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# Automated Settings of Overcurrent Relays Considering Transformer Phase Shift and Distributed Generators Using Gorilla Troops Optimizer 

Abdelmonem Draz (D), Mahmoud M. Elkholy and Attia A. El-Fergany *<br>Electrical Power and Machines Department, Zagazig University, Zagazig 44519, Egypt<br>* Correspondence: el_fergany@zu.edu.eg

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#### Abstract

The relative protective devices are cascaded in a proper sequence with a proper $\mathrm{min} / \mathrm{max}$ coordination time margin (CTM) to minimize the outage area of the network in case of fault condition. This manuscript addresses a new methodology based on the gorilla troops optimizer (GTO) to produce the best automated settings for overcurrent relays. In the GTO, the exploration and exploitation phases are realized using five methodologies. Three of them are used in the exploration phase and the other two in the exploitation phase. In the exploration phase, all gorillas are considered as candidate solutions and the best one is considered as the silverback gorilla. Then again, the exploitation phase comprises two steps: (i) the first one is the follow of silverback gorilla, and (ii) the second one is the competition for adult females. The latter mentioned offers an added advantage to the GTO framework to move forward steadily to global minima and to avoid trapping into local minima. Two test cases under numerous scenarios are demonstrated comprising an isolated real distribution network with distributed generations for the Agiba Petroleum company which is in the Western Desert of Egypt. The relay coordination problem is adapted as an optimization problem subject to a set of predefined constraints which is solved using the GTO including fixed and varied inverse IEC curves, in which the practical constraints including transformer phase shift and other scenarios for min/max fault conditions are dealt with. In due course, this current effort aims at proving the best strategy for achieving the smoothest coordination of overcurrent relays (OCRs), with the least obtained value of CTMs for the studied cases being established via the automated relay settings. At last, it can be pointed out that the GTO successfully dealt with this problem and was able to produce competitive answers compared to other competitors.


Keywords: optimal overcurrent relay coordination; smooth coordination; transformer phase shift; gorilla troops algorithm; optimization methods

MSC: 68T20

## 1. Introduction

Overcurrent (OC) and earth fault (EF) protections along the power system network play a vital role among other types of protection units for various voltage levels [1,2]. Cascading the operating sequence of these relative units is needed to minimize the outage of the power system to secure its operations. In regard to the EF, it is a simple process to achieve the coordination, especially since there are few units to be cascaded and, in general, the definite time (DT) characteristic is enough for this study. The latter is alternatively called the coordination of discrimination to ensure the arrangements of the operations of the main and backup OC protection units and to allow specific time margins, which are known as a coordination time margin (CTM). This time margin is normally varying from 0.2 ms to 0.4 s , and it actually depends on the technology and generation of the OC relays (OCRs). More specifically, between digital relays, the CTM of 0.2 s may be used and for electromechanical relays, the CTM is something around 0.5 s [2-4].

Manual achievement of the coordination is tedious and requires a lot of time. Thus, the computerized alternative to this is essential. Even for the available tools, it is still difficult to tackle these drawbacks as the interfering of the engineers is still required. In the last decade, many efforts have been performed to automate such studies with minimal interferences from the engineers. Among these methods are: expert systems [3], linear programming [5-7], the simplex method [8,9], random search [10], and mixed-integer non-linear programing [11]. The deficiencies of these aforementioned methods have been proven when they are applied to larger systems. On the other hand, many researchers have proposed various optimization methodologies to deal with the same problem, aiming to generate automated relay settings such as the slime mold algorithm (SMA) [12], water cycle algorithm [13,14], whale optimization algorithm [15,16], firefly algorithm [17], adaptive fuzzy directional bat algorithm [18], genetic optimizer [19], moth-flame optimization [20], JAYA [21,22], Harris Hawks' optimization [21,23], nature-inspired root tree algorithm [24], electromagnetic field optimization algorithm [25], and particle swarm optimization [26-28].

Further considerable efforts to accommodate microgrids and the involvement of distributed generators (DGs) in the coordination study have been reported, such as the methods for DGs-integrated distribution networks considering system dynamics [29,30], adaptive OC relay (OCR) coordination in grid-connected wind farms [31], adaptive OCR coordination scheme for windfarm-integrated power systems [32], optimum coordination of OCRs to enhance microgrid EF protection scheme [33], and optimal coordination of overcurrent relays in microgrids [34-38].

