



Article

# Second-Harmonic Generation of Blue Light in GaN Waveguides

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Featured Application: Nonlinear optical conversion of visible laser diode sources into the blue and UV spectral region.

**Abstract:** Second-harmonic generation was studied in III-metal-polar GaN films grown on sapphire substrates by metalorganic chemical vapor deposition and formed into ridge waveguides. Broadband near-IR femtosecond pulses of an optical parametric amplifier system were injected by end-fire coupling and the nonlinear response was measured while tuning the central wavelength. A prominent peak was found at 450 nm for 1140 nm thick and 10  $\mu$ m wide GaN waveguides. The measured second-harmonic peak was in agreement with the modal-dispersion phase matching condition calculated using the dispersion of the extraordinary refractive indices of GaN obtained by prism coupling.

Keywords: GaN waveguides; second-harmonic generation; modal-dispersion phase matching

#### 1. Introduction

The rapidly expanding field of photonics has a great need for efficient and compact coherent light sources in the blue and ultraviolet (UV) regions. Short wavelengths allow for precise focusing and generation of very fine patterns, while the high photon energy facilitates strong absorption in many materials, leading to efficient material processing [1,2]. Laser diode technology used for the generation of UV light involves a number of challenges including low carrier injection and high threshold pump power, a lack of transparent and UV-resistant optical materials, and increased sensitivity to defects and surface roughness. Surface roughness and other anomalies inside the crystal can lead to strong wavefront distortions and scattering losses, an effect encountered especially with short wavelengths like UV [1–4]. Studies have shown that AlGaN alloys offer unique properties and have great potential to overcome the disadvantages listed above. While there are some reports on the fabrication of AlGaN-based LEDs in deep UV [5–9], very limited information about direct-emitting AlGaN semiconductor lasers is available [10,11]. Recent studies have been conducted on AlGaN-based optically-pumped UV laser structures, but electrically-pumped lasers with emissions below 320 nm have not yet been demonstrated [11–13]. Challenges related to the fabrication of electrically pumped GaN-, Al-GaN- and AlN-based UV laser diodes mainly stem from; (1) the deep Si-donor and

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Mg-acceptor levels that hinder successful carrier injection; and (2) the high strain fields and dislocation densities that are due to large lattice mismatches between the substrate and active layers [14–16].

AlGaN alloys have unique linear and nonlinear optical characteristics that permit the utilization of this material for efficient nonlinear conversion into the blue and UV wavelength regions. The two most important properties are a wide transparency window and large nonlinear optical coefficients. Both GaN and AlN have a wide bandgap, corresponding to wavelengths shorter than the visible spectrum. The transparency window of GaN ranges from 13.6 μm to 365 nm, while AlN remains transparent down to 200 nm [2,17]. AlGaN belongs to the 6mm point group, which lacks a center of inversion, and thus has five nonzero nonlinear optical coefficients from which only the two independent components,  $d_{31}$  and  $d_{33}$ , need to be considered [2,18]. The experimental value of the largest second-order coefficient,  $d_{33}$ , ranges from 5.82 to 10.6 pmV<sup>-1</sup> [19]. Modal-dispersion phase matching or quasi-phase matching is required with AlGaN to exploit its nonlinearity since the birefringence is not sufficient to sustain an efficient second-harmonic generation (SHG), as was shown in our previous studies [20,21]. While SHG in GaN and AlGaN has been reported occasionally, only limited data are available for wavelengths below 500 nm. The limitations in this wavelength range are often related to low-quality materials or challenges in waveguide fabrication, which leads to significant scattering and losses. However, with the recent developments in metalorganic chemical vapor deposition growth (MOCVD) and the processing of GaN and AlGaN, new opportunities to investigate SHG in these wide bandgap materials have arisen.

For quasi-phase matching, a periodically modulated nonlinear structure is needed, which alternates the sign of the nonlinear coefficient in regular intervals and corrects for the relative phase mismatch between the fundamental and the frequency-doubled light without matching the phase velocities [22]. The polarity-controlled growth of +c and -c polarity regions of GaN can be achieved through adequate substrate preparation. The configuration in which the Ga-atoms bond, with three bonds toward the surface, is referred to as N-polar (or -c orientation), while the 180° rotated configuration is referred to as III-metal-polar (+c) [23].

