



Article Selecting Products Considering the Regret Behavior of Consumer: A Decision Support Model Based on Online Ratings

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Received: 16 April 2018; Accepted: 17 May 2018; Published: 21 May 2018



Abstract: With the remarkable promotion of e-commerce platforms, consumers increasingly prefer to purchase products online. Online ratings facilitate consumers to choose among products. Thus, to help consumers effectively select products, it is necessary to provide decision support methods for consumers to trade online. Considering the decision makers are bounded rational, this paper proposes a novel decision support model for product selection based on online ratings, in which the regret aversion behavior of consumers is formulated. Massive online ratings provided by experienced consumers for alternative products associated with several evaluation attributes are obtained by software finders. Then, the evaluations of alternative products in format of stochastic variables are conducted. To select a desirable alternative product, a novel method is introduced to calculate gain and loss degrees of each alternative over others. Considering the regret behavior of consumers in the product selection process, the regret and rejoice values of alternative products for consumer are computed to obtain the perceived utility values of alternative products. According to the prior order of the evaluation attributes provided by the consumer, the prior weights of attributes are determined based on the perceived utility values of alternative products. Furthermore, the overall perceived utility values of alternative products are obtained to generate a ranking result. Finally, a practical example from Zol.com.cn for tablet computer selection is used to demonstrate the feasibility and practically of the proposed model.

Keywords: decision support model; product selection; online ratings; regret theory; stochastic variables

1. Introduction

With the advent of the era of big data, trading on e-commerce platforms develops rapidly [1,2]. Consumers can effectively access product information and make purchase transactions on an e-commerce platform without the restriction of time [3–5]. For most consumers, the choice of purchasing product is related to the joy of product experience. With the help of the e-commerce platform, consumers can identify products based on their specific demands and then seek desirable ones. Nowadays, many e-commerce websites, e.g., Amazon (https://www.amazon.cn/), Zol.com.cn (http://www.zol.com.cn/), JD.com (https://www.jd.com/) and Taobao.com (https://www.taobao.com/) have provided platforms for consumers to select their products and share their online ratings or reviews on product experience. For instance, if a consumer wants to purchase a tablet computer due to occupational demand, before purchasing, he/she can browse an overall recommendation of tablet computers via Zol.com.cn which is an IT and business portal. Furthermore, e-commerce sites, such as Zol.com.cn, allow consumers who have already purchased tablet computers to post their personal evaluations publicly online, so that other consumers can get helpful references from these websites.

Figure 1 shows a list of tablet computers from Zol.com.cn (http://detail.zol.com.cn/tablepc/good_pic. html). Therefore, it is of great significant to explore the product selection problem oriented on online ratings and reviews in e-commerce platform.

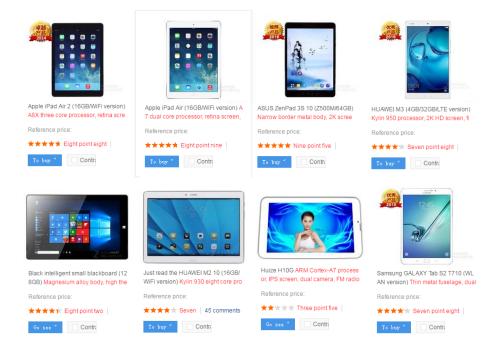


Figure 1. A list of tablet computers in Zol.com.cn.

Currently, the evaluation or selection of products oriented to online ratings or reviews has been paid attention by many scholars globally. To support consumer's selection and purchase decision, Fan et al. designed a novel method based on stochastic dominance and PROMETHEE-II method to rank the alternative products by using online ratings [6]. Yang et al. proposed a method to synthesize rich and heterogeneous information and further used it to rank products with Electronic Word of Mouth (eWOM) score [7]. Chen et al. visualized the market structure from different perspectives and formulated a Technique for Order Preference by Similarity to an Ideal Solution (TOPSIS)-based product selection model [8]. Najmi et al. presented a product ranking system that facilitates the online shopping experience according to online evaluations and description on the products [9]. Wu et al. developed a two-stage consumer decision model from the risk perspective to understand the role of online reviews in the consumers' Willingness-To-Pay (WTP) [10]. In the field of automobile product selection, Liu et al. proposed an approach on ranking products with online reviews [11]. The approach integrated the sentiment analysis technique and the intuitionistic fuzzy set theory. Using the mobile phone as research object, Peng et al. presented a fuzzy PROMETHEE method to rank alternative products based on online product reviews provided by consumers [12]. To effectively analyze consumer reviews for the purpose of monitoring consumer satisfaction with mobile phones, Kang and Park proposed a sentiment analysis and Vlsekriterijumska Optimizacija I Kompromisno Resenje (VIKOR) method to select the desirable mobile application [13]. A social appraisal mechanism (SAM) was proposed by Li et al. [14] Such mechanism combines social network analysis (SNA), intuitionistic fuzzy sets (IFSs), and the TOPSIS method to achieve social decision support for online users. Li et al. investigated the determinants of consumer satisfaction in hospitality venues by analyzing online reviews [15]. Li et al. introduced a fuzzy decision support technique based on Choquet Integral (CI), which is an aggregation function, into the multiple criteria decision making (MCDM) problem of hotel selection [16]. With respect to restaurant selection, Zhang et al. [17] established a decision support model to help independent tourists utilize social information on TripAdvisor.com.

Although existing literature has made significant contributions to product evaluation or selection problems based on online ratings or reviews, they mainly considered that the consumer is entirely rational. Actually, when the consumer realizes that selecting other products might have better results, he/she would feel regret selecting the current one. Otherwise, the decision maker may feel rejoice. Additionally, the methods to process online ratings or reviews are still rough. Since the scale of the online evaluations is massive, how to design an effective quantification method for the product selection problem is complicated and challenging. Therefore, it is essential to establish a reasonable model to address this problem with massive online evaluations.

Compared with traditional uncertainty problems, the evaluation or selection problem oriented on e-commerce sites with online evaluation data is more complex, because of the complexity of massive data processing. Therefore, this study aimed at proposing a decision support model to select the desirable product(s). To accomplish the overall objective for ranking and selecting products, there are two main tasks to be completed. First, the online evaluation data need to be crawled and normalized. Then, a reasonable model considering the regret behavior of consumers was built to support the product selection and purchase. Finally, a practical selection problem for the method was tested to demonstrate the feasibility of the proposed decision support model.

The remainder of this paper is organized as follows. In Section 2, several basic preliminaries of stochastic variable and regret theory are introduced. In Section 3, the problem formulation and the resolution process for selecting product are established based on online ratings. In Section 4, a novel decision support model is proposed. According to online ratings of products associated with each evaluation attribute, the evaluations of products in format of stochastic variables are constructed. Then, the gain and loss degrees of each alternative over others are calculated. Considering the regret aversion behavior of the consumer, the perceived utility values of alternatives associated with each attribute can be computed. Based on the prior order of evaluation attributes and the perceived utility values, the prior weights of evaluation attributes are determined. Thus, we proposed an aggregating method to derive the ranking of the products. A practical example of selecting products, taking Zol.com.cn as the carrier, is presented to illustrate the practicability of the proposed method in Section 5. Concluding remarks are given in Section 6.

