



Article Control of Wave Energy Converters with Discrete Displacement Hydraulic Power Take-Off Units

Shangyan Zou * 🕑 and Ossama Abdelkhalik

Department of Mechanical Engineering, Michigan Technological University, 1400 Townsend Dr, Houghton, MI 49931, USA; ooabdelk@mtu.edu

* Correspondence: szou2@mtu.edu; Tel.: +906-281-8230

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Abstract: The control of ocean Wave Energy Converters (WECs) impacts the harvested energy. Several control methods have been developed over the past few decades to maximize the harvested energy. Many of these methods were developed based on an unconstrained dynamic model assuming an ideal power take-off (PTO) unit. This study presents numerical tests and comparisons of a few recently developed control methods. The testing is conducted using a numerical simulator that simulates a hydraulic PTO. The PTO imposes constraints on the maximum attainable control force and maximum stroke. In addition, the PTO has its own dynamics, which may impact the performance of some control strategies.

Keywords: wave energy conversion; PTO units; hydraulic PTO; WEC control

1. Introduction and Background

The control of ocean WECs has received a great deal of attention over the past several decades. In recent years in particular there have been significant developments with respect to maximizing the harvested energy from WECs from a control system analysis and design perspective. Many of these control methods were proposed for ideal conditions in the absence of stroke or force limitations, and assuming ideal power take-off (PTO) units. This paper presents comparisons between some recently developed control methods; these simulations include a model for a hydraulic PTO, which consequently imposes constraints on the displacement of the buoy and on the maximum possible control force. These simulations also highlight some insight regarding the needed reactive power for some of the discussed control methods. Several earlier controllers were developed in [1–3] for WECs with hydraulic PTOs. A hydraulic system was validated using AMEsim in [4]. The control methods discussed in this paper are tested using hydraulic PTOs for the first time in this paper.

This section presents a review of hydraulic PTO units. Figure 1 is a general layout for a typical hydraulic PTO. The hydraulic system is composed of the actuator, the valve, the accumulators and the motor. The motion of the buoy will compress/decompress the chamber of the actuator and transfer the wave power to the hydraulic system. All the hydraulic systems can be categorized into three main groups: the constant-pressure, the variable-pressure, and the constant-variable pressure hydraulic systems [5,6].

1.1. Constant Pressure Configuration

The first configuration is constructed with a low-pressure (LP) accumulator and a high-pressure (HP) accumulator. This type of hydraulic system can be achieved with a simple mechanism, and the control level is low.

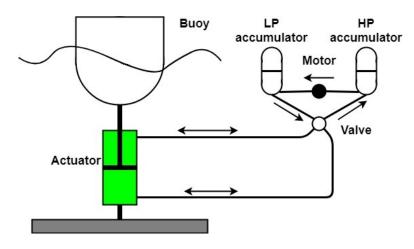


Figure 1. General layout for a hydraulic power take-off (PTO).

The typical configuration of a constant-pressure hydraulic system is presented in detail in [7,8], using phase control. Control of the constant-pressure hydraulic system is achieved by implementing auxiliary accumulators in [3]. The latching and declutching controls are demonstrated in [9] using a constant-pressure hydraulic system. Additionally, a declutching control is presented in [10] for controlling a hydraulic PTO by switching on and off using a by-pass valve. The method is also tested with the SEAREV WEC with an even higher energy absorption. A detailed image of a single acting hydraulic PTO system with the phase control is presented in [11,12]. The hydraulic system implemented in SEAREV is presented in [13]. In [14], a novel model of the hydraulic PTO of the Pelamis WEC is developed, with the ability to apply reactive power for impedance matching. In [15], a double-action WEC with an inverse pendulum is proposed. The authors of [15] report that a double-action PTO can supply the output power in each wave period without large instantaneous fluctuating power. A double-acting hydraulic cylinder array is developed in [16], where the model is found to be adaptive to different sea states to achieve higher energy extraction. The authors of [17] present the optimization of a hydraulic PTO of a WEC for an irregular wave where optimal damping is achieved by altering the displacement of the variable-displacement hydraulic motor. The authors of [18] present the design and testing of a hybrid WEC that obtains higher energy absorption than a single oscillating body with a hydraulic PTO. A discrete-displacement hydraulic PTO system is studied in [19] for the Wavestar WEC. An energy conversion efficiency of 70% is achieved. Additionally, adjustment of the force applied by the PTO is accomplished through implementing multiple chambers.

1.2. Variable Pressure

A variable-pressure hydraulic system is suggested in [20–22]. In this situation, the piston is connected directly to a hydraulic motor. This system can achieve better controllability, but the fluctuation of the output power is not negligible. Two hydraulic PTO systems are compared in [23], where constant-pressure hydraulic PTO and variable-pressure hydraulic PTO systems are compared. It was shown that a variable-pressure hydraulic PTO system would have a higher efficiency. The variable-pressure approach was also investigated in [24], where the hydraulic motor is used in order to remove the accumulator and control the output using the generator directly. A comparison between a constant-pressure system and a variable-pressure system was conducted in [25]; validation was conducted using AMEsim and demonstrated a good agreement. Power smoothing was achieved in [26] by means of energy storage.

1.3. Variable–Constant Pressure

The variable–constant pressure hydraulic system is constructed with two parts: the variable pressure part and the constant pressure part. The variable pressure part is accomplished by a

hydraulic transformer. A generic oil hydraulic PTO system, applied to different WECs, is introduced in [27]. The authors of [28] developed a PID controller, with the reactive power supplied by the hydraulic transformer (working as a pump). A suboptimal control is suggested in [28] for practical implementation in terms of the efficiency of the PTO.

2. WEC Dynamics

In this section, the WEC dynamic model used in this paper is briefed. In this paper, the floater used in the simulations is the Wavestar absorber [9]. The floater has a single degree of freedom motion which is the pitch rotation. The geometry of the proposed absorber is depicted in Figure 2.

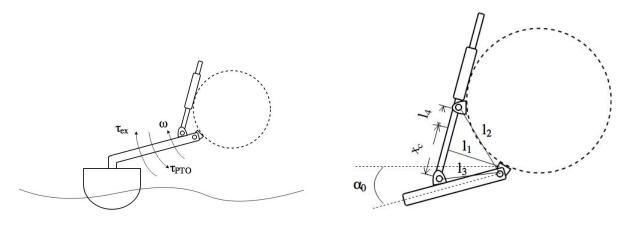


Figure 2. The geometry of the Wavestar absorber.

