## Article

# DFT Modelling of Cu Segregation in Al-Cu Alloys Covered by an Ultrathin Oxide Film and Possible Links with Passivity 

Pauline Cornette *, Dominique Costa * and Philippe Marcus<br>Institut de Recherche de Chimie Paris, CNRS-Chimie ParisTech (PSL) Research University, (UMR 8247), Equipe de Physico-Chimie des Surfaces, 11 rue Pierre et Marie Curie, 75005 Paris, France; philippe.marcus@chimie-paristech.fr<br>* Correspondence: pauline.cornette@chimie-paristech.fr (P.C.); dominique.costa@chimie-paristech.fr (D.C.); Tel.: +33-1-4427-2525 (D.C.)

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#### Abstract

We modelled with Density Functional Theory (DFT) an Al-Cu alloy covered with a passive film, with several Cu concentrations (from the limit of the isolated atom to the monolayer) at the interface with the oxide, as well as Guinier-Preston 1 (GP1) zones. At low (respectively high) concentration, Cu segregates in the first (respectively second) metal layer underneath the passive film. The Cu monolayer is the most stable configuration ( $-0.37 \mathrm{eV} / \mathrm{Cu}$ atom). GP1 zones were modelled, with a three-copper atom cluster in the alloy. The GP1 zone is slightly favoured with respect to the Cu monolayer under the oxide film. A low (respectively high) Cu concentration induces an electronic workfunction increase (respectively decrease) by 0.3 eV (respectively -0.4 to -0.6 eV ) as compared to pure Al. In contrast, without oxide, Cu segregation at the Al surface induces no workfunction change at low concentration and an increase of 0.3 eV of the workfunction at high concentration. Thus, the presence of oxide modifies the expected tendency of workfunction increase by adding a more noble metal. For the studied models, no spontaneous electron transfer occurs to the $\mathrm{O}_{2}$ molecule.


Keywords: DFT; aluminium; Al-Cu alloy; corrosion; passive film; electronic workfunction; dioxygen reduction reaction

## 1. Introduction

Al alloys are widely used in aeronautics and space. To obtain good mechanical properties, alloying elements are used. Alloys of the 2000 series contain copper. On $\mathrm{Al} / \mathrm{Cu}$ alloys, the passive film is mainly composed of Al oxide/hydroxide [1,2]. Metal Cu enrichment underneath the passive film is a common situation due to the preferential oxidation of Al in $\mathrm{Al}-\mathrm{rich} / \mathrm{Cu}$ alloy [3-7]. This Cu enrichment may alter the corrosion resistance properties of the passive film.

Since some years, theoretical studies based on first principles calculations have been developed to better understand corrosion and corrosion protection [6,8-13]. However, very few works exist on AlCu alloys. Hoshino et al. [14] showed that because of the strong hybridization of Aluminium $s p$ orbitals and metal d orbitals of transition atom in Al-M type alloys (where $M$ is the transition metal), the stability of the bulk alloy depends on the medium range interactions of $M$ atoms. Benali et al. [15] also investigate theoretically the $\mathrm{Al}-\mathrm{Cu}$ interactions in bulk phase at low Cu concentrations and found weak negative values of the mixing enthalpies, indicating a low tendency to form a solid solution at $T=0 \mathrm{~K}$. Models of copper segregation within a given layer of (111) aluminium surface were proposed. The layer formation energy has a strong dependence on its composition and its position with respect to the surface. Thus, at low copper concentration (less than $50 \%$ per layer), the system is more stable when the doped layer is buried one layer under the surface, whereas for more than $50 \%$ of copper
in the layer, the doped layer is more stable when buried two layers under the surface. Furthermore, at high copper concentration in the layer, the Cu atoms have a strong tendency to clusterize, in good agreement with the Al-Cu phase diagram.

Some DFT theoretical studies have dealt with microstructure alloy phase in surface including metastable precipitates formed during cooling of the alloy, as Guinier-Preston (GP) zones [16,17]. A multiscale approach [18] was applied to model $\mathrm{Al}_{2} \mathrm{Cu}-\theta$ phase, and was validated by the comparison with the morphology and microstructural experimental data. It was followed by several ab initio studies of Wolverton et al. [19-23] and Zhou et al. [24]. Wolverton et al. [20] and Wang et al. [25] showed that copper monolayers were more stable than bilayers. They also found that the formation energies decrease in absolute value with respect to copper concentration increasing for both bilayer or monolayer. Other studies have analysed the atomic structure and the formation enthalpy of mixed Al-Cu layer [26-28]. Benali et al. [15] found that GP1 (one monolayer of Cu atoms on a $\{100\}$ lattice plane) and GP2 (multilayers of Al and Cu atoms) zones segregation one and two layers under the surface is favoured, GP1 being more stable than GP2.

