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Triaxial Loading and Unloading Tests on Dry and Saturated Sandstone Specimens

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Featured Application: The specific application or a potential application of the work is related to deep mining and tunneling engineering.

Abstract: The brittle failure of hard rock due to the excavation unloading in deep rock engineering often causes serious problems in mining and tunneling engineering, and the failure process is always affected by groundwater. In order to investigate the effects of stress paths and water conditions on the mechanical properties and failure behavior of rocks, a series of triaxial compression tests were conducted on dry and saturated sandstones under various loading and unloading paths. It was found that when the sandstone rock samples are saturated by water, the cohesion, the internal friction angle and the Young's modulus will decrease but the Poisson's ratio will increase. The fracturing characteristics of the sandstone specimens are related to the initial confining pressure, the stress paths and the water conditions from both macroscopic and microscopic viewpoints. The failure of sandstone in unloading test is more severe than that under loading test, particularly for dry sandstone samples. In unloading test, the energy is mainly consumed for the circumferential deformation and converted into kinetic energy for the rock bursts. The sandstone is more prone to produce internal cracks under the effect of water, and the absorbed energy mainly contributes to the damage of rock. It indicates that the possibility of rockburst in saturated rock is lower than the samples in dry condition. It is important to mention that water injection in rock is an effective way to prevent rockburst in deep rock engineering.

Keywords: triaxial compression test; sandstone; rock mechanics; rock fracture; energy evolution

1. Introduction

The excavation of underground rock engineering is often affected by groundwater [1,2]. Under high geo-stress, high groundwater pressure is prone to cause engineering geological disasters, such as water inrush. It seriously affects the construction progress and personnel safety for underground rock engineering [3]. The excavation of underground engineering, in fact, is the triaxial loading and unloading processes of the surrounding rock masses. It is therefore important to carry out the triaxial loading and unloading tests with different water contents of the rocks in laboratory.

Considerable efforts have been devoted to the effects of water on rock failure. For the influence of water on the mechanical properties of rocks, it has been found that a small increase in the water content may significantly lower the strength and stiffness of the rocks [4–9]. The statistical and numerical analysis on 14 kinds of the rocks with different water contents were also carried out, and it

was found a negative exponential relationship between rock strength and moisture content [10]. Meanwhile, Li et al., [11] conducted the triaxial compression tests and found that the internal friction angle decreases while the cohesion increases when the meta-sedimentary rocks was saturated by water. Most of previous related studies were focused on the influence of water on the uniaxial or conventional triaxial strength of rocks [5-7,10]. However, few experimental and numerical studies are reported to discuss the effect of water content on the strength and deformability of the rocks under triaxial stress conditions [12–14]. In the practical engineering, the existence of groundwater not only affects the mechanical properties of rock, but also influences the damage degree and even the failure mode of the rock [15]. Zhou et al. [16] investigated the effects of water and joints on the properties of rock masses using the data from the Shirengou iron mine. Their numerical simulation results indicated that water is the critical factor for rock damage pattern. Several scholars also conducted experiments on deep rock and successfully showed a layered failure for saturated rock in tensile tests [17]. Spalling behaviors were studied in ture-triaxial unloading conditions and scanning electron microscope (SEM) observations revealed the distribution of microcracks in the fragments [18]. Besides, there are many studies related to rock uniaxial compression and tensile failure affected by water [19–22]. The deformation and failure of rock are energy-driven processes which include energy absorption, evolution, dissipation, and release [23–26]. Based on uniaxial and triaxial compression tests, Hua and You [27] studied the characteristics of rock energy evolution during unloading failure and concluded that the strain energy stored in rock material is sufficiently large to cause failure when it is released. Furthermore, water injection to reduce rockburst occurrences has also been discussed mainly on numerical simulation [28–30], and partially for experiments [2,31]. The numerical modeling showed that the peak stress can be reduced as water injection, which causes a significant reduction of internal energy stored within the rock, and the possibility of a rockburst occurrence may be reduced [28]. Moreover, the effects of water on rock energy evolution have also been studied [32–37], though it mainly concerns on uniaxial compression [34,35] and axial loading-unloading experiments [32,33,36,37]. Undoubtedly, the above study enriches our knowledge of the effect of water on rock failure and energy evolution. However, there are a few studies concern on the effect of water on rocks under triaxial tests, especially for the influence of unloading high confining pressure conditions, which represents a more realistic site environment.

Therefore, based on deep underground engineering such as mining and tunnel engineering under high geo-stress and water-rich conditions, this study is tried to investigate the combining effects of water content and high stress on the mechanical properties, failure and energy evolution of rocks in different stress paths. It is benefited the exploitation of deep resources and construction of deep rock engineering. Moreover, this study will be helpful to understand the effect of water on rock failure in high stress.

2. Materials and Methods

2.1. Specimen Preparation

Red sandstone samples which were obtained from a quarry in Yunnan Province, were used to test in the present study. A thin section analysis was carried out to examine the microstructure of the sandstone. It was identified as fine-grained sandstone by petrographic microscopy (Leica DM2700P, Leica Microsystems Inc., Wetzlar, German). The microstructure of the sandstone under plane polarization light (PPL) and cross polarization light (CPL) are illustrated in Figure 1. The mineral composition and grain size distribution of the sandstone specimen are listed in Table 1.

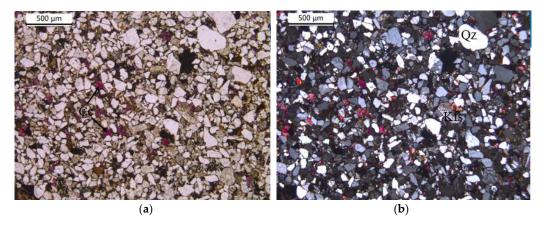


Figure 1. Polarized light micrographs of sandstone specimen: (**a**) plane polarization light (PPL); (**b**) cross polarization light (CPL). (Note: The letters Qz, Kfs and Cc represent quartz, potassium feldspar and calcite, respectively).

