



Article Study on the Wellbore Flow for Carbon Dioxide Fracturing

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Abstract: CO_2 fracturing has unparalleled advantages in the reservoir reform which can significantly improve oil and gas recovery in unconventional oil and gas resources. The wellbore flow behavior is one of the fundamental issues of CO_2 fracturing. A model of flow and heat transfer in the wellbore is developed in this paper, and wellbore temperature and pressure are coupled using an iterative method. The model is validated by measured data from the field. Wellbore pressure, temperature, CO_2 properties, and phase state along depth are observed and a sensitivity study is conducted to analyze the controlling factors for CO_2 fracturing. Results show that displacement is the key factor affecting CO_2 flow behavior in the wellbore and injection temperature has greater influence on CO_2 flow behavior than injection pressure and geothermal gradient; however, excess injection temperature brings enormous cost in wellbore pressure. CO_2 phase state is related to working parameters and it tends to stay in liquid state under higher displacement, which is matched with field tests. This study can help optimize the working parameters of CO_2 fracturing.

Keywords: Carbon dioxide fracturing; Wellbore flow model; Heat transfer; Phase state; Sensitivity analyses

1. Introduction

Carbon dioxide (CO₂) is an environmentally friendly waterless working fluid for fracturing [1]. CO₂ fracturing has been studied since the 1960s under the background of growing oil and gas demand. So far, CO₂ fracturing has been applied in many countries such as America, Canada, Germany, and China [2–4], showing unexceptionable advantages especially in unconventional oil and gas resources. Firstly, the mechanical properties of reservoir rock are changed after CO₂ immersion [5], which can reduce the breakdown pressure and facilitate secondary cracking. Secondly, the waterless CO₂ inhibits the swelling of clay mineral and eliminates water sensitivity [6], improving the permeability of the reservoir to some extent, which gives this technology enormous prospects. Thirdly, the low additive content in CO₂ fracturing fluid leads to the high flowback rate. Last but not least, CO₂ can increase the mobility of oil and replace the adsorbed CH₄ [6–8], enhancing oil and gas recovery (EOR). Furthermore, the mitigation of greenhouse gases such as CO₂ has become an increasing global demand in recent years [9], and CO₂ fracturing has the potential of improving the development of carbon capture [10–13], utilization, and storage (CCUS), which has both environmental and economic benefits.

Compared with traditional hydraulic fracturing, the pressure at the wellhead of CO_2 fracturing increases slowly and fluctuates, as shown in Figure 1, which is related to the compressibility of CO_2 .

The temperature–pressure condition and the properties of CO_2 are coupled in the wellbore due to the compressibility of CO_2 . Therefore, the wellbore flow and heat transfer behaviors are essential conditions to optimize the operating parameters during CO_2 fracturing.



Figure 1. (a) Fracturing curve of CO₂ fracturing; (b) fracturing curve of traditional hydraulic fracturing.

Many studies have been conducted on fluid flow and heat transfer in the wellbore since the 1950s. Ramey [14] proposed a semisteady model which only considered the unsteady heat transfer in the stratum outside the wellbore and first used the overall heat transfer coefficient to solve the equation. A number of later semisteady wellbore flow models were mostly improvements to Ramey's model. Raymond [15] developed a nonsteady model for temperature distribution during drilling fluid circulation, which was the basis of later nonsteady wellbore flow models. Eickmeier [16] presented a finite difference model for the early transient temperature performance in the wellbore during injection and production, appropriate for short-term operations such as fracturing. Hasan and Kabir [17–19] presented a solution to continuity, momentum, and energy conservation equations, and developed wellbore heat transfer models for various situations. Wang et al. [20] quantified the heat generated by the flow friction of high-yield production wells. As for CO_2 flow in the wellbore, the sensitivity of CO_2 properties to temperature and pressure results in the complexity of flowing temperature and pressure calculation. Plenty of research is devoted to the coupling of temperature and pressure during the CO₂ injection or circulation process in the wellbore. Cranshaw [21] developed a numerical model of CO_2 nonisothermal flow for production or injection wellbores, which matched single- or two-phase flow of CO₂. Gupta [22] first proposed drilling with supercritical CO₂ and established a simplified model of CO₂ circulation in the wellbore. Al-Adwani [23] quoted the high-precision Span–Wagner state equation for thermodynamic properties of CO₂ and improved the heat transfer model for supercritical CO₂ wellbore circulation. Many researchers [24–27] adopted the compressible fluid control equations to describe CO_2 flow in the wellbore in recent years, realizing the coupling of CO_2 properties with flow conditions such as temperature and pressure under different working environments to a large extent. Furthermore, a flow friction coefficient model considering CO₂ compressibility was developed which improves the accuracy of the pressure.

