

## Supporting Information for

# **Estimating diurnal courses of gross primary production for maize: a comparison of sun-induced chlorophyll fluorescence, light-use efficiency and process-based models**

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## **Introduction**

This supporting file provides a more detailed description of the method to determining water stress factor in the MuSyQ-GPP algorithm and results obtained using SIF686.

## **Text S1. Estimation of water stress factor in the MuSyQ-GPP algorithm**

The limited effect of water conditions on plant photosynthesis, ranging between 0.5 and 1, is derived following the algorithm

$$f_2(\beta) = 0.5 + 0.5E / E_p \quad (1)$$

where  $E$  and  $E_P$  represent actual and potential evapotranspiration, respectively.

In the MuSyQ-GPP algorithm, a modified Penman-Monteith (P-M) approach with biome-specific canopy conductance was used to estimate actual evapotranspiration (Qiao et al. 2015; Zhang et al. 2009). The available energy component for canopy ( $A_{\text{canopy}}$ ) and soil ( $A_{\text{soil}}$ ) are generated using FPAR

$$A_{\text{canopy}} = FPAR \times A \quad (2)$$

$$A_{\text{soil}} = (1 - FPAR) \times A \quad (3)$$

where  $A$  is approximated as net radiation consisting both net shortwave radiation and net longwave radiation. Vegetation transpiration is defined as

$$\lambda E_{\text{canopy}} = \frac{\Delta A_{\text{canopy}} + \rho C_p VPD g_a}{\Delta + \gamma(1 + g_a / g_c)} \quad (4)$$

where  $\lambda E_{\text{canopy}}$  ( $\text{W m}^{-2}$ ) is the latent heat flux of canopy,  $\Delta = d(e_{\text{sat}})/dT$  ( $\text{Pa K}^{-1}$ ) is the slope of the curve relating saturated water vapor pressure  $e_{\text{sat}}$  (Pa) to air temperature  $T$  (K),  $\rho$  ( $\text{kg m}^{-3}$ ) is air density,  $C_p$  ( $\text{J kg}^{-1} \text{K}^{-1}$ ) is the specific heat of air at constant pressure,  $VPD = e_{\text{sat}} - e$  (Pa) is the vapor pressure deficit of air,  $g_a$  ( $\text{m s}^{-1}$ ) is aerodynamic conductance and defined as  $0.01 \text{ m s}^{-1}$  in our study by referring to Zhang et al. (2008),  $\gamma$  ( $\text{Pa k}^{-1}$ ) is psychometric constant, and  $g_c$  ( $\text{m s}^{-1}$ ) is canopy conductance and can be described as

$$g_c = \frac{g_{\text{sx}}}{K_Q} \ln \left[ \frac{Q_h + Q_{50}}{Q_h \exp(-K_Q LAI) + Q_{50}} \right] \left[ \frac{1}{1 + VPD/D_{50}} \right] \quad (5)$$

where  $K_Q$  is the extinction coefficient for PAR,  $Q_h$  is the PAR at the top of canopy,  $Q_{50}$  and  $D_{50}$  are the values of APAR and water vapor deficit when stomatal conductance is half its maximum value, respectively. For our study, values of  $g_{\text{sx}}$ ,  $K_Q$  and  $D_{50}$  are assigned to  $0.0032 \text{ m s}^{-1}$ ,  $0.6$  and  $800 \text{ Pa}$ , respectively (Zhang et al., 2008).

Soil evaporation is calculated using a soil evaporation equation (Mu et al. 2011; Zhang et al. 2009):

$$\lambda E_{\text{soil}} = RH^{(VPD/k)} \frac{\Delta A_{\text{soil}} + \rho C_p VPD g_a}{\Delta + \gamma \times g_a / g_{\text{totc}}} \quad (6)$$

where  $\lambda E_{\text{soil}}$  ( $\text{W m}^{-2}$ ) is the latent heat flux of soil,  $RH$  is the relative humidity of air with

values ranging from 0 to 1,  $k$  (Pa) is a parameter to fit the complementary relationship and is empirically adjusted for different vegetation types, and  $g_{\text{totc}}$  ( $\text{m s}^{-1}$ ) is the corrected value of total aerodynamic conductance as described by Zhang et al. (2010).