Rock Composition	Grain Size (mm)	Mineral Content (%)		
Quartz	0.03 ~ 0.2	77		
Potassium feldspar	$0.05 \sim 0.2$	10		
Calcite	$0.01 \sim 0.08$	7		
Sericite	$0.01 \sim 0.02$	4		
Others	$0.01 \sim 0.1$	2		

Table 1. Mineral composition and grain size distribution of sandstone specimen.

Both oven-dried and water-saturated specimens were prepared to study the influence of water on triaxial failure of the sandstone samples. In drying process, the sandstone specimens were placed in an oven at 105 °C for 24 h, and then they were removed to a desiccator and weighed after cooling to room temperature. In saturation process, the specimens were placed in water and allowed to absorb water for 48 h under atmospheric pressure, and then specimens were taken out and weighed after removing surface moisture of the rock. These specimens were considered as saturated samples in this study. The natural water content of specimen was about 2.5% and the saturated water content was about 3.3%. The diameter (*D*) of the cylindrical specimens was 50 mm and the specimen height (*H*) was 100 mm. The density and the P-wave velocity of each testing specimen are provided in Table 2.

Table 2. Test scheme and physical parameters of sandstone specimens.

Group	Specimen No.	Density (kg/m ³)	P-Wave Velocity (m/s)	Initial Confining Pressure (MPa)	Unloading Point (MPa)	Loading Rate	Unloading Rate (MPa/min)
	TC-D-0	2387.3	2951	0		0.1 mm/min	
	TC-D-10	2380.4	2979	10		0.1 mm/min	
TC-D	TC-D-20	2387.5	2916	20		0.1 mm/min	
	TC-D-30	2398.3	3063	30		0.1 mm/min	
	TC-D-40	2382.1	3077	40		0.1 mm/min	
	TC-S-0	2456.8	3381	0		0.1 mm/min	
	TC-S-10	2459.8	3363	10		0.1 mm/min	
TC-S	TC-S-20	2464.1	3362	20		0.1 mm/min	
	TC-S-30	2459.7	3393	30		0.1 mm/min	
	TC-S-40	2450.0	3392	40		0.1 mm/min	

TU-D	TU-D-10	2380.7	3299	10	$0.8\sigma_{(10)}$	0.1 mm/min-1.5 MPa/min	3
	TU-D-20	2391.3	3292	20	$0.8\sigma_{(20)}$	0.1 mm/min-1.5 MPa/min	3
	TU-D-30	2387.8	3315	30	$0.8\sigma_{(30)}$	0.1 mm/min-1.5 MPa/min	3
	TU-D-40	2391.3	3313	40	$0.8\sigma_{(40)}$	0.1 mm/min-1.5 MPa/min	3
TU-S	TU-S-10	2454.7	3396	10	$0.8\sigma_{(10)}$	0.1mm/min-1.5 MPa/min	3
	TU-S-20	2457.7	3347	20	$0.8\sigma_{(20)}$	0.1 mm/min-1.5 MPa/min	3
	TU-S-30	2457.8	3349	30	0.8 ₍₃₀₎	0.1 mm/min-1.5 MPa/min	3
	TU-S-40	2457.7	3399	40	$0.8\sigma_{(40)}$	0.1 mm/min-1.5 MPa/min	3

Table 2. Cont.

2.2. Test Scheme

The triaxial tests including conventional triaxial compression tests (abbreviate to loading test) and unloading confining pressure tests (abbreviate to unloading test), were conducted by a servo-controlled material testing machine (MTS 815) (MTS Systems Corporation, Minnesota, USA) at laboratory of Central South University. Both of axial and circumferential strains can be recorded by extensometers.

Each test includes two experimental groups of dry and saturated sandstones respectively. Thus, the specimens are divided into four groups of dry and saturated sandstones in different loading and unloading tests (see in Table 2). The initial confining pressures (σ_3^0) were set as 10, 20, 30, and 40 MPa, respectively. Meanwhile, the unloading point for the confining pressure in unloading tests was set as the axial stress reaching 80% of the corresponding triaxial compression strength (such as $0.8\sigma_{(10)}$ and so on). Then, the axial loading method was changed from displacement control (0.1 mm/min) to loading control (1.5 MPa/min) at unloading point. In general, four sets of specimens were prepared, i.e., TC-D, TC-S, TU-D, TU-S. Specimens of set TC-D and TC-S, with the dry and saturated state respectively, were used in the conventional triaxial compression test. Specimens of set TU-D and TU-S, with the dry and saturated state respectively, were used in the unloading confining pressure test. And the number of specimen set represents for the corresponding confining pressure. For example, as shown in Table 2, TU-D-10 represents the unloading confining pressure test of dry specimen under the confining pressure of 10 MPa.

The detailed test procedures of the triaxial unloading test are listed as follows:

Step 1: Apply hydrostatic pressure on the specimen to an initial confining pressure (σ_2^0).

Step 2: Keep $\sigma_{3'}^0$ and increase axial stress to 80% of the corresponding triaxial compression strength by a displacement control method at 0.1 mm/min.

Step 3: Reach the unloading point, change the axial stress loading method from displacement control to load control at the unloading point.

Step 4: Increase the axial stress at 1.5 MPa/min and also reduce the confining pressure simultaneously by load control method at a specified unloading rate (3.0 MPa/min) until the failure of the rock specimen.

3. Results

3.1. Mechanical Properties

Figure 2 shows the variation of the peak strength with the initial confining pressure of dry and saturated sandstone specimens. It can be seen that the peak strength of sandstone specimen increases as the initial confining pressure increases, but the increase rate slows down with the increase of the

initial confining pressure. The difference of the peak strength between dry and saturated sandstones grows with the increasing of initial confining pressure. It means that the effect of water on rock strength is more remarkable under high confining pressure.