In this study, a wellbore flow model coupling CO_2 properties and temperature–pressure condition for CO_2 fracturing is developed. The model is solved by an iterative method. The temperature, pressure, and CO_2 properties profiles are analyzed based on the calculation results and the calculation is verified by data from CO_2 fracturing field test. Finally, the sensitivity analysis on the wellbore flow field is conducted.

2. Mathematic Model of Wellbore Flow

During CO_2 fracturing, hypothermic liquid CO_2 is pumped into the wellbore from the wellhead and gets heated [26,27] due to thermal absorption from the stratum. The compressibility of CO_2 leads to the coupling of CO_2 physical parameters with wellbore temperature–pressure conditions. Therefore, a theoretical model is proposed to describe the wellbore flow of the CO_2 fracturing injection process.

The mathematical models are based on the following assumptions: ① the unsteady-state heat transfer exists only in the stratum outside the hole wall; ② the fluid flow and heat transfer in the wellbore are in steady state; ③ the effects of longitudinal heat transfer and radiative heat transfer are ignored. The Hasan Equation shown in Appendix A is mostly used to deal with the unsteady-state heat transfer.

2.1. Temperature Field Model

The differential element of the wellbore is shown in Figure 2. The origin of coordinates is at the wellhead and the forward direction is downward along the axis. The steady-state mass conservation equation and energy conservation equation [28] in the *z* direction are as follows:

$$\frac{d(\rho v)}{dz} = 0 \tag{1}$$

$$\frac{\partial}{\partial z} \left[\rho v \left(h + \frac{v^2}{2} \right) \right] = \frac{1}{A} \frac{dq}{dz} + \rho v g \cos \theta \tag{2}$$

where *h* is the specific enthalpy of the fluid, J/kg; *v* is the fluid velocity, m/s; *t* is circulation time, s; *z* is the depth, m; ρ is density of CO₂, kg/m³; A is cross-sectional area, m²; *q* is the heat transfer per unit time, W; θ is the deviation angle, rad; *g* is acceleration of gravity, m/s².



Figure 2. A finite element in wellbore.

Substituting the continuity equation into the energy equation, Equation (2) can be simplified as:

$$\frac{dh}{dz} = \frac{1}{M}\frac{dq}{dz} + g\cos\theta - v\frac{dv}{dz}$$
(3)

where *M* is mass flow rate, kg/s.

According to the fundamental laws of thermodynamics, the expression of enthalpy change is

$$dh = c_p dT - c_p J_T dp \tag{4}$$

where c_p is the specific heat capacity of fluid, J/(Kg·K); J_t is Joule–Thomson coefficient, K/MPa; p is the pressure of fluid, MPa.

The temperature increment in a finite element can be obtained by combining Equations (3) and (4):

$$\frac{dT}{dz} = \frac{1}{c_p} \left(\frac{1}{M} \frac{dq}{dz} + g \cos \theta - v \frac{dv}{dz} \right) + J_T \frac{dp}{dz}$$
(5)

The heat transfer between CO_2 and the stratum outside the wellbore is

$$dq = \left(\frac{T_e - T_f}{R_{ef}}\right) dz \tag{6}$$

where T_e is the formation temperature, K; T_f is fluid temperature in the wellbore, K; R_{ef} is thermal resistance of formation to the wellbore fluid. The expression of R_{ef} is shown in Appendix B.

2.2. Pressure Field Model

The pressure drop can be derived from the momentum conservation equation of compressible fluid. On the basis of assumptions, when the wellbore flow is in steady state, the pressure drop of fluid is given by:

$$\frac{dp}{dz} = \rho g \cos \theta - \rho v \frac{dv}{dz} - f v^2 \frac{\rho}{2d_i}$$
(7)

where *p* is the pressure of fluid, MPa; ρ is the density of fluid, kg/m³; *v* is flow velocity, m/s; *d_i* is the inner diameter of the pipe, m; *f* is the friction coefficient of fluid, dimensionless.