The WEC dynamic model can be described based on linear wave theory by Equations (1) to (9):

$$J_{rigid}\ddot{\theta} = \tau_{ex} + \tau_{res} + \tau_{rad} - \tau_G - \tau_{PTO} \tag{1}$$

where J_{rigid} is the moment of inertia of the rigid body. θ is the pitch rotation of the floater. τ_{ex} is the wave excitation torque acting on the buoy, τ_{res} is the restoring momentum, τ_{rad} is the radiation torque, and τ_G is the torque caused by the gravity. The PTO torque is τ_{PTO} which is applied by the hydraulic cylinder. The equation of motion can be further expanded as:

$$\ddot{\theta} = \frac{1}{J_{rigid} + J_{\infty}} (\tau_{ex} - \tau_{PTO} - K_{res}\theta - h_r * \dot{\theta})$$
⁽²⁾

where J_{∞} is the moment of the added mass at infinite frequency, K_{res} is the coefficient of the hydro-static restoring torque, and h_r is the radiation impulse response function. In Equation (2), the radiation torque is expanded as:

$$\tau_{rad} = -J_{\infty}\ddot{\theta} - \tilde{\tau}_{rad} \tag{3}$$

$$\tilde{\tau}_{rad} = h_r * \dot{\theta} \tag{4}$$

The * operation is the convolution between the impulse response function and the angular velocity $\dot{\theta}$ which can be approximated by a state space model as:

$$\dot{x}_r = A_r x_r + B_r \dot{\theta} \tag{5}$$

$$\tilde{\tau}_{rad} = C_r x_r + D_r \theta \tag{6}$$

$$\tau_{ex} = h_{ex} * \eta \tag{7}$$

Hence, the convolution can also be approximated by a state space model as:

$$\dot{x}_e = A_e x_e + B_e \eta \tag{8}$$

$$\tau_{ex} = C_e x_e \tag{9}$$

where A_e , B_e , and C_e are the excitation matrices which are identified from the excitation impulse response function. The parameters of the floater are listed in Table 1. The viscous damping is not considered in the proposed dynamic model because it is assumed to be negligible based on linear wave theory. In this designed study the extreme wave motion will not be achieved due to the limited capacity of the PTO unit. As a result, the small wave assumption can be held. The frequency response of the proposed WEC dynamic model without control is shown in Figure 3.

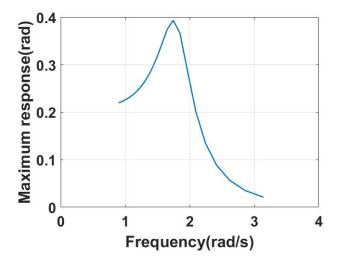


Figure 3. The frequency response of the dynamics of the Wavestar absorber.

3. The Hydraulic PTO System

In this paper, the Discrete Displacement Cylinder (DDC) hydraulic system is used to apply the PTO torque. A simplified illustration for this system is shown in Figure 4. More details about the DDC hydraulic system can be found in [19].

As shown in Figure 4, the DDC hydraulic system is mainly composed of the actuator/cylinder, the manifold valves, the manifold accumulators, and the generator. The PTO torque is computed in the Equation (10) as the product of the cylinder force and the moment arm:

$$\tau_{PTO} = F_c l_1 \tag{10}$$

where the moment arm can be expressed by Equation (11):

$$l_1 = \frac{l_2 l_3 \sin(\theta - \alpha_0)}{x_c + l_4}$$
(11)

$$x_c = -l_4 + \sqrt{-2l_2 l_3 \cos(\theta - \alpha_0) + (l_2^2 + l_3^2)}$$
(12)

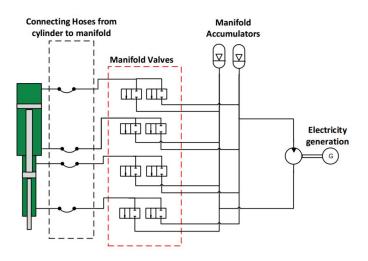


Figure 4. The layout of the Discrete Displacement Cylinder (DDC) hydraulic system.

3.1. The Hydraulic Cylinder

The actuator force F_c is generated by the hydraulic cylinder and can be computed by Equations (13) and (14):

$$\tilde{F}_c = -p_{A1}A1 + p_{A2}A2 - p_{A3}A3 + p_{A4}A4$$
(13)

$$F_c = \tilde{F}_c - F_{fric} \tag{14}$$

where p_{Ai} is the pressure of the *i*th chamber and Ai is the area of the piston. F_{fric} is the cylinder friction force. The dynamics of the chamber pressure can be described by flow continuity Equations (15) to (18):

$$\dot{p}_{A1} = \frac{\beta(p_{A1})}{A1(x_{c,max} - x_c) + V_{0,A1}} (Q_{A1} - v_c A1)$$
(15)

$$\dot{p}_{A2} = \frac{\beta(p_{A2})}{A2x_c + V_{0,A2}} (Q_{A2} + v_c A2) \tag{16}$$

$$\dot{p}_{A3} = \frac{\beta(p_{A3})}{A3(x_{c,max} - x_c) + V_{0,A3}}(Q_{A3} - v_c A3)$$
(17)

$$\dot{p}_{A4} = \frac{\beta(p_{A4})}{A4x_c + V_{0,A4}} (Q_{A4} + v_c A4)$$
(18)

where $V_{0,A1}$, $V_{0,A2}$, $V_{0,A3}$, and $V_{0,A4}$ are the volumes of the connecting hoses of different chambers. $x_{c,max}$ is the maximum stroke of the cylinder. x_c and v_c are the position and velocity of the piston, respectively, which are defined positive down. $\beta(p_{Ai})$ is the effective bulk modulus of the fluid based on different pressures, and is assumed to be constant in this study. Additionally, Q_{Ai} is the flow from the connecting hose to the *i*th chamber. The cylinder friction is expressed by Equation (19):

$$F_{fric} = \begin{cases} \tanh(av_c) \mid \tilde{F}_c \mid (1 - \eta_c), & \text{if } F_c v_c > 0\\ \tanh(av_c) \mid \tilde{F}_c \mid (\frac{1}{\eta_c} - 1) & \text{otherwise} \end{cases}$$
(19)

where *a* is the coefficient used to smooth the friction curve versus velocity. η_c is a constant efficiency of the cylinder.

3.2. The Hoses

The hoses connected between the cylinder and the manifold valves are modeled by Equations (20) and (21) which refer to [19]:

$$\dot{Q}_{out} = \frac{(p_1 - p_2)A_{hose} - p_f(Q_{out})A_{hose}}{\rho l_{hose}}$$
(20)

$$\dot{p}_1 = \frac{(Q_{in} - Q_{out})\beta}{A_{hose}l_{hose}} \tag{21}$$

where Q_{in} and Q_{out} are the fluid flows in and out of the hose, and p_1 and p_2 are the pressures of the inlet and outlet of the hose, respectively. A_{hose} is the area of the hose, l_{hose} is the length of the hose, ρ is the fluid density, and $p_f(Q_{out})$ is the pressure drop across the hose. The pressure drop across a straight pipe/hose can be modeled by the equation:

$$p_{\lambda} = \frac{0.3164 l_{hose} \rho}{2Re^{0.25} d_{hose}} \frac{Q_{out} | Q_{out} |}{(0.25d_{hose}^2 \pi)^2} (0.5 + 0.5 \tanh(\frac{2300 - Re}{100})) + \frac{128 \nu \rho l_{hose} Q_{out}}{\pi d_{hose}^4} (0.5 + 0.5 \tanh(\frac{-2300 + Re}{100}))$$
(22)

where ν is the kinematic viscosity of the fluid. *Re* represents the Reynold number which can be computed by Equation (23):

$$Re = \frac{v_{out} d_{hose}}{v}$$
(23)

Equation (22) combines the pressure loss of the laminar flow and the turbulent flow by the hyperbolic-tangent expression. Consequently, a continuous transition of the pressure loss between the laminar and turbulent flow can be created. When the Reynold number is less than 2200, $(0.5 + 0.5 \tanh(\frac{2300-Re}{100}))$ is close to zero, which means the pressure drop is contributed by the laminar flow. On the other hand, when the Reynold number is greater than 2400, $(0.5 + 0.5 \tanh(\frac{-2300-Re}{100}))$ is close to zero, which means the pressure drop is contributed by the laminar flow. Another source of pressure drop is the fitting loss, which can be computed by Equation (24):

$$p_{\zeta} = \zeta \frac{\rho}{2} Q_{out} \mid Q_{out} \mid \frac{1}{(0.25d_{hose}^2 \pi)^2}$$
(24)

where ζ is the friction coefficient for a given fitting type. Finally, the total resistance in the hose with *n* line pieces and *m* fittings can be computed by Equation (25):

$$p_f(Q_{out}) = p_{\lambda,1}(Q_{out}) + \dots + p_{\lambda,n}(Q_{out}) + p_{\zeta,1}(Q_{out}) + \dots + p_{\zeta,m}(Q_{out})$$
(25)

In this paper, the pressure loss of the hoses is modeled by the Equation (26):

$$p_f(Q_{out}) = p_\lambda(Q_{out}) + p_{\zeta,M}(Q_{out}) + p_{\zeta,C}(Q_{out})$$
(26)

where $p_{\zeta,M}$ represents the fitting resistance which considers the internal pressure drops in the manifold and $p_{\zeta,C}$ represents the cylinder inlet loss.