None of the presented works have considered an alloy surface covered with oxide. However, it is important to understand the role of the presence of the oxide film on the thermodynamics of Cu segregation, and clusterization at the alloy/passive film interface. Several models of oxidized Al are found in the literature: Poberznik and Kokalj [13] explained why the O monolayer on Al has attractive lateral interactions which allows the oxide growing. Lantony et al. [29] studied the first steps of O adsorption on Al , and the formation of a $\gamma$-like ultrathin film. Costa et al. [6] modelled an hydroxylated $\gamma$-(111) $\mathrm{Al}_{2} \mathrm{O}_{3}$ film on $\mathrm{Al}(111)$. Baran et al. [30] studied $\gamma-\mathrm{Al}_{2} \mathrm{O}_{3}$ films on Al and found that the electronic properties of the film depend on the oxide thickness.

In the present work, we present a study of Cu location and concentration in the alloy covered with a passive film composed of hydroxylated $\mathrm{Al}_{2} \mathrm{O}_{3}$. The energetics of Cu segregation, and monolayer formation underneath the passive film is calculated. In addition, structural phases as GP zones are considered. The electronic analysis of each system is performed in order to understand the potential influence of the alloy composition underneath the passive film on the passivity. Mainly, the electronic workfunction is taken as an indicator of the cathodic corrosion resistance. Indeed, as stated by Huang et al. [31], this parameter is a measure of the difficulty for changing the electronic state of the solid, which is related to the corrosion behavior of materials. A higher work function corresponds to a more stable electron state and thus a higher resistance to corrosion reactions. Huang et al. [31] also established the link between the electron workfunction and macroscopic properties, as interfacial bond strength and mechanical properties.

## 2. Methods

### 2.1. Calculations

All calculations were performed using the periodic density functional theory (DFT) method based on the generalized gradient approximation (GGA) [32], employing the Perdew, Burke and Ernzerhof (PBE) [33] exchange-correlation functional as implemented in the plane-wave program Vienna ab initio simulation package (VASP) [34].The projector-augmented wave (PAW) potentials [35,36] were used for the core electron representation with a PAW core radius of $1.52 \AA$ for oxygen.

For the bulk materials, the simulation supercells contained 4 atoms for Al and Cu , and 120 atoms for $\gamma-\mathrm{Al}_{2} \mathrm{O}_{3}(111)$. A converged K -points mesh of $(6 \times 6 \times 6)$ was used for each bulk $\mathrm{Al}, \mathrm{Cu}$ and $(4 \times 1 \times 4)$ for $\mathrm{Al}_{2} \mathrm{O}_{3}$. Within this approach, the bulk lattice constants are $\mathrm{a}=4.05 \AA$ for $\mathrm{Al}, \mathrm{a}=3.63 \AA$ for Cu , and $\mathrm{a}=9.78 \AA, \mathrm{~b}=8.32 \AA$ and $\mathrm{c}=13.56 \AA\left((111) \gamma-\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ in good agreement with experimental values and previous studies $[6,15]$. The unit cell of the supported oxide film model for segregation study has dimensions of $\left(8.58 \times 9.90 \times 58 \AA^{3}\right)$ and a surface of $0.85 \mathrm{~nm}^{2}$. For GP1 zone, the dimensions of the unit cell are $\left(8.58 \times 19.81 \times 58 \AA^{3}\right)$ with a corresponding surface area of $1.7 \mathrm{~nm}^{2}$.

For each calculation, the quality of the basis set is determined by a single parameter, the energy cutoff ( $E_{\text {cut }}$ ). In this work, we used $E_{\text {cut }}=520 \mathrm{eV}$ and a smearing $\sigma=0.01 \mathrm{eV}$ was applied. A dipolar correction was applied along the $z$ axis. The integration in reciprocal space was performed with a Monkhorst-Pack [37] grid $(3 \times 3 \times 1)$. Dispersion forces were considered in the D2 Grimme approach [38]. Geometry optimizations performed all along this work were considered converged when the forces were inferior to $10^{-4} \mathrm{eV}$ per cell.

### 2.2. Models

The slab containing 8 metallic aluminium layers supporting a $9 \AA$ thick hydroxylated aluminium oxide film is shown in Figure 1. The oxide film has a stoichiometry of $\mathrm{Al}_{2} \mathrm{O}_{2.57}$ and exhibits a hydroxyl density of $14.4 \mathrm{OH} / \mathrm{nm}^{2}[6,39]$. It is composed of $\gamma$-alumina (111). This face is polar, with alternance of oxygen planes and Al planes. The Al planes contain Al with either octaedric or tetrahedral coordination. We showed in our previous work that the oxide layer has an Al octaedric plane at the interface with the metal. This Al plane is named here the interfacial Al layer. It was shown in our previous work that the Al atoms of this plane have a metallic character.