Thanks to the low viscosity of CO_2 and the large fluid mass flow rate during CO_2 fracturing, it is easy to reach turbulence in the wellbore. Regarding the calculation of the friction coefficient, the formula proposed by Z.Y. Wang [29] was chosen:

$$\frac{1}{\sqrt{f}} = -2.34 \lg \left(\frac{\varepsilon}{17.2de} - \frac{9.26}{\text{Re}} \lg \left(\left(\frac{\varepsilon}{29.3de}\right)^{0.95} + \left(\frac{18.35}{\text{Re}}\right)^{1.108}\right)\right)$$
(8)

where ε is the absolute roughness, m; *de* is equivalent diameter, m; Re is Reynolds number, dimensionless.

3. Solution Procedure

Compared with traditional hydraulic fracturing fluid, the properties of CO_2 are no longer constant for CO_2 fracturing. To avoid the calculated errors accumulating with well depth, the physical property model with high accuracy is selected and a coupling computation method is adopted.

3.1. Physical Properties of CO₂

The properties of CO_2 are sensitive to the change of temperature and pressure. Tiny changes in temperature and pressure may cause significant fluctuations in CO_2 properties, and the phase change of CO_2 could also be reflected by fluctuations in CO_2 properties, so it is important to calculate properties of CO_2 accurately.

The Span–Wagner equation [30] has high accuracy in calculating thermodynamic properties of CO_2 , especially in supercritical areas. Therefore, the Span–Wagner equation is chosen to calculate thermodynamic properties of CO_2 including density, specific heat capacity, Joule–Thomson coefficient, and specific enthalpy in this paper. For transfer properties of CO_2 , the Vesovic model [31] is used to calculate the heat conductivity of CO_2 , and the Fenghour model [32] is used to calculate the viscosity of CO_2 .

3.2. Coupling Computation Methodology

During the injection process of CO_2 fracturing, the temperature and pressure in the wellbore and CO_2 properties are coupled with each other. Both temperature and pressure vary with well depth

along with CO₂ flow. Therefore, the calculation of temperature, pressure, and CO₂ properties must be coupled in the process of iteration.

The wellbore is divided into N units along the direction of well depth. To ensure the calculation unit is much shorter than the well depth, the CO₂ properties of each and every calculation unit can be considered as constant. The injection temperature (T_0) and pressure (p_0) are regarded as initial conditions.

For the *i*th calculation unit, the iterative method is as follows:

(1) The temperature and pressure of (*i*-1)th calculation unit are used as the starting of the iteration, marked as T_i^0 , p_i^0 , so the temperature (*dT*) and pressure (*dp*) increment can be estimated according to Equation (5) and Equation (7). Then, temperature and pressure of *i*th calculation unit, marked as T_i^1 , p_i^1 , can be obtained.

(2) The new temperature and pressure increment, dT' and dp', also can be calculated with the known of T_i^1 , p_i^1 .

(3) The calculated dT' and dp' are compared with the initial dT and dp. If the differences between the calculated values are within the error tolerance, the calculation ends and the calculation of the next unit begins; if not, replace T_i^0 and p_i^0 with new values and return to (1).

4. Results and Discussion

The original parameters used in the model are shown in Table 1, and the wellbore configuration is shown in Figure 3. All above conditions are from a well which actually conducted CO_2 fracturing in the Sulige gas field Sudong block. The measured data at the bottom hole, such as injecting displacement, bottom hole pressure, and bottom hole temperature, are exhibited in Figure 4. In order to match the actual CO_2 fracturing, tubing and annulus synchronous injection is applied as the injection mode during the calculation in this paper, noted as casing injection.

No.	Variables	Symbol	Value	Unit
1	Well depth	Н	3250	m
2	Borehole diameter	d_w	0.121	m
3	Formation pore pressure	p_{po}	28.16	MPa
4	Surface temperature	T_{eo}	298	Κ
5	Injection temperature	T_0	258	Κ
6	Injection pressure	p_0	8	MPa
7	Geothermal gradient	G	2.8	K/100m
8	Initial breakdown pressure	p_f	66.02	MPa
9	Initial formation compressible strength	σ_c	135.077	MPa
10	Tensile strength	σ_t	$\sigma_{\rm c}/12$	MPa
11	Initial elastic modulus	Ε	18.7070	GPa
12	Thermal expansion coefficient of rock	σ_m	3×10^{-5}	K^{-1}
13	Initial Poisson ratio	ν	0.242	-
14	Porosity	ϕ	0.05	-
15	Maximum horizontal in situ stress gradient	σ_H	1.9	g/cm ³
16	Minimum horizontal in situ stress gradient	σ_h	1.45	g/cm ³
17	Overburden gradient	σ_v	2.3	g/cm ³
18	Biot's parameter	α	1.0	-

Table 1. Basic parameters for the model.



