided into three subsystems: dangerousness, sensitivity, and vulnerability.

The dangerousness indices describe the abnormal degree of nature and society. Among them the extreme precipitation and temperature are the main inducement of droughts. Generally, the higher the dangerousness the easier the drought disaster appears. That is, precipitation anomaly percentage (I_{11} : %), homogenization of precipitation and temperature (I_{12}), soil moisture from November to April (I_{13} : %), per capita water resources (I_{14} : m^3/person) and reservoir water storage capacity (I_{15} : %) are chosen to describe the dangerousness subsystem. Among them, soil moisture from November to April is determined by rate of water content of soil weight and the relative moisture of soil; reservoir water storage capacity is equal to reservoir water storage capacity at the end of year divided by average water storage capacity.

The sensitivity indices mainly describe the responsiveness to drought. The sensitivity of hazard-inducing environment includes: climate, soil, economic development level, basic irrigation facilities and other natural, social, economic and ecosystems. The greater the sensitivity, the larger

the losses of drought. The rural per capita net income (I_{21} : Yuan), agricultural irrigation water consumption per acre (I_{22} : m^3/μ), water quantity per acre (I_{23} : m^3/μ), rate of irrigated cultivated land (I_{24} : %), water-saving irrigation proportion (I_{25} : %), security area ratio (I_{26} : %), electromechanical drainage and irrigation area ratio (I_{27} : %), drought relief investment level (I_{28} : %) and emergency response ability (I_{29}) are chosen to depict the sensitivity subsystem. Among them, the drought relief investment level refers to the level of actual investment that is needed in order to mitigate the loss caused by drought and emergency response ability refers to the ability of the region to respond to drought. Both factors are determined by experts' experience.

The vulnerability indices reflect the anti-disaster capability. The higher the value vulnerability of hazard-affected bodies, the greater the loss will be. The agricultural population density (I_{31} : person/ km^2), crop planting proportion (I_{32} : %), grain output per unit area (I_{33} : kg/ μ), agricultural output value density (I_{34} : ten thousand/ km^2), drought rate (I_{34} : %) and hazard rate (I_{35} : %) are selected to depict the vulnerability subsystem. Among them, the crop planting proportion is equal to crop areas divided by land areas; agricultural output value density is equal to gross agricultural production divided by land areas.

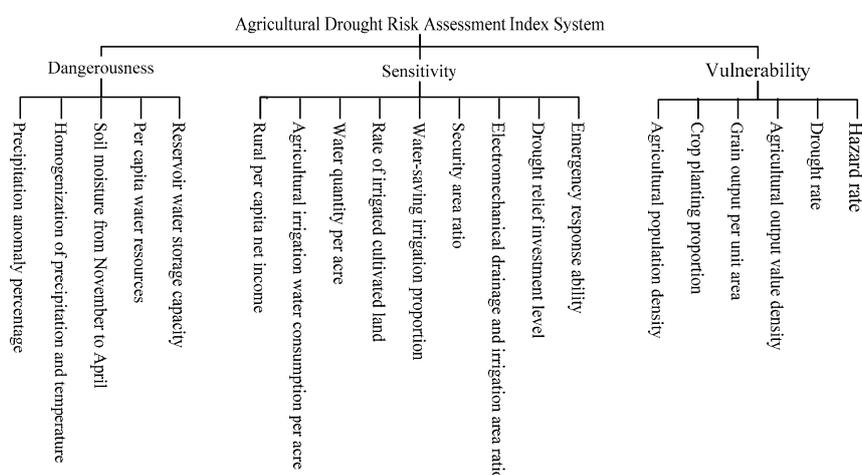


Figure 4. Agricultural drought risk assessment index system.