2. Preliminaries

In this section, some basic preliminaries of stochastic variable and regret theory are introduced, which are used throughout this paper.

2.1. Stochastic Variables

To begin with, for notational convenience, let ξ , a stochastic variable, be the consequence of an action. The definitions of stochastic variable and its expected value are introduced firstly [18–20].

Definition 1. Suppose $X^+ = \{x_1, x_2, ..., x_l\}$ is the domain with $x_1 < x_2 < \cdots < x_l$. A variable ξ may take all the possible values $x_i \in X^+$. Assume $p(x_i)$ is the probability that ξ equals to x_i , with $p(x_i) \ge 0$ for any $x_i \in X^+$, and $\sum_{i=1}^l p(x_i) = 1$, then ξ is a discrete stochastic variable in X^+ . The cumulative distribution function of ξ is $F(x) = p(\xi \le x) = \sum_{x_i \le x} p(x_i)$.

Definition 2. Suppose $X^+ = [a, b]$ is the domain with a < b. A variable ξ may take all the possible values in X^+ . Assume f(x) is the probability that ξ equals to $x \in X^+$, with $f(x) \ge 0$ and $\int_a^b f(x)dx = 1$, then ξ is a continuous stochastic variable in X^+ . The cumulative distribution function of ξ is $F(x) = p(\xi \le x) = \int_a^x f(t)dt$.

Definition 3. Let ξ be a discrete stochastic variable in $X^+ = \{x_1, x_2, \dots, x_l\}$ with $0 < x_1 < x_2 < \dots < x_l$, and $P(\xi = x_i) = p(x_i)$ be the probability that stochastic variable ξ is equal to x_i , with $0 \le p(x_i) \le 1$ for any $x_i \in X^+$, and $\sum_{i=1}^l p(x_i) = 1$. The expected value of ξ is defined as

$$E(\xi) = \sum_{i=1}^{l} x_i p(x_i) \tag{1}$$

Definition 4. *Let* ξ *be a continuous stochastic variable, and* f(x) *be the probability density function of stochastic variable* ξ *. The expected value of* ξ *is defined as*

$$E(\xi) = \int_{-\infty}^{\infty} x f(x) dx$$
⁽²⁾

2.2. Regret Theory

Regret theory, which was developed independently by economists Bell [21] and Loomes and Sugden [22], is a classical behavioral theory for decision making. The basic proposition of regret theory is that individuals are not only concerned about the utility consequence of alternatives, but also concerned about the comparison of the utility consequence with other alternatives. If the utility consequence of an alternative falls short of the other alternative, individuals will experience regret; if it is better than the other alternative, they will experience rejoice [21,22]. Further, individuals are usually more sensitive to regret than to rejoice. Thus, disappointment is a psychological reaction to an outcome whether prior to or after the other outcome. The greater is the negative deviation to other alternative, the greater is the degree of regret, and vice versa.

Later on, based on regret theory, some tools for measuring regret or rejoice degrees are proposed subsequently [23–25]. Regret–rejoice function is a key point in regret theory. Assume *A* and *B* are two choices whose utility consequence are x_1 and x_2 . If we take x_2 as a reference point associated with *A*, then the regret–rejoice function is represented as follows [24,25]:

$$R(\Delta x) = 1 - \exp(-\delta \Delta x) = 1 - \exp(-\delta(x_1 - x_2))$$
(3)

where Δx is the deviation of consequence between x_1 and x_2 , $0 < \delta < 1$ is the regret aversion parameter, and the larger δ is, the greater regret aversion degree of the decision maker is. $R(\Delta x)$ is the regret–rejoice value under the situation for choosing *A* instead of *B*. The regret–rejoice function with different regret aversion parameter δ is shown as Figure 2.

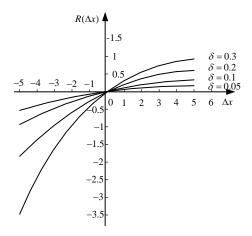


Figure 2. The regret–rejoice function $R(\Delta x)$.

From regret–rejoice function above, some interesting characteristics are summarized as follows:

Property 1. *The regret–rejoice function* $R(\Delta x)$ *is a monotonically increasing concave function, with* $R'(\Delta x) > 0$ *and* $R''(\Delta x) < 0$.

Property 2. If $\Delta x < 0$, then the decision maker feels regret, $R(\Delta x) < 0$, and $|R(\Delta x)|$ is the regret degree. On the contrary, if $\Delta x > 0$, then the decision maker feels rejoice, $R(\Delta x) > 0$, and $R(\Delta x)$ is the rejoice degree. If $\Delta x = 0$, then neither regret nor rejoice can be felt by the decision maker, and $R(\Delta x) = 0$.

Property 3. Suppose x_1 , x_2 and x_3 are three utility consequences, and x_3 is the reference utility point. For $\forall 0 < \delta < 1$, if $\Delta x_1 = x_1 - x_3 > 0$, $\Delta x_2 = x_2 - x_3 < 0$ and $|\Delta x_1| = |\Delta x_2|$, then we have $|R(\Delta x_2)| > |R(\Delta x_1)| = R(\Delta x_1)$. That is, the decision maker is usually more sensitive to negative deviation than to the same degree of positive deviation, i.e., regret aversion.

3. Problem Formulation and Resolution Procedure

3.1. Formulation of the Problem

Considering a problem that is selecting the most desirable product(s) in e-commerce website. By an advance screening, several acceptable products are determined, which are regarded as the alternatives set. However, different products have different advantages and disadvantages on different attributes. Thus, the consumer hesitates among the several alternative products. Besides, the consumer may have regret aversion behavior in the decision process. To select a desirable product, several evaluation attributes are considered, which are determined according to the consumer's personal online ratings. To support the consumer's selection and purchase, many online ratings of the alternative products concerning the attributes are crawled from the related e-commerce platform. The problem considered in this paper is how to rank the products based on the online ratings.

For convenience, throughout this paper, the following notations are used in the problem. Suppose $M = \{1, 2, 3, \dots, m\}$, $N = \{1, 2, 3, \dots, n\}$ and $S = \{1, 2, 3, \dots, s\}$ are three sets of subscripts. Suppose $\Theta = \{\Theta_1, \Theta_2, \dots, \Theta_m\}$ with $m \ge 2$ is a set of alternative products, where Δ_i expresses the *i*th alternative product, $i \in M$. Usually, the alternatives set Θ can be predetermined by the consumer. $O = \{O_1, O_2, \dots, O_n\}$ with $n \ge 2$ is a finite set of evaluation attribute, where O_j denotes the *j*th evaluation attribute, $j \in N$. Usually, the set O can be determined by two sources. One is provided by consumer indirectly and the other is derived from online evaluations. Assume $\Omega = (\omega_1, \omega_2, \dots, \omega_n)^T$ is a vector of attribute weights, where ω_j is the weight assigned to attribute O_j with $\omega_j \ge 0$ for $\forall j \in N$, and $\sum_{j=1}^n \omega_j = 1$. However, sometimes the weight vector of evaluation attribute is unknown. The prior order of evaluation attributes is provided by the consumer. In addition, suppose $B = \{B_1, B_2, \dots, B_s\}$ is the rating scales set used by an electronic platform, where B_q is the *q*th rating scale, $q \in S$. U_{ij} is the total number of online ratings for product Θ_i associated with attribute O_j . In fact, U_{ij}^q and U_{ij} should be derived in this study.