In this work, we show the feasibility of III-metal polar GaN waveguides for SHG using modal-dispersion phase matching (MDPM), which takes advantage of the fact that the waveguide modes of different orders have different effective refractive index dispersion relations [24,25]. More specifically, we demonstrate the generation of light with  $\lambda$  = 450 nm in 1140 nm thick and 10  $\mu$ m wide GaN waveguides. Due to the dependence of the effective refractive index on the dimensions of the waveguide and the wavelength, the pump waveguide mode of order p at pump wavelength  $\lambda_p$  and the SHG waveguide mode of order q > p at  $\lambda_{\rm SHG} = \lambda_q/2$  can be phase matched. The demonstration of SHG in AlGaN waveguides in the blue spectral region is understood as a step to extend the wavelengths of coherent light sources into the ultraviolet C spectral region via SHG. The final goal is to efficiently generate coherent light down to 200 nm through quasi-phase matching using periodically polled AlN waveguides [26].

The effective refractive index of the waveguide mode at a particular wavelength depends on the refractive indices of the waveguide and the substrate, and on the dimensions of the waveguide [27,28]. To excite the largest nonlinear coefficient  $d_{33}$ , the polarization of in-coupled and out-coupled light is set to transverse magnetic (TM), and therefore the extraordinary refractive indices of the GaN and sapphire substrate must be taken into account. We used the dispersion of the extraordinary index for III-metal-polar GaN waveguides as obtained by a prism coupling study and described by the Sellmeier dispersion formula [21]:

$$n_{\rm e}^2 = 1 + \frac{A\lambda^2}{\lambda^2 - B^2} \tag{1}$$

where A = 4.3 and B = 195.4 nm. The extraordinary refractive index dispersion relationship for sapphire is given in the work of Malitson and Dodge [29]. In this study, an isotropic approximation [21,30] and a planar waveguide approximation [27] were used for the calculation of effective refractive indices due to weak birefringence and the large width-to-thickness ratio of the waveguides used.

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The second-harmonic power in a planar waveguide, where linear losses at pump and second harmonic generation (SHG) wavelengths are neglected, is expressed as [24]:

$$P_{2\omega} = \frac{32\omega^2 [d_{33}]^2 \varepsilon_{2\omega} n_{\text{eff},\omega}^2}{9\pi^2 W \varepsilon_0 c_0^3 \varepsilon_\omega^2 n_{\text{eff},2\omega}^3} L^2 P_\omega^2 \Gamma h(\Delta \beta)$$
(2)

where L is the interaction length, W is the waveguide thickness,  $P_{\omega}$  is the fundamental power at the waveguide front facet,  $n_{\text{eff},2\omega}$  and  $n_{\text{eff},\omega}$  are the effective extraordinary refractive indices of the waveguide modes at the fundamental and SHG frequencies, respectively. The function h ( $\Delta\beta$ ) is given by:

$$h(\Delta\beta) = \sin c^2 \left(\frac{\Delta\beta L}{2}\right) \tag{3}$$

This function represents a wave-vector mismatch term, where  $\Delta\beta$  describes the difference between the propagation constants of the pump and SH waves.

The overlap integral  $\Gamma$  [24]:

$$\Gamma_{p,q}(\lambda) = \frac{9\pi^2}{16W^2} \left[ \int \psi_{q,\lambda/2}(z) \psi_{p,\lambda}^2(z) dz \right]^2 \tag{4}$$

is a dimensionless quantity normalized to 1 when the two interacting modes  $\psi_{p,\lambda(z)}$  and  $\psi_{q,\lambda/2(z)}$ —that are the transverse field distributions of the optical field amplitudes associated with the waveguide modes p and q at the fundamental and SH frequencies [24,31]—perfectly overlap in the transverse direction. It limits the number of waveguide modes that lead to efficient nonlinear conversion.

### 2. Materials and Methods

In this study, III-metal-polar GaN waveguides were used. A 1200 nm thick Ga polar GaN was grown on a low-temperature AlN buffer layer on sapphire using an MOCVD reactor. The growth temperature was 1040 °C with Ga ( $C_2H_5$ )<sub>3</sub> (triethylgallium) and NH<sub>3</sub> as the source gases. Details on the growth can be found elsewhere [31–35]. To transform planar waveguides into rectangular waveguides of selected widths, a standard photolithography process was used with the resulting waveguide widths ranging from 3–50 µm [35,36]. The final measurements were performed on samples with parallel waveguides of 10 µm width and 10 µm spacing.

