



Article

A Time-Symmetric Resolution of the Einstein's Boxes Paradox

Michael B. Heaney

Independent Researcher, 3182 Stelling Drive, Palo Alto, CA 94303, USA; mheaney@alum.mit.edu

Abstract: The Einstein's Boxes paradox was developed by Einstein, de Broglie, Heisenberg, and others to demonstrate the incompleteness of the Copenhagen Formulation of quantum mechanics. I explain the paradox using the Copenhagen Formulation. I then show how a time-symmetric formulation of quantum mechanics resolves the paradox in the way envisioned by Einstein and de Broglie. Finally, I describe an experiment that can distinguish between these two formulations.

Keywords: quantum foundations; time-symmetric; Einstein's boxes; Einstein-Podolsky-Rosen (EPR)

1. Introduction

A grand challenge of modern physics is to resolve the conceptual paradoxes in the foundations of quantum mechanics [1]. Some of these paradoxes concern nonlocality and completeness. For example, Einstein believed the Copenhagen Formulation (CF) of quantum mechanics was incomplete. He presented a thought experiment (later known as "Einstein's Bubble") explaining his reasoning at the 1927 Solvay conference [2]. In this experiment, an incident particle's wavefunction diffracts at a pinhole in a flat screen and then spreads to all parts of a hemispherical screen capable of detecting the wavefunction. The wavefunction is then detected at one point on the hemispherical screen, implying the wavefunction everywhere else vanished instantaneously. Einstein believed that this instantaneous wavefunction collapse violated the special theory of relativity, and the wavefunction must have been localized at the point of detection immediately before the detection occurred. Since the CF does not describe the wavefunction localization before detection, it must be an incomplete theory. In an earlier paper, I analyzed a one-dimensional version of this thought experiment with a time-symmetric formulation (TSF) of quantum mechanics [3], showing that the TSF did not need wavefunction collapse to explain the experimental results.

Einstein, de Broglie, Heisenberg, and others later modified Einstein's original thought experiment to emphasize the nonlocal action-at-a-distance effects. In the modified experiment, the particle's wavefunction was localized in two boxes which were separated by a space-like interval. This modified thought experiment became known as "Einstein's Boxes." Norsen wrote an excellent analysis of the history and significance of the Einstein's Boxes thought experiment using the CF [4].

Time-symmetric explanations of quantum behavior predate the discovery of the Schrödinger equation [5] and have been developed many times over the past century [6–33]. The TSF used in this paper has been described in detail and compared to other TSFs before [3,31–33]. Note in particular that the TSF used in this paper is significantly different than the Two-State Vector Formalism (TSVF) [12,23,24]. First, the TSVF postulates that a quantum particle is completely described by two state vectors, written as $\langle \phi | | \psi \rangle$, where $| \psi \rangle$ is a retarded state vector satisfying the retarded Schrödinger equation $i\hbar\partial|\psi\rangle/\partial t = H|\psi\rangle$ and the initial boundary conditions, while $\langle \phi |$ is an advanced state vector satisfying the advanced Schrödinger equation $-i\hbar\langle\phi|\partial/\partial t = \langle\phi|H$ and the final boundary conditions. In contrast, the TSF postulates that the *transition* of a quantum particle is completely described by a complex transition amplitude density $\phi^*\psi$, defined as the algebraic product of the two wavefunctions. Second, the TSVF postulates that wavefunctions collapse upon



Citation: Heaney, M.B. A
Time-Symmetric Resolution of the
Einstein's Boxes Paradox. *Symmetry*2022, 14, 1217. https://doi.org/
10.3390/sym14061217

Academic Editor: Tuong Trong Truong

Received: 11 May 2022 Accepted: 10 June 2022 Published: 13 June 2022

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2022 by the author. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/).

Symmetry **2022**, 14, 1217 2 of 8

measurement, while the TSF has no collapse postulate. The particular TSF used in this paper is a type IIB model in the classification system of Wharton and Argaman [34].

Section 2 explains the paradox associated with the CF of the Einstein's Boxes thought experiment, as described by de Broglie. Section 3 reviews a CF numerical model of the thought experiment which does not resolve the paradox. Section 4 describes a TSF numerical model of the thought experiment which resolves the paradox. Section 5 discusses the conclusions and implications.