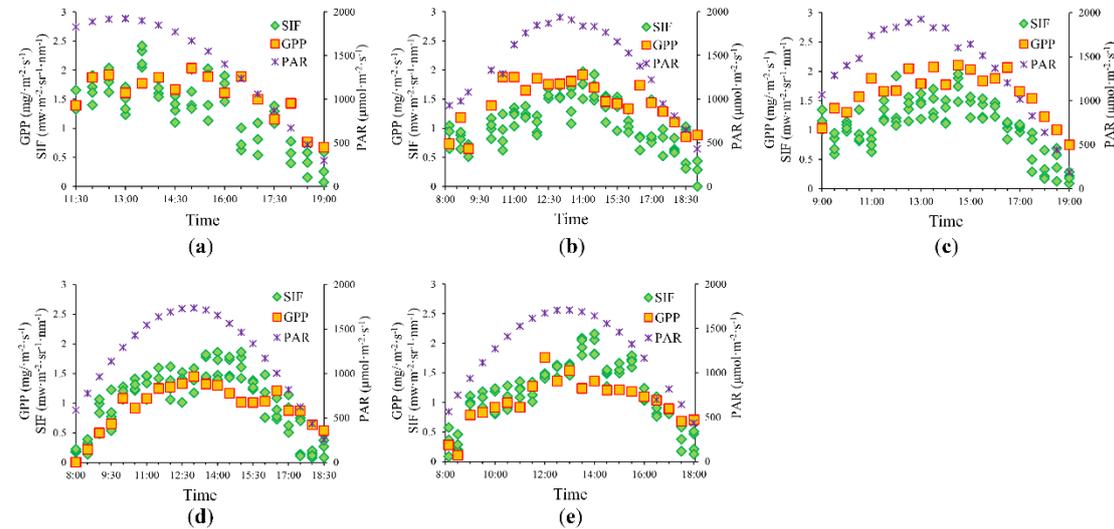
The potential evapotranspiration,  $E_p$ , is calculated using the Priestley and Taylor (P-T) equation (Priestley and Taylor, 1972).

$$\lambda E_p = \varphi A \frac{\Delta}{\Delta + \gamma} \quad (7)$$

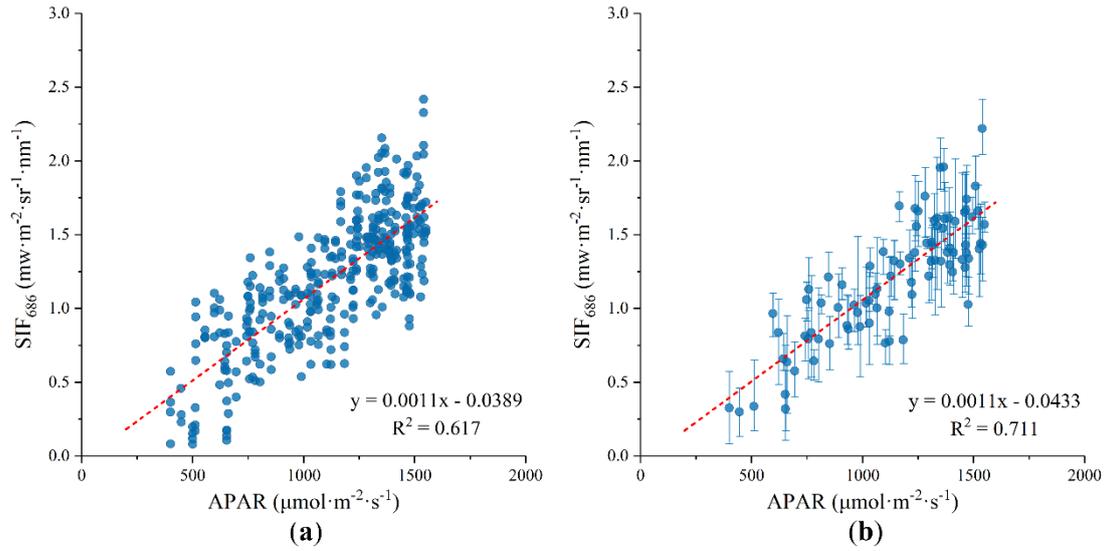
where the P-T coefficient  $\varphi$  was set to 1.26 following Priestley and Taylor (1972) in the study.

