



Article Novel Charge Ordering in the Trimer Iridium Oxide BaIrO₃

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Abstract: We have prepared polycrystalline samples of the trimer Ir oxide BaIrO₃ with face-shared Ir_3O_{12} trimers, and have investigated the origin of the phase transition at 182 K by measuring resistivity, thermopower, magnetization and synchrotron X-ray diffraction. We propose a possible electronic model and transition mechanism, starting from a localized electron picture on the basis of the Rietveld refinement. Within this model, BaIrO₃ can be basically regarded as a Mott insulator, when the Ir_3O_{12} trimer is identified to one pseudo-atom or one lattice site. The transition can be viewed as a transition from the Mott insulator phase to a kind of charge ordered insulator phase.

Keywords: face-sharing; Iridium oxide; charge order; structure-property relation

1. Introduction

Strongly correlated electrons are seen in a certain class of solids in which the Coulomb repulsion is too strong to hold a simple one-electron picture based on the band theory. They have occupied a central position in condensed matter sciences for many decades, and have attracted keen interests from vast numbers of researchers since the discovery of high-temperature superconducting copper oxides in 1986. They store a macroscopic number of degeneracy and entropy based on spin and charge degrees of freedom on each lattice site at high temperature [1,2], and release them through various phase transitions towards 0 K. Various forms of phase transitions and ordered states have been discovered one after another with the progress in the studies of strongly correlated electrons. In this context, understanding of new phase transitions and ordered states is a major purpose for strong-correlation physics.

BaIrO₃ (18*R* phase) is an interesting oxide as a playground for a new phase transition. The crystal structure is schematically shown in the inset of Figure 1b, in which the three IrO₆ octahedra are connected with one another in a face-sharing network, and form an Ir₃O₁₂ trimer structure, as indicated in light brown and dark yellow. The trimers are connected with each other in a corner-sharing network and construct zig-zag chains along the *c* axis and corrugated honeycomb lattices in the *ab* plane. Owing to the low crystal symmetry of C2/m, two trimers are inequivalent in the unit cell, as painted in different colors in the inset of Figure 1b.

The study of this oxide has a rather long history; Donohue *et al.* first reported the synthesis and structure of this material in the 60s, [3], and later Gai *et al.* [4] studied the poly-types of 5H and 6H. Chamberland [5] extensively studied the relationship of the poly-types to the synthetic routes, and further found a magnetic phase transition near 200 K. The physical and chemical properties of the poly-types have been measured rather recently because of difficulty in the sample synthesis [6,7]. Siegrist and Chamberland [8] prepared single crystals and determined the crystal symmetry of C2/m, which can be viewed as pseudo-rhombohedral *R*-centered. Later Powell and Battle [9] identified that this magnetic order is ferromagnetic, by measuring the temperature hysteresis and the magnetization-field curve. Linsay et al. [10] measured the remnant magnetization to demonstrate the ferromagnetic ground state. Cao et al. [11] measured the transport and optical properties of a single-crystal sample of $BaIrO_3$, and found that the ferromagnetic order accompanies rapid increase in the resistivity below $T_c \sim 180$ K. In addition, they observed a gap-like structure in the optical conductivity below around 1000 cm⁻¹, and attributed this transition to charge-density-wave (CDW) formation with ferromagnetic order. They further found the additional two temperature anomalies near 80 and 30 K. Although the 80-K anomaly was ill-defined, the 30-K anomaly was detected by other groups in a muon-spin-relaxation experiment [12] and in a nonlinear conduction measurement [13]. Kini et al. [14] measured the specific heat of BaIrO₃ and observed a small jump of 2 J/mol K around 180 K, not around 30 and 80 K. They also found that the thermopower rapidly increases below T_{c} , and pointed out the existence of a charge gap below T_c . Maiti *et al.* [15] discussed the CDW state through photoemission spectroscopy.

In this paper, we try to address the nature and mechanism of the 180-K phase transition in BaIrO₃ on the basis of the electronic states constructed from a localized electron picture. A concern in the CDW scenario is that there is no evidence for the lattice distortion at T_c . In conventional CDW materials, a lattice modulation of $2k_F$ emerges below T_c through the electron-phonon interaction, where k_F is the Fermi wavenumber [16]. To the best of our knowledge, no superlattice reflections below T_c have been reported in BaIrO₃, and this implies that the charge gap opens without translational-symmetry breaking. We have investigated the structure-property relationship through synchrotron X-ray diffraction, and propose a possible mechanism of the transition.