Note that this paper only concerns a single quantum particle interfering with itself and not multiple quantum particles entangled with each other.

2. The Einstein's Boxes Paradox

The Einstein's Boxes paradox was explained by de Broglie as follows [35]:

Suppose a particle is enclosed in a box B with impermeable walls. The associated wave ψ is confined to the box and cannot leave it. The usual interpretation asserts that the particle is "potentially" present in the whole of the box B, with a probability $|\psi|^2$ at each point. Let us suppose that by some process or other, for example, by inserting a partition into the box, the box B is divided into two separate parts B_1 and B_2 and that B_1 and B_2 are then transported to two very distant places, for example to Paris and Tokyo. The particle, which has not yet appeared, thus remains potentially present in the assembly of the two boxes and its wavefunction ψ consists of two parts, one of which, ψ_1 , is located in B_1 and the other, ψ_2 , in B_2 . The wavefunction is thus of the form $\psi = c_1\psi_1 + c_2\psi_2$, where $|c_1|^2 + |c_2|^2 = 1$.

The probability laws of [the Copenhagen Formulation] now tell us that if an experiment is carried out in box B_1 in Paris, which will enable the presence of the particle to be revealed in this box, the probability of this experiment giving a positive result is $|c_1|^2$, while the probability of it giving a negative result is $|c_2|^2$. According to the usual interpretation, this would have the following significance: because the particle is present in the assembly of the two boxes prior to the observable localization, it would be immediately localized in box B_1 in the case of a positive result in Paris. This does not seem to me to be acceptable. The only reasonable interpretation appears to me to be that prior to the observable localization in B_1 , we know that the particle was in one of the two boxes B_1 and B_2 , but we do not know in which one, and the probabilities considered in the usual wave mechanics are the consequence of this partial ignorance. If we show that the particle is in box B_1 , it implies simply that it was already there prior to localization. Thus, we now return to the clear classical concept of probability, which springs from our partial ignorance of the true situation. But, if this point of view is accepted, the description of the particle given by ψ , though leading to a perfectly exact description of probabilities, does not give us a complete description of the physical reality, because the particle must have been localized prior to the observation which revealed it, and the wavefunction ψ gives no information about this.

We might note here how the usual interpretation leads to a paradox in the case of experiments with a negative result. Suppose that the particle is charged, and that in the box B_2 in Tokyo a device has been installed which enables the whole of the charged particle located in the box to be drained off and in so doing to establish an observable localization. Now, if nothing is observed, this negative result will signify that the particle is not in box B_2 and it is thus in box B_1 in Paris. But this can reasonably signify only one thing: the particle was already in Paris in box B_1 prior to the drainage experiment made in Tokyo in box B_2 . Every other interpretation is absurd. How can we imagine that the simple fact of having observed *nothing* in Tokyo has been able to promote the localization of the particle at a distance of many thousands of miles away?

Symmetry **2022**, 14, 1217 3 of 8

3. The Conventional Formulation of Einstein's Boxes

The version of Einstein's Boxes proposed by de Broglie is experimentally impractical. We will use Heisenberg's more practical version [36], shown in Figure 1. The Conventional Formulation (CF) postulates that a single free particle wavefunction with a mass m is completely described by a retarded wavefunction $\psi(\vec{r},t)$ which satisfies the initial conditions and evolves over time according to the retarded Schrödinger equation:

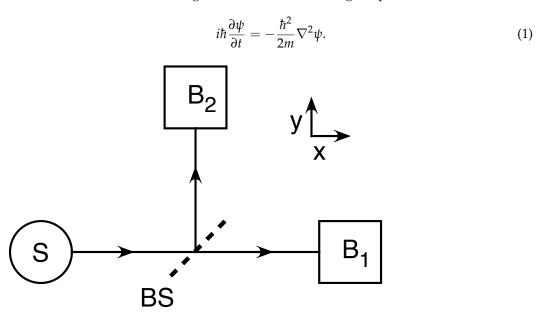


Figure 1. The modified Einstein's Boxes thought experiment. The source S can emit single-particle wavefunctions on command. Each wavefunction travels to the balanced beam splitter BS and then to box B_1 and box B_2 . The two boxes are separated by a space-like interval.