3.3. The Directional Valves

The two-way two-position directional valves are used in this model. The flow across the valve can be described by the following orifice Equation (27):

$$Q_{v} = sign(\Delta p)C_{d}A_{v}(\alpha)\sqrt{\frac{2}{\rho} \mid \Delta p \mid}$$
(27)

where Δp is the pressure difference cross the valve, C_d is the discharge coefficient, and $A_v(\alpha)$ is the opening area which can be computed by Equations (28)–(30):

$$A_v(\alpha) = \alpha A_0 \tag{28}$$

$$\dot{\alpha} = \begin{cases} \frac{1}{t_v}, & \text{if } u_v = 1\\ -\frac{1}{t_v}, & \text{if } u_v = 0 \end{cases}$$
(29)

$$0 \leqslant \alpha \leqslant 1 \tag{30}$$

where A_0 is the maximum opening area of the valve. In this paper, a total of eight valves are used to control the actuator force. The t_v represents the opening and closing time of the valve. The shifting algorithm of the valve applied in this paper can be further improved [29] to reduce the pressure oscillations and improve the energy efficiency. Moreover, the different opening time has a significant impact on the cylinder pressure [30]. The opening time t_v is selected to be 30 ms in this paper to avoid the cavitation or pressure spikes and to have a relatively fast response to the reference control command. Since the focus of this paper is to examine the controllers' performance practically, the influence of different opening times is not investigated in this paper.

3.4. The Pressure Accumulators

The accumulators in the DDC system are used as pressure sources and also for energy storage. The dynamics of the pressure accumulator can be modeled with the Equations (31)–(33) [19]:

$$\dot{p}_{acc} = \frac{Q_{acc} + \frac{1}{1 + \frac{R}{C_v}} \frac{V_g}{T} \frac{1}{\tau_a} (T_w - T)}{\frac{V_{a0} - V_g + V_{ext}}{\beta} + \frac{1}{1 + \frac{R}{C_v}} \frac{V_g}{p_{acc}}}$$
(31)

$$\dot{V}_g = -Q_{acc} + \dot{p}_{acc} \frac{V_{a0} - V_g + V_{ext}}{\beta}$$
(32)

$$\dot{T} = \frac{1}{\tau_a} (T_w - T) - \frac{RT}{C_v V_g} \dot{V}_g$$
(33)

where p_{acc} is the pressure of the accumulator, Q_{acc} is the inlet flow to the accumulator, R is the ideal gas constant, C_v is the gas specific heat at constant volume, T_w is the wall temperature, τ_a is the thermal time constant, β is the bulk modulus of the fluid in the pipeline volume V_{ext} , V_{a0} is the size of the accumulator, V_g is the gas volume, and T is the gas temperature. Hence the state of the accumulator contains the pressure, the gas volume and the gas temperature. Initially, the state can be specified based on the standard gas law by Equation (34):

$$V_g = \frac{T}{T_0} \frac{p_{a0}}{p_a} V_{a0}$$
(34)

where p_{a0} is the pre-charged pressure of the gas at the temperature T_0 .

3.5. The Hydraulic Motor

For the system presented in this paper, there are 4 chambers and 2 different pressures: the high pressure and the low pressure. The hydraulic motor is connected between the high pressure accumulator and the low pressure accumulator. The flow of the hydraulic motor can be modeled by Equation (35):

$$Q_M = D_w \omega_M - \Delta p C_{Q1} \tag{35}$$

where D_w is the displacement of the hydraulic motor, which is constant for a fixed displacement motor, Δp is the pressure across the motor, C_{Q1} is the coefficient of the flow loss of the motor, and ω_M is the rotational speed of the motor which is defined by Equation (36):

$$\omega_M = \frac{p_{avg,exp}\psi}{p_H k_{gen} D_M} \tag{36}$$

where $p_{avg,exp}$ is the expected average power output, p_H is the pressure of the high pressure accumulator, k_{gen} is the number of generators, D_M is the total motor displacement, and ψ is a coefficient for the motor speed control to prevent the high pressure from depletion or saturation which is formulated by Equations (37) and (38):

$$k = \frac{4}{\left(p_{H,max} - p_{H,min}\right)} \tag{37}$$

$$\psi = \begin{cases} k(p_H - p_{H,min}), & \text{if } p_H > p_{H,min} \\ 0, & \text{otherwise} \end{cases}$$
(38)

To achieve the desired motor speed introduced in Equation (36), the generator torque control needs to be included. In this paper, the generator and inverter are not modeled and the desired motor speed is assumed achievable. The power in the hydraulic motor can be computed by Equation (39):

$$P_M = \Delta p Q_M \tag{39}$$

This completes the modeling of DDC hydraulic system; the control algorithm is introduced in the next section.

4. The Control Algorithm

Two parts will be presented in this section: the control method for the buoy and the force-shifting algorithm for controlling the valves. The control method for controlling the buoy computes a reference value for the control force at each time step. This reference control force is then used as an input to the PTO, and the actual control force that results from the PTO is computed using the force-shifting algorithm. Each of the two parts is detailed below.

4.1. The Buoy Control Method

Several control methods will be tested in this paper using a simulator that simulates the PTO unit. Some of these controller were originally developed for heave control. It is relatively straightforward, however, to extend a control method from the heave motion to the pitch motion. For example, the singular arc (SA) control method [31] can be used to compute the control torque by the following Equation (40):

$$\tau_{PTO}(s) = \frac{N(s)}{D(s)} \tag{40}$$

where:

$$N(s) = (J_{total}s^{2} + (C_{r}(sI + A_{r})^{-1}B_{r} - D_{r})s + K_{res})\tau_{ex}(s)$$

$$D(s) = s(C_{r}(sI + A_{r})^{-1}B_{r} - C_{r}(sI - A_{r})^{-1}B_{r} - 2D_{r})$$
(41)

where the excitation torque can be expressed as Fourier series expansion by Equation (42):

$$\tau_{ex} = \sum_{i=1}^{n} \Re(\tau_{c,ex}(\omega_i)\eta(\omega_i)e^{i(-\omega_i t + \phi_i)})$$
(42)

An inverse Laplace transformation is then applied to the SA control to obtain the control in the time domain. The required information to compute the control is the time *t*, the excitation torque coefficient $\tau_{c,ex}$, the wave frequency vector $\vec{\omega}$ and the time domain phase shift vector $\vec{\phi}$.

A reference control method is the feedback proportional-derivative (PD) control. The PD control takes the form of Equation (43):

$$\tau_{PTO} = K\theta + B\dot{\theta} \tag{43}$$

where *K* is the proportional gain and *B* is the derivative gain.