2. Experimental Section

Polycrystalline samples of BaIr_{1-*x*}Ru_{*x*}O₃ ($x \le 0.1$) were prepared using a conventional solid-state reaction. A stoichiometric mixture of powder sources of BaCO₃ (99.9%), RuO₂ (99.9%) and Ir (99%) was thoroughly ground in an agate mortar. The mixture was then pre-sintered in an alumina crucible at 900 °C for 12 h in air, and was pressed into pellets after re-grinding. The pellets were sintered at 1000 °C for 36 h in air.

The synchrotron X-ray diffraction was taken at BL8A & 8B (Photon-Factory, KEK, Tsukuba, Japan). The X-ray energy was adjusted to be 18 keV, which was carefully calibrated using a standard powder sample of CeO₂. Powder samples were sealed in a silica-glass capillary of 0.1-mm diameter, and the capillary was rotated by an angle of 30° from the sample-stage axis during measurement. The sample temperature was controlled using a cool helium gas or nitrogen gas. The diffraction patterns were analyzed using the Rietveld refinement with Rietan-FP code [17].

The resistivity was measured with a four-probe technique using a home-made measurement system in a liquid-helium cryostat. The thermopower was measured with a two-probe method using a home-made measurement system in a liquid-helium cryostat, and the thermopower of the measurement leads was carefully subtracted. The temperature difference was typically 0.5 K which was monitored with a copper-constant differential thermocouple. The magnetization was measured with a commercial product of Quantum Design Magnetic-Property-Measurement-System.

3. Results

Figure 2 shows a synchrotron X-ray diffraction pattern of BaIrO₃ at room temperature. Since the scattering intensity of oxygen is 100 times weaker than that of Ba and Ir, we gave up determining the atomic position of oxygen atoms, but instead employed the values reported in the literature [8]. Then, we optimized the atomic positions of Ba and Ir atoms above 100 K by iterating the calculation until the R_{wp} and S_R values reached less than 3 % and 4%, respectively. We accepted worse values of $R_{wp} = 3\% - 4.5\%$ for the data below 100 K. The experimental data are compared with the refinement at 300, 150 and 34 K in Figure 2b–d, respectively. As shown in Figure 2, the refinement is satisfactory; there are neither detectable impurity phases nor poly-type phases, and the deviation from the refinement seems small enough to discuss the atomic positions of the Ir atoms. We measured the diffraction patterns around T_c carefully, and found no trace of superlattice reflections. This consolidates that the phase transition does not accompany the violation of translational symmetry, also indicating that this is unlikely to be a CDW transition.

Figure 1a shows the transport properties of the polycrystalline sample of BaIrO₃ obtained from the same batch as used in the X-ray measurement. The resistivity is non-metallic at all temperatures with an anomalous increase near $T_c = 182$ K. We should note that the resistivity above T_c is of activation type as indicated by the dotted line shown in the inset of Figure 1a. The slope of the dotted line gives a rough estimate of the activation gap E_g^{ρ}/k_B around 240 K, which is small in comparison with a band gap of conventional semiconductors. This is comparable to or even smaller than k_BT , and it is nontrivial whether or not we may regard this non-metallic behavior as activation-type transport. According to the band calculation of BaIrO₃ [18–20], the electronic states above T_c are *metallic* with no gap in the density of states.



Figure 1. (a) resistivity and thermopower of a polycrystalline sample of BaIrO₃. The inset shows the Arrhenius plot of the resistivity, in which the dotted line indicates the activation transport above the transition temperature T_c ; (b) magnetization M divided by an external field H of 500 Oe of the same sample. The dotted line represents $T_c = 182$ K. The inset shows the schematic picture of the crystal structure of BaIrO₃.