The problem addressed in this study is how to select the most desirable alternative product(s) from the finite alternative set Θ based on the online ratings and evaluation attributes with prior order, consider the regret aversion behavior of the consumer. In Figure 3, taking the selection of tablet computers as an example, the formulation of ranking and selection of tablet computers through online ratings is described concretely.

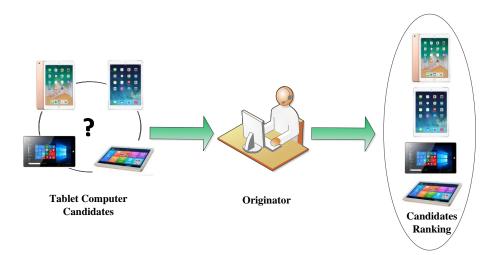


Figure 3. The problem of ranking tablet computers through online ratings.

3.2. Framework and Processing for the Problem

To solve the above decision-making problem, a resolution process of selecting products is proposed as shown in Figure 4. In Figure 4, the resolution process can be divided into two parts: (1) preparatory phase, i.e. crawling the related online ratings data and constructing the stochastic evaluations of products; and (2) ranking phase, i.e. considering the behavior of the consumer, a ranking method for products is proposed. A brief illustration of each part is given below.

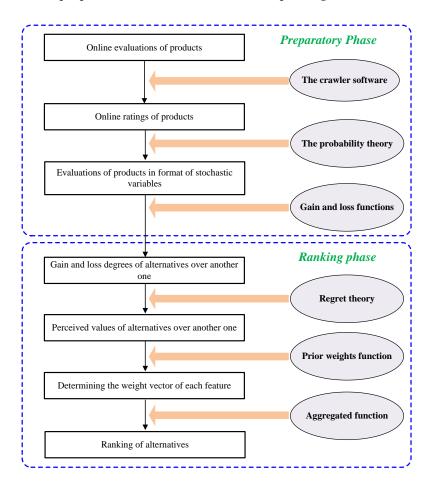


Figure 4. The resolution procedure for the problem of ranking products through online ratings.

Preparatory Phase. Based on the alternative products and the evaluation attributes considered by the consumer, the online ratings of the alternative products concerning all attributes are crawled from the related website using web crawler software and are preprocessed using the probability theory. Further, based on the probabilistic theory method and online ratings of products, the evaluations of products in format of stochastic variables are constructed.

Ranking Phase. According to online ratings of products associated with each evaluation attribute, the evaluations of products in format of stochastic variables are constructed. Then, the gain and loss degrees of each alternative over others is calculated. Considering the regret aversion behavior of the decision maker, based on the regret–rejoice function, the perceived utility values of alternatives associated with each attribute is computed. Based on the prior order of evaluation attributes and the perceived utility values of the products, the prior weights of evaluation attributes are determined. Thus, the aggregating method obtains the ranking of the products.

4. The Proposed Stochastic Decision Model Considering Consumer's Regret Behavior

Based on the resolution process shown in Figure 4, a description of the proposed method for ranking and selecting products through online ratings is given in this section, where the description for determining the stochastic evaluations information is in Section 4.1. Then, the method for calculating gain and loss degrees of alternative over others is established in Section 4.2. The regret and rejoice perceived values of alternatives is proposed in Section 4.3. Based on the stochastic evaluations and attribute prior order provided by consumer, the prior weight vector of attribute is determined in Section 4.4. Finally, in Section 4.5, the method for obtaining the ranking result of products is presented.

4.1. Determining the Stochastic Evaluation Information

In this paper, to provide a decision support model to select desirable(s) product, the online ratings for the products concerning all evaluation attributes should be considered. Thus, the preparatory phase can be further divided into two parts: (1) crawling online ratings for the alternative with respect to all attributes; and (2) preprocessing online ratings to alternatives' assessments in format of stochastic variables. Thee detailed description of each part is given below.

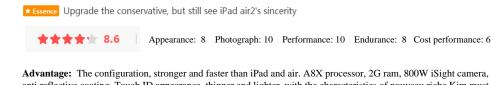
Nowadays, some web crawlers have been presented, which can be used to derive the online evaluations. Currently, some websites encourage consumers to post their evaluations according to a pre-established framework of evaluation attributes. For example, Zol.com.cn constructs a framework on the attributes of products, and encourages the consumers to post their ratings and reviews according to the framework. In this paper, the crawler software named Octopus collector is used to obtain online ratings. According to the alternative products set, i.e., $\Theta = \{\Theta_1, \Theta_2, \dots, \Theta_m\}$, the online ratings with respect to alternative products can be crawled and collected from the related website. Besides, a situation where ratings are posted according to the pre-established framework of attributes set $O = \{O_1, O_2, \dots, O_n\}$, for example, an online rating and review for Apple iPad Air 2 from Zol.com.cn, is shown in Figure 5 (http://detail.zol.com.cn/372/371503/review.shtml). In this figure, we can obtain the five attributes for selecting tablet computers, i.e., appearance, photograph, performance, endurance and cost performance. With respect to five attributes, the online ratings of tablet computers are provided by every consumer.

We suppose $B = \{B_1, B_2, \dots, B_s\}$ is a rating scales set used by an electronic platform. To accurately describe the differences, in this paper, the evaluations of alternative products are represented as evaluations in format of stochastic variables. After crawling the online ratings, based on Excel, the statistical data aare summarized. Suppose U_{ij} is the total number of online ratings for products Θ_i associated with attribute O_j . U_{ij}^q is the number scale B_q used as the online ratings for products Θ_i associated with attribute O_j .

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anti reflective coating, Touch ID appearance, thinner and lighter, with the characteristics of nouveau riche Kim must. Shortcomings: Expensive! Your host, your accessories! There is not much difference between iPad and air, at least not yet seen that A8X and A7 have much difference, super night shot noise. Accessories too stingy! Summery: IPad 16G is not necessary, really is not enough to use. See no difference between air2 and air performance, air friends do not suggest to buy. 64G RMB3800 some 3950 feet out of the water against Hong kong.



Figure 5. An online rating and review for Apple iPad Air 2 from Zol.com.cn.

