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Supplementary materials to the paper titled:

A Hybrid MCDM Approach Based on Fuzzy MEREC-G and Fuzzy RATMI

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Table S1. Example 1

Fuzzy MEREC-G												
Combined Fuzzy Decision Matrix*												
Alternatives	Criteria											
	Quality	Expenses	Delivery	Source	Flexibility	Communication	Reliability	Max	Max	Max	Max	Max
	Min	Max	Min	Max	Max	Max	Max	Min	Max	Max	Min	Max
Russia	0.2500	0.3600	0.4800	0.2300	0.3600	0.4900	0.2500	0.3800	0.5000	0.2700	0.3900	0.5100
Romania	0.3300	0.4400	0.5400	0.3800	0.5000	0.6200	0.3100	0.4300	0.5400	0.2500	0.3800	0.5000
Ukraine	0.2600	0.3900	0.5200	0.2700	0.3800	0.4800	0.4200	0.5400	0.6600	0.4500	0.5600	0.6800
Australia	0.3800	0.5000	0.6300	0.3800	0.5000	0.6200	0.2900	0.4100	0.5300	0.2200	0.3400	0.4600
Syria	0.2800	0.4000	0.5300	0.3400	0.4600	0.5800	0.3300	0.4400	0.5500	0.3500	0.4800	0.6000

* This table is adopted from (Magableh, G.M. Evaluating Wheat Suppliers Using Fuzzy MCDM Technique. *Sustainability* **2023**, *15*, 10519. <https://doi.org/10.3390/su151310519>)

Normalized Decision Matrix												
Alternatives	Criteria											
	Quality	Expenses	Delivery	Source	Flexibility	Communication	Reliability	Max	Max	Max	Max	Max
Russia	0.5208	0.6944	1.0000	0.3710	0.5806	0.7903	0.5000	0.6579	1.0000	0.3971	0.5588	0.7059
Romania	0.4630	0.5682	0.7576	0.6129	0.8065	1.0000	0.4630	0.5814	0.8065	0.3676	0.5588	0.7353
Ukraine	0.4808	0.6410	0.9615	0.4355	0.6129	0.7742	0.3788	0.4630	0.5952	0.6618	0.8235	1.0000
Australia	0.3968	0.5000	0.6579	0.6129	0.8065	1.0000	0.4717	0.6098	0.8621	0.3235	0.5000	0.6765
Syria	0.4717	0.6250	0.8929	0.5484	0.7419	0.9355	0.4545	0.5682	0.7576	0.5147	0.7059	0.8824

The changes in the overall performance of alternatives												
Alternatives	Criteria											
	Quality	Expenses	Delivery	Source	Flexibility	Communication	Reliability	Max	Max	Max	Max	Max
Russia	0.4503	0.6242	0.8078	0.4726	0.6403	0.8355	0.4529	0.6290	0.8078	0.4681	0.6438	0.8490
Romania	0.5532	0.7131	0.8795	0.5314	0.6783	0.8453	0.5532	0.7108	0.8717	0.5717	0.7148	0.8833
Ukraine	0.5311	0.6775	0.8241	0.5386	0.6818	0.8500	0.5495	0.7097	0.8826	0.5074	0.6537	0.8195
Australia	0.5786	0.7445	0.9174	0.5437	0.6954	0.8641	0.5645	0.7237	0.8826	0.5957	0.7445	0.9137
Syria	0.5098	0.6691	0.8351	0.4978	0.6530	0.8296	0.5113	0.6783	0.8549	0.5023	0.6576	0.8365

Resulting effect and weights of the Fuzzy MEREC-G												
Removal Effect												
E1	E2	E3	E4	E5	E6	E7						
Min	Max	Min	Max	Max	Max	Max						
2.6217	3.4284	4.2640	2.5842	3.3488	4.2245	2.6313	3.4515	4.2997	2.6452	3.4144	4.3021	2.3296
Fuzzy Weights												
W1	W2	W3	W4	W5	W6	W7						
Min	Max	Min	Max	Max	Max	Max						
0.0887	0.1481	0.2435	0.0874	0.1447	0.2413	0.0890	0.1491	0.2456	0.0895	0.1475	0.2457	0.0788
Crisp Weights												
W1*	W2*	W3*	W4*	W5*	W6*	W7*						
Min	Max	Min	Max	Max	Max	Max						
0.1541	0.1512	0.1552	0.1542	0.1433	0.1442	0.1446						