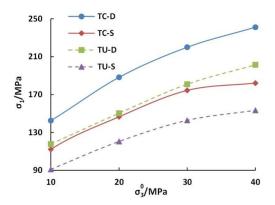


Figure 2. Peak strength of sandstone specimens.

Figure 3 illustrates the strength parameters of different groups of specimens under triaxial loading and unloading tests. The strength parameters of sandstone specimens are differed in different stress paths. The strength parameters of *C* (cohesion) and φ (internal friction angle) under loading conditions are higher than those of unloading tests with the same water condition. Meanwhile, both *C* and φ values of saturated sandstones are lower than those of dry sandstones, which indicate that water has a deep impact in decreasing strength parameters (*C* and φ) of sandstone samples. When the sandstone samples are saturated by water, their shear strength parameters are reduced, where changes in results of φ are more remarkable. The weakening of strength parameters further affects the ultimate bearing capacity of sandstone.

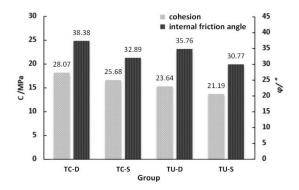


Figure 3. Strength parameters of sandstone specimens.

The values of the axial strain (ε_1 , ε'_1), circumferential strain (ε_3 , ε'_3), and volumetric strain (ε_v , ε'_v) at the unloading point (σ_3^0) and the critical failure point (σ_3^f) are listed in Table 3. It can be seen that the absolute value of volumetric strain for rock in unloading test is greater than that of rock samples in conventional triaxial compression test, particularly for saturated samples. It means that the characteristics of volume expansion of rock under unloading conditions are more pronounced than the rock samples in loading tests. In addition, the incremental rates of circumferential strain are several times larger than those of axial strain from unloading point to critical failure point. The rock failure occurs mainly for the circumferential expansion under unloading conditions. Furthermore, except for the initial confining pressure of 20 MPa, the confining pressures of saturated sandstones at failure point (σ_3^f) are higher than that for dry sandstones which indicate that saturated sandstones fail earlier than dry sandstones. This is due to the fact that the structures of rock samples are weaker when they are saturated by water as compared to structures of dry rock samples.

Group	Specimen		Unloa	ding Point		Critical Failure Point				
1	Number	$\sigma_3^0 \qquad \epsilon_1$		ϵ_3	ε_v	σ_3^f	$\epsilon_{1}^{'}$	$\epsilon_{3}^{'}$	$\epsilon_v^{'}$	
	TC-D-10	10	-	-	-	10	0.0110	-0.0084	-0.0058	
	TC-D-20	20	-	-	-	20	0.0136	-0.0085	-0.0034	
TC-D	TC-D-30	30	-	-	-	30	0.0156	-0.0118	-0.008	
	TC-D-40	40	-	-	-	40	0.0218	-0.0166	-0.0114	
	TC-S-10	10	-	-	-	10	0.0118	-0.0124	-0.013	
TCC	TC-S-20	20	-	-	-	20	0.0137	-0.0122	-0.0107	
TC-S	TC-S-30	30	-	-	-	30	0.0180	-0.0104	-0.0028	
	TC-S-40	40	-	-	-	40	0.0185	-0.0100	-0.0015	
	TU-D-10	10	0.0063	-0.0012	0.0039	1.52	0.0077	-0.0080	-0.0083	
	TU-D-20	20	0.0082	-0.0025	0.0032	14.82	0.0137	-0.0116	-0.0095	
TU-D	TU-D-30	30	0.0088	-0.0019	0.005	15.51	0.0123	-0.0104	-0.0085	
	TU-D-40	40	0.0096	-0.0022	0.0052	20.01	0.0145	-0.0135	-0.0125	
TUC	TU-S-10	10	0.0063	-0.0017	0.0029	4.56	0.0085	-0.0095	-0.0105	
	TU-S-20	20	0.0086	-0.0020	0.0046	10.56	0.0103	-0.0134	-0.0165	
TU-S	TU-S-30	30	0.0082	-0.0025	0.0032	19.73	0.0118	-0.0100	-0.0082	
	TU-S-40	40	0.0082	-0.0018	0.0046	21.61	0.0137	-0.0136	-0.0135	

Table 3. Critical strain values of sandstone specimens at the unloading point and the critical failure point of sandstone specimens.

The relationship between the deformation parameters (i.e., the Young's modulus, *E*, and the Poisson's ratio, μ) and the initial confining pressure (σ_3^0) is shown in Figure 4. As shown in Figure 4a, *E* values of sandstone firstly increase and then decrease as the initial confining pressure increases. Meanwhile, *E* values of dry sandstones are significantly higher than that of saturated sandstones in both loading and unloading tests. In Figure 4b, μ values of sandstone increase with the increase of initial confining pressure. Because the sandstone specimens are more prone to produce cracks paralleling to axial loading direction with the release of circumferential constraint in unloading test, the Poisson's ratio of the sandstone in unloading test is higher than that of dry specimen under the same stress path. The bearing capacity decreases, and the Young's modulus of the sandstone decreases while the Poisson's ratio increases.

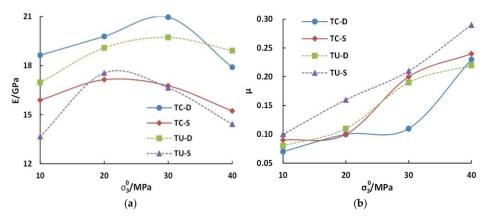


Figure 4. Variation of the deformation parameters of sandstone with the initial confining pressure (**a**) Young's modulus; and (**b**) Poisson's ratio.