In addition to the above two control methods, simulated in this paper are model predictive control (MPC) [32], shape-based (SB) control [33], proportional-derivative complex conjugate control (PDC3) [34], and pseudo-spectral (PS) control [35]. Each one of these methods is well documented in the literature, so the details of each control methods are avoided in this paper.

In the original developments, the SA control and the PDC3 control compute a control force that is equivalent to the complex conjugate control (C3), and hence the maximum possible harvested energy in the linear domain. However, the C3 does not account for constraints on the buoy displacement. In fact, since the C3 criterion is to resonate the buoy with the excitation force, the motion of the buoy always violates displacement constraints when controlled using the SA and PDC3 controls. On the other hand, the MPC, SB, and PS control methods compute a control force in an optimal sense, taking displacement constraints into account. Figure 5 shows a simulation for 5 min for the above six control methods when a constraint on the buoy displacement is assumed. The simulation parameters are detailed in Section 5. This simulation does not account for the PTO dynamics and is here presented to highlight the impact of including the PTO into the simulations in Section 5. As can be seen from Figure 5, among the six control methods, the MPC and PD controls performed best, then the SB method, then the PS, and then the PDC3 and SA methods. The two methods (SA and PDC3) that perform best without displacement constraints actually have the poorest performance when accounting for the constraints.

4.2. The Force-Shifting Algorithm

The force-shifting algorithm (FSA) is introduced in this section. The FSA used in this paper is described by Equation (44):

$$\{F_{c}(t) = \vec{F}[k] \mid k = arg \ min \mid F_{ref}(t) - \vec{F}[k] \mid\}$$
(44)

where F_{ref} is the reference control force (computed for instance using one of the six control methods described above), and \vec{F} is the vector of the possible discrete values for the force. With different permutations of valve openings, it is possible to produce different levels of constant forces, as shown in Figure 6, where it is assumed that $p_H = 200$ bar and $p_L = 20$ bar. The FSA selects the discrete force level that is closest to the reference control force. It is noted here that the discrete force changes over time due to the fluctuation of the pressures in the accumulators.

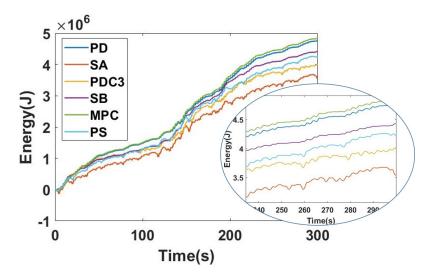


Figure 5. When accounting for displacement constraints, some unconstrained methods harvest less energy. PD: proportional-derivative; SA: singular arc; PDC3: proportional-derivative complex conjugate control; SB: shape-based; MPC: model predictive control; PS: pseudo-spectral.

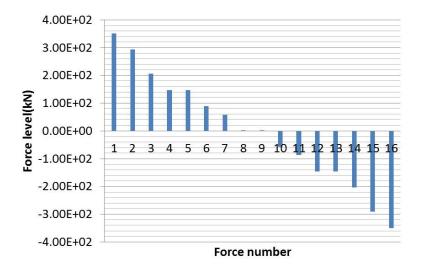


Figure 6. An example for all discrete possible values for a PTO force.

5. Simulation Tool

A tool for simulating the dynamics of the WEC including the motion dynamics, the hydrodynamic/hydrostatic force calculations, and the PTO hardware model was developed in MathWorks Simulink[®]. The detailed Simulink model of the wave energy conversion system is shown in Figure 7. The Plant block simulates the dynamics of the buoy. The PTO block simulates all the equations of the valves, hoses, and accumulators. As can be seen in Figure 7, the excitation force is an input that is computed outside the Plant block. The control force command is computed in the block 'Control Command'. Despite the name, six different controllers were tested in the 'Control Command' block. A detailed Simulink model of the hydraulic system is shown in Figure 8, this model is inside the PTO block in Figure 7.

The parameters of the dynamic model of the wavestar used in the simulations in this paper are listed in Table 1.

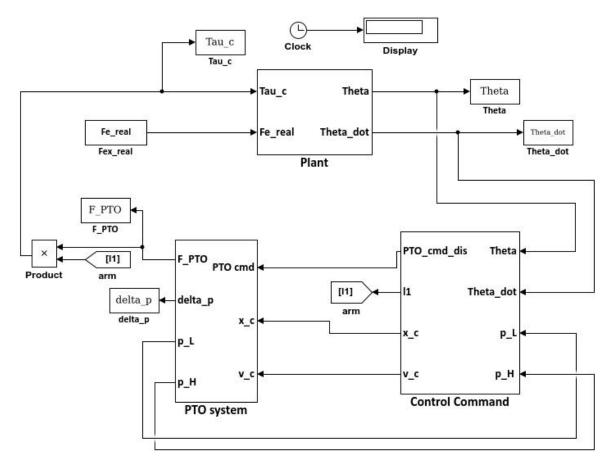


Figure 7. The Simulink model of the wave energy conversion system.

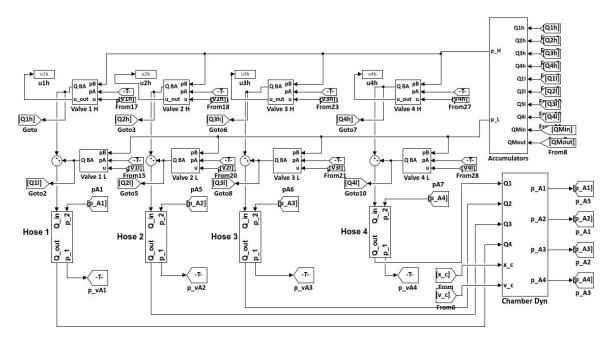


Figure 8. The Simulink model of the hydraulic PTO system.

Symbol	Value	Unit
Jtot	$3.8 imes10^6$	kg m ²
K _{res}	$14 imes 10^6$	Nm/rad
The transfer function $H_r(s)$		
$(b_0, b_1,, b_5)$	*	
$(a_0, a_1,, a_5)$	**	
The transfer function $H_{ex}(s)$		
(b_0, b_1)	***	
$(a_0, a_1,, a_4)$	****	

Table 1. Model parameters for the Wavestar.

5.1. Wave Model

Irregular waves are simulated in this study using the stochastic Pierson–Moskowitz (PM) spectrum. The spectral density is defined by Equation (45):

$$S(\omega) = \frac{5H_{m0}^2}{\omega_p \omega_n^5} e^{-\frac{5}{4\omega_n^4}}$$
(45)

where $\omega_n = \omega/\omega_p$, ω_p is the peak frequency, and H_{m0} is the significant height of the wave. The wave used in the simulation has a significant height of 1.75 m and a peak period 5.57 s. The reason to select the PM spectrum is because it is a more conservative choice by considering the power absorption estimation. The JONSWAP spectrum, which is frequently applied, has a narrow frequency band. However, the PM spectrum has a wider frequency band which makes the energy extraction more difficult. Consequently, the PM spectrum is applied in this paper to prevent overestimation of the performance of the controller. With regard to the significant height and peak period applied in the simulation, they are selected from the validated wave climate in [9,36] for the Wavestar C5. The proper range so that the wave for C5 can have major energy absorption is with a significant height from 0.5 m to 3 m and peak period from 2 s to 7 s. The wave climate applied in this paper is in the middle of the range to avoid losing generality.

5.2. The System Losses

The system losses are computed in this study. The system losses include the pressure loss of the hoses, the flow loss of the generator, and the friction of the cylinder. The pressure loss is shown in Figure 9, in which the vertical line represents the transition between the laminar flow and the turbulent flow when the Reynold number is Re = 2300, for each of the two possible directions of the fluid flow. The amount of the flow loss and the friction force of the cylinder are shown in Figures 10 and 11. All the system parameters used in the simulations in this paper are listed in Table 2.