Figure 1a presents a cross-sectional scanning electron microscopy (SEM) image of a waveguide facet that was used to couple-in the light into the waveguides. A cross-sectional trench was prepared using the following procedure: First, a 1 µm thick platinum protective layer was deposited using an ion-beam induced deposition with a 0.43 nA beam current; next, a cross-section using a 6.5 nA ion beam was milled. This was followed by a 80 pA milling of the exposed cross-section to obtain a polished surface. The thickness of the GaN waveguides was determined by the SEM analysis of the cross-sectional samples to be around 1150 nm. Although the waveguides exhibited very smooth surfaces, the analysis of the image taken by a CCD camera mounted above the sample revealed that most of the light scattering took place at the side surfaces of the waveguides. To confirm this, SEM images from the side facets were also recorded. It was found that the roughness of the sides was especially high for the waveguides with a stripe width below 5 µm. This is highlighted by a direct comparison of waveguides with a side roughness of 3 µm and 20 µm wide, as presented in Figure 1b. In addition, sidewall roughness is relatively more important in narrower waveguides, therefore, most SHG measurements were performed on GaN waveguides of 10 µm width and 1 mm length. In order to produce waveguides of an appropriate length, straight lines perpendicular to the waveguide direction were scribed by a UV laser on the back of the sapphire wafer. The wafer was then cleaved along the scribed lines.

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The fabricated waveguides were used to probe SHG in GaN waveguides at room temperature. Figure 2 presents schematics of the experimental setup used to investigate the nonlinear response in GaN waveguides. A Ti:sapphire laser was used as the excitation source. Typical excitation wavelengths were in the range of 850–950 nm, which led to a second-harmonic response in the blue. Femtosecond pulses were injected into the waveguide by the end-fire coupling technique. The SHG signal generated in the waveguide was separated from the pump wave and analyzed with a spectrograph and a photon counting camera.

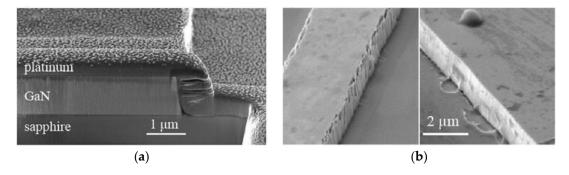
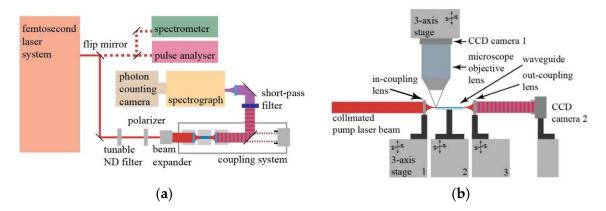


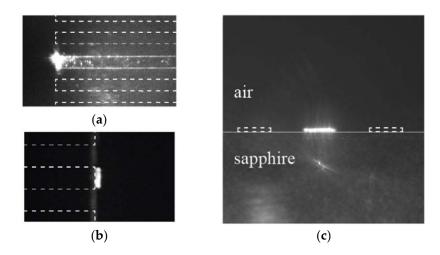
Figure 1. (a) Cross-sectional scanning electron microscopy (SEM) image of a III-polar GaN waveguide. The image is taken at an oblique angle of  $52^{\circ}$ . A platinum layer has been deposited prior to making the cross-section in order to protect the uppermost part of the waveguide during the focused ion beam (FIB) etching. The measured thickness of the GaN waveguides used in the experiment is around 1150 nm. (b) Comparison of the side roughness of GaN waveguides which are 3 μm (left) and 20 μm (right) wide. A higher sidewall roughness is observed for narrower waveguides. As a result, the GaN waveguides used for second-harmonic generation (SHG) were at least 10 μm wide.

The output of the femtosecond laser system was nearly identical to that of a transform-limited fundamental pulse with a tunable central wavelength. The pulse duration was 40 fs (full-width at half-maximum, FWHM), the repetition rate was 1 kHz, and the spectral width was 30 nm (FWHM). The pulse energy was wavelength dependent from 1 to 100  $\mu$ J and could be controlled by a tunable neutral density (ND) filter, which was used before the end-fire coupling system. The beam diameter was adapted with a beam expander to the size of the in-coupling lens for efficient focusing. The coupling lenses and sample holder were mounted on xyz translation stages enabling precise positioning of the focal point of the laser beam onto the front facet of the waveguide. The output beam was focused onto the front face of the waveguide using a lens with a 10 mm focal length. The size of the beam at the waveguide facet was approximately 10  $\mu$ m. This is equal to the waveguide width in order to dominantly excite the fundamental mode in the y-direction. The efficiency of coupling was constantly monitored with two CCD detectors as shown in Figures 2b and 3a–c. The out-coupled light was collimated and filtered, and the SHG signal was directed to the detection system. The camera was operated using the gated regime and was synchronized to the femtosecond system repetition rate.