Figure 1. Slab model (a) Aluminium oxide supported by pure aluminium; (b) Aluminium oxide supported by an alloy with a full layer of copper in position $l=1$. Aluminium atoms are in grey, copper atoms in yellow, oxygen atoms in red and hydrogen atoms in white.

The first full metal layer under this Al interface layer is referred here with the index $l=1$, then $l=2$ represents the next underneath metal layer and $l=3$ the third metal layer. The layer $l=4$ is considered as a bulk layer.

To study the effect of alloying with $\mathrm{Cu}, 1,2,3,4,5,10$ and 12 copper atoms by layer or a copper concentration in the layer of $8,16,25,33,42,83$ and $100 \%$ respectively were considered. The Cu atoms were placed in the layer in the most homogeneous possible repartition and trying to avoid small clusters formation.

The models of the GP zones are shown in the corresponding Section 3.4.

### 2.3. Electronic and Charge Analysis

DOS curves were obtained using a grid of $3 \times 3 \times 1$ K-points. The electronic work function was obtained by analysing the LOCPOT file provided in VASP, and reporting the difference between the vacuum potential near the surface and the metal Fermi level. Our periodic cells exhibit two different surfaces, the pure metal surface at the bottom and the oxide film at the top. Thus, we could calculate directly the electronic workfunction difference with the pure metal, measuring the difference between the vacuum level near the surface of the oxide film and the vacuum level near the surface of the
metal. For the $\mathrm{Al}(111)$ surface, a calculated value of 4.1 eV was obtained, to be compared with the experimental value of 4.25 eV [40].

In preliminary tests, we increased the $\mathrm{Al}(111)$ slab thickness up to nineteen layers, as recommended in reference [15]. We concluded that a six layer slab is enough to reproduce the main electronic features of the metal. In the present study, a slab of eight metallic layers is used. We also checked the variation of the electronic workfunction with the vacuum height. All tests confirmed that the model used was sufficiently robust.

Atomic charges were obtained using the Bader charge analysis [41]. With this method the mean Al and O charges in bulk $\mathrm{Al}_{2} \mathrm{O}_{3}$ are +2.49 e and -1.66 e , respectively. This allowed us to calculate the charge transfer between the metal and the oxide film.

### 2.4. Energetics

The segregation energy corresponds to the driving force for surface segregation. It is defined as the variation of energy per atom of copper resulting from the exchange of one or more copper atoms in a volume of layer transferred to the surface. It is calculated by:

$$
\begin{equation*}
E_{\mathrm{seg}}\left(c_{l}\right)=\frac{E\left(c_{l}, x\right)-\lim _{l \rightarrow \infty} E\left(c_{l}, x\right)}{c_{l}} \tag{1}
\end{equation*}
$$

In this equation, $c_{l}$ is the concentration of copper in the layer $l$ and $E\left(c_{l}, x\right)$ the total energy of a semi-infinite alloy $\mathrm{Al}_{(1-x)} \mathrm{Cu}_{x}$ at a copper concentration $c_{l}$ in the layer. The energy of segregation tends to 0 when $l$ approaches infinity.

As explained in the reference [15], the segregation energy is a way to measure the copper tendency to form aggregates in a given layer. At the lowest concentration of copper, we substituted one atom by layer and buried this atom to the layer $l=4$. The equivalent concentration is therefore $c_{l}=1 / 12$ or $8 \%$ per layer or $0.93 \%$ by volume. At this concentration, the $\mathrm{Cu}-\mathrm{Cu}$ distance is $8.3 \AA$. Hoshino et al. [14,42] showed using theoretical calculations that the $\mathrm{Cu}-\mathrm{Cu}$ interaction in Al is negligible for Cu atoms distances are $>5.5 \AA$. To this respect, we can consider this concentration as the infinite dilution limit for copper. The segregation energy is the difference between the energy of substituting Nl Al atoms by Cu atoms in a layer, and the same in the bulk at infinite dilution and is written:

$$
\begin{equation*}
E_{\mathrm{seg}}\left(\frac{N l}{N}\right)=\frac{E_{\text {slab }}(N l)-E_{\text {slab }}(0)}{N l}+\mu_{\mathrm{Al}}\left(x_{\mathrm{Al}} \rightarrow 1\right)-\mu_{\mathrm{Cu}}\left(x_{\mathrm{Cu}} \rightarrow 0\right) \tag{2}
\end{equation*}
$$