Let $B = \{B_1, B_2, \dots, B_s\}$, $P_{ij} = \{(B_q, p_{ij}^q) | q = 1, 2, \dots, s\}$, in format of stochastic variable, be the evaluation value for product Θ_i associated with attribute O_j . The probability that the alternative product Θ_i on attribute O_j is expressed as B_q is defined as p_{ij}^q , $i = 1, 2, \dots, m$; $j = 1, 2, \dots, n$; $q = 1, 2, \dots, s$.

$$P_{ij} = \begin{cases} p_{ij}^{1}, x = B_{1} \\ p_{ij}^{2}, x = B_{2} \\ \vdots \\ p_{ij}^{q}, x = B_{q} \\ \vdots \\ p_{ij}^{s}, x = B_{q} \end{cases}, i = 1, 2, \cdots, m; j = 1, 2, \cdots, n,$$

$$i = 1, 2, \cdots, m; j = 1, 2, \cdots, n,$$

$$i = 1, 2, \cdots, m; i = 1, 2, \cdots, n, q = 1, 2, \cdots, s$$

$$(4)$$

where
$$p_{ij}^q = \frac{U_{ij}^q}{\sum_{q=1}^s U_{ij}^q}$$
, $i = 1, 2, \cdots, m, j = 1, 2, \cdots, n, q = 1, 2, \cdots, s$

4.2. Calculation of the Gain and Loss Degrees

In the process of decision making, the consumer will compare alternative products to other products, If he/she selects an alternative product instead of a better one, he/she may feel regret for this selection. On the contrary, the consumer may feel rejoice. Thus, to measure the perceived utility values of alternatives to select the desirable alternative, the gain and loss degrees of alternatives with respect to others should be calculated. We suppose g_{ik}^{j} and l_{ik}^{j} are gain degree and loss degree of alternative Θ_{i} with respect to Θ_{k} on attribute O_{j} .

$$g_{ik}^{j} = \sum_{B_{q}, B_{h} \in \mathbf{B}, B_{q} > B_{h}} (B_{q} - B_{h}) p_{ij}^{q} p_{kj}^{h},$$
(5)

$$l_{ik}^{j} = \sum_{B_{q}, B_{h} \in \mathbf{B}, B_{q} < B_{h}} (B_{q} - B_{h}) p_{ij}^{q} p_{kj}^{h}$$
(6)

For gain degree g_{ik}^{l} and loss degree l_{ik}^{l} , the following properties are provided.

Property 4. (*Complementarity*) For $\forall i, k \in M$ and $\forall j \in N$, we obtain $g_{ik}^j + l_{ki}^j = 0$ and $l_{ik}^j + g_{ki}^j = 0$.

Property 5. (Compensatory) Let E_{ij} and E_{kj} be expectations of stochastic variables P_{ij} and P_{kj} . For $\forall j \in N$, we obtain $g_{ik}^j + l_{ik}^j = E_{ij} - E_{kj}$. For $\forall j \in N$, we obtain $g_{ik}^j + l_{ik}^j = E_{kj} - E_{ij}$.

Proof. For $\forall i \in N$, based on Equations (5) and (6), we can obtain that

$$g_{ik}^{j} + l_{ik}^{j} = \sum_{B_{q}, B_{h} \in \mathbf{B}, B_{q} > B_{h}} (B_{q} - B_{h}) p_{ij}^{q} p_{kj}^{h} + \sum_{B_{q}, B_{h} \in \mathbf{B}, B_{q} < B_{h}} (B_{q} - B_{h}) p_{ij}^{q} p_{kj}^{h}, i, k \in M; \ j \in N.$$
(7)

The expectations E_{ij} and E_{kj} of stochastic variables P_{ij} and P_{kj} are given as

$$E_{ij} = \sum_{B_q \in \mathcal{B}} B_q p_{ij}^q, i \in M; j \in N,$$
(8)

$$E_{kj} = \sum_{B_q \in \mathbf{B}} B_q p_{kj}^q, k \in M; j \in N,$$
(9)

Since stochastic variables P_{ij} and P_{kj} are independent [18], we obtain $g_{ik}^{j} + l_{ik}^{j} = \sum_{B_q, B_h \in \mathbf{B}, B_q > B_h} (B_q - B_h) p_{ij}^q p_{kj}^h + \sum_{B_q, B_h \in \mathbf{B}, B_q < B_h} (B_q - B_h) p_{ij}^q p_{kj}^h = \sum_{B_q, B_h \in \mathbf{B}} (B_q - B_h) p_{ij}^q p_{kj}^h = \sum_{B_q, B_h \in \mathbf{B}, B_q > B_h} (B_q - B_h) p_{ij}^q p_{kj}^h$ $\sum_{B_a \in \mathbf{B}} B_q p_{ij}^q - \sum_{B_k \in \mathbf{B}} B_h p_{kj}^h$. Thus, it can be observed that $g_{ik}^j + l_{ik}^j = E_{ij} - E_{kj}$.

Property 6. (*Middle Boundary*) For $\forall j \in N$, we have $g_{ik}^j \ge g_{ki}^j$ if and only if $E_{ij} \ge E_{kj}$. For $\forall j \in N$, we obtain $g_{ik}^j \ge g_{ki}^j$ if and only if $E_{ij} \le E_{kj}$.

Proof. For $\forall j \in N$, if $g_{ik}^j \geq g_{ki}^j$, we obtain $g_{ik}^j - g_{ki}^j = g_{ik}^j + l_{ik}^j \geq 0$ according to Property 4. According to Property 5, we obtain $E_{ij} - E_{kj} \geq 0$, i.e., $E_{ij} \geq E_{kj}$. In contrast, if $E_{ij} \geq E_{kj}$, we obtain $g_{ik}^{j} + l_{ik}^{j} = g_{ik}^{j} - g_{ki}^{j} \ge 0$, i.e., $g_{ik}^{j} \ge g_{ki}^{j}$. Similar to the above proof, we can prove $g_{ik}^{j} \ge g_{ki}^{j}$ if and only if $E_{ij} \le E_{kj}$. \Box

Property 7. (*Transitivity*) For $\forall i, k, h \in M$ and $\forall j \in N$, if $g_{ik}^j \ge |l_{ik}^j|$ and $g_{kh}^j \ge |l_{kh}^j|$, then $g_{ih}^j \ge |l_{ih}^j|$.

Proof. For $\forall j \in N$, if $g_{ik}^j \ge |l_{ik}^j|$, i.e., $g_{ik}^j \ge g_{ki}^j$, we obtain $E_{ij} \ge E_{kj}$ according to Property 6. If $g_{kh}^j \ge |l_{kh}^j|$, i.e., $g_{kh}^j \ge g_{hk}^j$, we obtain $E_{kj} \ge E_{hj}$ by Property 6; thus, $E_{ij} \ge E_{hj}$. According to Property 6, it can be observed that $g_{ih}^j \ge g_{hi}^j$, i.e., $g_{ih}^j \ge |l_{ih}^j|$. \Box

Example 1. Let ξ_{ij} and ξ_{kj} be two interval stochastic variables whose probability distributions are shown as in Table 1.

Table 1. The probability distributions of ξ_{ij} and ξ_{kj} .