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**Figure 2.** (a) Top view of the experimental setup with the end-fire coupling system. Femtosecond pulses of vertical polarization are adequately attenuated with a neutral density (ND) filter and coupled into GaN waveguides with their polar axis vertical. The out-coupled signal is vertically polarized and is filtered with a shortpass filter and the SHG signal is analyzed with the spectrograph connected to the photon counting camera. (b) Side-view of the end-fire coupling system. Coupling lenses and a sample holder are mounted on *xyz* translation stages, which enable precise positioning of the focal point of the laser beam onto the front facet of the waveguide.

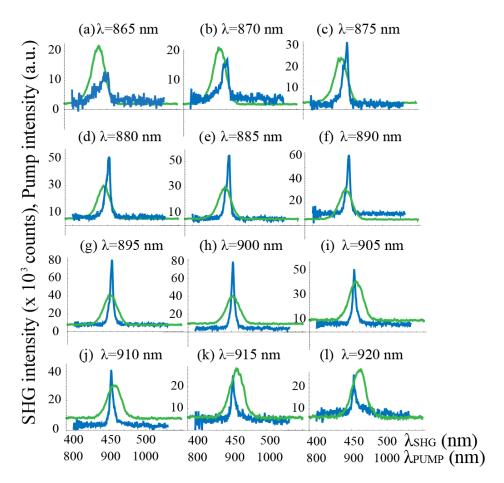


**Figure 3.** Light propagation observed by CCD camera 1, shown in Figure 2b, mounted above the sample: (a) At in-coupling and (b) out-coupling positions. (c) Out-coupling recorded by CCD camera 2, shown in Figure 2b. White dashed lines represent waveguide positions where they are not easily seen. Note that all waveguides have a stripe width of  $10 \mu m$ .

## 3. Results and Discussion

Figure 4 shows the second-harmonic response of GaN waveguides to excitation with different wavelengths ranging from 850 nm to 950 nm. The green curves show the spectral distribution of the excitation source and the blue curves show the corresponding SH response. A clear, relatively strong peak of the SHG signal was observed at a constant wavelength of 450 nm while scanning the pump wavelength spectrum. Maximum SHG response (blue curve) can be seen in Figure 4g,h with the central pump wavelengths of 895 nm and 900 nm. In order to explain the SHG peak at 450 nm the dispersions of the effective refractive indices for the pump and SHG waveguide modes were analyzed.

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**Figure 4.** SHG signal counts (blue) measured in 10 min from a 1 mm long GaN waveguide at different central wavelengths of the pump (green). Note the different wavelength scale for the pump and SHG.

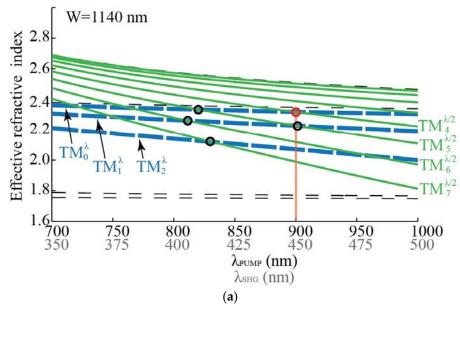
In Figure 5a the dispersion curves for a 1140 nm thick GaN waveguide on a sapphire substrate are shown. For the calculation, a planar waveguide approximation was used [27]. This was justified as the waveguides were 10  $\mu$ m wide. Extraordinary refractive indices for GaN in the measured pump- and SHG-wavelength ranges are given by Equation (1). As indicated by the circles in Figure 5, the MDPM condition is true for the interaction between the fundamental pump mode and the fourth SHG mode, and for the first pump mode and fifth SHG mode, both at a pump wavelength  $\lambda$  of approximately 900 nm:

$$TM_0^{\lambda} + TM_0^{\lambda} \rightarrow TM_4^{\lambda/2} \tag{5}$$

$$TM_1^{\lambda} + TM_1^{\lambda} \rightarrow TM_5^{\lambda/2} \tag{6}$$

where  $\lambda$  is the pump wavelength. Both possible waveguide interactions are schematically shown in Figure 5b.