Here, $N$ is the total number of atoms per layer, $N l$ the copper atom number per layer, $E_{\text {slab }}(N l)$ the slab total energy for $N$ copper atoms, $\mu_{\mathrm{Al}}$ is the chemical potential of aluminium in pure aluminium (here $\mu_{\mathrm{Al}}\left(x_{\mathrm{Al}} \rightarrow 1\right)$ is equivalent to the cohesive energy in Al ) and $\mu_{\mathrm{Cu}}\left(x_{\mathrm{Cu}} \rightarrow 0\right)$ the chemical potential of copper at infinite dilution in the alloy $\mathrm{Al}_{(1-x)} \mathrm{Cu}_{x}$. The chemical potential of Al and Cu are evaluated as in the reference [15]. Note that for an isolated Cu atom in the fourth layer, the energy of Cu dilution in Al is -0.147 eV , a value very near that of Cu dilution in bulk $\mathrm{Al}(-0.14 \mathrm{eV})$. This difference $(0.007 \mathrm{eV})$ is small enough to allow us to consider that Cu in the fourth layer is our internal reference for Cu in a dilute solid solution.

At increasing copper concentration, Cu aggregates form with interacting $\mathrm{Cu}(\mathrm{Cu}-\mathrm{Cu}$ distances $<5.5 \AA$ ). In this case, applying Equation (2) results into the sum of aggregation and segregation energies. Therefore, to get the segregation energy only, the solid reference energy taken is that of the aggregate formation in the bulk. In other words, we separate the aggregation energy from the segregation energy and consider the segregation of an already formed Cu aggregate from the bulk to the surface. The segregation energy is thus calculated by:

$$
\begin{equation*}
E_{\text {seg }}\left(\frac{N l}{N}\right)=\frac{E_{\text {slab }}(N l)-E_{\text {slab }}\left(N l_{b}\right)}{N} \tag{3}
\end{equation*}
$$

In this equation $N l$ is the number of copper atoms in the layer $l, N$ is the number of atoms per layer, $E_{\text {slab }}(N l)$ the slab energy and $E_{\text {slab }}\left(N l_{b}\right)$ the energy of the slab where copper is buried in the layer $l_{b}, l_{b}$ being large enough to converge to the value of the crystal. $l_{b}=4$ is considered as the representative configuration of the condensed phase volume.

In the present work, we used Equation (2) for studying the GP zone formation. Equation (3) at higher concentrations was used for the other situations, i.e., specifically Cu segregation. Obviously, at low Cu concentrations, Equations (2) and (3) are equivalent.

## 3. Results

We study Al based alloy with different Cu locations and concentrations in the first metallic layers under the oxide film, and GP zone, all models being covered with an aluminium oxide film. We substituted one or several aluminium atom(s) by copper in the first, second, third or fourth layer (taken as a reference of the bulk) of the (111) surface under the oxide film. We increased the copper concentration in each layer up to form a copper complete layer and varied its position from the surface to the bulk. Thus, by simply comparing the energy in the layer $l=1,2$ or 3 with respect to the energy of Cu in $l=4$, we could obtain the energy of Cu segregation from the bulk towards the third, second and first layer underneath the interface with the oxide (Equation (3)).

### 3.1. Energetics of Cu in Al(111) Covered by an Oxide Layer as a Function of Cu Concentration and Location

We first present the overall energetic results. As mentioned in the introduction, two trends were identified in literature on metallic Al [15]: The tendency for Cu aggregation, and that of Cu segregation towards the surface. Here, we study if these general trends observed on $\mathrm{Al}(111)$ are maintained when an oxide layer covers the surface. Figure 2 reports the energies of Cu segregation and / or aggregation in the first layers under the oxide film, calculated with Formula (2). The reference is one Cu atom in the $l=4$ layer, which is the internal reference for Cu at the infinite dilution limit in the Al bulk (Equation (2)). For comparison, we also reported data that we calculated for the oxide-free $\mathrm{Al}(111)$ surface.


Figure 2. Energy of Cu segregation and aggregation/ Cu atom (calculated with Formula (2)) in the $\mathrm{Al}(111)$ slab covered with the oxide film as a function of the location of Cu underneath the oxide-metal interface, in the layer $l . l=1$ is the first layer underneath the metal oxide interface, and $l=4$ is the fourth layer underneath the metal-oxide interface, as shown in Figure 1. Nl is the number of Cu atoms in the layer (see Formula (2)). Data obtained for the oxide-free $\mathrm{Al}(111)$ surface are also indicated. As stated in the text, the reference energy is the isolated Cu atom in the $l=4$ layer, which is representative of the Cu infinite dilution in bulk Al.