3.2. Fracturing Characteristics

Figure 5 shows the failure modes of dry and saturated sandstones in conventional triaxial compression tests. It is found from Figure 5a,b that the spalling and tensile cracks are visible under

uniaxial compression. When the initial confining pressure increases to 10 MPa, axial or radial tensile cracks are often produced along the shear plane, and then tensile cracks develop and form a macroscopic failure surface, which even breaks earlier than the main shear fracture, as shown in Figure 5d. It indicates that the failure mode of rock specimens shows a combined tension and shear failure under low initial confining pressure condition ($\sigma_3^0 \le 10$ MPa). However, under high initial confining pressures ($\sigma_3^0 > 10$ MPa), a main shear fracture passes through the entire specimen usually extend to the end of specimen. The specimens are cut into two triangular vertebral bodies by the main fracture, and the main failure surface of sandstone develops from the end of specimen to the side surface as the increase of initial confining pressure. Shear failure occurs under high initial confining pressures ($\sigma_3^0 > 10$ MPa), and a single shear fracture dominates the failure processes. Besides, all dry sandstone specimens show structural failure while some saturated sandstone specimens fail partly, as shown in Figure 5, implying that the failure characteristics of dry sandstones are more severe than those of saturated sandstones.

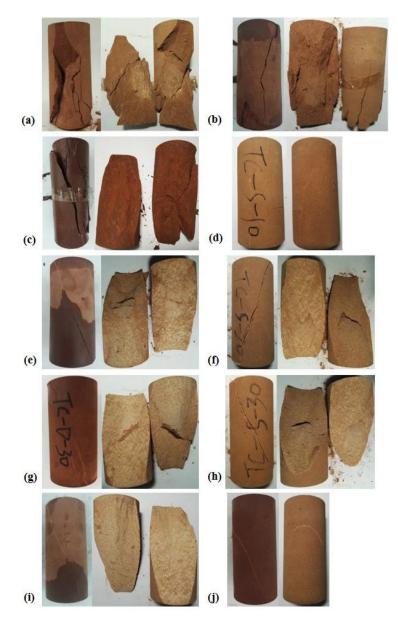


Figure 5. Failure modes of dry and saturated sandstones in conventional triaxial compression tests: (a) TC-D-0; (b) TC-S-0; (c) TC-D-10; (d) TC-S-10; (e) TC-D-20; (f) TC-S-20; (g) TC-D-30; (h) TC-S-30; (i) TC-D-40; (j) TC-S-40.

Figure 6 shows the failure modes of dry and saturated sandstones in unloading confining pressure tests. When the initial confining pressure is 10 MPa, the rock tends to produce longitudinal tensile cracks approximately parallel to the loading direction, as the reduction of circumferential constraints in unloading test. Tensile cracks propagate and coalesce with the shear crack, leading to the final failure of rock specimens. When the initial confining pressure is 20 MPa, there are numerous rock fragments caused by shear friction on the rock failure plane, implying that the rock specimen undergoes shear failure and forms a macroscopic shear surface. Meanwhile, longitudinal (Figure 6c) and radial (Figure 6d) tensile cracks are often produced at the lower part of the triangular vertebral body. Combined shear and tension failure occurs for the rock specimen. Under high initial confining pressures ($\sigma_3^0 > 20$ MPa), shear failure dominates the failure process in unloading tests, which is the same as the conventional triaxial compression test. The shear friction of the rock is severe, and a lot of rock fragments are observed on the failure surface. Besides, by comparing failed rock fragments, it can be found that the failure characteristics of dry sandstones are more violent than those of saturated sandstones under unloading test.

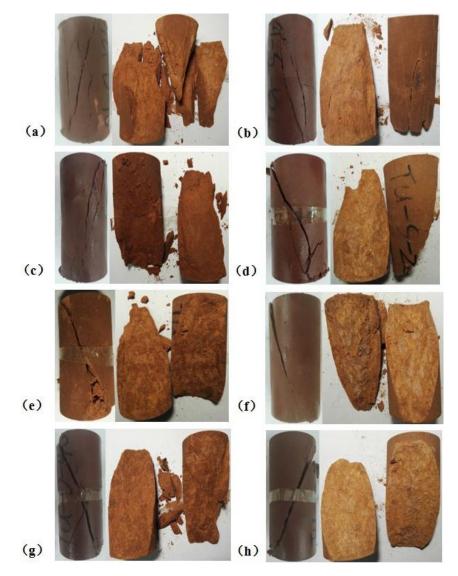


Figure 6. Failure modes of dry and saturated sandstones in unloading confining pressure tests: (a) TU-D-10; (b) TU-S-10; (c) TU-D-20; (d) TU-S-20; (e) TU-D-30; (f) TU-S-30; (g) TU-D-40; (h) TU-S-40.

The phenomenon of volume expansion occurs significantly in the triaxial tests, particularly for the saturated rock in unloading confining pressure test. The failure characteristics of sandstone in unloading test are more violent than those under triaxial loading test.

In order to compare and analyze the microscopic and macroscopic failure characteristics of the rocks under different confining pressures, stress paths and water contents, the microscopic analysis of dry and saturated sandstones with an initial confining pressure of 10 and 40 MPa were carried out using the scanning electron microscopy (SEM) method. Figure 7 shows the SEM photos of sandstone fractures with the initial confining pressure 10 and 40 MPa in conventional triaxial compression test. In Figure 7a,c, the spalling fractures occurs in microscopic view under the initial confining pressure of 10 MPa, which is similar to the macroscopic spalling failure of rock specimen. The microscopic fractures retain sharp and smooth crystal surfaces. Meanwhile, the tearing traces (left arrows) are formed in Figure 7b, which are the typical microscopic characteristics of tensile failure [25,38]. Besides, there are tiny rock fragments (as shown at two sides of Figure 7a,d) and slip scratches (as shown in Figure 7d) left behind by shear friction [39]. It means that the micro-cracks of sandstone are shown as a combined tension and shear failure under low initial confining pressures ($\sigma_3^0 = 10$ MPa represents low initial confining pressure). It is consistent with the macroscopic failure characteristics of sandstone. However, under high initial confining pressures ($\sigma_3^0 = 40$ MPa), the microscopic fractures of the rock are stepped and serrated as shear effect [40]. In addition, there are lots of rock fragments left in the low-lying area, as illustrated in Figure 7e–h. Furthermore, the slip scratches along the crystal are also existed in Figure 7e. The rock crystals were cut off and angular edges were flattened in Figure 7h. The fractures almost have no traces of tension failure on the microscopic section of sandstone. Under high initial confining pressure conditions, the microscopic failure of sandstone is dominated by shear, which is consistent with the macroscopic failure characteristics of sandstone in the conventional triaxial compression test.