4.2. Evaluate Drought Risk Based on IDM-VFS Model

Based on the agricultural drought risk assessment index system and IDM-VFS model, firstly the ANP was combined with entropy to determine the weight of drought risk indices; then the information diffusion model was adopted to determine the level classification standards of drought risk assessment indices; and then the VFS model was employed to calculate the drought risk values in dangerousness, sensitivity, and vulnerability, respectively. Finally, the comprehensive drought risk grade was obtained and the risk zoning map was drawn. For demonstration purposes, Shilin has been chosen as an example to discuss the risk assessment of drought in detail.

4.2.1. The Index Values of Shilin from 2000 to 2010

For better readability, the index values were shown in terms of dangerousness, sensitivity, and vulnerability, respectively (see Tables 1–3).

Table 1. Index values of dangerousness for drought risk assessment in Shilin.

Year	Precipitation Anomaly Percentage (%)	Homogenization of Precipitation and Temperature	Soil Moisture from November to April (%)	Per Capita Water Resources (m ³ /person)	Reservoir Water Storage Capacity (%)
2000	6.25	1.44	58.14	1849.19	−38.07
2001	4.47	1.39	76.86	1997.33	−35.85
2002	14.23	0.85	69.07	2232.97	−13.73
2003	−2.56	−1.32	51.76	1844.74	−25.11
2004	−3.95	1.49	62.40	2104.12	10.25
2005	−9.24	0.02	59.38	2034.91	26.95
2006	−5.10	−0.78	52.36	1678.53	28.76
2007	2.44	1.34	69.07	2093.22	5.34
2008	−6.78	1.62	68.63	2139.32	38.48
2009	−34.74	−3.74	35.05	1221.31	−2.25
2010	−29.03	−2.32	50.29	1530.61	5.25

Table 2. Index values of sensitivity for drought risk assessment in Shilin.

Year	Rural Per Capita Net Income (Yuan)	Agricultural Irrigation Water Consumption Per Acre (m ³ /mu)	Water Quantity Per Acre (m ³ /mu)	Rate of Irrigated Cultivated Land (%)	Water-Saving Irrigation Proportion (%)	Security Area Ratio (%)	Electromechanically Drainage and Irrigation Area Ratio (%)	Drought Relief Investment Level	Emergency Response Ability
2000	1831	358.70	5306.44	28.26	52.55	11.65	8.25	10.05	50
2001	1995	354.44	5770.84	28.30	52.64	11.63	8.23	8.43	55
2002	2166	361.57	6579.76	28.62	52.66	11.85	8.30	9.70	55
2003	2312	413.94	5518.92	28.96	52.61	11.94	8.85	12.75	60
2004	2741	314.20	6336.76	29.34	52.68	11.95	8.60	12.47	60
2005	3089	368.43	6262.12	29.81	52.14	12.14	8.53	14.51	65
2006	3339	278.66	5285.88	30.67	53.90	12.81	8.98	17.24	70
2007	3708	221.14	6616.81	31.37	61.40	13.04	9.08	15.86	70
2008	4216	211.06	6750.69	31.26	65.44	13.05	8.97	18.35	75
2009	4790	199.24	3832.90	31.12	66.15	13.74	8.87	16.47	75
2010	5704	100.18	4780.11	31.15	69.80	13.77	8.80	14.65	80

Table 3. Index values of vulnerability for drought risk assessment in Shilin.

Year	Agricultural Population Density (Person/km ²)	Crop Planting Proportion (%)	Grain Output Per Unit Area (kg/mu)	Agricultural Output Value Density (Ten Thousand/km ²)	Drought Rate (%)	Hazard Rate (%)
2000	119.82	12.99	327.11	13.42	2.30	2.21
2001	120.24	12.93	326.26	15.13	10.22	9.12
2002	117.14	12.90	322.38	16.42	34.21	29.28
2003	117.74	13.00	313.41	17.21	11.17	7.49
2004	119.23	13.98	316.03	37.34	6.92	4.63
2005	119.40	14.54	309.08	38.55	2.13	1.66
2006	125.36	14.73	304.00	38.79	17.95	15.66
2007	121.13	14.83	303.14	44.42	13.85	8.12
2008	121.67	16.48	281.59	52.68	20.05	16.05
2009	122.38	16.81	274.03	56.14	15.67	4.18
2010	125.00	17.96	258.09	59.15	35.19	31.74

4.2.2. Determine the Weight of Agricultural Drought Risk Indices

Index weight was determined by combined entropy weight method and ANP. The weight of agricultural drought risk assessment indices was shown in Table 4.