In the $l=4$ layer, we found that increasing the Cu concentration up to the Cu ML is energetically favourable. Without oxide, we found nearly the same energy of Cu ML formation ( -0.15 eV without oxide, -0.18 eV with oxide). The tendency of energy gain with increasing Cu concentration in a given layer is observed also for the $l=3$ and $l=2$ layers. We observe the stabilization of the system by Cu aggregation to form a full layer underneath the Al /oxide interface, the most stable configuration being a full Cu layer in $l=2$ position. But for $l=1$, at the interface with the oxide, albeit all Cu concentrations are energetically favored with respect to infinite dilution in the bulk, the full Cu layer is slightly less stable than partial Cu contents with $\mathrm{Nl}=10,4$ and 5 Cu atoms.

In the next paragraph we focus on the Cu segregation energy.

### 3.2. Copper Segregation at the Interface with the Passive Film

### 3.2.1. Energy of Segregation

Figure 3 shows the segregation energy relative to the layer position for different Cu concentrations. Cu segregation from $l=4$ to the first metallic plane $(l=1)$, just under the oxide film, is always favourable. For concentrations higher than $8 \%$ per layer $(N l=1)$, segregation to $l=2$ is also favoured, whereas segregation of a single Cu atom from $l=3$ to $l=2$ is unfavorable by 0.05 eV . Figure $3 \mathrm{~b}, \mathrm{c}$ show that the energy of segregation of Cu from the bulk to the $l=2$ plane decreases with increasing concentration, whereas the reverse is observed in $l=1$ plane. Comparing energies in $l=2$ and $l=1$, segregation from $l=2$ to $l=1$ is favoured for $N l=1,2,3,4$ and 5 Cu atoms in the plane, athermic for $N l=10 \mathrm{Cu}$ atoms and endothermic for a full Cu layer. Copper location $l=3$ is still slightly different from bulk.


Figure 3. Cont.


Figure 3. (a) Evolution of the segregation energy of copper to the $\mathrm{Al}(111) / \mathrm{Al}_{2} \mathrm{O}_{3}$ interface for different concentrations with respect to the doped layer position 1 in the slab. With respect to Figure 2, Figure 3a shows results calculated with Formula (3), thus, for each position and concentration, the energy reference is the same concentration of Cu in the $l=4$ position; (b) Segregation energy of copper in the layer $l=1$ as a function of the number of Cu atoms in the layer. $N l$, formula (3); (c) Segregation energy of copper in the layer $l=2$ with respect to the number of Cu atoms in the layer Nl Formula (3). Lines are guides to the eye.

It is interesting to note that the favoured positions for Cu move closer to the interface in presence of the oxide film. It was shown that without the oxide film, the favoured positions are in $l=2$ and $l=3$ plane [15]. The first aluminium layer of the oxide film might stabilize the copper atoms close to the interface. Indeed, this interface layer has metal properties and can be considered as a layer with vacancies ( 10 aluminium atoms against 12 in the metal plane); thus the nature of the first neighbours of the $l=1$ layer of the oxide covered alloy is not so different from the environment of the $l=2$ layer in the uncovered alloy. The most stable configuration thus consists in a Cu monolayer under one Al metal layer $(l=2)$.

We have highlighted a segregation phenomenon to the metal/oxide interface for all Cu concentrations, with a stabilisation in $l=1$ at low Cu concentration, and in $l=2$ for concentrations higher than $\mathrm{Nl}=1$, i.e., $8 \% \mathrm{Cu}$ per layer.

### 3.2.2. Charge Analysis and Electronic Workfunction

Cu Located in the $l=1$ Layer
Figure 4 shows the average electron charge per atom of the plane $l=1$ and of the Al atoms of the oxide interface, as a function of the copper concentration in the first metallic layer $l=1$. The amount of charge evolves monotonously with the Cu concentration: The more substitution of aluminium by copper, the more negative charge is transferred to the layer $l=1$. For a full Cu layer at $l=1$, a charge transfer of $0.87 \mathrm{e} / \mathrm{Cu}$ occurs from the oxide layer towards the Cu layer. This charge transfer originates from the oxidation of the Al interface layer from $\mathrm{Al}^{+1.6}$ to $\mathrm{Al}^{2+}$ (Figure 4), which nearly recover the charge of Al ions in $\mathrm{Al}_{2} \mathrm{O}_{3}$ (for $\mathrm{Al}^{2.5+}$ in bulk $\mathrm{Al}_{2} \mathrm{O}_{3}$ ). The other layers of the oxide film are not impacted. The charge transfer from the interface layer to $l=1$, induces the formation of a net dipole; an electric field attractive for the electrons originating from the metal is created between the interface aluminium positively charged and the negative copper of the metallic plane. This field induces a workfunction decrease (see Figure 5).