The thermopower also shows an anomaly near T_c , below which it rapidly enhances with decreasing temperatures. As Kini *et al.* pointed out [14], this is a clear indication of the charge gap in the density of states [21,22], strongly indicating an insulating nature below T_c . The thermopower takes a broad maximum near 100 K, and goes towards zero with decreasing temperature. We think

this behavior is a crossover between the activation-type transport from 100 to 180 K and the hopping conduction in the impurity states below 100 K [23]. The thermopower above T_c is difficult to interpret; the magnitude is as small as that of metals, but the temperature dependence seems of activation type just above T_c . We evaluate an activation energy E_g^S/k_B to be 90 K by assuming $S = E_g^S/eT$. Again, this activation energy is comparable or smaller than k_BT . We will come back to this point later.



Figure 2. (**a**) synchrotron X-ray diffraction pattern of $BaIrO_3$ at room temperature. For the details of the refinement, see text. Comparison between the observed data and the refinement at (**b**) 300 K; (**c**) 150 K; and (**d**) 34 K.

Figure 1b shows the magnetization divided by an external field of 500 Oe measured in the field-cooling process. Around the same temperature of T_c , the magnetization suddenly shows up with decreasing temperature. This ferromagnetic behavior is consistent with the previous reports [10,11,24,25]. From this figure, the magnetization at 4 K is evaluated to be around 100 emu/mol, which corresponds to a saturation magnetization of 0.016 μ_B /Ir. This unusually small moment is consistent with the previous works [10,11,24,25], and is associated with weak ferromagnetism of itinerant magnets. However, the electronic ground state of this oxide is an insulator with a finite energy gap in the density of states, and the origin of the ferromagnetism is yet to be explored.

Figure 3a–d show the lattice parameters plotted as a function of temperature obtained from the Rietveld refinement of the X-ray diffraction patterns. The relative uncertainty is less than 0.01%, and the size of the error bars are smaller than the size of the closed circles. All the parameters smoothly change with temperature across T_c , indicating a nature of second-order transition. By having a closer look at the data in Figure 3a, one finds a slight cusp in the *a*-axis length near T_c as a piece of evidence for finite electron-lattice coupling.



Figure 3. (**a**–**d**) lattice parameters of BaIrO₃. (**a**) *a*-; (**b**) *b*-; and (**c**) *c*-axis length; (**d**) monoclinic angle β ; (**e**) The intra-timer Ir-Ir bond length *d*₁₂ and *d*₃₄; and (**f**) the inter-timer angle Φ . The inset schematically designates *d*₁₂, *d*₃₄ and Φ .

The *c*-axis length parallel to the zig-zag chain of the trimers exhibits remarkable and nontrivial temperature dependence; it increases with decreasing temperature as shown in Figure 3c. Such negative temperature dependence is difficult to understand from solely lattice effects [26] except for ZrW_2O_8 [27]. The negative expansion is not observed in CDW materials [16,28], and can be another piece of evidence that this transition is not CDW-like, but, rather, the negative lattice expansion comes from various electronic origins [29]. Prime examples are Invar alloy [30], BaNiO₃ [31] and Mn₃*A*N (A = Cu, Zn, Ga) [32], in which electronic or magnetic instability tightly couples with the lattice. The slopes of the negative expansion in the *c*-axis length significantly change across T_c as shown by the dotted lines, clearly indicating that the negative expansion characterizes the phase transition of the title compound. One may notice that the angle β also increases with decreasing temperature. Since the increase in β reduces the lattice volume, the *c* axis tends to expand in spite of the volume shrinkage at low temperature.

In order to clarify the structural origin of the negative expansion in the *c*-axis length, we examined what kind of atomic displacement is responsible, and have finally arrived at the intra-trimer Ir-Ir bond length. As schematically shown in the inset of Figure 3e, there are four crystallographically inequivalent Ir sites labeled 1, 2, 3 and 4. We define the bond length between Ir1 and Ir2 as d_{12} and that between Ir3 and Ir4 as d_{34} . As shown in Figure 3e, d_{34} increases with decreasing temperature, whereas d_{12} remains constant. This clearly indicates that the two timers are more inequivalent at lower temperatures. The data are somewhat scattered in comparison with the lattice parameters, possibly because the latter is determined only by the 2θ values of the diffraction peaks whereas the former needs accuracy in the relative intensity. Nevertheless, we emphasize that d_{12} and d_{34} were independently determined at each temperature within an uncertainty of 10^{-4} , and that increasing inequivalence at low temperatures is inherent in this oxide. In addition, we have ascribed the structural origin for the temperature dependence of β to the inter-timer angle Φ as indicated at the inset of Figure 3e. Figure 3f shows Φ plotted as a function of temperature, where Φ increases with decreasing temperature. We can summarize the above results as follows: One trimer of Ir3–Ir4–Ir3 elongates with decreasing temperature, and concomitantly the lattice distorts to accept the elongation.