The "retarded wavefunction" and "retarded Schrödinger equation" are simply the usual wavefunction and Schrödinger equation, described as retarded to distinguish them from the "advanced wavefunction" and "advanced Schrödinger equation," which will be defined below. We will use units where $\hbar=1$ and assume the wavefunction $\psi(\vec{r},t)$ is a traveling Gaussian with an initial standard deviation $\sigma=50$, initial momentum $k_x=0.4$, and mass m=1. We will also assume that each box contains a detector whose eigenstate is the same Gaussian as that emitted by the source. The CF assumes that a single-particle wavefunction emitted from a source S will travel to the beam splitter BS, where half of it will pass through BS and continue to box B_1 while the other half will be reflected from BS and travel to box B_2 . Let us assume the two halves reach the boxes at the same time.

Figure 2 shows how the wavefunction's CF probability density $\psi^*\psi$ evolves over time, assuming the initial condition is localization in the source S. At t=0, $\psi^*\psi$ is localized inside the source S. At t=1000, $\psi^*\psi$ is traveling toward the beam splitter BS. At t=3000, $\psi^*\psi$ has been split in half by the beam splitter, and the two halves are traveling toward box B_1 and box B_2 . At $t=4000-\delta t$, half of $\psi^*\psi$ arrives at box B_1 , while the other half arrives at box B_2 . Upon a measurement at box B_2 at t=4000, the CF postulates that in 50% of the runs, the half wavefunction in box B_2 collapses to zero, while simultaneously, the half wavefunction in box B_1 collapses to a full wavefunction $\phi(\vec{r},t)$, which we will assume has the same shape and size as the initial wavefunction. It was believed by de Broglie that this prediction of the CF was absurd: "How can we imagine that the simple fact of having observed *nothing* in [box B_2] has been able to promote the localization of the particle [in box B_1] at a distance of many thousands of miles away?"

Symmetry **2022**, 14, 1217 4 of 8

The CF assumes that the probability P_c for the collapse in box B_1 is $P_c = A_c^* A_c$, where the subscript c denotes the CF and the CF transition amplitude A_c for the collapse is

$$A_c = \int_{-\infty}^{\infty} \phi^*(x, y, 4000) \frac{1}{\sqrt{2}} \psi(x, y, 4000) dx dy, \tag{2}$$

where t=4000 is the time of wavefunction collapse and the "quantum" factor $\frac{1}{\sqrt{2}}$ accounts for the initial wavefunction $\psi(x,y,t)$ being split in half when it reaches box B_1 . Plugging in numbers gives a collapse probability $P_c=0.43$. This probability is not 1/2 because the evolved wavefunction at t=4000 is not identical in shape to the detector eigenstate.

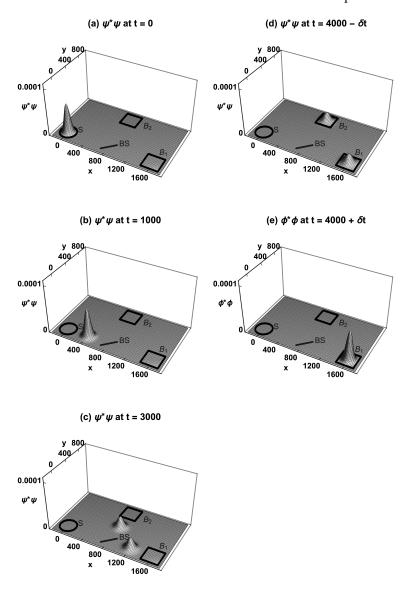


Figure 2. The Conventional Formulation (CF) explanation of the Einstein's Boxes experiment with a single-particle wavefunction emitted from source S. (a) The probability density $\psi^*\psi$ is localized inside S. (b) $\psi^*\psi$ has left S and is traveling toward the beam splitter BS. (c) $\psi^*\psi$ has been split in half by BS, and the two halves are traveling toward boxes B_1 and B_2 . (d) The two halves arrive at B_1 and B_2 . (e) A measurement at either B_1 or B_2 at t=4000 causes either ψ to collapse to zero in B_2 and to a full wavefunction in B_1 (shown) or ψ to collapse to zero in B_1 and to a full wavefunction in B_2 (not shown).