6. Simulation Results

The above Simulink tool is used to simulate the performance of the above six control methods. The energy extracted by method is shown in Figure 12. In this simulation, there are limitations on the maximum stroke and the maximum control force. In addition, the PTO dynamics are simulated. The maximum control force in the cylinder in the simulations presented in this paper is assumed to be 215 kN. The maximum allowable displacement in the simulations presented in this paper is assumed to be 1.2 m. As can be seen in Figure 12, the MPC and PD control methods harvest the highest energy level compared to the other methods. The SB method comes next. The SA, PDC3, and PS control methods come next, and the three of them perform about the same. For further analysis of the performance of the controllers, the capture width ratio (CWR) is evaluated:

 $[\]label{eq:constraint} \begin{array}{l} * = (0.0001, 0.0144, 0.624, 8.16, 13.1, 1.44) \times 10^6; \\ *** = (0.001, 0.0906, 1.67, 6.31, 13.3, 9.18); \\ **** = (0.036, 0.39, 1.5, 2.6, 1.6). \end{array}$

$$CWR = \frac{P_{ave}}{DP_w} \tag{46}$$

where P_{ave} is the average power extraction of the buoy, P_w is the wave energy transport, and D is the characteristic dimension of the buoy. The CWRs of the MPC, PD, SB, SA, PDC3, and PS controllers are 51.21%, 50.92%, 44.68%, 37.60%, 37.14%, and 36.86% respectively. According to the [36], the CWR of the performance of the floater with the applied wave ranges from 40% to 50%. Hence, the performance of the proposed controllers is in the reasonable range in terms of energy extraction. Comparing Figure 12 to Figure 5 we can see that by including the PTO model, the performance of the SA method improves slightly, while the performance of the PS degrades slightly, and as a result the three methods PS, SA, and PDC3 perform about the same. The performance of the MPC, PD, and SB control methods actually slightly improve when the PTO model is included.

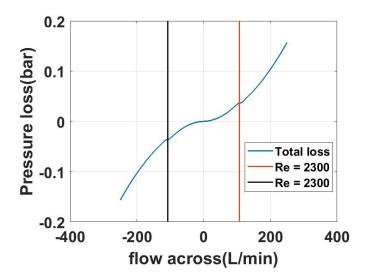


Figure 9. The pressure loss of the hose which has a 1-m length and 3.81×10^{-2} m diameter with different flow rates across the hose.

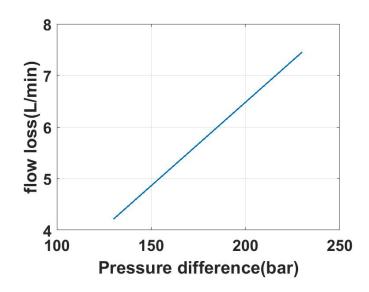


Figure 10. The flow loss of the generator.

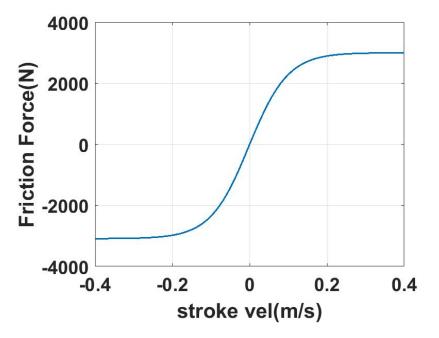


Figure 11. The friction force of the cylinder with different velocities when the cylinder force is 100 kN.

Another important result to examine is the output mechanical power at the actuator and the output power from the generator. These two quantities are compared in Figure 13. From the figure we can tell that the power absorbed in the generator side is much smoother than the power extracted by the actuator. The hydraulic accumulators act as a power capacitor for energy storage, resulting in this relatively smooth power profile at the generator output. As can be seen in the figure also, the actuator power includes reactive power; these are the times at which the actuator power is negative. At these times, the PTO actually pumps power into the ocean through the actuator. The generator output power does not have any reactive power, confirming that all the reactive power come from the accumulators.

The efficiency of the system is defined by Equation (47):

$$\eta_{out} = \frac{P_{gen}}{P_{actuator}} \tag{47}$$

The efficiency depends on the control method. For example, in this test case, the efficiency of the SB controller is 80.15%, for the MPC it is 72.58%, for the PS it is 67.34%, for the SA it is 64.36%, and for the PD controller it is 71.76%, over 300 s.

In the context of comparing the performance of different control methods, it is important to highlight one significant difference between them that emanates from the theory behind each control method. Each of the MPC, SB, and PS control methods requires wave prediction. That is, wave information (or excitation force) is needed over a future horizon at each time step in the simulation. In the simulations in this paper, this future horizon is assumed to be 0.6 s for the SB and MPC control methods, and is assumed to be 60 s for the PS control. Wave prediction is assumed perfect in these simulations. Non-perfect wave prediction would affect the results obtained using these methods. The PD, SA, and PDC3 control methods do not need future wave prediction.

This simulation tool also provides detailed operation information that is useful for characterizing different components in the system. For example, the generator speed is computed in the simulation, and is shown in Figure 14. As shown in the figure, the speed is oscillating around 1200 RPM.

Symbol	Value	Unit
Length of the arms		
<i>l</i> ₂	3	m
<i>l</i> ₃	2.6	m
l_4	1.6	m
Length of the hoses C2M		
l _{A1}	1	m
l_{A2}	1	m
l_{A3}	1	m
l _{A4}	1	m
Diameter of the hoses C2M		
d_{A1}	1.5	in
d_{A2}	1.5	in
d_{A3}	1.5	in
<i>d</i> _{A4}	1.5	in
Maximum stroke		
x _{c,max}	3	m
Area of the chambers		
A_1	$113.4 imes 10^{-4}$	m ²
<i>A</i> ₂	$32.55 imes 10^{-4}$	m ²
A_3	$80.85 imes 10^{-4}$	m ²
A_4	162.75×10^{-4}	m ²
Max Area of the valves		
A ₀₁	$1.6 imes10^{-4}$	m ²
A ₀₂	$1.6 imes10^{-4}$	m ²
A ₀₃	$1.6 imes10^{-4}$	m ²
A_{04}	$1.6 imes 10^{-4}$	m ²
Accumulator size		
V _{a0}	$100 imes 10^{-3}$	m ³
Pressure drop coef		
ζ _M	1.3	
ζς	1	
Specific time constant S		
τ_l	23	S
$ au_h$	34	S
Initial pressure of the accumulators		
p _{a,l}	20	bar
p _{a,h}	130	bar
Initial angle		
α ₀	1.0821	rad
Control parameters		
K	$-9.16 imes 10^6$	Nm/rad
В	$4.4 imes10^6$	Nms/rac
Valve opening time		
t_v	30×10^{-3}	s
	*	-

Table 2. The data used in the simulation of the overall WEC system.

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Symbol	Value	Unit
Wall temperature		
T _w	50	°C
Ideal gas constant		
R	276	J/kg/K
Gas specific heat at constant volume		
	760	J/kg/K
Motor displacement		
D_w	100	cc/rev
Flow loss coefficient		
<i>C</i> _{Q1}	$5.4 imes 10^{-12}$	m ³ /s/Pa
Fluid bulk modulus		
β	$1.5 imes10^9$	Pa

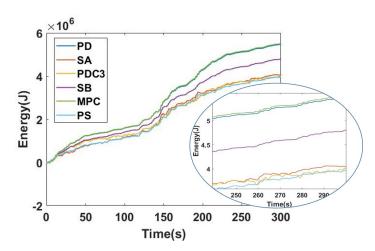


Figure 12. The energy extracted accounting for displacement and force constraints, including the hydraulic system dynamics model.