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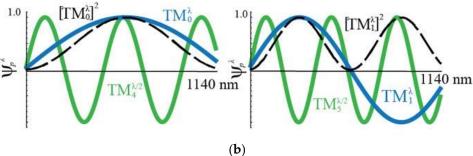


Figure 5. (a) Dispersions of the effective refractive indices for the pump (dashed blue lines) and SHG (green lines) waveguide modes in a GaN waveguide with a thickness of 1140 nm. Dashed black lines represent the dispersions of the extraordinary refractive indices of bulk GaN, given in Equation (4) [20] and sapphire [26]. The red circle indicates the modal-dispersion phase matching (MDPM) interaction, which is responsible for the measured SHG signal. (b) Overlapping of the electric field distributions,  $\psi_p^{\lambda}$ , for two possible waveguide interactions responsible for the measured SHG signal. The waveguide modes at the pump wave are presented with blue lines, modes at the SHG wavelength with green lines, while squares of pump modes  $\left[\psi_p^{\lambda}\right]^2$  are presented with black dotted lines.

The fulfillment of the phase matching is only one of the necessary conditions for efficient SHG generation. In waveguide interactions, the overlap integral  $\Gamma$ , detailed in Equation (4), must also be considered. Although phase-matching conditions for two combinations of waveguide modes at the pump wavelength of 900 nm are met, the overlap integrals reveal that the interaction from Equation (5) is dominant and thus responsible for the measured SHG peak. Taking only the overlap into account, the conversion efficiency for the MDPM interaction described by Equation (6) is 35 times lower than that described by Equation (5). Furthermore, it could not be measured separately in our waveguides. In Table 1 the overlap integrals are compared for other possible interactions indicated by black circles in Figure 5. The interaction:

$$TM_1^{\lambda} + TM_1^{\lambda} \to TM_6^{\lambda/2} \tag{7}$$

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shows the largest overlap. However, the excitation of the first pump mode was less efficient, therefore, this SH peak was not observed. A small additional peak in Figure 4a could be attributed to this interaction.

The total efficiency of SHG can be estimated as the following: Taking the large waveguide aspect ratio (1.1  $\mu$ m to 10  $\mu$ m), losses by reflection at the front surface, and coupling to the unwanted waveguide modes into account, approximately 4% of a 1 mW input beam is coupled into the pump mode for conversion. Inside the waveguide, propagation losses were also observed, mainly due to the scattering from the waveguide sidewalls as shown in Figure 3a. However, these were negligible in comparison with the coupling losses. By using Equation (2) it was estimated that nearly 100 nW of blue light was generated.

**Table 1.** Comparison of different values of overlap integrals  $\Gamma_{p,q}^{\lambda}$ , where  $\lambda$  is the pump wavelength. The calculations shown are for possible modal-dispersion phase matching (MDPM) interactions indicated in Figure 5a.

$TM_p^\lambda + TM_p^\lambda  o TM_q^{\lambda/2}$	$rac{\Gamma_{p,q}^{\lambda}}{\Gamma_{0,0}^{\lambda=900~ ext{nm}}}$
$p = 0, q = 4, \lambda = 900 \text{ nm}$	$6.34 \times 10^{-4}$
$p = 1, q = 5, \lambda = 900 \text{ nm}$	$1.81\times10^{-5}$
$p = 0, q = 5, \lambda = 815 \text{ nm}$	$1.44 \times 10^{-6}$
$p = 1$ , $q = 6$ , $\lambda = 810$ nm	$1.83 \times 10^{-3}$
$p = 2$ , $q = 7$ , $\lambda = 825$ nm	$9.10\times10^{-5}$

#### 4. Conclusions

In this study, we measured the nonlinear response of GaN waveguides grown on sapphire substrates through modal-dispersion phase matching. We compared experimental results to the calculations of the effective refractive index and the overlap of different combinations of waveguide modes. The relatively strong SHG peak obtained was in agreement with the theoretical predictions, therefore confirming the adequateness of the dispersion calculations and the accuracy of the measured refractive indices of GaN waveguides obtained by prism coupling in our previous study. This study can be seen as a first step towards integrated devices that emit coherent light in the blue and UV spectral regions based on second-harmonic generation in polarity controlled AlGaN waveguides.

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Conflicts of Interest: The authors declare no conflicts of interest.

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