As mentioned above, it is difficult to determine the atomic position of the oxygen atoms from the synchrotron X-ray diffraction used in the present experiment, and this constraint prevents us from

evaluating the formal valence of Ir ions using bond-valence-sum calculation. In the next section, we try to estimate the formal Ir valence by using the atomic position data for oxygen from [8]. Nevertheless, we may infer from d_{12} and d_{34} that the average number of d electrons in the Ir3–Ir4–Ir3 timer is *larger* than that in the Ir1–Ir2–Ir1 trimer, for d electrons feel the static Coulomb repulsion with one another to stay as far as possible. We further speculate that a finite fraction of charge rapidly transfers at T_c between the two trimers, and also expect that this charge transfer is a driving force for the phase transition. In this respect, this charge transfer should be associated with the CDW scenario by Cao *et al.* [11]. One essential difference from the conventional CDW is that the two trimers are already inequivalent above T_c , and this charge transfer causes no superlattice reflections with holding the same unit cell at all temperature.

4. Discussion

Having the above results in mind, let us propose here a possible electronic model for BaIrO₃ starting from the localized picture. As schematically drawn in Figure 4a, one Ir ion has the electronic configuration of $(5d)^5$ in the triply degenerate t_{2g} level, for the formal valence of Ir is 4+. Since the oxygen octahedron is trigonally distorted, the t_{2g} level lifts the degeneracy to have the a_{1g} and doubly-degenerate e'_g levels. In the present case, the octahedron is compressed along the (111) direction of the local coordinate, and thus the a_{1g} level is the higher level with one electron occupied.

There is a strong hybridization between the a_{1g} levels within a trimer owing to the short intra-trimer Ir-Ir distance, and a kind of molecular orbital is expected to be formed within the trimer as shown in the right side of Figure 4a, where we denote the bonding, non-bonding and anti-bonding orbitals made of the three a_{1g} orbitals as B, NB and AB, respectively. By putting the three electrons from the bottom, we find one electron in the non-bonding orbital. Thus, we may regard this state as half-filling, when we identify one trimer to one pseudo-atom. In this sense, we propose that BaIrO₃ is a half-filled trimer solid.

Very recently, Ir compounds have attracted extensive interest as a strong spin-orbit interaction system, in which the total angular momentum of j dominates the band structure [34]. A recent X-ray absorption study has revealed the strong spin-orbit nature in BaIrO₃, and the highest occupied level should be regarded as the e'' level rather than the a_{1g} level from the t_{2g} levels as shown in Figure 4b [33]. Even in such a case, we can make similar molecular orbitals. The highest occupied state then corresponds to the NB e'' instead of the NB a_{1g} , and is unlikely to alter the picture of the half-filled trimer solid (compare the left and right sides of Figure 4c,d. As is widely accepted, half-filled electron systems is unstable against Mott insulator phase in the presence of electron-electron correlation. We propose the normal state of BaIrO₃ is essentially in the Mott insulator phase, and name this "trimer Mott insulator".

Let us discuss here about the charge transport above T_c . According to the Landau theory of metal-insulator transition [35], there is a critical end point above which metals and insulators cannot be distinguished. In fact, the transport properties above the critical end point can be viewed as either bad metals or bad insulators, as reported in V₂O₃ [36] and κ -(BEDT-TTF)Cu[N(CN)₂]Cl [37]. We propose that the normal state of BaIrO₃ should be understood basically in terms of trimer Mott insulator, with the critical end point below T_c . If so, the charge transport seems to show intermediate properties between metal and insulator, which are exemplified by the small activation energies of E_g^{ρ} and E_g^{S} . Zhao *et al.* [38] have found that external pressure increases the resistivity to enhance the insulating nature of the title compound. They further found that the transition temperature decreases with pressure. Kida *et al.* [25] have also found the large pressure dependence of T_c in the magnetization measurement. Their results indicate that the pressure stabilizes the insulating normal state, being consistent with our trimer-Mott-insulator picture above T_c . Cao *et al.* [39] have also stated that BaIrO₃ is in the verge of a metallic state.