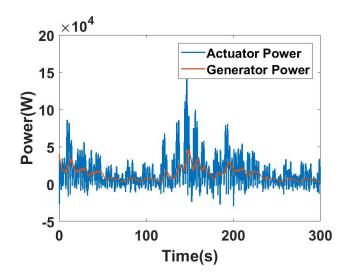


Figure 13. The power extracted by the actuator and the generator.

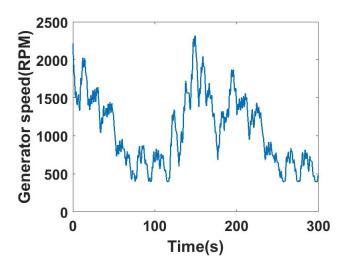


Figure 14. The generator speed.

To present detailed plots for the response of the buoy, only one control method is selected as a sample to avoid excessive figures in the paper. The SB method is selected here to present the detailed WEC response in this section. The angular displacement of the buoy is shown in Figure 15; the maximum angular displacement is about 10 degrees and it is below 5 degrees most of the time. The angular velocity of the buoy is shown in Figure 16. The cylinder force and the PTO torque are shown in Figures 17 and 18, respectively. Both the reference and actual values are plotted in each of the two figures. As can be seen in Figure 17, the control force is below the force limit of 215 kN. The accumulator pressure is shown in Figure 19. The high pressure is oscillating around 100 bar, while the low pressure is stable around 20 bar. The chamber pressure is shown in Figure 20. Significant fluctuations can be observed when the hydraulic system is extracting energy. This is necessary to be able to track the reference control command effectively. However, those fluctuations may be reduced by increasing the valve opening area or including relief valves.

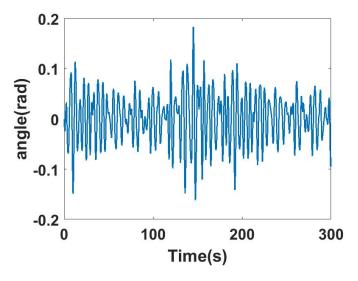


Figure 15. The rotational angle.

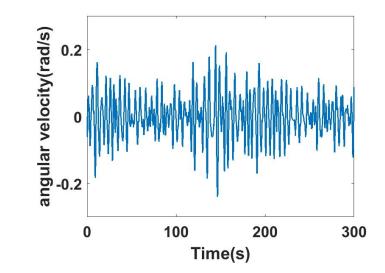


Figure 16. The angular velocity.

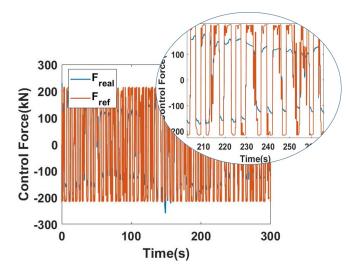


Figure 17. The cylinder force.

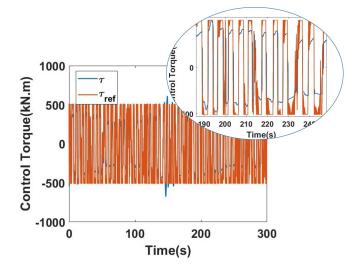


Figure 18. The PTO torque.

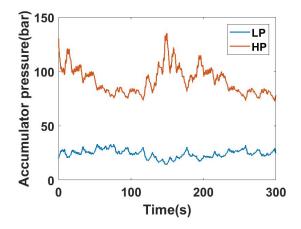


Figure 19. The pressure of the accumulator.

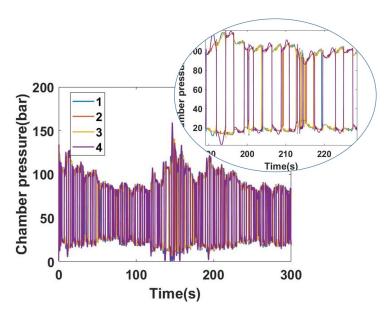


Figure 20. The chamber pressure.

7. Discussion

In this paper, different recent control methods are tested using a simulation tool that simulates a hydraulic PTO system. In a theoretical test (where PTO is assumed to track the reference control command ideally and in the absence of all constraints,) the SA controller has the best performance in terms of energy extraction. However, the performance of the SA controller with the hydraulic system model included is the poorest among the tested six control methods. To get more insight into this phenomenon, consider Table 3 that presents data for three controllers (SA, PD, and PDC3) in the theoretical test case. As can be seen in Table 3, the energy extracted by the PD controller in this theoretical test is about 60% of that of the SA controller. However, the buoy maximum displacement associated with the SA control is significantly greater than that of the PD control (almost three times higher) which makes it more difficult to achieve. Similarly, the maximum control force required by the SA control is significantly greater than that of the PD control, which means a PTO might not be able to track the command force at all times when using a SA control, while it is more likely to track a command force generated using a PD control. The data of the PDC3 control in Table 3 also highlights that the PDC3 control in this test case generates about the same level of average power, but in a higher displacement range and with higher force capability. This indicates that including a model for the PTO would result in favorable performance for the PD control compared to the PDC3. To highlight

the impact of the PTO model on the performance of the different control strategies, consider Table 4. The data are presented for all the six control methods. As can be seen from Table 4, all the control methods reached the maximum possible control capacity allowable by the PTO. Since this maximum control force is well below that needed by the SA in Table 3, the amount of harvested energy in this practical case is significantly less than that computed in the theoretical case (13.49 kW compared to 35.11 kW in average power). The drop in energy harvested using the PD control however is less since the maximum force needed theoretically was as high as that of the SA. The displacement of the PDC3 reached the maximum displacement allowable by the WEC (1.2 m.) This is expected since the PDC3 tends to increase the displacement and hence it would reach a limit imposed by the WEC system.

Symbol	Value	Unit
The SA controller		
F _{PTO,max}	3705	kN
$x_{c,max} - x_{c,min}$	3.2	m
Pave	35.11	kW
The PD controller		
F _{PTO,max}	1119	kN
$x_{c,max} - x_{c,min}$	1.1	m
Pave	21.00	kW
The PDC3 controller		
F _{PTO,max}	1404	kN
$x_{c,max} - x_{c,min}$	1.6	m
Pave	21.08	kW

Table 3. Capacity requirement of the controllers without hydraulic system.

Table 4. Capacity requirement of the controllers with hydraulic system.

Symbol	Value	Unit
The SA controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	0.96	m
Pave	13.49	kW
The PD controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	1.1	m
Pave	18.26	kW
The PDC3 controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	1.2	m
Pave	13.32	kW
The SB controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	0.8	m
Pave	16.02	kW
The MPC controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	1.1	m
Pave	18.37	kW
The PS controller		
F _{PTO,max}	215	kN
$x_{c,max} - x_{c,min}$	0.90	m
Pave	13.22	kW

8. Conclusions

The main conclusion of this paper is that a controller that is optimal in theoretical analysis might not be optimal when tested in a practical test environment. In particular, this paper sheds light on considerations that need to be accounted for in designing a control method for WEC systems. The first of these considerations is the limitation of the maximum possible PTO control force. This limitation impacts methods such as the singular arc control which is a control method developed in an optimal sense using classical optimal control theory. The second consideration is the limitation due to the maximum possible displacement of the WEC system. This limitation impacts the optimality of some control methods such as the multi-resonant proportional derivative control that is derived in an optimal sense to satisfy the complex conjugate criterion. Another consideration is the capability of the PTO to track the control command. The hydraulic PTO presented in this paper produces discrete levels of control forces and hence the dynamics of this PTO need to be accounted for in designing a control system for practical energy harvesting.