B _i	2	4	6	8	10
p_{ij}^q	0.3	0.2	0.25	0.35	0.2
p_{kj}^{h}	0.3	0.2	0	0.55	0.4

By using Equations (5) and (6), we could obtain the gain and loss degrees of P_{ij} over P_{ki} , respectively.

$$g_{ik}^{j} = \sum_{B_{q},B_{h} \in S, B_{q} > B_{h}} (B_{q} - B_{h}) p_{ij}^{q} p_{kj}^{h}$$

= $(B_{2} - B_{1}) p_{ij}^{2} p_{kj}^{1} + (B_{3} - B_{1}) p_{ij}^{3} p_{kj}^{1} + (B_{3} - B_{2}) p_{ij}^{3} p_{kj}^{2} + \dots + (B_{5} - B_{4}) p_{ij}^{5} p_{kj}^{4} = 0.5$

4.3. Determining the Stochastic Evaluation Information

In addition to comparing the selected alternative with other options, the consumer has a behavior characteristic of regret aversion. That is, the consumer is more sensitive with loss degree to the same magnitude of gain degree. To calculate the perceived values of alternatives, let s_{ik}^{j} and t_{ik}^{j} be the rejoice value and regret value of alternative Θ_{i} relative to Θ_{k} on attribute O_{j} . Based on the function of regret–rejoice [24,25], s_{ik}^{j} and t_{ik}^{j} can be obtained by

$$s_{ik}^{j} = 1 - \exp(-\delta g_{ik}^{j}) \ i, k \in M; \ j \in N,$$

$$(10)$$

$$t_{ik}^{j} = 1 - \exp(-\delta l_{ik}^{j}), i, k \in M; \ j \in N,$$
(11)

where $0 < \delta < 1$ is the regret aversion parameter, which measures the level of regret aversion of the decision maker.

According to Equations (10) and (11), several interesting properties are summarized as follows:

Property 8. $0 \le s_{ik}^{j} \le 1$ and $t_{ik}^{j} < 0$.

Property 9. s_{ik}^{j} and t_{ik}^{j} increase monotonically as the gain degree g_{ik}^{j} and loss degree l_{ik}^{j} increase, respectively.

Furthermore, the perceived utility matrix $\Phi_j = [\varphi_{ik}^j]_{m \times m}$ on attribute O_j can be established. In the matrix $\Phi_j = [\varphi_{ik}^j]_{m \times m'}$, the element φ_{ik}^j , which combines rejoice degree s_{ik}^j and regret degree t_{ik}^j , denotes the perceived utility value of alternative Θ_i over alternative Θ_k for attribute O_j which combines rejoice degree s_{ik}^j and regret degree t_{ik}^j . It is given by

$$\varphi_{ik}^{j} = s_{ik}^{j} + t_{ik}^{j}, i, k \in M; \ j \in N.$$
(12)

Based on Equations (10)–(12), the following characteristics can be obtained.

Property 10. If $\varphi_{ik}^j = s_{ik}^j + t_{ik}^j > 0$, then alternative Θ_i net superior to Θ_k for attribute O_j . If $\varphi_{ik}^j = s_{ik}^j + t_{ik}^j < 0$, then alternative Θ_k net superior to Θ_i for attribute O_j .

After obtaining the perceived utility value φ_{ik}^{j} of alternative Θ_{i} over Θ_{k} on attribute O_{j} , the overall perceived utility value z_{ij} of alternative Θ_{i} on attribute O_{j} can be integrated by

$$z_{ij} = \sum_{k=1}^{m} \varphi_{ik}^{j}, i \in M, \ j \in N.$$
(13)

4.4. Determination of Evaluation Attributes' Weights

In this study, for evaluation attributes set $O = \{O_1, O_2, \dots, O_n\}$, we suppose the prior order of evaluation attributes is provided by consumer. Without loss of generality, we suppose $O_1 \succ O_2 \succ \dots \succ O_n$. To aggregated the perceived utility values z_{ij} into overall perceived utility value Z_i , the prior weight vector Ω should be determined. In the following, we determine the prior weight ω_j^i of evaluation attribute O_j based on the perceived utility value z_{ij} of alternative Θ_i on evaluation attribute O_j .

Taking the alternative Θ_i as an example, first, let the weight of highest evaluation attribute O_1 be $\sigma_1^i = 1$. Then, the others relative prior weight σ_i^i of evaluation attribute O_j is defined as

$$\sigma_j^i = \sigma_{j-1}^i f_{i,j-1} = \prod_{q=1}^{j-1} f_{iq}, i \in M, \ j \in N, j \neq 1.$$
(14)

Here, we use a sigmoid non-linear transformation function to transform the perceived utility value z_{ij} into f_{ij} :

$$f_{ij} = \frac{1}{1 + e^{-\alpha z_{ij}}}, i \in M, j \in N.$$
 (15)

where $\alpha > 0$ is the parameter of transformation function.

Then, we normalize the relative prior weight σ_j^i of prior evaluation attribute O_j into prior weight ω_i^i :

$$\omega_j^i = \frac{\sigma_j^i}{\sum_{j=1}^n \sigma_j^i}, i \in M, \ j \in N.$$
(16)

According to Equations (14)–(16), interesting properties are summarized in the following.

Property 11. For $\forall i \in M$, $\forall j \in N$, we have $0 < f_{ij} \leq 1$, and $f_{ij}' > 0$, i.e., f_{ij} increase monotonically as the perceived utility value z_{ij} .

Proof. Since $\forall i \in M$, and $\forall j \in N$, we have $f_{ij} = \frac{1}{1+e^{-\alpha z_{ij}}}$, that is $0 < f_{ij} \le 1$, $f_{ij}' = 1 + e^{-\alpha z_{ij}} + \frac{1}{1+e^{-\alpha z_{ij}}} > 0$, f_{ij} increase monotonically as the perceived utility value z_{ij} . \Box

Property 12. For $\forall i \in M$, $\forall j, l \in N$, if $O_j \succ O_l$, j < l, we have $\omega_j^i \ge \omega_l^i$. That is, the evaluation attribute weight of high prior is not less than the evaluation attribute weight of the lower prior.

Proof. Since $\forall i \in M$ and $\forall j \in N$, if $O_j \succ O_l$ for j < l, then we have $\sigma_l^i = \prod_{q=1}^{l-1} f_{iq} = \sigma_j^i \prod_{q=j}^{l-1} f_{iq}$ based on

Equation (14), and $\prod_{q=j}^{l-1} f_{iq} \leq 1$ based on based on Equation (15). Thus, $\sigma_j^i \geq \sigma_l^i$. Based on Equation (16),

we have $w_j^i \ge w_l^i$. That is the evaluation attribute weight of high prior is not less than the evaluation attribute weight of the lower prior. \Box

4.5. Ranking Alternatives

After determining the prior weights of evaluation attributes as well as the perceived utility values of alternatives on all attributes, the overall perceived utility value Z_i of alternative Θ_i can be computed as

$$Z_i = \sum_{j=1}^n z_{ij} \omega_j^i, i \in M.$$
(17)

According to perceived utility value Z_i , the ranking list of alternatives can be derived. A larger value of Z_i indicates that Θ_i is a better alternative.