Table 4. Weight of agricultural drought risk assessment indices.

Index	Weight	Index	Weight
Precipitation Anomaly Percentage (%)	0.0439	Security Area Ratio (%)	0.0196
Homogenization of Precipitation and Temperature	0.0537	Electromechanical Drainage and Irrigation Area Ratio (%)	0.0552
Soil Moisture from November to April (%)	0.0900	Drought Relief Investment Level (%)	0.0157
Per Capita Water Resources (m ³ /person)	0.0743	Emergency Response Ability	0.0652
Reservoir Water Storage Capacity (%)	0.0618	Agricultural Population Density	0.0248
Rural Per Capita Net Income (yuan)	0.0803	Crop planting Proportion (%)	0.0230
Agricultural Irrigation Water Consumption Per Acre (m ³ /mu)	0.0534	Grain Output Per Unit Area (kg/mu)	0.0594
Water Quantity Per Acre (m ³ /mu)	0.0594	Agricultural Output Value Density (ten thousand/km ²)	0.0703
Rate of Irrigated Cultivated Land (%)	0.0302	Drought Rate (%)	0.0399
Water-saving Irrigation Proportion (%)	0.0212	Hazard Rate (%)	0.0584

4.2.3. Calculate the Level Classification Standards of Agricultural Drought Risk Assessment Indices

The level classification standards of each agricultural drought risk assessment index are determined by IDM. Firstly, the index values were taken as samples of information diffusion, then the exceeding probability of each indicator were calculated; finally, the level classification standards of each drought risk assessment index were obtained (see Table 5).

Table 5. Level classification standards of each agricultural drought risk assessment index.

Index	Drought Level Standards				
	First Level Lowest	Second Level Lower	Third Level Moderate	Forth Level Higher	Fifth Level Highest
Precipitation Anomaly Percentage (%)	>−9.1	−24.5−−9.1	−33.1−−24.5	−44.5−−33.1	<−44.5
Homogenization of Precipitation and Temperature	>−0.3	−0.7−−0.3	−1.3−−0.7	−2.6−−1.3	<−2.6
Soil Moisture from November to April (%)	>70	56–70	44–56	33–44	<33
Per Capita Water Resources (m ³ /person)	>5180	3680–5180	1680–3680	680–1680	<680
Reservoir Water Storage Capacity (%)	>80	50–80	30–50	−10–30	<−10
Rural Per Capita Net Income (yuan)	>5500	4275–5500	2775–4275	1048–2775	<1048
Agricultural Irrigation Water Consumption Per Acre (m ³ /mu)	<140	140–292	292–594	594–819	>819
Water Quantity Per Acre (m ³ /mu)	>1613	1315–1613	1197–1315	829–1197	<829
Rate of Irrigated Cultivated Land (%)	>63	50–63	34–50	25–34	<25
Water-saving Irrigation Proportion (%)	>46	36–46	27–36	12–27	<12
Security Area Ratio (%)	>31	24–31	24–19	14–19	<14
Electromechanical Drainage and Irrigation Area Ratio (%)	>28	22–28	14–22	6–14	<6
Drought Relief Investment Level (%)	>17	15–17	13–15	9–13	<9
Emergency Response Ability	>90	70–90	40–70	20–40	<20
Agricultural Population Density	<50	50–136	136–286	286–378	>378
Crop Planting Proportion (%)	<6	6–18	18–25	25–40	>40
Grain Output Per Unit Area (kg/mu)	>450	350–450	250–350	150–250	<150
Agricultural Output Value Density (ten thousand/km ²)	>56	36–56	15–36	5–15	<5
Drought Rate (%)	<7	7–12	12–24	24–31	>31
Hazard Rate (%)	<5	5–11	11–20	20–25	>25