## Text S2. Performance of the SIF<sub>686</sub>-based GPP model

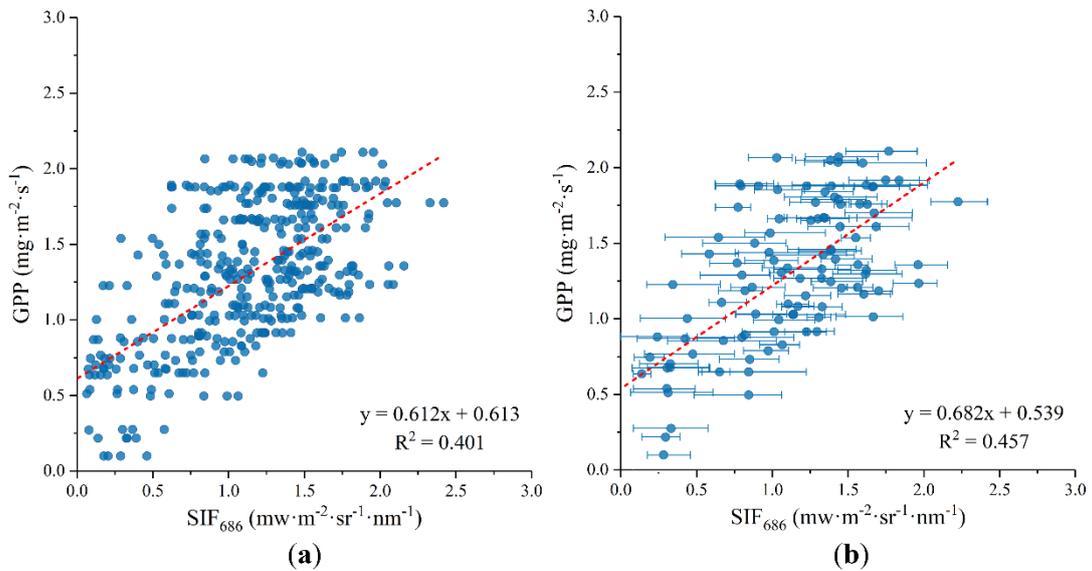
SIF<sub>686</sub> was less correlated with GPP than SIF<sub>760</sub>. The optical absorption at far-red band of a leaf is smaller than 10%, while it is over 90% at the red band (Jacquemoud and Baret, 1990). The reabsorption of SIF<sub>686</sub> influenced by chlorophyll content and canopy structure is larger than that of SIF<sub>760</sub> (Liu et al. 2016, 2017). Therefore, SIF<sub>686</sub> values presented a larger diversity than SIF<sub>760</sub> at the four positions of the canopy and the SIF<sub>686</sub>-based GPP model showed a much limited performance than SIF<sub>760</sub>.



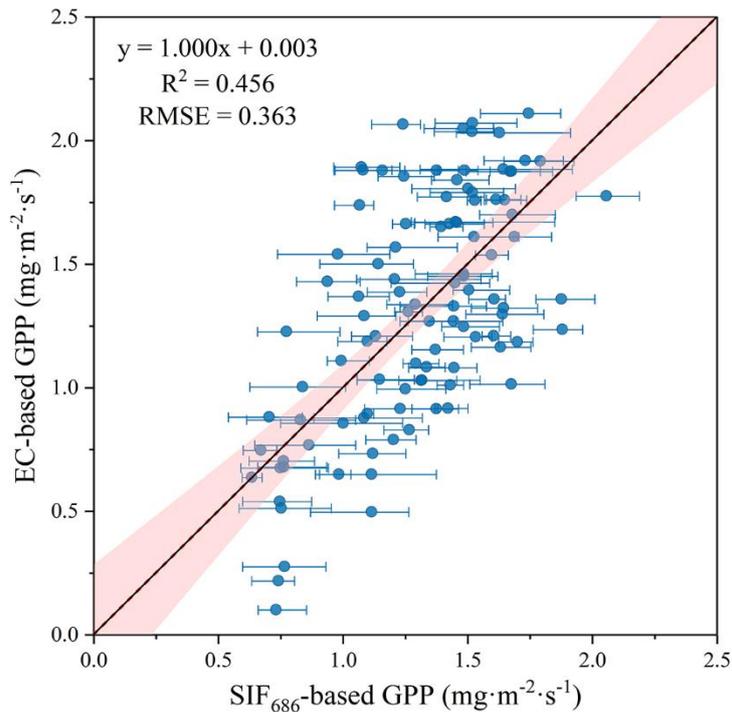
**Figure S1.** Diurnal patterns of PAR, GPP and SIF<sub>686</sub> during the experiment: (a) July 10th. (b) July 17th. (c) July 18th. (d) August 21st. (e) August 22nd.



**Figure S2.** Relationship between APAR and (a) individual SIF<sub>686</sub> and (b) averaged SIF<sub>686</sub>. The error bar indicates the range of SIF<sub>686</sub> values for four measurements.



**Figure S3.** Relationship between (a) individual SIF<sub>686</sub> and GPP, (b) averaged SIF<sub>686</sub> and GPP. The error bars indicate the range of SIF<sub>686</sub> values for the four measurements.



**Figure S4.** Relationships between SIF<sub>686</sub>-based GPP and EC-based GPP during the experiment period. The red shades represent the 95% confidence bands for the regression functions.

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