Fuzzy RATMI

The fuzzy weighted decision-making matrix

Alternatives	Quality		Expenses		Delivery		Source		Flexibility		Communication		Reliability		
	Min	Max	Min	Max	Min	Max	Min	Max	Min	Max	Min	Max	Min	Max	
Russia	0.0462	0.1028	0.2435	0.0324	0.0840	0.1907	0.0445	0.0981	0.2456	0.0355	0.0824	0.1735	0.0333	0.0830	0.1883
Romania	0.0411	0.0841	0.1845	0.0536	0.1167	0.2413	0.0412	0.0867	0.1981	0.0329	0.0824	0.1807	0.0505	0.1127	0.2363
Ukraine	0.0426	0.0949	0.2342	0.0381	0.0887	0.1868	0.0337	0.0690	0.1462	0.0592	0.1215	0.2457	0.0333	0.0808	0.1772
Australia	0.0352	0.0741	0.1602	0.0536	0.1167	0.2413	0.0420	0.0909	0.2117	0.0290	0.0737	0.1662	0.0431	0.1021	0.2215
Syria	0.0418	0.0926	0.2175	0.0479	0.1073	0.2257	0.0405	0.0847	0.1860	0.0461	0.1041	0.2168	0.0357	0.0872	0.1957

The fuzzy magnitude of components' values

Qk		Qh	
0.1195	0.2588	0.5363	0.0642

Results of the Fuzzy MCRAT method

Alternatives	Vik		Vih		Z11,i		Z22,i		tr(Z)~		tr(Z)		Rank				
	Max	Min	Max	Min	D~	ms(Mi~)	ms(Mi)	Rank									
Russia	0.0703	0.1773	0.3989	0.0642	0.1421	0.3459	0.0084	0.0459	0.2139	0.0041	0.0202	0.1196	0.0125	0.0661	0.3336	0.1017	5
Romania	0.0976	0.2225	0.4739	0.0582	0.1208	0.2707	0.0117	0.0576	0.2542	0.0037	0.0172	0.0936	0.0154	0.0748	0.3478	0.1104	2
Ukraine	0.0971	0.2175	0.4614	0.0544	0.1174	0.2761	0.0116	0.0563	0.2475	0.0035	0.0167	0.0965	0.0151	0.0730	0.3429	0.1083	3
Australia	0.1045	0.2354	0.4981	0.0548	0.1173	0.2655	0.0125	0.0609	0.2671	0.0035	0.0167	0.0918	0.0160	0.0776	0.3590	0.1142	1
Syria	0.0875	0.2047	0.4454	0.0582	0.1255	0.2862	0.0105	0.0530	0.2389	0.0037	0.0178	0.0990	0.0142	0.0708	0.3378	0.1059	4

Results of the Fuzzy RAMS technique

Alternatives	Max		Min		Median		Median Similarity		ms(Mi)	Rank				
	QK~	QH~	QH~	D~	ms(Mi~)		ms(Mi~)	ms(Mi)						
	0.1195	0.2588	0.5363	0.0642	0.1421	0.3459	0.0678	0.1476	0.3191					
Russia	0.0703	0.1773	0.3989	0.0642	0.1421	0.3459	0.0476	0.1136	0.2640	0.1492	0.7696	3.8920	1.1866	5
Romania	0.0976	0.2225	0.4739	0.0582	0.1208	0.2707	0.0568	0.1266	0.2729	0.1780	0.8573	4.0232	1.2718	2
Ukraine	0.0971	0.2175	0.4614	0.0544	0.1174	0.2761	0.0567	0.1236	0.2688	0.1744	0.8369	3.9638	1.2476	3
Australia	0.1045	0.2354	0.4981	0.0548	0.1173	0.2655	0.0590	0.1315	0.2822	0.1849	0.8905	4.1611	1.3180	1
Syria	0.0875	0.2047	0.4454	0.0582	0.1255	0.2862	0.0525	0.1201	0.2647	0.1646	0.8132	3.9025	1.2200	4

Alternatives rankings according to the Fuzzy RATMI method

Alternatives	Fuzzy MCRAT		Fuzzy RAMS		Majority Index		Ei	Rank		
	tr*	0.1017	ms*	1.1866	Ei					
	tr-	0.1142	ms-	1.3180	Ei					
	tr(Zi)	ms(Mi)	ms(Mi)	ms(Mi)	Ei					
Russia	0.1017	1.1866	0.0000	5						
Romania	0.1104	1.2718	0.6695	2						
Ukraine	0.1083	1.2476	0.4959	3						
Australia	0.1142	1.3180	1.0000	1						
Syria	0.1059	1.2200	0.2929	4						