4.2.4. Calculate Agricultural Drought Risk in Terms of Three Subsystems

According to Table 5, the interval matrix, bound matrix and point value matrix were established, and then, based on Equations (10)–(16), the relative membership degree matrix and integrated membership degree were obtained, and finally the drought risk was calculated in terms of dangerousness, sensitivity, and vulnerability, respectively. The risk values of agricultural drought in Shilin from 2000 to 2010 were shown in Table 6.

Table 6. Agricultural drought risk values of Shilin from 2000 to 2010.

Year	Dangerousness	Sensitivity	Vulnerability
2000	1.35	2.87	2.98
2001	1.50	3.21	3.05
2002	1.28	3.98	3.09
2003	2.07	3.19	3.01
2004	1.65	3.89	2.93
2005	2.48	3.86	3.08
2006	2.35	3.71	3.06
2007	1.54	3.46	3.04
2008	1.72	3.35	3.08
2009	4.22	3.17	3.00
2010	3.88	2.96	3.10
Average	2.19	3.42	3.04

From Table 6, the dangerousness of 2009 is higher than other years. The vulnerability of 2010 is more serious than other years. In 2009, the precipitation was less than the normal level, the temperature was higher, and the water source in soil moisture was lower, resulting in the drought relief being difficult. The average risk value of dangerousness is 2.19, the average risk value of sensitivity is 3.42, and the average risk value of vulnerability is 3.04.

Adopting the same methods and procedures, we can obtain the average agricultural drought risk values of the other 24 counties in terms of dangerousness, sensitivity, and vulnerability, respectively (see Table 7).

Table 7. Agricultural drought dangerousness, sensitivity, and vulnerability, respectively.

County	Dangerousness	Sensitivity	Vulnerability
YiLiang	2.02	2.59	2.13
ShiLin	2.19	3.42	3.04
QiLin	1.75	2.10	2.02
MaLong	1.69	2.98	2.97
LuLiang	1.73	2.72	2.46
ShiZong	2.79	2.60	3.10
LuoPing	1.90	3.32	2.67
FuYuan	1.99	3.69	2.95
ZhanYi	2.53	2.99	2.97
HongTa	1.75	2.45	1.44
JiangChuan	1.66	2.46	1.46
ChengJiang	1.79	2.84	1.54
TongHai	1.66	2.64	2.02
HuaNing	1.67	2.66	1.83
ErShan	2.13	2.80	2.75
GeJiu	1.68	3.38	2.16
KaiYuan	2.93	3.28	2.97
MengZi	1.57	3.80	2.33
JianShui	1.51	3.71	2.95
ShiPing	1.64	3.49	3.18
MiLe	1.88	3.91	3.23
LuXi	1.64	3.68	2.87
YanShan	1.72	3.62	2.70
QiuBei	2.76	3.72	2.82
GuangNan	1.86	4.12	3.12

The dangerousness of droughts shows obvious regional characteristics in 25 counties in Nanpan River Basin. The dangerousness of KaiYuan, ShiZong, QiuBei, and ZhanYi are higher, while JianShui, LuXi, ShiPing, JiangChuan, TongHai are lower from 2000 to 2010. The major influence factors of dangerousness are meteorological conditions and water resources. The Precipitation decreased from east to west gradually, and the west regions are relatively short of water from 2000 to 2010.

The sensitivity of QiLin and HongTa are lower, while GuangNan, MiLe, QiuBei, LuXi, and ShiPing are higher. The drought sensitivity mainly depends on natural resources and drought resistance level. Water resource distribution in the Nanpan River Basin is uneven. In recent years, the local government has increased investment in drought resistant. However, the drought resistant investments in GuangNan, and QiuBei are lower, resulting in higher sensitivity.