Figure 4. Evolution of the average electron charge per atom in the interfacial Al layer (orange, right $y$ axis) and the layer $l=1$ (blue, left $y$ axis) depending on the copper fraction in the metallic layer $l=1$.


Figure 5. Workfunction (eV) of the alloys (a) for a complete monolayer of copper; (b) for $N l=1 \mathrm{Cu}$ atom in the layer, a concentration of $8 \% \mathrm{Cu}$ in the layer, infinite dilution limit, as a function of the position of the doped layer. Position $i$ corresponds to the layer $l=i(i=1$ to 4$)$. The position " $\mathrm{Al}^{\prime}$ corresponds to pure aluminum.

We mention for comparison that in the absence of oxide, the workfunction of $\mathrm{Al}(111)$ (calculated as 3.98 in the present work) is not modified by the presence of Cu at low concentration at the surface, and is increased by 0.3 eV when a full Cu monolayer is at $l=1$. Indeed, Cu being more noble than Al , has a workfunction of 4.6 eV higher than that of $\mathrm{Al}(4.2 \mathrm{eV})$, an increase in electronic workfunction is expected when Cu is at the Al surface.

We thus observe a drastic change in the electronic properties of the Cu-doped $\mathrm{Al}(111)$ surface in the presence of an oxide layer, the charge transfer from metal/oxide interfacial Al to Cu inducing a lowering of the electronic workfunction.

Full Cu Layer at Depths $l=2,3,4$
When a full Cu layer is in the position $l=2$, a charge transfer occurs between the Cu plane and the $l=1$ layer of Al metal with a value of 0.34 e /at charge (not shown). The charge transfer to the Al ions of the oxide at the interface with the metal is $-0.05 \mathrm{e} / \mathrm{at}$, thus the oxide is not affected by the presence of the Cu layer. The workfunction (Figure 5a) is lower and the system is more stabilized. Again, the reserve is observed on the $\mathrm{Al}(111)$ surface without oxide, for which we calculate a workfunction increase of 0.18 eV with respect to pure $\mathrm{Al}(111)$ for a full Cu layer at $l=2$.

When the full Cu layer is in position $l=3$ and $l=4$, we observe a charge transfer to the above neighbour plane, but no charge transfer to the interface Al , and in consequence, no significative modification of the workfunction with respect to pure Al (all calculated workfunctions are around 4.6 eV ) (Figure 5a).The same is found without oxide.

Cu at Low Concentration
At very low Cu concentration (i.e., $\mathrm{Nl}=1,8 \%$ per layer or $1 \%$ per slab concentration), the charge transfer between Cu and the oxide, 0.02 e /at when the Cu is in $l=1$ (Figure 4 ) and negligible when the Cu is at $l=2$ and $l=3$. This suggests that covalent bonds are formed between Cu and Al in the metal, see also Section 3.2.3.

Figure 5 b shows that the workfunction is higher relative to pure aluminium (covered with oxide) when the Cu atom is at the interface or sub-interface, in the $l=1, l=2$ or $l=3$ layer. We observe that the more stable the position of the dispersed Cu in the metal layer, the higher the workfunction, the ranking of stability and of workfunctions being $l=1(+0.3 \mathrm{eV})>l=3(+0.2 \mathrm{eV})>l=2(+0.1 \mathrm{eV})$. The formation of $\mathrm{Cu}-\mathrm{Al}$ bonds in the metal may explain this trend, as it is known that the increase of bond strength induces an increase in the workfunction [31]. The workfunction of pure Al covered by the oxide layer $(4.60 \mathrm{eV})$ is nearly recovered when the Cu atom is in $l=4(4.55 \mathrm{eV})$.

These results contrast with those obtained in the absence of oxide, for which Cu at low concentration has no effect on the $\mathrm{Al}(111)$ workfunction, whatever the Cu location at and underneath the surface.

### 3.3. Electronic Density of States Analysis

To better understand the effects of Cu on the electronic workfunction, the DOS analysis was performedin two extreme cases, $N l=1$, one copper atom and $N l=12$, one Cu monolayer in layer $l=1$ (see Figure 6 which shows a zoom on the valence band edges). The valence band edge of the oxide on Al with a single copper atom is slightly lower than that for the oxide on pure aluminium. As the charge transfer from Cu to the oxide is negligible, we attribute the VB stabilisation in the case of $\mathrm{Nl}=1$ to the formation of $\mathrm{Al}-\mathrm{Cu}$ bonds at the interface, that stabilize the levels of the interfacial Al atoms and in consequence the levels of the oxide at the interface.