Based on the above analysis, the decision procedures of the proposed method and flowchart (Figure 6) for handling the selection problem with online ratings can be summarized as follows:

- Step 1. Crawl the online ratings and construct evaluation in format of stochastic variable P_{ij} .
- Step 2. Construct gain matrix $G_j = [g_{ik}^j]_{m \times m}$ and loss matrix $L_j = [l_{ik}^j]_{m \times m}$ on attribute O_j according to Equations (5) and (6).
- Step 3. Obtain perceived utility matrix $\Phi_j = [\varphi_{ik}^j]_{m \times m}$ on attribute O_j according to Equations (10)–(12).
- Step 4. Determine the prior weight vector $\Omega_i = (\omega_1^i, \omega_2^i, \cdots, \omega_n^i)^T$ associated with Θ_i according to Equations (13)–(16).
- Step 5. Calculate overall perceived utility value Z_i of alternative Θ_i according to Equation (17).
- Step 6. Determine the alternatives ranking result.

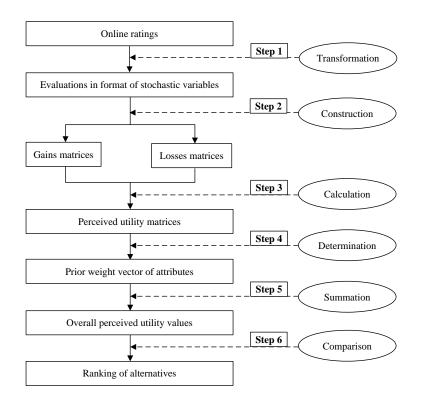


Figure 6. The flowchart of the proposed method.

5. A Case Study

We used the case of selecting a desirable tablet computer through online ratings in ZOL website to explain the practicality of the proposed decision support model.

A consumer wants to buy a tablet computer because of the occupational requirement. However, since the consumer has limited knowledge on electronic products, it is difficult to select an optimal or satisfying alternative tablet computer in time. Thus, it is necessary to decide using an e-commerce platform. ZOL website (http://www.zol.com.cn/) is one of the leading e-commerce platforms in China, which locates in the sales promotion of IT interactive portal. ZOL website collects product data for information technology on professional online video interactive marketing as one of the complex media. It is also the CBS interactive group interactive media company's flagship media in China. It provides many kinds of online ratings and reviews about electronic products.

By limiting the brand, basic function and price of tablet computers, five alternative tablet computers were initially screened by the consumer on ZOL website. The consumer needs to select a desirable tablet computer from the following five alternative tablet computers.

 Θ_1 : Apple iPad mini 2 Θ_2 : GALAXY Tab S T800 Θ_3 : MI Pad Θ_4 : ASUS ZenPad 3S 10 Θ_5 : Apple iPad Air 2

Based on the information of the e-commerce services platform, the following five attributes associated with alternative tablet computers are considered: appearance (O₁), photograph (O₂), performance (O₃), endurance (O₄) and cost performance (O₅). The prior order of the attributes is $O_3 \succ O_5 \succ O_2 \succ O_4 \succ O_1$. The consumer provides the prior order of evaluation attributes as a weight vector of the five evaluation attributes, which are denoted as $\Omega = (\omega_1, \omega_2, \omega_3, \omega_4, \omega_5)^T$. The proposed method in Section 4 is applied to rank these five alternative tablet computers. The calculation processes and discussion are expressed below.

5.1. Methodology and Results

Because the original data obtained from e-commerce websites are complex and massive, we must further convert the original data into structural data. First, we used crawl software to extract the online ratings of five tablet computers on evaluation attributes from the website of ZOL.COM.CN. The total numbers of the online ratings for tablet computers are 471, 144, 138, 102 and 429, respectively. On this website, the scales set of ratings is $B = \{B_1 = 2, B_2 = 4, B_3 = 6, B_4 = 8, B_5 = 10\}$. Then, the total number of each scale for each tablet computer on each evaluation attribute can be counted. Thus, the stochastic evaluations P_{ij} of alternative tablet computer Θ_i concerning attribute O_j are formatted as distributed information using Equation (4). Thus, we form the distribution linguistic decision matrix of five alternative tablet computers of five attributes as shown in Tables 2–6.

Table 2. The stochastic evaluations on attribute O₁.

Alternatives	Evaluations in Format of Stochastic Variables								
Alternatives	2	4	6	8	10				
Θ_1	0.204	0.184	0.263	0.118	0.23				
Θ_2	0.259	0.259	0.241	0.107	0.098				
Θ_3	0.455	0.210	0.210	0.042	0.084				
Θ_4	0.179	0.277	0.295	0.116	0.134				
Θ_5	0.184	0.170	0.220	0.135	0.291				

Alternatives	Evaluations in Format of Stochastic Variables								
Alternatives	2	4	6	8	10				
Θ_1	0.204	0.184	0.263	0.118	0.23				
Θ_2	0.259	0.259	0.241	0.107	0.098				
Θ_3	0.455	0.210	0.210	0.042	0.084				
Θ_4	0.179	0.277	0.295	0.116	0.134				
Θ_5	0.184	0.170	0.220	0.135	0.291				

Table 3. The stochastic evaluations on attribute O₂.

Alternatives	Evaluations in Format of Stochastic Variables									
Alternatives	2	4	6	8	10					
Θ_1	0.204	0.184	0.263	0.118	0.23					
Θ_2	0.259	0.259	0.241	0.107	0.098					
Θ_3	0.455	0.210	0.210	0.042	0.084					
Θ_4	0.179	0.277	0.295	0.116	0.134					
Θ_5	0.184	0.170	0.220	0.135	0.291					

Table 5. The stochastic evaluations on attribute O₄.

Alternatives	Evaluations in Format of Stochastic Variables								
Alternatives	2	4	6	8	10				
Θ ₁	0.204	0.184	0.263	0.118	0.23				
Θ_2	0.259	0.259	0.241	0.107	0.098				
Θ_3	0.455	0.210	0.210	0.042	0.084				
Θ_4	0.179	0.277	0.295	0.116	0.134				
Θ_5	0.184	0.170	0.220	0.135	0.291				

Alternatives	Evaluations in Format of Stochastic Variables								
Alternatives	2	4	6	8	10				
Θ_1	0.204	0.184	0.263	0.118	0.23				
Θ_2	0.259	0.259	0.241	0.107	0.098				
Θ_3	0.455	0.210	0.210	0.042	0.084				
Θ_4	0.179	0.277	0.295	0.116	0.134				
Θ_5	0.184	0.170	0.220	0.135	0.291				

Table 6. The stochastic evaluations on attribute O₅.