HongTa and JiangChuan are located in the lowest drought vulnerability area, while MaLong and GuangNan are in the highest. The vulnerability of drought is the reflection of industrial structure and crop planting conditions. HongTa, JiangChuan, and TongHai are lower crop planting proportion and agricultural population density so they belong to the lower drought vulnerability counties. The crop planting proportion in MaLong and GuangNan is more than 15% and the agricultural population density is higher, leading to the highest drought vulnerability.

The comparisons in terms of drought dangerousness, sensitivity, and vulnerability, respectively in Nanpan River Basin was shown in Figure 5.

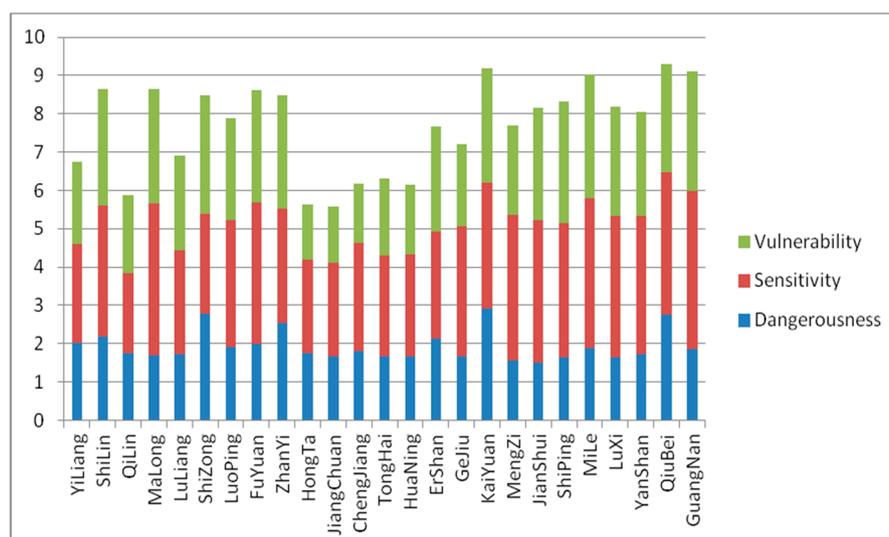


Figure 5. Comparison of drought dangerousness, sensitivity, and vulnerability, respectively in Nanpan river basin.

4.2.5. Calculate the Comprehensive Risk Assessment of Agricultural Droughts

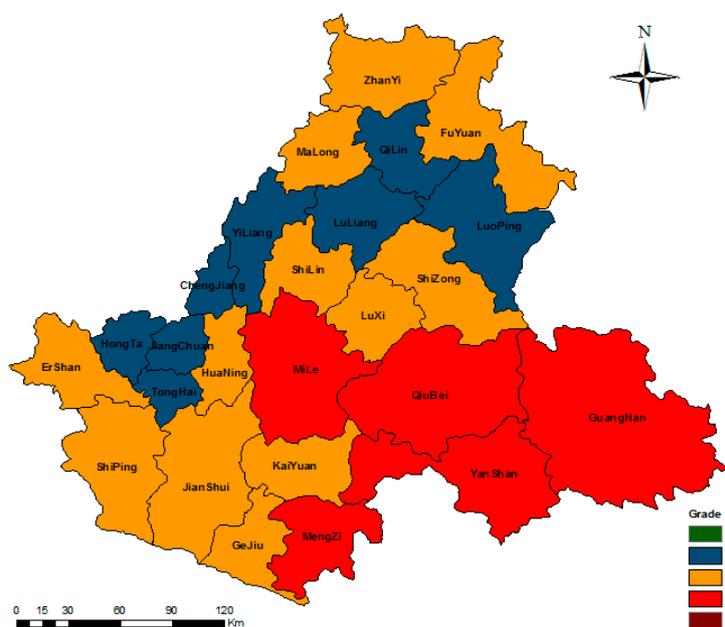
The comprehensive agricultural drought risk grades in Nanpan River Basin were shown in Table 8.