Symmetry **2022**, 14, 1217 5 of 8

4. The Time-Symmetric Formulation of Einstein's Boxes

The TSF postulates that quantum mechanics is a theory about *transitions* described by the transition amplitude density $\phi^*\psi$, where ψ is a retarded wavefunction that obeys the retarded Schrödinger equation $i\hbar\partial\psi/\partial t=H\psi$ and satisfies the initial boundary conditions, while ϕ^* is an advanced wavefunction that obeys the advanced Schrödinger equation $-i\hbar\partial\phi^*/\partial t=H\phi^*$ and satisfies the final boundary conditions. As in the TSVF, ψ can be interpreted as a retarded wavefunction from the past initial conditions, and ϕ^* can be interpreted as an advanced wavefunction from the future final conditions [3]. We will assume the same wavefunctions $\psi(\vec{r},t)$ and $\phi(\vec{r},t)$ as in the CF above.

An electron (e.g.) can be absorbed by a few molecules in a detector. The number of few-molecule sites in a detector is orders of magnitude larger than the number of square centimeter sites in a detector. This makes it overwhelmingly more likely that the electron will be absorbed in an area localized to a few square nanometers than much larger areas. This could explain why the transition amplitude density refocuses to a localized area at the detector. Note that there exist two unitary solutions based on the initial conditions, but time-symmetric theories also require the final conditions, which are that the particle is always found in either one or the other box. Let us then assume the final conditions are either a transition amplitude density localized in box B_1 or a transition amplitude density localized in box B_2 .

Figure 3 shows the TSF explanation of the Einstein's Boxes thought experiment, assuming that the final condition is a particle transition amplitude density localized in box B_1 . At t=0, $|\phi^*\psi|$ is localized inside the source S. At t=1000, $|\phi^*\psi|$ is traveling toward the beam splitter BS. At t=3000, $|\phi^*\psi|$ has passed through the beam splitter and is traveling toward box B_1 . $|\phi^*\psi|$ is zero on the path from BS to B_2 because ϕ^* is zero on this path. At $t=4000-\delta t$, $|\phi^*\psi|$ arrives at box B_1 . Upon a measurement at box B_2 at t=4000, no particle transition amplitude density is found. Upon a measurement at box B_1 at t=4000, one particle's transition amplitude density is found. The one-particle transition amplitude density was localized inside box B_1 before the measurement was made.

The TSF assumes the probability P_t for the transition from localization in the source S to localization in box B_1 is $P_t = \frac{1}{2}A_t^*A_t$, where the subscript t denotes the TSF, the "classical" probability factor $\frac{1}{2}$ accounts for the fact that there are two equally likely possible final states, and the TSF amplitude A_t for the transition is

$$A_t = \int_{-\infty}^{\infty} \phi^*(x, y, t) \psi(x, y, t) dx dy, \tag{3}$$

Plugging in numbers gives a TSF transition probability $P_t = 0.43$, which is identical to the CF collapse probability result. Note that there is no transition amplitude density collapse in the TSF, so there is no need to specify the time of collapse in the integrand.