Figure 3. Wellbore configuration chart.



Figure 4. Curve of measured data at bottom hole during CO_2 fracturing.

4.1. Model Validation and Wellbore Temperature–Pressure Distribution

The measured bottom hole temperature decreases with the injection of CO_2 as shown in Figure 4. In order to verify the reliability of the model, the data point with an injection time of 2 h is chosen. The displacement of CO_2 is 4 m³/min and the injection temperature and pressure are 258 K and 26.21 MPa, respectively. The measured and calculated values of bottom hole temperature and pressure are displayed in Table 2, while the errors are within 1%, which proves the rationality of wellbore temperature and pressure calculation.

Table 2. Model validation of wellbore flow model (injection pressure is 26.21MPa).

<i>Q</i> (m ³ /min)	Comparison Items	Measured Values	Calculated Values	Error (%)
4.0	Bottom hole temperature (K)	288.75	287.10	0.57
	Bottom hole pressure (MPa)	52.81	53.22	0.78

Previous studies have shown that displacement [27] is the key factor affecting temperature and pressure of CO_2 in the wellbore. The calculations of wellbore temperature and pressure distributions under difference displacement are shown in Figures 5 and 6.



Figure 5. Pressure distribution under different displacement.



Figure 6. Temperature distribution under different displacement.

The pressure distribution in the wellbore under different displacement can be seen in Figure 5. It can be seen that the wellbore pressure increases linearly with well depth increasing, while pressure gradient increases first and then decreases with the increase of CO_2 displacement; as demonstrated in Figure 7, the bottom hole pressure increases first and then decreases with displacement increasing. This is because wellbore pressure is affected by both the gravity head and the flow friction. With the

increase of displacement, the magnitude of pressure increment caused by gravity head and flow friction dominates the change of pressure gradient. According to Figures 5 and 7, when CO_2 displacement is up to 7 m³/min, wellbore pressure grows slowly with well depth due to the excessive flow friction.



Figure 7. Bottom hole pressure and temperature under different displacement.

Figure 5 demonstrates the temperature distribution in the wellbore under different displacement. It can be seen that the temperature increases with the increase of well depth, while the bottom hole temperature decreases with displacement increasing, as shown in Figure 7. According to Figures 6 and 7, CO_2 turns from liquid state into supercritical state under low displacement; however, it stays in liquid state until reaching the bottom hole under high displacement. This phenomenon has been verified in field tests, as shown in Figure 4.

4.2. CO₂ Phase State and Physical Properties Distribution

Because of the large difference between the injected fluid and geothermal temperature during CO_2 fracturing, CO_2 would absorb heat and might undergo phase change as approaching the bottom hole. A pressure–enthalpy diagram is adopted to analyze the phase transition process in the wellbore for CO_2 fracturing, as presented in Figure 8. During the flow process from the wellhead to the bottom hole, CO_2 transforms from liquid state into supercritical state under lower displacement, while it stays in liquid state under higher displacement, which is consistent with the conclusion drawn from Figures 6 and 7.



Figure 8. CO₂ phase distribution in the wellbore.

 CO_2 density and viscosity profiles are illustrated by Figures 9 and 10. It can be seen from the diagrams that the trends of the density and viscosity of CO_2 in the wellbore are matching. The density and viscosity of CO_2 both tend to rise first and then reduce along the flow direction under different displacement, and the density and viscosity under the displacement of 1.5 m³/min are lower than those under the displacement of 4.5 m³/min. This is related to the undulation of heat exchange and flow friction caused by displacement increasing.



Figure 9. Density profile in the wellbore.



Figure 10. Viscosity profile in the wellbore.