Based on the assessment results, the comprehensive risk zoning map in Nanpan River Basin was drawn.

From Figure 6, it can be see that the comprehensive risk drought in Nanpan River Basin has regional characteristics. The comprehensive drought risk in Mengzi, Mile, Yanshan, Qiubei, Guangnan is higer, while that in Yiliang, Qilin, Luliang, Luoping, Hongta, Jiangchuan, Chengjiang, Tonghaiis lower. The risk level in the central, western and northwestern areas lower than the eastern area in the Nanpan River Basin. Moreover, most areas of Nanpan River Basin experience moderate drought.

Table 8. Comprehensive agricultural drought risk in Nanpan river basin.

Country	Risk Level	Country	Risk Level
YiLiang	2	HuaNing	3
ShiLin	3	ErShan	3
QiLin	2	GeJiu	3
MaLong	3	KaiYuan	3
LuLiang	2	MengZi	4
ShiZong	3	JianShui	3
LuoPing	2	ShiPing	3
FuYuan	3	MiLe	4
ZhanYi	3	LuXi	3
HongTa	2	YanShan	4
JiangChuan	2	QiuBei	4
ChengJiang	2	GuangNan	4
TongHai	2		

**Figure 6.** Distribution of comprehensive drought risk in the Nanpan River Basin.

5. Discussion and Conclusions

With global climate change, droughts are occurring more frequently in China, and drought risk assessment is important for drought management. However, drought is a fuzzy phenomenon and there is a lack of sufficient data. It is difficult to depict it accurately through traditional statistics, especially in small sample problems. Therefore, some fuzzy and uncertainty theories have been developed to assess the risk of drought. The variable fuzzy sets (VFS) can make full use of various index data to obtain comprehensive risk evaluation results. The information diffusion method (IDM) can transform a sample observed value into a fuzzy set and is capable of dealing with small sample problems. Meanwhile, IDM can extract useful information and establish the level classification standards of agricultural drought risk assessment indices, which is helpful to determine the relative membership function of VFS. Therefore, in this research, a new model for agricultural drought risk assessment based on information diffusion and variable fuzzy sets was proposed. In the IDM-VFS model, VFS was adopted to assess the dangerousness, sensitivity, and vulnerability of agricultural drought and the comprehensive agricultural drought risk of the Nanpan River Basin.

According to the natural disaster system theory and actual situation of Nanpan River Basin, an integrated agricultural drought risk index system with drought dangerousness indices, drought sensitivity indices, and drought vulnerability indices was established. In the support of integrated index system and IDM-VFS model, the Nanpan River Basin in Yunnan province was taken as a case study area. There are many studies of drought around the world, but very few in the Nanpan River Basin. Previous studies in the Nanpan River Basin have focused on the spatial and temporal distribution of drought events and the links with some climate indices. Considering the integrated impact of dangerousness of hazard-formative factors, sensitivity of hazard-inducing environment, and vulnerability of hazard-affected bodies, to establish an integrated index system of agricultural drought risk in Nanpan River Basin is helpful to support drought risk management and develop effective mitigation strategies in this region. The results showed that KaiYuan, ShiZong, QiuBei, and ZhanYi have higher dangerousness, due to water shortage. Moreover, the sensitivity and vulnerability in GuangNan are higher than other regions because of lower drought resistance level and higher crop planting proportion. The comprehensive drought risk shows apparent regional characteristics, the central, western and northwestern counties have lower risk than the eastern counties. In addition, most areas of the Nanpan River Basin are located in a moderate drought risk region. The results are consistent with the actual situation of the Nanpan River Basin and can provide reference and decision-making for the emergency management department. However, due to the complexity of risk assessment of droughts, the formation mechanism, and risk management of regional drought need to be studied further.

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