Symmetry **2022**, 14, 1217 6 of 8

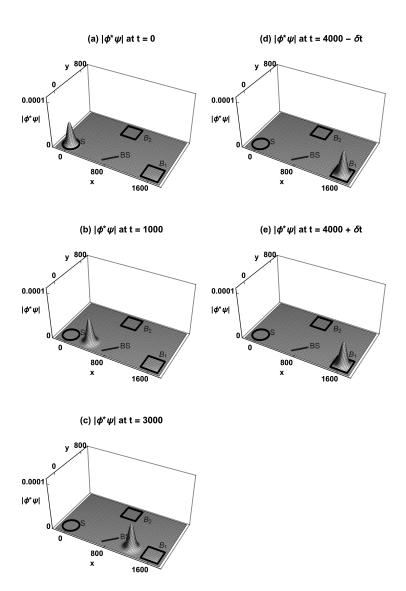


Figure 3. The time-symmetric formulation (TSF) explanation of the Einstein's Boxes experiment, with a single-particle transition amplitude density emitted from source S and detected at box B_1 . (a) The absolute value of the transition amplitude density $|\phi^*\psi|$ is localized inside S. (b) $|\phi^*\psi|$ has left S and is traveling toward the beam splitter SS. (c) $|\phi^*\psi|$ has passed through SS and is traveling toward box SS and is traveling toward box SS are zero on the path from SS to SS because SS is zero on this path. (d) $|\phi^*\psi|$ arrives at SS are SS Measurements at SS and is transition amplitude density in SS and is transition amplitude density in SS and is density in SS and is traveling toward box SS because SS is zero on this path. (d) $|\phi^*\psi|$ arrives at SS and is transition amplitude density in SS and is traveling toward box SS because SS is zero on this path. (d) $|\phi^*\psi|$ arrives at SS are SS is zero on the path from SS to SS because SS is zero on this path. (e) Measurements at SS are density in SS and is traveling toward box SS and is traveling toward box SS is zero on the path from SS to SS because SS is zero on this path. (d) $|\phi^*\psi|$ arrives at SS is zero on the path from SS to SS because SS is zero on this path.

5. Discussion

To the best of my knowledge, this is the first time a TSF has been shown to resolve the Einstein's Boxes paradox. The TSF resolves the paradox in the ways that Einstein and de Broglie envisioned. The transition amplitude density $\phi^*\psi$ "localises the particle during the propagation [2]," and $\phi^*\psi$ "was already in Paris in box B_1 prior to the drainage experiment made in Tokyo in box B_2 [35]." None of the problems associated with wavefunction collapse occur. The TSF appears to give the sought-after exact description of the probabilities and a complete description of the physical reality.

One might wonder if a theory based on transition amplitude densities will be able to reproduce all of the predictions of the CF. In 1932, Dirac showed that all the experimental predictions of the CF of quantum mechanics can be formulated in terms of transition probabilities [37]. The TSF inverts this fact by postulating that quantum mechanics is a

Symmetry **2022**, 14, 1217 7 of 8

theory which experimentally predicts *only* the transition probabilities. This implies that the TSF has the same predictive power as the CF.

The TSF has the additional benefit of being consistent with the classical explanation of the Einstein's Boxes thought experiment. As the size of the "particle" becomes larger and it starts behaving more like a classical particle, it will always go to either one box or the other. There is a logical continuity between its behavior in the quantum and classical regimes, in contrast to the CF predictions.

In the TSF example above, we assumed the transition probabilities for the two boxes were the same. Now consider the case where the two transitions are not equally likely. For a very unlikely transition, the pre-experiment estimate of the TSF transition amplitude density $\phi^*\psi$ is tiny, while for a very likely transition, the pre-experiment estimate of $\phi^*\psi$ is large. However, this does not mean that $\phi^*\psi$ itself is a smaller-sized field in the event of an unlikely outcome. Before an experiment is conducted, we have classical ignorance of which transition will occur. We normalize the wavefunctions ψ and ϕ^* to unity and calculate the expected probability for each transition based on $\phi^*\psi$. After the experiment is complete, we know which of the two possible transitions actually occurred, so we renormalize the $\phi^*\psi$ of that transition to give a transition probability of one and renormalize the other $\phi^*\psi$ to zero. Note that this is an update of our classical ignorance of which transition occurred and not a physical wavefunction collapse. This may explain why the CF collapse postulate appears to work.

A central issue raised by the Einstein's Boxes paradox is the question of which elements of quantum theory should be thought of as elements of reality (ontic) and which elements are merely states of knowledge (epistemic). The TSF transition amplitude density $\phi^*\psi$ and the wavefunctions ψ and ϕ^* should be thought of as elements of reality, with the understanding that $\phi^*\psi$ is the TSF equivalent of a real particle wavefunction while ψ and ϕ^* are the TSF equivalents of virtual particle wavefunctions. For multiple particles, $\phi^*\psi$ lives in a higher dimensional configuration spacetime, which should be thought of as the stage for reality [32]. The CF concept of a superposition of paths after the beam splitter then becomes just a state of knowledge in the TSF. In reality, only one path is taken; we just do not know in advance which one. Since the TSF assumes that the sources and sinks are randomly emitting ψ and ϕ^* wavefunctions, it is a probabilistic theory. In analogy with the classical theory of special relativity, the TSF transition amplitude density can be thought of as a quantum worldtube. The higher dimensional configuration spacetime is then the quantum equivalent of Minkowski spacetime.