Then, according to Equations (5) and (6), based on the evaluations of alternatives in format of stochastic variables, the gain matrix $G_j = \left[g_{ik}^j\right]_{m \times m}$ and loss matrix $L_j = \left[l_{ik}^j\right]_{m \times m}$ on attribute O_j are constructed. Considering the regret behavior of consumer, the perceived utility matrix $\Phi_j = \left[\varphi_{ik}^j\right]_{m \times m}$ can be calculated according to Equations (10)–(12). Here, we suppose the parameter $\delta = 0.3$. Given space limitations in this paper, we only give the perceived utility matrices in the following:

$\Phi_1 = \begin{pmatrix} -0.0210 \\ 0.0310 \\ -1.0157 \\ 0.0841 \\ -0.1228 \end{pmatrix}$	-0.0670 -0.0135 -1.0980 0.0411 -0.1707	-0.4507 0.4839 -0.1916 0.5174 0.3747	-0.1178 -0.0627 -1.1900 -0.0066 -0.2236	$ \begin{array}{c} 0.0529 \\ 0.1034 \\ -0.9018 \\ 0.1549 \\ -0.0464 \end{array} \right), \\$
$\Phi_2 = \begin{pmatrix} -0.0493 \\ 0.1843 \\ -1.4375 \\ 0.1685 \\ -0.1092 \end{pmatrix}$	-0.2900 -0.0124 -1.9725 -0.0309 -0.3518	$\begin{array}{c} 0.5061 \\ 0.6298 \\ -0.2387 \\ 0.6246 \\ 0.4622 \end{array}$	-0.2714 0.0030 -1.9209 -0.0151 -0.3331	$ \begin{array}{c} -0.0185 \\ 0.2146 \\ -1.3810 \\ 0.1988 \\ -0.0772 \end{array} \right), $
$\Phi_3 = \begin{pmatrix} -0.0269\\ 0.0302\\ -1.9168\\ 0.0037\\ -0.1464 \end{pmatrix}$	-0.0828 -0.0211 -2.0790 -0.0502 -0.2040	$\begin{array}{c} 0.6112 \\ 0.6321 \\ -0.2419 \\ 0.6248 \\ 0.5320 \end{array}$	-0.0546 0.0044 -1.9917 -0.0232 -0.1750	$\begin{array}{c} 0.0500\\ 0.1064\\ -1.7610\\ 0.0802\\ -0.0663 \end{array}\right),$
$\Phi_4 = \begin{pmatrix} -0.0527 \\ -0.1835 \\ -1.1147 \\ 0.0342 \\ -0.2129 \end{pmatrix}$	$\begin{array}{c} 0.0646 \\ -0.0526 \\ -0.9136 \\ 0.1449 \\ -0.0864 \end{array}$	0.4290 0.3425 -0.2090 0.4803 0.3267	-0.1342 -0.2721 -1.2706 -0.0415 -0.3034	$ \begin{array}{c} 0.0501 \\ -0.0739 \\ -0.9220 \\ 0.1304 \\ -0.0991 \end{array} \right), \\$
$\Phi_5 = \begin{pmatrix} -0.1228 \\ -0.1977 \\ -0.7540 \\ 0.3714 \\ -0.2080 \end{pmatrix}$	-0.0006 -0.0611 -0.5889 0.4387 -0.0831	0.1692 0.1090 -0.2821 0.5538 0.1053	-0.7922 -0.9385 -1.7243 -0.0426 -0.9056	$ \begin{array}{c} -0.0813 \\ -0.1569 \\ -0.6858 \\ 0.4015 \\ -0.1623 \end{array} \right). $

Then, the perceived utility value z_{ij} of alternative Θ_i on attribute O_j can be calculated by Equation (13). The perceived utility matrix is shown as follows:

$$Z = [z_{ij}]_{5\times5} = \begin{pmatrix} 0.2977 & -0.1231 & 0.4969 & 0.3568 & -0.8276 \\ 0.5421 & 1.0192 & 0.7520 & -0.2396 & -1.2452 \\ -4.3969 & -6.9505 & -7.9904 & -4.4299 & -4.0352 \\ 0.7909 & 0.9460 & 0.6352 & 0.7483 & 1.7228 \\ -0.1888 & -0.4090 & -0.0598 & -0.3751 & -1.2538 \end{pmatrix}$$

Based on prior order of evaluation attributes and Equations (14)–(16), the prior weights vectors of evaluation attributes associated with product A_i are $\Omega_1 = (0.030, 0.115, 0.512, 0.055, 0.288)^T$, $\Omega_2 = (0.031, 0.104, 0.503, 0.065, 0.297)^T$, $\Omega_3 = (0, 0.002, 0.980, 0.001, 0.017)^T$, $\Omega_4 = (0.062, 0.171, 0.419, 0.105, 0.243)^T$, and $\Omega_5 = (0.020, 0.097, 0.563, 0.043, 0.277)^T$. By aggregating the perceived utility values of alternatives on different attributes using Equation (17), the overall perceived utility values are:

$$Z_1 = 0.031, Z_2 = 0.114, Z_3 = -7.918, Z_4 = 0.974, Z_5 = -0.442$$

According to the descending order of the values of Z_i , the ranking result of these five alternatives are obtained as follows:

$$\Theta_4 \succ \Theta_2 \succ \Theta_1 \succ \Theta_5 \succ \Theta_3$$

5.2. Analysis on the Effect of the Parameter of Regret Aversion

In this section, to show the robustness of the proposed method, we design a sensitivity analysis for our proposal. In a real decision-making situation, due to the different focuses of the decision makers, their regret aversion degrees are different. The degrees of regret aversion are embodied in different regret aversion parameters. Thus, different regret aversion parameters might be used by different decision makers.

We suppose that the parameter δ can be assigned different numbers: $\delta = 0.3$, $\delta = 0.5$, $\delta = 0.7$ and $\delta = 0.9$. Different δ s yield different results, as shown in Table 7.

Thus, the ranking results under the different parameter are Table 7, in which the ranking results are similar but not identical. If $\delta = 0.3$ or $\delta = 0.5$, the ranking result is $\Theta_4 \succ \Theta_2 \succ \Theta_1 \succ \Theta_5 \succ \Theta_3$. In the case of $\delta = 0.7$ or $\delta = 0.9$, the ranking result is $\Theta_4 \succ \Theta_1 \succ \Theta_2 \succ \Theta_3 \succ \Theta_3$. Thus, the parameter δ reflects regret aversion degree of consumer, which directly leads to the different ranking results.

Tablet -	$\delta = 0.2$	3	$\delta = 0.5$		0.5 $\delta = 0.5$		$\delta = 0.$	9
Computer	Perceived Utility Values	Ranking						
Θ_1	0.031	3	-0.554	3	-1.577	2	-2.975	2
Θ_2	0.114	2	-0.522	2	-1.742	3	-3.511	3
Θ_3	-7.918	5	-21.250	5	-48.828	5	-106.007	5
Θ_4	0.974	1	1.142	1	1.078	1	0.836	1
Θ_5	-0.114	4	-1.417	4	-2.778	4	-4.286	4

Table 7. The different results with different parameter δ .

5.3. Comparison Analysis

In this subsection, to show the better feasibility of the proposed method, we take the example from Fan and coworkers' study [6]. Furthermore, we compare the proposed method with the previously designed ones by Fan et al. [6] and Kang and Park [13]. The problem formulation and comparison process are shown as follows.