Figure 4. A model for the electronic states of BaIrO₃ starting from a localized electron picture. (a) the electronic configuration of Ir^{4+} in a regular and trigonally distorted IrO_6 (left). The highest occupied orbitals of Ir_3O_{12} trimer (center) and the molecular orbital formation (right). B, NB and AB denote bonding, non-bonding and anti-bonding orbitals, respectively; (b) the electronic configuration of Ir^{4+} in the strong spin-orbit coupling limit (taken from [33]); (c) the electronic states of BaIrO₃ above T_c . 1–2–1 and 3–4–3 correspond to the inequivalent Ir_3O_{12} trimers; The case for strong spin-orbit coupling is drawn in the right side. (d) the electronic states of BaIrO₃ below T_c .

Figure 4c schematically shows the trimer Mott insulator phase above T_c . The Ir1–Ir2–Ir1 trimer is in the higher level because of the shorter intra-trimer Ir–Ir bond length. All the timers have one electron in the NB a_{1g} or e'' level, and the energy difference $\Delta \varepsilon$ is too small to cause charge transfer. As the intra-trimer Ir–Ir bond length of the Ir3–Ir4–Ir3 trimer increases with decreasing temperature, $\Delta \varepsilon$ is expected to increase. At a certain temperature, a rapid increase of $\Delta \varepsilon$ and a charge transfer simultaneously happen, and the electronic states schematically drawn in Figure 4d realize below T_c , where the NB orbital of the Ir1–Ir2–Ir1 trimer is empty and that of the Ir3–Ir4–Ir3 timer is fully occupied. From the view point of valence change, the Ir⁴⁺ state changes into a disproportionate state of Ir^{3.67+} and Ir^{4.33+} in the neighboring trimers. We regard this state as a kind of charge ordered state rather than CDW state, because this has no relation to the Fermi surface information such as nesting or $2k_F$ [16]. We therefore propose that the transition at 180 K in BaIrO₃ is a phase transition from the trimer Mott insulator phase to the trimer charge ordered phase.

We will try a rough estimate for the formal Ir valence ν using the bond valence sum calculation [40] given by $\nu = \sum_{i=1}^{6} \exp[(d_0 - d_i)/0.37]$, where d_i is the Ir-O bond length in a IrO₆ octahedron in units of angstrom, and $d_0 = 1.87$ Å for Ir⁴⁺ [41]. Since the positions of oxygen atoms are not well determined in the present refinement, we have instead employed the atomic position data at 300 K from [8] and have calculated ν as listed in Table 1. The 300-K data indicate that the two trimers already have different charges; the Ir1–Ir2–Ir1 trimer has a net charge of 12.23, whereas the Ir3–Ir4–Ir3 trimer has a 0.45-shorter value of 11.78. Unlike the related ruthenate Ba₄Ru₃O₁₀ [42], the charge is not disproportionated within trimer significantly. A slight difference (0.16 for Ir1 and Ir2; 0.07 for Ir3 and Ir4) may correspond to the bonding orbital widely spread within trimer, as is pointed out in [43]. For the calculation of the 16-K values, we used our data of d_{12} and d_{34} shown in Figure 3e, and assume that the trimers uniformly expand or shrink with temperature. Namely, we assume that the Ir-O bond lengths change with temperature in the same ratio as the Ir-Ir bond lengths. For the Ir3–Ir4–Ir3 trimer, d_{34} increases from 2.615 to 2.640 Å from 300 down to 16 K, and thus the Ir-O bond lengths at 16 K equals the 300-K value multiplied by a factor of 2.640/2.615 = 1.0096, while they remain unchanged for the Ir1–Ir2–Ir1

trimer. With this assumption, ν for Ir3 and Ir4 is further reduced from the values at 300 K, as was discussed in the last paragraph of Section 3. At 16 K, the Ir1–Ir2–Ir1 trimer has a net charge of 12.23, whereas the Ir3–Ir4–Ir3 trimer has a 1.05-shorter value of 11.18. This is in a reasonable agreement with the picture in Figure 4d in spite of our rough and bold assumption.