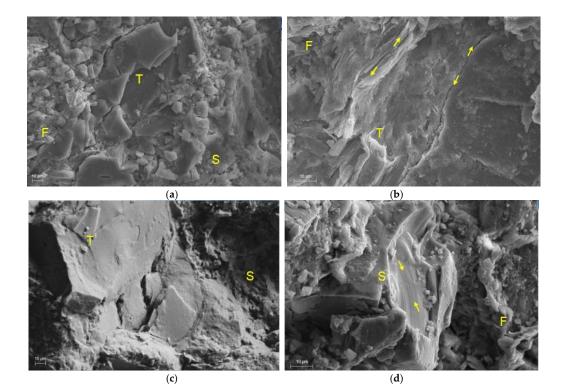


Figure 7. Cont.

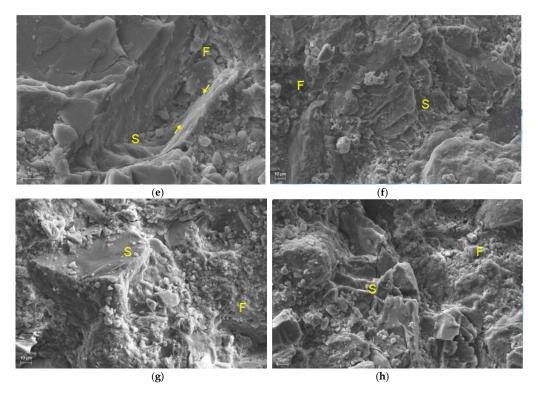


Figure 7. Typical scanning electron microscopy (SEM) images of sandstone fractures with the initial confining pressure 10 and 40 MPa in conventional triaxial compression tests: (**a**,**b**) TC-D-10; (**c**,**d**) TC-S-10; (**e**,**f**) TC-D-40; (**g**,**h**) TC-S-40 (Note: Opposite arrows and inverse arrows represent slip trace and tensile trace respectively; and the letters F, S and T represent fragments, shear crack and tensile crack, respectively).

Figure 8 shows the SEM photos of sandstone fractures with the initial confining pressure 10 and 40 MPa in unloading confining pressure tests. It can be seen clearly from Figure 8 that there are visible tensile cracks in dry and saturated sandstones under different confining pressures. In Figure 8a,c,e,g,h, the microscopic section shows sharp angular edges and smooth crystal surfaces. Moreover, there are evident traces of tension and spalling fractures in microscopic view. The microscopic section exhibit a typical tensile failure. In addition, as shown in Figure 8b,d,f, there are a large number of rock fragments left behind on the roughly microscopic section. The scratches caused by shear friction appear on the right part of Figure 8h. The microscopic failure section also shows shear failure characteristics. Thus, the microscopic failure of sandstone mainly shows a combined tension and shear failure in unloading test. It is consistent with macroscopic failure of sandstone under low initial confining pressure, but it is different from macroscopic failure of sandstone under high initial confining pressure, where the specimen only shows shear failure in macroscopic view.

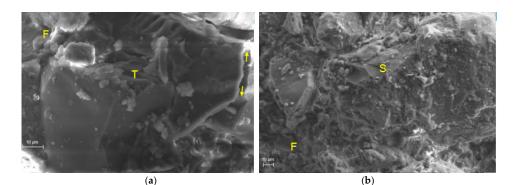


Figure 8. Cont.

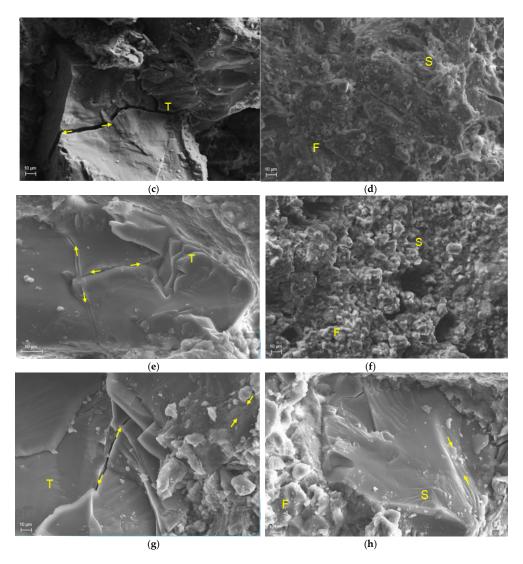


Figure 8. Typical SEM images of sandstone fractures with the initial confining pressure 10 and 40 MPa in unloading confining pressure tests: (**a**,**b**) TC-D-10; (**c**,**d**) TC-S-10; (**e**,**f**) TC-D-40; (**g**,**h**) TC-S-40 (Opposite arrows and inverse arrows represent slip trace and tensile trace respectively; and the letters F, S and T represent fragments, shear crack and tensile crack, respectively).

3.3. Energy Evolution of Rock Failure

Based on the relevant strain energy calculation formula and the experimental data, the strain energy evolution curves can be obtained with loading time [41,42]. The typical time history curves of strain energy for dry and saturated sandstone specimens under different initial confining pressures are shown in Figure 9. The initial confining pressures of 10 MPa and 40 MPa represent low and high confining pressures respectively. The strain energy curves for other specimens under low or high confining pressures are similar to these curves in each testing group.