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Author Contributions: Shangyan Zou and Ossama Abdelkhalik designed the study and analyzed the data. Shangyan Zou wrote the paper and Ossama Abdelkhalik revised the paper.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

Symbol	Meaning	SI Units
A _{hose}	Area of the hose	m ²
A_v	Instantaneous opening area of the valve	m ²
A_0	Maximum opening area of the valve	m ²
A1	Piston area of chamber 1	m ²
A2	Piston area of chamber 2	m ²
A3	Piston area of chamber 3	m ²
A4	Piston area of chamber 4	m ²
В	Feedback controller gain on the angular velocity	N.m.s.rad ⁻¹
C_d	Valve discharge coefficient	-
C_{Q1}	Flow loss coefficient of the hydraulic motor	${ m m}^3.{ m s}^{-1}.{ m Pa}^{-1}$
C_v	Gas specific heat at constant volume	$J.(kg.K)^{-1}$
CWR	Capture width ratio	-
d _{hose}	Diameter of the hose	m
D	Characteristic dimension of the buoy	m
D_M	Total hydraulic motor displacement	m ³
D_w	Hydraulic motor displacement	m ³
F_c	Force applied by the cylinder	Ν
F _{fric}	Friction force of the cylinder	Ν
F _{ref}	Reference control force	Ν
h_{ex}	Wave excitation torque impulse response function	N.m
h_r	Radiation torque impulse response function	N.m
H_{m0}	Wave significant height	m
Jrigid	Rigid body inertia	kg.m ²
J_{∞}	Moment of the added mass	kg.m ²
k _{gen}	Number of generators	-
Kres	Hydrostatic stiffness coefficient	$N.m.rad^{-1}$

Κ	Feedback controller gain on the angular position	$N.m.rad^{-1}$
l _{hose}	Length of the hose	m
p _{acc}	Pressure in the accumulator	Pa
pavg,exp	Expected average power output	W
p_{A1}	Pressure in chamber 1	Pa
p_{A2}	Pressure in chamber 2	Pa
p_{A3}	Pressure in chamber 3	Pa
p_{A4}	Pressure in chamber 4	Pa
p_f	Pressure drop across the hose	Ра
p_H	Pressure of the high pressure accumulator	Ра
p_L	Pressure of the low pressure accumulator	Ра
p_{ζ}	Pressure drop of the fitting	Ра
p_{λ}	Pressure drop across a straight pipe/hose	Pa
Pactuator	Actuator power extraction	W
Pave	Average extracted power	W
Pgen	Generator power output	W
P_M	Motor power output	W
P_w	Wave energy transport	$W.m^{-1}$
Qacc	Inlet flow to the accumulator	$m^3.s^{-1}$
Q_{A1}	Inlet flow to chamber 1	$m^3.s^{-1}$
Q_{A2}	Inlet flow to chamber 2	$m^3.s^{-1}$
Q_{A3}	Inlet flow to chamber 3	$m^3.s^{-1}$
Q_{A4}	Inlet flow to chamber 4	$m^3.s^{-1}$
Q_{in}	Inlet flow of the hose	$m^3.s^{-1}$
Q_{out}	Outlet flow of the hose	$m^3.s^{-1}$
R	Ideal gas constant	$kg.m^2.(s^2.K)^{-1}$
Re	Reynold's number	-
S	Wave spectral density	m ² .s.rad ⁻¹
t_v	Valve opening and closing time	S
\tilde{T}	Gas temperature	К
T_w	Hydraulic accumulator wall temperature	К
u_v	Valve opening and closing signal	-
v_c	Instantaneous piston velocity	$m.s^{-1}$
vout	Velocity of the outlet flow of the hose	$m.s^{-1}$
V_{a0}	Accumulator size	m ³
Vext	Accumulator external volume of the pipeline	m ³
V_g	Accumulator gas volume	m ³
$V_{0,A1}$	External volume of the connecting hose to chamber 1	m ³
$V_{0,A2}$	External volume of the connecting hose to chamber 2	m ³
V _{0,A3}	External volume of the connecting hose to chamber 3	m ³
V _{0,A4}	External volume of the connecting hose to chamber 4	m ³
x_c	-	m
	Instantaneous stroke of the cylinder	111
$x_{c.max}$	Instantaneous stroke of the cylinder Maximum stroke of the cylinder	m
x _{c,max} β	Instantaneous stroke of the cylinder Maximum stroke of the cylinder Effective bulk modulus of the fluid	
β	Maximum stroke of the cylinder Effective bulk modulus of the fluid	m
β ζ	Maximum stroke of the cylinder	m
β ζ η	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation	m Pa -
β ζ η η _c	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency	m Pa -
β ζ η	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency	m Pa -
β ζ η η _c η _{out}	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency Angular position of the arm	m Pa - m -
β ζ η η _c η _{out} θ	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency Angular position of the arm Kinematic viscosity of the fluid	m Pa - m - rad m ² .s ⁻¹
β ζ η ηc ηout θ ν	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency Angular position of the arm	m Pa - m - - rad
β ζ η ηc ηout θ ν ρ	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency Angular position of the arm Kinematic viscosity of the fluid Fluid density Accumulator thermal time constant	m Pa - m - - rad m ² .s ⁻¹ kg.m ⁻³
β ζ η η _c η _{out} θ ν ρ τ _a	Maximum stroke of the cylinder Effective bulk modulus of the fluid Fitting loss coefficient Wave elevation Cylinder efficiency Electricity generation efficiency Angular position of the arm Kinematic viscosity of the fluid Fluid density	m Pa - m - - rad m ² .s ⁻¹ kg.m ⁻³ s

τ_{rad}	Torque due to the radiation wave	N.m
φ	Random phase shift	rad
ψ	Motor speed control coefficient	-
ω	Wave frequency	$rad.s^{-1}$
ω_M	Angular velocity of the hydraulic motor	$rad.s^{-1}$
ω_p	Peak frequency of the wave	$rad.s^{-1}$