4.3. Sensitivity Analyses on Controlling Factors for CO₂ Fracturing

During CO₂ fracturing, the displacement, injection temperature, and pressure can be adjusted directly. The temperature and pressure distribution under different displacement have been analyzed in Section 4.1, so the influence of injection temperature and pressure on wellbore flow behavior of CO₂ will be discussed in this section. Geothermal gradient is usually within a certain limit in one block; for the Sudong block where the working well is located, the measured geothermal gradient is 2.7–3.2 K/100 m. Therefore, the effect of geothermal gradient on wellbore temperature and pressure distribution is also considered in this section.

Figure 11 shows the influence of injection temperature on pressure and temperature distribution of CO_2 fracturing. As can be seen in Figure 11b, there is an overall rise in wellbore temperature with the increase of injection temperature, while the temperature gradient in the wellbore almost remains unchanged. In addition, the injection temperature is in negative correlation with wellbore pressure, which means the pressure gradient in the wellbore reduces as injection temperature rises, as demonstrated in Figure 11a.



Figure 11. Effect of injection temperature: (a) CO₂ pressure profile; (b) CO₂ temperature profile.

As a whole, the supercritical well depth (i.e., the well depth for CO_2 reaching supercritical phase) decreases with the increase of injection temperature, and when injection temperature exceeds critical temperature (304.13 K), CO_2 maintains supercritical state in the wellbore. However, excess injection temperature brings enormous cost in wellbore pressure, hence, it needs to be seriously considered whether to raise the injection temperature during CO_2 fracturing.

The effect of injection pressure on pressure and temperature distribution during CO₂ fracturing is shown in Figure 12. The increase of injection pressure would lead to a rise of the whole wellbore pressure and the pressure gradient remains unchanged according to Figure 12a. As exhibited in Figure 12b, the whole wellbore temperature reduces as injection pressure increases, but the change is very small.

Moreover, it can be drawn from Figures 11 and 12 that the rising temperature has a greater impact on the wellbore flow behavior of CO_2 compared to the rising pressure. This is because the physical properties, especially density and viscosity, fluctuate sharply with a great temperature rise under the temperature–pressure condition of CO_2 fracturing.



Figure 12. Effect of injection pressure: (a) CO₂ pressure profile; (b) CO₂ temperature profile.

Figure 13 presents the influence of the geothermal gradient on the pressure and temperature distribution in the process of CO_2 flow in the wellbore. As can be seen in Figure 13, there is little impact of geothermal gradient on wellbore pressure. Although wellbore temperature increases with the increase of geothermal gradient, as shown in Figure 13, the increase is not obvious. The reason for this phenomenon is that higher displacement will weaken the heat exchange between the stratum and CO_2 in the wellbore, and the temperature increment caused by geothermal gradient needs to be accumulated with well depth, which makes the increase of fluid temperature in the wellbore insufficient to change the wellbore pressure.

In general, the displacement and injection temperature have greater impact on CO_2 flow behavior and phase state than injection pressure under the temperature–pressure condition of CO_2 fracturing. Nevertheless, excess injection temperature has an adverse effect on wellbore pressure, so displacement is the key factor affecting CO_2 flow behavior in the wellbore during CO_2 fracturing. Moreover, the influence of thermal gradient on wellbore flow is not obvious within one block during CO_2 fracturing.



Figure 13. Effect of geothermal gradient: (a) CO₂ pressure profile; (b) CO₂ temperature profile.

5. Conclusions

A coupled model is proposed to predict the flow field of CO_2 fracturing in this paper. The model is based on compressible fluid flow equations and solved by coupling temperature and pressure with an iterative method. According to the calculated results, wellbore pressure, temperature, CO_2 properties, and phase state along depth are gained and a sensitivity study is conducted to analyze the controlling factors for CO_2 fracturing. The conclusions are as follows:

(1) The bottom hole pressure increases first and then decreases, and the bottom hole temperature decreases with an increase in displacement. The bottom hole temperature tends to keep a lower level under sustained high displacement, which has been verified in field tests.

(2) Both the pressure and temperature are highly coupled with physical properties of CO_2 . CO_2 turns from liquid state into supercritical state under low displacement, while it tends to maintain liquid state in the whole wellbore under high displacement.

(3) Under the temperature–pressure condition of CO_2 fracturing, the injection temperature has a greater impact on the wellbore flow behavior of CO_2 compared to the injection pressure, whereas excess injection temperature is adverse to pressure rising in the wellbore. Besides, the influence of thermal gradient on wellbore flow is not obvious within one block during CO_2 fracturing.