Finally, the CF predicts a rapid oscillating motion of a free particle's wavefunction in empty space. Schrödinger discovered the possibility of this rapid oscillating motion in 1930, naming it zitterbewegung [38]. This prediction of the CF is inconsistent with Newton's first law, since it implies a free particle's wavefunction does not move with a constant velocity. The TSF predicts zitterbewegung will never occur [3]. Direct measurements of zitterbewegung are beyond the capability of current technology, but future technological developments should allow measurements to confirm or deny its existence. Given the technology, one possible way to test for zitterbewegung would be to hold an electron in the ground state in a parabolic potential and then turn off the potential while looking for radiation at the zitterbewegung frequency of $10^{21} \, \mathrm{s}^{-1}$. This could distinguish between the CF and the TSF.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable. **Data Availability Statement:** Not applicable.

Acknowledgments: I thank Travis Norsen and David A. Fotland for helpful conversations.

Conflicts of Interest: The author declares no conflict of interest.

Symmetry **2022**, 14, 1217 8 of 8

References

1. Smolin, L. *The Trouble with Physics: The Rise of String Theory, the Fall of a Science, and What Comes Next;* Houghton Mifflin Company: New York, NY, USA, 2006; pp. 3–17.

- 2. Bacciagaluppi, G.; Valentini, A. *Quantum Theory at the Crossroads: Reconsidering the 1927 Solvay Conference*; Cambridge University Press: Cambridge, UK, 2009.
- 3. Heaney, M.B. A symmetrical interpretation of the Klein-Gordon equation. Found. Phys. 2013, 43, 733–746. [CrossRef]
- 4. Norsen, T. Einstein's Boxes. Am. J. Phys. 2005, 73, 164. [CrossRef]
- 5. Tetrode, H.M. Über den Wirkungszusammenhang der Welt. Eine Erweiterung der klassischen Dynamik. *Z. Phys.* **1922**, 10, 317–328. Available online: http://www.mpseevinck.ruhosting.nl/seevinck/Translation_Tetrode.pdf (accessed on 20 January 2021). [CrossRef]
- 6. Lewis, G.N. The nature of light. *Proc. Natl. Acad. Sci. USA* 1926, 12, 22. [CrossRef]
- 7. Eddington, A.S. *The Nature of the Physical World: Gifford Lectures Delivered at the University of Edinburgh, January to March* 1927; The Macmillan Co.: New York, NY, USA, 1928; pp. 216–217.
- 8. Costa de Beauregard, O. Mécanique Quantique. Compt. Rend. 1953, 236, 1632–1634.
- 9. Watanabe, S. Symmetry of physical laws. Part III. prediction and retrodiction. Rev. Mod. Phys. 1955, 27, 179–186. [CrossRef]
- 10. Watanabe, S. Symmetry in time and Tanikawa's method of superquantization in regard to negative energy fields. *Prog. Theor. Phys.* **1956**, *15*, 523–535. [CrossRef]
- 11. Sciama, D. Determinism and the Cosmos. In *Determinism and Freedom in the Age of Modern Science*; Hook, S., Ed.; Collier Books: New York, NY, USA, 1961; pp. 90–91.
- 12. Aharonov, Y.; Bergmann, P.G.; Lebowitz, J.L. Time symmetry in the quantum process of measurement. *Phys. Rev.* **1964**, *134*, B1410–B1416. [CrossRef]
- 13. Davidon, W.C. Quantum physics of single systems. Il Nuovo C. B 1976, 36, 34–40. [CrossRef]
- 14. Roberts, K.V. An objective interpretation of Lagrangian quantum mechanics. Proc. R. Soc. Lond. A 1978, 360, 135–160.