References

- António, F.d.O.; Justino, P.A.; Henriques, J.C.; André, J.M. Reactive versus latching phase control of a two-body heaving wave energy converter. In Proceedings of the IEEE Control Conference (ECC), European, Budapest, Hungary, 23–26 August 2009; pp. 3731–3736.
- 2. Bacelli, G.; Ringwood, J.V.; Gilloteaux, J.C. A control system for a self-reacting point absorber wave energy converter subject to constraints. *IFAC Proc. Vol.* **2011**, *44*, 11387–11392.
- 3. Ricci, P.; Lopez, J.; Santos, M.; Ruiz-Minguela, P.; Villate, J.; Salcedo, F. Control strategies for a wave energy converter connected to a hydraulic power take-off. *IET Renew. Power Gener.* **2011**, *5*, 234–244.
- 4. You-Guan, Y.; Guo-fang, G.; Guo-Liang, H. Simulation technique of AMESim and its application in hydraulic system. *Hydraul. Pneum. Seals* **2005**, *3*, 28–31.
- 5. Ferri, F.; Kracht, P. Implementation of a Hydraulic Power Take-Off for wave energy applications. Department of Civil Engineering, Aalborg University: Aalborg, Denmark, 2013.
- Plummer, A.; Cargo, C. Power Transmissions for Wave Energy Converters: A Review. In Proceedings of the 8th International Fluid Power Conference (IFK), Dresden, Germany, 26–28 March 2012; University of Bath: Bath, UK, 2012.
- 7. Antonio, F.d.O. Modelling and control of oscillating-body wave energy converters with hydraulic power take-off and gas accumulator. *Ocean Eng.* **2007**, *34*, 2021–2032.
- 8. António, F.d.O. Phase control through load control of oscillating-body wave energy converters with hydraulic PTO system. *Ocean Eng.* **2008**, *35*, 358–366.
- 9. Hansen, R.H. Design and Control of the Powertake-Off System for a Wave Energy Converter with Multiple Absorbers. Ph.D. Thesis, Department of Energy Technology, Aalborg University: Aalborg, Denmark, 2013.
- 10. Babarit, A.; Guglielmi, M.; Clément, A.H. Declutching control of a wave energy converter. *Ocean Eng.* **2009**, *36*, 1015–1024.
- 11. Eidsmoen, H. Tight-moored amplitude-limited heaving-buoy wave-energy converter with phase control. *Appl. Ocean Res.* **1998**, *20*, 157–161.
- 12. Eidsmoen, H. *Simulation of a Slack-Moored Heaving-Buoy Wave-Energy Converter with Phase Control;* Norwegian University of Science and Technology: Trondheim, Norway, 1996.
- Josset, C.; Babarit, A.; Clément, A. A wave-to-wire model of the SEAREV wave energy converter. *Proc. Inst. Mech. Eng. Part M* 2007, 221, 81–93.
- 14. Henderson, R. Design, simulation, and testing of a novel hydraulic power take-off system for the Pelamis wave energy converter. *Renew. Energy* **2006**, *31*, 271–283.
- 15. Zhang, D.; Li, W.; Ying, Y.; Zhao, H.; Lin, Y.; Bao, J. Wave energy converter of inverse pendulum with double action power take off. *Proc. Inst. Mech. Eng. Part C* 2013, 227, 2416–2427.
- 16. Antolín-Urbaneja, J.C.; Cortés, A.; Cabanes, I.; Estensoro, P.; Lasa, J.; Marcos, M. Modeling innovative power take-off based on double-acting hydraulic cylinders array for wave energy conversion. *Energies* **2015**, *8*, 2230–2267.
- 17. Cargo, C.; Hillis, A.; Plummer, A. Optimisation and control of a hydraulic power take-off unit for a wave energy converter in irregular waves. *Proc. Inst. Mech. Eng. Part A* **2014**, *228*, 462–479.
- Sun, K.; Ge, W.; Luo, L.; Liang, H.; Xu, C.; Leng, J.; Yuan, Z.; Huang, H. Research on the hydraulic power take-off unit of a hybrid wave energy converter. In Proceedings of the IEEE OCEANS 2016-Shanghai, Shanghai, China, 10–13 April 2016; pp. 1–4.
- 19. Hansen, R.H.; Kramer, M.M.; Vidal, E. Discrete displacement hydraulic power take-off system for the wavestar wave energy converter. *Energies* **2013**, *6*, 4001–4044.

- Hansen, R.H.; Andersen, T.O.; Pedersen, H.C. Model based design of efficient power take-off systems for wave energy converters. In Proceedings of the 12th Scandinavian International Conference on Fluid Power, SICFP, Tampere, Finland, 18–20 May 2011; Tampere, Finland; Tampere University Press: Tampere, Finland, 2011; pp. 35–49.
- 21. Kamizuru, Y. Development of Hydrostatic Drive Trains for Wave Energy Converters; Shaker Verlag GmbH, Germany, 13 November 2014.
- 22. Hals, J.; Taghipour, R.; Moan, T. Dynamics of a force-compensated two-body wave energy converter in heave with hydraulic power take-off subject to phase control. In Proceedings of the 7th European Wave and Tidal Energy Conference, Porto, Portugal, 11–13 September 2007; pp. 11–14.
- 23. Costello, R.; Ringwood, J.; Weber, J. Comparison of two alternative hydraulic PTO concepts for wave energy conversion. In Proceedings of the 9th European Wave and Tidal Energy Conference (EWTEC), Southampton, UK, 5–9 September 2011.
- 24. Kamizuru, Y.; Liermann, M.; Murrenhoff, H. Simulation of an ocean wave energy converter using hydraulic transmission. In Proceedings of the 7th International Fluid Power Conference, Aachen, Germany, 22–24 March 2010.
- 25. Penalba, M.; Sell, N.P.; Hillis, A.J.; Ringwood, J.V. Validating a wave-to-wire model for a wave energy converter—Part I: The Hydraulic Transmission System. *Energies* **2017**, *10*, 977–999.
- 26. Schlemmer, K.; Fuchshumer, F.; Böhmer, N.; Costello, R.; Villegas, C. Design and control of a hydraulic power take-off for an axi-symmetric heaving point absorber. In Proceedings of the 9th European Wave and Tidal Conference, Southampton, UK, 5–9 September 2011.
- 27. Gaspar, J.F.; Calvário, M.; Kamarlouei, M.; Soares, C.G. Power take-off concept for wave energy converters based on oil-hydraulic transformer units. *Renew. Energy* **2016**, *86*, 1232–1246.
- 28. Sánchez, E.V.; Hansen, R.H.; Kramer, M.M. Control performance assessment and design of optimal control to harvest ocean energy. *IEEE J. Ocean. Eng.* **2015**, *40*, 15–26.
- 29. Hansen, A.H.; Pedersen, H.C. Reducing pressure oscillations in discrete fluid power systems. *Proc. Inst. Mech. Eng. Part I* 2016, 230, 1093–1105.
- 30. Hansen, R.H.; Andersen, T.O.; Pedersen, H.C.; Hansen, A.H. Control of a 420 kn discrete displacement cylinder drive for the wavestar wave energy converter. In Proceedings of the ASME/BATH 2014 Symposium on Fluid Power and Motion Control, Bath, UK, 10–12 September 2014.
- 31. Zou, S.; Abdelkhalik, O.; Robinett, R.; Bacelli, G.; Wilson, D. Optimal control of wave energy converters. *Renew. Energy* **2017**, *103*, 217–225.
- 32. Hals, J.; Falnes, J.; Moan, T. Constrained Optimal Control of a Heaving Buoy Wave-Energy Converter. *J. Offshore Mech. Arct. Eng.* **2011**, 133, 1–15.
- 33. Abdelkhalik, O.; Robinett, R.; Zou, S.; Bacelli, G.; Coe, R.; Bull, D.; Wilson, D.; Korde, U. On the control design of wave energy converters with wave prediction. *J. Ocean Eng. Mar. Energy* **2016**, *2*, 473–483.
- 34. Song, J.; Abdelkhalik, O.; Robinett, R.; Bacelli, G.; Wilson, D.; Korde, U. Multi-resonant feedback control of heave wave energy converters. *Ocean Eng.* **2016**, *127*, 269–278.
- Herber, D.R.; Allison, J.T. Wave energy extraction maximization in irregular ocean waves using pseudospectral methods. In Proceedings of the 39th Design Automation Conference, Portland, OR, USA, 4–7 August 2013; p. V03AT03A018.
- 36. Kramer, M.; Marquis, L.; Frigaard, P. Performance evaluation of the wavestar prototype. In Proceedings of the 9th European Wave and Tidal Conference, Southampton, UK, 5–9 September 2011.



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