For conventional triaxial compression tests, as shown in Figure 9a–d, several typical stages can be divided corresponding to the points in the stress-time curves. When the rock specimen is under low initial confining pressure ($\sigma_3^0 = 10$ MPa), as shown in Figure 9a,c, the curves of total strain energy (U) and elastic strain energy (U_e) almost overlap, and the dissipative strain energy (U_d) is relatively low in the micro-cracks compaction stage (OA) and the elastic deformation stage (AB). It indicates that the energy absorbed from the test machine is basically converted into U_e . However, while the rock specimen is under high initial confining pressure ($\sigma_3^0 = 40$ MPa), particularly for the saturated sandstone as shown in Figure 9d, the curves of U and U_e begin to separate gradually and there are few increases of U_d in the elastic deformation stage (AB). In the crack initiation and expansion stage (BC), when the rock is under low initial confining pressure, the curves of U and U_e separate gradually at point B. Meanwhile, U_d starts to increase from this point, owing to the development of plastic deformation and propagation of micro-cracks of the specimens. When the rock is under high initial confining pressure, U, U_e , and U_d increase steadily where the increase rate of U_d is the minimum among them. During the unstable crack development up to the failure stage (CD), the increase rate of U_e slows down, and U_e reaches the elastic energy storage limit at the peak strength point D. U_d increases rapidly in this stage, illustrating accelerated growth of micro-cracks, and the failure approaches. In the post-failure stage (DE), U_e releases quickly to a small value, and U_d increases rapidly to a large value. The absorbed strain energy is basically transformed into U_d , which contributes to the development of internal cracks and a large shear deformation along the fracture surface. However, U still increases rapidly as the large axial deformation at this stage. Finally, the specimen shows a brittle failure.

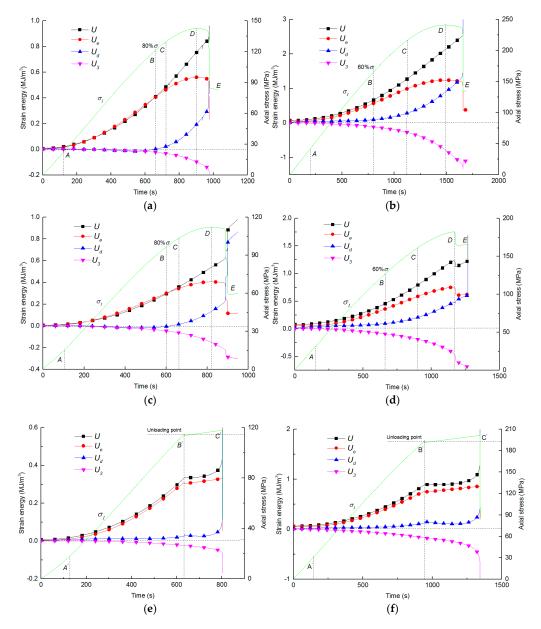


Figure 9. Cont.

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200

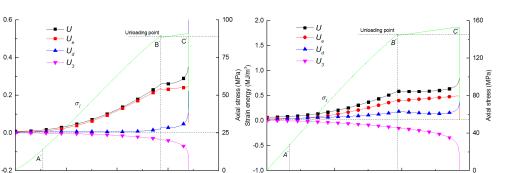
400

Time (s)

(**g**)

600

Strain energy (MJ/m³)



400

Figure 9. Typical strain energy and axial stress time curves: (a) TC-D-10; (b) TC-D-40; (c) TC-S-10; (d) TC-S-40; (e) TU-D-10; (f) TU-D-40; (g) TU-S-10; (h) TU-S-40.

800

For the unloading confining pressure tests, the strain energy time curves of sandstone specimens are shown in Figure 9e-h. The characteristics of strain energy curves in unloading tests are quite different from conventional triaxial compression tests, especially from the unloading point. Before the unloading point, in the micro-cracks compaction stage and the elastic stage (OB'), the curves of U and U_e almost overlap with a low initial confining pressure (10MPa), while the curves of U and U_e begin to separate under a high initial confining pressure (40MPa). The variation trend is similar with the loading test. However, after unloading point (B'C'), U and U_d increase steadily while U_e shows a slow rate of increase. Meanwhile, since the rock is still under the effect of axial loading in this stage, the energy is still absorbed from the test machine. The absorbed energy is mainly converted into U_d , which is used for the development and expansion of micro-cracks within the rock. When reaching the failure point (C'), U_d and circumferential strain energy (U_3) grow rapidly, and the stress-time curve falls down immediately. At this moment, U_e releases rapidly because of the propagation of rock cracks. Following the point C', almost all of the releasable strain energy is released. Meanwhile, U_d and U_3 increase to the maximum value. Finally, the rock specimen fails violently due to the unloading of confining pressure.

Undoubtedly, there are some differences in the energy evolution laws of the rocks under different confining pressure conditions, particularly in the elastic deformation stage in triaxial loading and unloading process. During the elastic deformation stage, the curves of U and U_e almost overlap when the rock specimen is under low initial confining pressure, and almost all of the absorbed energy is converted into U_e . However, when the rock is under high initial confining pressure, the curves of U and U_e begin to separate, and the absorbed energy is basically stored as U_{e} and partially converted as U_d . It is manifested that the internal damage has occurred earlier under the high initial confining pressure conditions, and the internal micro-cracks of rock begin to develop and propagate during the elastic deformation stage. Especially for the saturated sandstone under high initial confining pressures, the curves of U and U_e separate significantly in Figure 9h, which signifies that the water effect on rock energy evolution are nonnegligible, and it has a significant influence on the deformation and failure process of rock under high initial confining pressures. In addition, the curves separate at the point where the axial stress is about 80% of the peak strength for low initial confining pressure condition, while the curves separate at the point where the axial stress is about 60% of the peak strength under high initial confining pressure. It also indicates that the internal damage and micro-cracks develop earlier under high initial confining pressure than that under low confining pressure conditions.