We also observe that the presence of a full Cu layer at $l=1$ induces a shift in the VB of the oxide towards higher energies. This trend is in agreement with the formation of the interfacial dipole that induces a workfunction decrease.

The energy gap (see Figure 6 and Table 2) varies as the workfunction, with values of 4.37 eV for the monolayer copper, 4.48 eV for pure aluminium (covered with oxide) and 4.53 eV for Al (covered with oxide) with a single copper atom.


Figure 6. Comparison of the valence band edges of the inner layer of the supported oxide on pure $\mathrm{Al}, \mathrm{Al}$ with a single copper atom and Al with a copper monolayer in $l=1$ (a.u.: Arbitrary units). The reference energy is set to the vacuum level.

To summarize, (see Table 1) the present calculations suggest that the electronic levels inside the oxide depend on the presence and concentration of Cu at the near interface region of the Al metal: Segregation of Cu at low (respectively high) concentration under the passive film induces an increase (respectively decrease) of the electronic workfunction and of the electronic gap. Finally, the ability of the surface to transfer an electron to $\mathrm{O}_{2}$ was studied following the same procedure as in our previous works [6,39]. We found that the workfunction decrease calculated here is not high enough to induce an electron transfer towards $\mathrm{O}_{2}$.

In the absence of oxide, the segregation of the more noble, Cu metal, at high concentration at the $\mathrm{Al}(111)$ surface, induces an increase of the workfunction; we showed here that the presence of the oxide inverts this trend, as a charge transfer from the first metallic layers to the oxide induces a workfunction decrease.

Table 1. Summary of the calculated properties of the different models of passive film on Al and AlCu alloy considered in this work: Pure aluminium, a single copper at the oxide/metal interface, a copper monolayer in $l=1$, a copper monolayer in $l=2$.

| Composition of the Metal <br> Layers Under the Oxide Film | OxideBand <br> Gap (eV) | Valence Band <br> Level/Vacuum (eV) | Workfunction <br> 申e (eV) |
| :---: | :---: | :---: | :---: |
| Pure Al | 4.48 | -6.00 | 4.60 |
| $N l=1 \mathrm{Cu}$ | 4.53 | -6.09 | 4.91 |
| $N l=12 \mathrm{Cu}, l=1$ | 4.37 | -5.84 | 4.25 |
| $N l=12 \mathrm{Cu}, l=2$ | $4.78^{*}$ | $-6.44^{*}$ | $4.00^{*}$ |

* Data not shown in the Figures.


### 3.4. Copper Segregation in GP Zones

Experimental and theoretical results have shown that the GP1 zones are more stable than the GP2 [15]. We therefore focus on the GP1 zones only. We start from the idea developed by Benali [15] indicating an increased stability of the system by a multilayer segregation instead of a monolayer segregation. We thus model the GP1 zones with a cluster of 3 copper atoms in the (100) plane of the metallic slab of aluminium (111) covered with the oxide film. In GP1 zones, clusters with 3 copper atoms in the (100) plane are separated by 7 aluminium (100) planes. As seen in the previous section, two localizations ( $l=1$ and $l=2$ ) of copper are favoured. We consider two configurations or cluster orientations: In the first configuration, two copper atoms are in the plane $l=1$ and the third atom in the plane $l=2$, and in configuration 2 one copper atom is in the plane $l=1$ and the other two in the plane $l=2$. Configurations 2 and 1 are thus symmetrical configurations. We also investigate two positions: Position 1, or interface position, when the nearest copper to the interface is in $l=1$ position and position 2, or sub-interface position, when the nearest copper to the interface copper is in $l=2$ (see Figure 7).


Figure 7. Models of GP1 zone considered. (a) Configuration 1 and position 1; (b) configuration 2 and position 1; (c) configuration 1 and position 2; (d) configuration 2 and position 2.

Table 2 shows the results obtained for the copper segregation energies (in eV per atom) of the GP1 zones calculated from the Equation (2) as a function of their in-depth positions relative to the interface and for the different configurations considered. The interface position (1) is 40 meV more stable than the sub-interface position (2) for configuration 1 and 20 meV for configuration 2. In addition, configuration 1 is also always more stable than configuration 2 , by $40 \mathrm{meV} /$ at for position 1 and by about $30 \mathrm{meV} /$ at for position 2 . We have a system stabilization by a bilayer segregation in interface and sub-interface. The most favourable position is the position 1 (interface position) and the configuration 1 (two copper atoms in the upper position), as shown in Figure 7a. So, the most stable position of the copper doped layers is in the interface under the oxide film, with segregation energy of $-160 \mathrm{meV} /$ at (calculated for the limit of the isolated atom in the bulk). By comparison, we calculated bulk clusterisation energy for both configurations and found $-60 \mathrm{mV} / \mathrm{at}$. The three copper atoms energy in a monolayer under the oxide film is $-140 \mathrm{meV} /$ at while the most stable multilayer is $-160 \mathrm{meV} / \mathrm{at}$. Therefore, the bilayer formation is slightly favoured over the monolayer one. These results confirm the tendency to formation and segregation of GP1 just below the metal/oxide interface.