Example. [6] A consumer wants to buy an SUV from the following five alternatives: Θ_1 : Jeep, Compass; Θ_2 : Mazda, CX5; Θ_3 : Subaru, Forester; Θ_4 : Toyota, Highlander; and Θ_5 : Chevolet, Kopacz. Based on

the information provided by the e-commerce services platform (http://www.autohome.com.cn/), the following eight attributes associated with alternative SUVs are considered: Trunk space (O_1), Power (O_2), Control (O_3), Fuel consumption (O_4), Comfortability (O_5), Appearance (O_6), Cost performance (O_7) and Price (O_8). First, the consumer provides the weight vector of attributes: $\Omega = (0.05, 0.15, 0.1, 0.2, 0.1, 0.15, 0.1, 0.15)^T$. The corresponding online product ratings are extracted from the website of Autohome (http://www.autohome. com.cn/). Then, the evaluations of products are formulated as distribution information presented in Table 8.

Alternative SUVs	Rating Scales				Attri	butes			
		01	O ₂	O ₃	O_4	O ₅	O ₆	O ₇	O ₈
	1	6	1	1	6	2	1	6	4
	2	21	14	3	53	25	1	58	12
Θ_1	3	256	163	48	282	305	46	392	132
	4	790	652	382	572	632	208	655	573
	5	282	525	921	442	391	1099	244	634
	1	5	6	6	7	6	6	12	9
	2	5	13	2	3	13	2	30	3
Θ_2	3	66	157	5	20	283	68	464	53
	4	981	908	106	198	979	378	975	480
	5	728	701	1666	1557	504	1331	304	1240
	1	0	0	1	3	2	0	10	2
	2	2	5	0	15	22	3	82	23
Θ_3	3	46	75	12	139	358	122	478	210
	4	385	651	286	538	714	661	724	695
	5	1061	763	1195	799	389	708	200	564
	1	0	5	5	1	0	1	17	4
	2	0	7	20	27	4	0	98	7
Θ_4	3	2	199	228	173	71	50	569	84
	4	29	770	689	564	493	424	530	521
	5	1394	444	483	660	857	950	211	809
	1	0	4	3	13	1	0	0	0
	2	1	19	4	88	8	5	13	4
Θ_5	3	6	378	83	456	143	91	226	24
	4	121	720	560	582	659	581	734	233
	5	1135	142	613	124	452	586	290	1002

Table 8. The distribution evaluations of products.

The methods developed by Fan et al. [6] and Kang and Park [13] as well as our method presented in Section 4 are separately applied to rank these five alternative SUVs. Since first two methods only address the situation that consumer is entirely rational, to make the comparison worthwhile, we also suppose that the consumer is entirely rational. Consequently, we first assume that the regret–rejoice function is R(x) = x. Then, the different degrees of consumer's regret behavior are considered subsequently. The ranking results are listed in Table 9.

Table 9. Comparison of results obtained using the three methods.

	Ranking of Alternatives	
The method prese	$\Theta_2 \succ \Theta_4 \succ \Theta_1 \succ \Theta_3 \succ \Theta_5$	
The method p	$\Theta_2 \succ \Theta_3 \succ \Theta_4 \succ \Theta_1 \succ \Theta_5$	
_	Considering entire rationality	$\Theta_2\succ \Theta_3\succ \Theta_4\succ \Theta_1\succ \Theta_5$
The proposed method in this study	Considering regret behavior ($\delta = 0.1, 0.3, 0.5$)	$\Theta_2\succ \Theta_3\succ \Theta_4\succ \Theta_1\succ \Theta_5$
The proposed memod in this study	Considering regret behavior ($\delta = 0.7$)	$\Theta_2\succ \Theta_3\succ \Theta_4\succ \Theta_1\succ \Theta_5$
	Considering regret behavior ($\delta = 0.9$)	$\Theta_3\succ\Theta_2\succ\Theta_4\succ\Theta_1\succ\Theta_5$

As shown in Table 9, the trend of sorting results by using the mentioned methods are similar, except the first ranking result is quite different from others. With respect to the first method provided by Kang and Park [13], the assessments that are transformed from online reviews were slightly rough.

Moreover, some information on different evaluation levels is partially ignored. Therefore, comparing the results, the method proposed in this study can avoid information loss when transforming the online reviews into crisp evaluations. Furthermore, by using our method, more accurate overall compromise values of alternative SUVs can be generated to obtain a more persuasive ranking result. With respect to the method based on stochastic dominance theory provided by Fan et al. [6], the ranking result is completely consistent with the one given by this study. However, by stochastic dominance theory, the dominance relationship between any two alternatives can be determined. According to the dominance relationship, the dominance degree of a product over another one can be calculated subsequently. The method to determine the dominance relationship and dominance degrees has a higher computational complexity than the proposed method. Additionally, in this study, the different degrees of consumer's regret behavior are considered, which improves the feasibility of the decision results in dealing with the realistic problem.

6. Conclusions

The decision-making problem for products selection oriented on online evaluations has important theoretical significance and practical application value. To facilitate the selection of products for consumers, an effective decision-making support model needs to be investigated. In this paper, with respect to selection of products, a decision support model is proposed based on massive online ratings. In the proposed method, by crawling the massive online ratings for products provided by different reviewers, quantitative information is prepared for decision making process. Then, considering the regret aversion behavior of consumer, the perceived utility values of consumer for alternatives is proposed. It provides one more valid tool for uncertain decision-making problem with stochastic variables information.

Compared with existing studies, this research has the following contributions. On the one hand, from a realistic perspective, the product selection problem oriented on massive online ratings is investigated to propose a novel decision model to support selection and purchase. Then, the regret aversion behavior of consumer is considered, which is more realistic than other methods based on online evaluations. On the other hand, from a theoretical point of view, to preserve the integrity of the raw data as much as possible, we processed the massive ratings into stochastic evaluations. This avoids the information loss or distortion in the existing methods. Then, a more accurate method of comparison any two stochastic variables is constructed to calculate rejoice values and regret values of alternatives, subsequently.

For future studies, to make the decision result more comprehensive, it is worth noting that online reviews can be considered as well as online ratings [11,12]. Further, since the evaluation attribute is unknown, mining evaluation attributes from online reviews needs to be investigated. Additionally, evaluation on green supply chain, population resources and environment by public participation [26–28] can be incorporated into future investigations.

Author Contributions: X.L. and P.L. proposed the topic explored in this paper. X.L. and P.L. discussed and designed the decision support model. X.L. and Z.L. conducted the sensitivity analysis and comparison analysis in the case study. X.L. wrote the paper. In addition, Y.S. in Shandong University of Finance and Economics thoroughly reviewed and improved the paper. All authors have discussed and contributed to the manuscript. All authors have read and approved the final manuscript.

Acknowledgments: This work was jointly supported by the National Natural Science Foundation of China (NSFC, Project Nos. 71771140 and 71701111), the Humanities and Social Sciences Research Project of Ministry of Education of China (Nos. 17YJC630077 and 17YJA630065), the Shandong Province Social Science Planning Project (No. 16DGLJ06), the Project of Shandong Province Higher Educational Science and Technology Program (No. J17KA189) and Natural Science Planning Project of Shandong province (No. ZR2017MG007).

Conflicts of Interest: The authors declare no conflict of interest.

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