The dissipation of energy leads to the development and propagation of internal cracks, which is the main reason of rock failure. It has been proved that the use of U_d/U is more favorable to analyze rock deformation and failure process instead of dissipative strain energy (U_d) [25,43]. The variation curves of U_d/U with the loading time under different confining pressures are shown in Figure 10.

1200

800

Time (s)

(h)

The U_d/U exhibits some typical evolution stages as shown in Figure 10. In the conventional triaxial compression test, it increases initially, then decreases, and then increases slowly; finally, it increases rapidly at the failure stage of the rock. However, the curve increases initially, and then it decreases to a nearly smooth platform; finally, it increases sharply in unloading tests. During the failure stage, the elastic strain energy accumulated within the rock releases instantaneously, prompting rock fractures and damages. Meanwhile, it has been testified that the faster dissipation of rock energy causes the crack to propagate and penetrate faster, and then the failure of the rock occurs more suddenly [42,44]. In the conventional triaxial compression test, the energy dissipation curve increases along a skew line, showing a gradual increase trend. In contrast, the energy dissipation curve shows a nearly vertical increase for the triaxial unloading test, indicating a sudden and violent brittle failure of rock specimens.

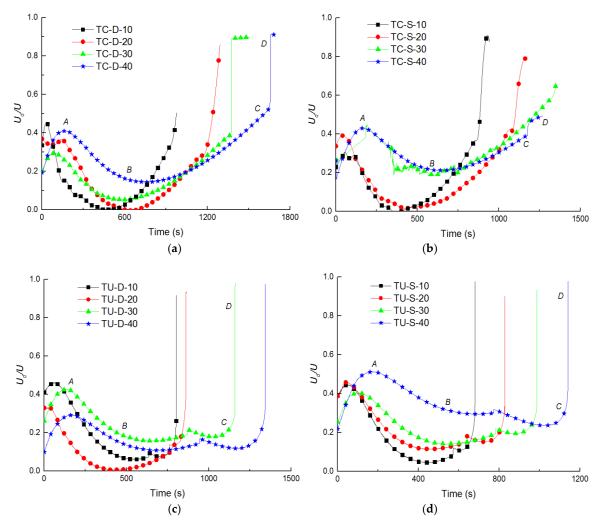


Figure 10. Evolution of U_d/U with loading time under triaxial loading and unloading tests for dry and saturated sandstone specimens (**a**) TC-D; (**b**) TC-S; (**c**) TU-D; (**d**) TU-S.

The relationship between the U_d/U and initial confining pressure at the corresponding critical failure point is plotted in Figure 11. The U_d/U values increase as σ_3^0 increases. When the rock specimen is under high initial confining pressures, it has more time for specimen deformation and damage. Thus the dissipative strain energy takes a large proportion of the total absorption energy in the rock. The deformation and failure process of rock in loading tests includes the micro-cracks compaction stage (OA), the elastic deformation stage (AB), the crack initiation and propagation stage (BC), the unstable crack development up to the failure stage (CD), the post-failure stage (DE) and so on. However, the rock in unloading tests enters the failure stage almost directly from the elastic deformation stage.

Thus, relatively fewer cracks develop inside the rock, resulting in less dissipation of rock energy and the energy is mainly consumed for the circumferential deformation and converted into kinetic energy for the failure of rock, such as rockbursts. The U_d/U of rock in unloading test is significantly lower than that of conventional triaxial compression test, as shown in Figure 11. Furthermore, the U_d/U of saturated rock is greater than dry rocks in the deformation and failure process of triaxial tests. Saturated by water, the internal friction strength of the rock is weakened as the water immersion, which results the rocks more prone to be deformed and damaged. With the accumulated damage within the rock, the energy account for the dissipation increases and the energy release decreases, leading to a relatively moderate failure of saturated rock, and there are less possibilities for rockbursts. It is also one of the basic theoretical foundations for the rockburst prevention through water injection in engineering. In addition, comparing the influence of stress paths and water conditions of the rock in Figure 11, it can be found that the effect of stress paths on energy evolution is more pronounced than the water conditions of the rock.

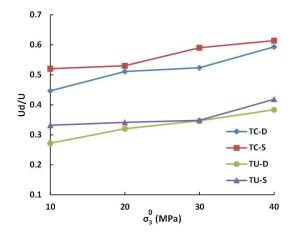


Figure 11. Variation of the U_d/U values with the initial confining pressure for dry and saturated sandstone specimens at the critical failure point.

4. Discussion

When a rock specimen approaches the failure point, U_e can be quickly released and it may be transformed into U_d . In the conventional triaxial compression test, the internal cracks develop completely within the rock specimen. However, the unloading failure usually occurs abruptly, and the rock specimens fail violently with loud fracturing noise, which has the characteristics of rockburst as observed in deep rock excavation engineering.

Table 4 lists the average strain energy values of sandstone specimens at the unloading point and the critical failure point in present triaxial tests. In the conventional triaxial compression test, U_d is larger than U_3 at critical failure point of the rock, implying that the energy consumption is mainly used for the micro-crack initiation and internal damage of the rock. In contrast, under unloading tests, the energy consumption during the failure process of rock specimens mainly contributes to the circumferential strain (ε_3) as the reduction of confining pressure, and thus U_3 is larger than U_d as shown in Table 4. Moreover, the following energy incremental value can be calculated based on the data in Table 4.

$$\Delta U_e = U'_e - U_e, \Delta U_d = U'_d - U_d, \Delta U_1 = U'_1 - U_1, \Delta U_3 = U'_3 - U_3 \tag{1}$$