- 15. Rietdijk, C.W. Proof of a Retroactive Influence. Found. Phys. 1978, 8, 615–628. [CrossRef]
- 16. Cramer, J.G. The transactional interpretation of quantum mechanics. Rev. Mod. Phys. 1986, 58, 647–687. [CrossRef]
- Hokkyo, N. Variational formulation of transactional and related interpretations of quantum mechanics. Found. Phys. Lett. 1988, 1, 293–299. [CrossRef]
- 18. Sutherland, R.I. Density formalism for quantum theory. Found. Phys. 1998, 28, 1157–1190. [CrossRef]
- 19. Pegg, D.T.; Barnett, S.M. Retrodiction in quantum optics. J. Opt. B Quantum Semiclass. Opt. 1999, 1, 442-445. [CrossRef]
- 20. Wharton, K.B. Time-symmetric quantum mechanics. Found. Phys. 2007, 37, 159–168. [CrossRef]
- 21. Hokkyo, N. Retrocausation acting in the single-electron double-slit interference experiment. *Stud. Hist. Philos. Sci. B Stud. Hist. Philos. Mod. Phys.* **2008**, *39*, 762–766. [CrossRef]
- 22. Miller, D.J. Quantum mechanics as a consistency condition on initial and final boundary conditions. *Stud. Hist. Philos. Sci. B Stud. Hist. Philos. Mod. Phys.* **2008**, *39*, 767–781. [CrossRef]
- 23. Aharonov, Y.; Vaidman, L. The Two-State Vector Formalism: An Updated Review. In *Time in Quantum Mechanics*; Muga, G., Sala Mayato, R., Egusquiza, I., Eds.; Springer: Berlin/Heidelberg, Germany, 2008; pp. 399–447.
- 24. Aharonov, Y.; Popescu, S.; Tollaksen, J. A time-symmetric formulation of quantum mechanics. *Phys. Today* **2010**, *63*, 27–32. [CrossRef]
- 25. Wharton, K.B. A novel interpretation of the Klein-Gordon equation. Found. Phys. 2010, 40, 313–332. [CrossRef]
- 26. Gammelmark, S.; Julsgaard, B.; Mølmer, K. Past quantum states of a monitored system. *Phys. Rev. Lett.* **2013**, 111, 160401. [CrossRef]
- 27. Price, H. Time's Arrow and Archimedes' Point: New Directions for the Physics of Time; Oxford University Press: New York, NY, USA, 1997.
- 28. Corry, R. Retrocausal models for EPR. Stud. Hist. Philos. Mod. Phys. 2015, 49, 1–9. [CrossRef]
- 29. Schulman, L.S. Time's Arrows and Quantum Measurement; Cambridge University Press: New York, NY, USA, 1997.
- 30. Drummond, P.D.; Reid, M.D. Retrocausal model of reality for quantum fields. *Phys. Rev. Res.* **2020**, 2, 033266-1–033266-15. [CrossRef]
- 31. Heaney, M.B. A symmetrical theory of nonrelativistic quantum mechanics. *arXiv* **2013**, arXiv:1310.5348.
- 32. Heaney, M.B. A Time-Symmetric Formulation of Quantum Entanglement. *Entropy* **2021**, *23*, 179. [CrossRef] [PubMed]
- 33. Heaney, M.B. Causal Intuition and Delayed-Choice Experiments. Entropy 2021, 23, 23. [CrossRef]
- 34. Wharton, K.B.; Argaman, N. Colloquium: Bell's theorem and locally mediated reformulations of quantum mechanics. *Rev. Mod. Phys.* **2020**, 92, 021002. [CrossRef]
- 35. de Broglie, L. The Current Interpretation of Wave Mechanics: A Critical Study; Elsevier: Amsterdam, The Netherlands, 1964; pp. 28–29.
- 36. Heisenberg, W. The Physical Principals of the Quantum Theory; Dover Publications: Mineola, NY, USA, 1949; p. 39.
- 37. Dirac, P.A.M. Relativistic quantum mechanics. Proc. R. Soc. Lond. Ser. A 1932, 136, 453-464.
- 38. Schrödinger, E. Über die kräftefreie Bewegung in der relativistischen Quantenmechanik. *Sitz. Preuss. Akad. Wiss. Phys. Math. Kl.* **1930**, 24, 418–428.