Table 2 also reports the segregation energies in absence of oxide layer. It appears that position 2 with the highest copper content in the layer underneath the surface $(l=2)$ is the most stable position in absence of oxide, whereas the position 1 , with the highest Cu in the interface layer ( $l=1$ ), is the most stable in presence of oxide. Furthermore, whereas for position 2, configuration 1 and 2 are isoenergetic in absence of oxide, the configuration 1, position1 is clearly the most favored configuration under the oxide.

It is interesting to compare the energy of three Cu atoms coplanar in $l=1$, under the oxide film to that of the GP1 formation. The energy associated to three copper atoms under the oxide film is $-140 \mathrm{meV} /$ at while for the GP1 it is $-160 \mathrm{meV} /$ at. These results show a tendency to formation and segregation of GP1 in configuration 1 and position1 just below the metal/oxide interface. This suggests that clusterization in the bilayer is stabilized as compared to the monolayer formation.

Table 2. Segregation energy (in $\mathrm{eV} / \mathrm{at}$ ) for the formation of copper aggregates in an aluminum slab covered by an oxide film according to the position and configuration of the doped layers. See Figure 7 for the illustration of the different configurations.

| Configuration | Position 1 | Position 1 in <br> Absence of Oxide | Position 2 | Position 2 in <br> Absence of Oxide | Bulk Position |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Configuration 1 | -0.16 | -0.08 | -0.12 | -0.13 | -0.06 |
| Configuration 2 | -0.11 | -0.08 | -0.09 | -0.12 | -0.06 |

## 4. Discussion and Conclusions

In this work, $\mathrm{Al}-\mathrm{Cu}$ alloys covered by an ultrathin, hydroxylated $\mathrm{Al}_{2} \mathrm{O}_{3}$ film have been modelled. We investigated different distributions of Cu in Al : Pure $\mathrm{Al}, \mathrm{Cu}$ segregated at the oxide-metal interface at different concentrations, and GP zones. In the model, aluminium atoms are substituted by copper atoms in the metallic layers underneath the oxide film.

Copper segregation is favoured in the first (respectively second) layer underneath the oxide film at low (respectively high) concentration. The presence of the oxide reinforces the tendency to Cu segregation just underneath the Al surface (interface with oxide) as evidenced for oxide-free Al [15].

The study of the electronic properties revealed two different regimes:
Copper at low concentration $(N l=1)$ at the metal/oxide interface induces an increase in the workfunction as compared to pure $\mathrm{Al} / \mathrm{Al}_{2} \mathrm{O}_{3}$, whereas no significant modification of the workfunction is observed when Cu at low concentration ( $<8 \%$ ) segregates at the Al surface.

At high copper concentration, for a Cu ML at the metal/oxide interface or sub-interface, the oxide electronic levels are destabilised by a charge transfer from the metal (copper atoms) to the oxide, inducing a decrease of the electronic workfunction. These results are opposite to that obtained without the oxide film where the workfunction increases when the copper monolayer is at the Al surface or sub-surface.

These results can be compared to those obtained by Huang et al. [31], who found that Ni-Cu alloys have a workfunction increasing with the Ni content (the more noble metal). In acidic solution, no oxide layer is formed on the alloy surface, the resistance to corrosion increases with the Ni content, and this was attributed to the increase of workfunction. However, in neutral solution, the alloys are covered with an oxide film, and the corrosion resistance increased with the Cu content in the alloy. We are now able to explain that the presence of an oxide film might inverse the tendency of workfunction increasing with the increase in the noble element.

The important decrease of the workfunction of $0.4-0.6 \mathrm{eV}$ observed at full Cu layer suggests that the system is less resistant to electron transfer.

The study of the GP zones showed that multilayers are slightly more stable than the monolayer.
Further work on $\mathrm{Al}_{2} \mathrm{Cu}$ covered with $\mathrm{Al}_{2} \mathrm{O}_{3}$ are in progress to complete the present study in taking in consideration intermetallic phases. Future works will also include the presence of Cu in the oxide.

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