Table 1. Estimation of the formal Ir valence. The atomic positions for 300 K are employed from [8]. For the data at 16 K, we assume that Ir-O bond length changes with the same ratio as d_{12} and d_{34} . Namely, we use the same Ir-O bond lengths as at 300 K for Ir1 and Ir2, and values 0.96%-larger than at 300 K for Ir3 and Ir4.

Temperature	Ir1	Ir2	Ir3	Ir4
300 K	4.13	3.97	3.95	3.88
16 K	4.13	3.97	3.75	3.68

Here, let us compare our model with band calculations reported previously [18–20]. Whangbo and Koo [18] have pointed out that the density of states of Ir2 and Ir4 (the central Ir ion in the trimer) show pseudo gap at the Fermi energy. This is explained in terms of molecular orbital. The highest occupied states belong to the non-bonding orbital of the a_{1g} or e'' state of the Ir ion, which has a node at the center of the trimer. Note that the non-bonding orbital is expressed by $(\varphi_L - \varphi_R)/\sqrt{2}$, where φ_L and φ_R are the a_{1g} or e'' state at the left and right edges of the trimer. The hybridization effects are also seen in other calculations [19,20], and in particular, the calculation with strong spin-orbit interaction [20] gives a small Mott gap which is consistent with the observed small activation energies of E_g^{ρ} and E_g^S . Since the band calculation was based on the structure at room temperature, the calculated insulating states should be those above T_c .

Our proposed model can explain various experimental results at least semi-quantitatively. It explains bad metal/bad insulator behavior above T_c , a charge gap below T_c without translational-symmetry breaking, and the transition susceptible to external pressure. Since one electron in the NB a_{1g} or e'' state per trimer is responsible for magnetism, we can understand the small effective magnetic moment of 0.16 μ_B per Ir above T_c [11,24]. The transition is basically an insulator-insulator transition, which can give anomalous critical exponents [24]. This transition looks similar to the neutral-ionic transition in the charge transfer organic complexes showing non-linear conduction [44,45]. BaIrO₃ also shows giant non linear conduction at low temperature [13], the origin of which may be compared with the organic complexes. Within our model, however, the weak ferromagnetism is difficult to understand, for all the trimers are nonmagnetic below T_c . The ideal charge transfer of e in Figure 4c,d may not occur in real materials, but only a fraction of e may move between the trimers. In such a case, all the trimers can be slightly magnetic and may show ferromagnetism with the much smaller moment of 0.016 μ_B below T_c .

It would be fair to point out controversial points and limitations of our model. First, Figure 4 is an oversimplified picture where transfer energies except for the intra-timer case are neglected. In a real material, the complicated band structure may invalidate our model, although the band calculations reported so far do not always explain the experimental results satisfactorily. Secondly, the strong correlation, *i.e.*, the on-site Coulomb repulsion forces the electron density to be as homogeneous as possible and disfavors the charge transfer from one trimer to another. The proposed charge order may come from a delicate balance among the on-site Coulomb repulsion, the energy difference between the two timers, and the transfer energies. A more complete theoretical modeling is needed to advance further. Third, IrO₆ octahedra are distorted so that there are no pure a_{1g} and e'_g orbitals in a strict sense. Accordingly the molecular orbital such as NB a_{1g} may be misleading. Even in such a case, one hole on Ir⁴⁺ of $(5d)^5$ occupies the non-degenerate, highly occupied orbital (say ϕ_i for Ir*i*). Then, we can make linear combinations from ϕ_1 and ϕ_2 for one Ir trimer, from ϕ_3 and ϕ_4 for the other trimer. Again we can construct a one electron in a corresponding non-bonding-like state for one trimer, and find the essence of our model left unchanged. To examine the validity of our model, we have investigated the impurity effects on the 182-K transition for a set of polycrystalline samples of $BaIr_{1-x}Ru_xO_3$. Figure 5 shows the magnetization and the resistivity of the samples. The phase transition is systematically and drastically suppressed with the Ru concentration x, and essentially vanishes at only 10% substitution; For x = 0.1, the resistivity is non-metallic without any trace of anomalies at all temperatures measured, whereas a tiny trace of the weak ferromagnetic phase of x = 0 is visible in the magnetization measurement. The resistivity for x = 0.1 indicates the electronic states above T_c is essentially insulating, being consistent with the picture of the trimer Mott insulator. The inset of Figure 5a shows the intra-trimer Ir-Ir bond lengths for the x = 0.1 sample, where the two lengths of d_{12} and d_{34} are essentially temperature-independent, and identical. Concomitantly the negative expansion of the *c*-axis is severely suppressed (not shown). The Ru substitution simultaneously suppresses the 182 K-transition and the electron transfer from Ir1–Ir2–Ir1 to Ir3–Ir4–Ir3, and therefore these two phenomena are two sides of the same coin. We further note that the charge order is known to be vulnerable to impurities [46], while the charge density wave is more or less robust against impurities [47].