(4) Displacement is the key factor affecting CO_2 flow behavior in the wellbore during CO_2 fracturing.

Because of the good compressibility and high permeability of CO_2 , it is easy for CO_2 to intrude into the reservoir rock and cause rock damage. And the pressure and temperature distributions in

the wellbore significantly affect the fracture initiation and propagation in the reservoir. According to CO_2 flow behavior in the wellbore, the fracture initiation and propagation under the real bottom hole temperature–pressure condition can be analyzed for further research.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A. Semianalytical Method for Formation Heat Transfer

The Hasan Equation [33] is the most widely used semianalytical method for the unsteady heat transfer in the stratum.

The dimensionless temperature is used to represent the unsteady heat transmission of the formation in the Hasan Equation,

$$T_D = \begin{cases} 1.1281 \sqrt{t_D} \left(1 - 0.3 \sqrt{t_D} \right) & t_D \le 1.5 \\ (0.4063 + 0.5 \ln t_D) \left(1 + \frac{0.6}{t_D} \right) & t_D > 1.5 \end{cases}$$
(A1)

where $t_D = \frac{at}{R_e^2}$ is dimensionless time; *a* is thermal diffusion coefficient of formation, m²/s; *t* is time, s; R_e is radius of the interface between the formation and wellbore, m.

Appendix B. Thermal Resistance of Wellbore

In order to ensure the sand-carrying and fracturing scale, annulus synchronously injecting is the most used injection mode for CO₂ fracturing.

The expressions of thermal resistance between the stratum and annulus fluid, and between the annulus and tubing fluid, are as follows, respectively,

$$R_{ea} = \frac{T_D}{2\pi\lambda_e} + \left(\frac{1}{2\pi\lambda_{ca}}\ln\frac{d_{co}}{d_{ci}} + \frac{1}{2\pi\lambda_{ce}}\ln\frac{d_b}{d_{co}} + \cdots\right) + \frac{1}{h_{ao}\pi d_{ci}}$$
(A2)

$$R_{at} = \frac{1}{h_{ti}\pi d_{ti}} + \frac{1}{2\pi\lambda_t}\ln\frac{d_{to}}{d_{ti}} + \frac{1}{h_{to}\pi d_{to}}$$
(A3)

where T_D is dimensionless temperature, for characterizing the formation temperature distribution during the circulation; λ_e is the heat conductivity of formation, W/(m·K); h_{ao} is the heat convection coefficient of the outer wall in the annulus, W/(m²·K); h_{ti} is the heat convection coefficient of the inner wall of tubing, W/(m²·K); h_{to} is the heat convection coefficient of the outer wall of tubing, W/(m²·K); λ_{ce} is the heat conductivity of the cement ring, W/(m·K); λ_{ca} is the heat conductivity of casing, W/(m·K); λ_t is the heat conductivity of tubing, W/(m·K); d_b is the diameter of the barefoot hole, m; d_{ci} is the inner diameter of casing, m; d_{co} is the outer diameter of casing, m; d_{ti} is the inner diameter of tubing, m; d_{to} is outer diameter of tubing, m.

The heat convection coefficient can be obtained by calculating the fluid Nusselt number. The expressions of Nu at the inner wall of tubing, Equation (A4), outer wall of tubing, Equation (A5), and outer wall of annulus, Equation (A6), are as follows.

$$Nu = 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^n \tag{A4}$$

$$Nu_{De} = 0.02 \text{Re}^{0.8} \text{Pr}^n \left(\frac{D_2}{D_1}\right)^{0.53}$$
(A5)

$$Nu_{De} = 0.023 \text{Re}^{0.8} \text{Pr}^{1/3} \left(\frac{D_2}{D_1}\right)^{0.45}$$
(A6)

where Pr is Prandtl number, dimensionless; D_1 and D_2 are the inner and outer diameters of the annular, m, respectively. All the expressions of Nu are derived from the Dittus–Boelter formula [34].

With the sufficient displacement of CO_2 fracturing, the thermal resistance between the stratum and annulus fluid is much smaller than that between the annulus and tubing fluid, according to the calculation, R_{at} is less than 1% of R_{ea} . Therefore, the temperature difference between the fluid in the annulus and tubing can be ignored (i.e., the fluid temperature in the wellbore can be regarded as a whole).

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