It can be inferred that $\Delta U_e < 0$, $\Delta U_d > 0$ in unloading tests, and U_e converts into U_d for the development and propagation of internal cracks from the unloading point to the failure point. Meanwhile, the present study discovered that $\Delta U_d > \Delta U_e$. The dissipative energy includes not only

the energy converted from U_e , but also the newly absorbed energy from the test machine. In unloading test, there is the following relationship between the dry and saturated rock:

$$\Delta U_e^{TU-D} \ge \Delta U_e^{TU-S}, \Delta U_d^{TU-D} \ge \Delta U_d^{TU-S}$$
⁽²⁾

It implies that the failure of dry specimens is more severe than the saturated specimen. Furthermore, $\Delta U_1 + |\Delta U_e| - |\Delta U_3| - \Delta U_d > 0$ at the critical failure point also exists in unloading test. The energy absorbed by the rock from test machine is mainly consumed for the development of internal fractures, axial deformation, and circumferential deformation, while partly remained. The residual energy $(\Delta U_1 + |\Delta U_e| - |\Delta U_3| - \Delta U_d)$ may account for the kinetic energy due to rockbursts, which may occur in the unloading process such as rock excavation with high in-situ stresses in hard rock. Besides, it can be obtained that:

$$0 < \Delta U_1^{TU-S} + \left| \Delta U_e^{TU-S} \right| - \left| \Delta U_3^{TU-S} \right| - \Delta U_d^{TU-S} < \Delta U_1^{TU-D} + \left| \Delta U_e^{TU-D} \right| - \left| \Delta U_3^{TU-D} \right| - \Delta U_d^{TU-D}$$
(3)

There is more residual energy for dry rock than saturated rock. It implies that the rock burst is more likely to occur in dry rock, and water infusion is effective to reduce the possibility of rockbursts in the excavation of deep underground rock engineering.

Table 4. Strain energy of sandstone specimens at the unloading point and the critical failure point in triaxial test.

Group	σ_3^0 (MPa)		Ur	loading Poi	nt		Critical Failure Point				
		U(MJ/m ³)	$U_1(MJ/m^3)$	$U_e(MJ/m^3)$	$U_d(MJ/m^3)$	$U_3(MJ/m^3)$	$U'(MJ/m^3)$	$U_1'(MJ/m^3)$	$U_e'(\mathrm{MJ/m^3})$	$U_d'(MJ/m^3)$	$U_3'(MJ/m^3)$
	10	-	-	-	-	-	0.85	1.01	0.41	0.43	-0.17
TC-D	20	-	-	-	-	-	1.31	1.62	0.73	0.59	-0.33
IC-D	40	-	-	-	-	-	1.80	2.54	0.84	0.95	-0.79
	60	-	-	-	-	-	2.52	3.75	1.02	1.50	-1.30
	10	-	-	-	-	-	0.66	0.90	0.32	0.34	-0.25
TC-S	20	-	-	-	-	-	0.95	1.40	0.44	0.50	-0.48
IC-5	40	-	-	-	-	-	1.60	1.98	0.56	0.94	-0.82
	60	-	-	-	-	-	1.62	2.40	0.62	0.99	-0.85
-	10	0.33	0.35	0.31	0.02	-0.02	0.45	0.50	0.33	0.12	-0.06
TU-D	20	0.59	0.66	0.53	0.06	-0.10	0.83	1.13	0.55	0.27	-0.36
10-D	40	0.75	0.82	0.61	0.13	-0.11	1.01	1.34	0.66	0.35	-0.37
	60	0.89	1.01	0.74	0.15	-0.17	1.35	1.98	0.83	0.52	-0.69
	10	0.26	0.28	0.24	0.02	-0.03	0.36	0.48	0.24	0.12	-0.12
	20	0.38	0.43	0.32	0.06	-0.08	0.52	0.85	0.34	0.18	-0.35
TU-S	40	0.54	0.64	0.41	0.10	-0.15	0.71	1.15	0.46	0.25	-0.48
	60	0.59	0.66	0.42	0.17	-0.15	0.85	1.48	0.50	0.36	-0.70

5. Conclusions

- (1) The peak strength difference between dry and saturated sandstones grows with the increasing of initial confining pressure, and the effect of water on rock strength is more remarkable under high initial confining pressures. As a result, when the sandstone specimens are saturated by water, the values of cohesion, internal friction angle and Young's modulus are decreased whereas the Poisson's ratio is increased.
- (2) In the conventional triaxial compression test, both macroscopic and microscopic failure of the rocks show a combined tension and shear fracture under low initial confining pressure ($\sigma_3^0 \le 10$ MPa), but it shows shear fracture under high initial confining pressure ($\sigma_3^0 > 10$ MPa). The microscopic failure of the rock in unloading test mainly shows a combined tension and shear fracture, which is consistent with the macroscopic failure of sandstone under low initial confining pressure ($\sigma_3^0 \le 20$ MPa). However, under high initial confining pressure conditions ($\sigma_3^0 \ge 20$ MPa), it mainly shows shear fracture in macroscopic view. The failure of sandstone in unloading test is more violent than that the failure under triaxial loading test, particularly for dry sandstones.
- (3) The energy evolution processes confirm that there are some differences for rock specimens under different confining pressures, particularly for the elastic deformation stage. During this stage,

the total energy (U) and elastic strain energy (U_e) curves are almost overlapped when the rock specimen is under low initial confining pressures. However, when the rock is under high initial confining pressures, U and U_e begin to separate, and the absorbed energy is basically stored as U_e , partially as the dissipative strain energy (U_d). The internal damage has occurred and the internal cracks of the rock develop earlier under the high initial confining pressure conditions.

(3) The energy consumption during the failure process mainly contributes to crack initiation and internal damage in loading tests. In unloading test, the energy is mainly consumed for the circumferential deformation and converted into kinetic energy for rock failure. The failure of the saturated rock is relatively moderate because the absorbed energy is mainly used for internal damage and only a part of energy is used for release. Rockburst phenomenon is tended to occur for dry rocks, especially under triaxial unloading conditions. It also indicates that the water injection of the rock may be effective to prevent rockbursts under high in-situ stresses conditions.

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