Figure 5. The impurity effect on the 182-K transition. (a) resistivity ρ of polycrystalline samples of BaIr_{1-x}Ru_xO₃. The inset shows the intra-trimer Ir-Ir bond lengths for the x = 0.1 sample. The two trimers have the identical, temperature-independent bond length; (b) magnetization *M* divided by an external field *H* of 500 Oe of the same samples.

A similar type of the phase transition occurs in the organic salt β -(meso-DMBEDT-TTF)₂PF₆ [48]. Many conductive organic salts with a chemical formula of A_2B consists of a dimer molecule of A_2 as a composition unit. In the present case, two molecules of meso-DMBEDT-TTF form a dimer structure, and share one hole per dimer to behave as *dimer Mott insulators* [49]. Okazaki *et al.* [50] identified the phase transition in this compound at 70 K to a transition from dimer Mott insulator phase to charge ordered insulator phase. This results from a competition between the intra- and inter-dimer Coulomb interactions, which causes intrinsic inhomogeneous state detected through infrared microscope measurement. As is similar to BaIrO₃, this organic salt also shows non-linear conduction below T_c [51].

Finally, we briefly comment that we have applied a similar molecular orbital concept to the related timer Ru oxide $Ba_4Ru_3O_{10}$ in which the three face-shared RuO_6 octahedra form a Ru_3O_{12} trimer [22,42,52]. This related oxide shows a phase transition at 105 K, where a metallic, paramagnetic state changes into an insulating, antiferromagnetic state at low temperature. However, the electronic

states are different; In this related oxide, each trimer is three electrons short because Ru^{4+} has four 4*d* electrons. On the basis of a similar molecular orbital approach, we have to consider partially occupied e'_g orbitals. In this case, the static electronic potential is deeper at the center of the trimer, and a finite fraction of charge is expected to transfer from the edge. Namely, intra-timer charge transfer drives the phase transition in Ba₄Ru₃O₁₀. This makes a stark contrast to the inter-trimer charge transfer in BaIrO₃. The intra-trimer charge disproportionation has been also discussed from the local-density-approximation calculations [43,53].

5. Conclusions

In summary, we have prepared polycrystalline samples of the trimer oxide BaIrO₃ with the face-shared Ir_3O_{12} trimers, and have measured the resistivity, thermopower, magnetization and synchrotron X-ray diffraction from room temperature down to 4 K. On the basis of the structure analysis, we have made a model for the electronic states of this oxide and have pointed out that this oxide can be regarded as a kind of Mott insulator, when the Ir_3O_{12} trimer is identified to one lattice site. Within the same framework, the 182-K transition can be viewed as a transition from the trimer Mott insulator phase to the trimer charge-ordered phase, which is essentially different from conventional charge density wave as was used to be a candidate for the transition. We have further succeeded in explaining various properties above T_c such as the non-metallic resistivity and thermopower, the large pressure effect, and the unusually small effective magnetic moment. We expect that the proposed concept of trimer solid will be applied to other face-shared transition metal oxides.

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