Further to the above, a comprehensive survey has been presented in [2,39], in which the readers are invited to go through such efforts. Extra heuristic-based optimizers are still being used by the esteemed researchers in order to improve the quality of the relay coordination outcome with the ultimate objective of generating an automated setting. Until this moment, many trials have been performed in the same manner. More recently, the gradient-based optimizer [40], various versions of differential evolution [41-43], stochastic fractal search algorithm [44], flower pollination for combination between arc-flash and coordination [45], harmony search algorithm [46], grey wolf optimizer [47], and so on [48-56], have been presented. Moreover, the practical coordination model is investigated in distribution networks penetrated with motors and transformers as declared in [57]. Adaptive protection coordination in distribution networks with DGs is deployed in [58], while the implementation of unsupervised learning techniques is exploited in [59] for the coordination of OCRs in microgrids.

Taking a closer look at the above-mentioned survey, numerous methods have been undertaken to attain the optimal settings for OC relays in traditional and smart grids as well, yet there is still room for improvement to include more constraints to attain industrial trust and meet the requirements. In the same context, and in line with the no-freelunch theorem, the authors are motived to employ the gorilla troops-based optimization (GTO) method [60] to tackle this problem with the hope of having a competitive outcome compared to the existing results available in the literature. In GTO, the exploration and exploitation processes are realized using five methodologies. It can be confirmed that the GTO has been applied successfully to estimate the ungiven parameters of the single and double-diode models [61]. In this context, the deployment of GTO is exploited in [62] to solve the optimization problem of the integration of renewable-based DGs in power systems.

In this current effort, the GTO is used to produce the optimal settings in an automated manner of OCRs for two test cases under different intentional scenarios with the minimal interference of users, and in which new concepts for understanding the point at which to start the relay coordination for $\mathrm{min} / \mathrm{max}$ fault scenarios are proposed. The first case is a 15-bus network with DGs which is widely used in the literature, and the second case is a real power network based in West Desert in Egypt for the Agiba petroleum company.

## 2. Optimization Problem Formulation

It is obviously known that the relation between the fault current passing through the relay $\left(I_{f}\right)$ and the relay operating time $\left(t_{r i}\right)$ is an inverse one as shown in (1).

$$
\begin{equation*}
t_{r i}=\frac{a}{\left(\frac{I_{f}}{I_{p u}}\right)^{\mathcal{B}}-1} \cdot T_{D} \tag{1}
\end{equation*}
$$

where: $I_{p u}$ is the relay current pickup, $T_{D}$ is the relay time dial setting, and $a$, and are constants varying with the relay type characteristics (CCs) as presented in Table 1. Figure 1 presents four standardized TCCs extracted from the IEC 60255-3 standard [1] plotted using a log-to-log scale.

Table 1. Constant values for various IEC standard curves.

| Standard | TCC Type | $\boldsymbol{a}$ | $\boldsymbol{B}$ |
| :---: | :---: | :---: | :---: |
| IEC | NI | 0.14 | 0.02 |
| IEC | VI | 13.50 | 1.00 |
| IEC | EI | 80.00 | 2.00 |
| IEC | LI | 120.00 | 1.00 |



Figure 1. A log-to-log plot for IEC 60255-3 TCCs.
The optimization process of OCRs in this paper threads through dedicated and ordered steps as follows:

1. Preparing the model which includes the relay pairs definition, the level of fault currents, and the lower and upper boundaries of the decision variables.
2. Constructing the fitness optimized function (FOF) that tends to minimize the total operating time (TOT) of the primary relays as disclosed in (2).

$$
\begin{equation*}
F O F=\sum_{i=1}^{N_{P}} t_{r i} \tag{2}
\end{equation*}
$$

where: $N_{P}$ is the total number of the primary relays in the study case.
3. Defining the lower and upper boundaries of independent and dependent constraints. The decision variables needed to be optimized represent the independent ones as demonstrated in (3)-(7).

$$
\begin{gather*}
I_{p u i, \text { min }} \leq I_{p u i} \leq I_{p u i, \text { max }}  \tag{3}\\
I_{p u i, \text { min }} \geq O L C \times I_{\text {full load }}  \tag{4}\\
I_{p u i, \text { max }} \leq S F \times I_{f, \text { min }}  \tag{5}\\
T_{D i, \text { min }} \leq T_{D i} \leq T_{D i, \max }  \tag{6}\\
T C C_{i, \text { min }} \leq T C C_{i} \leq T C C_{i, \max } \tag{7}
\end{gather*}
$$

where: $I_{p u i, \text { min }}$, and $I_{p u i, m a x}$ are the minimum and maximum values of the relay current pickup, respectively. In practice, $I_{\text {pui,min }}$ shall be greater than the equipment full load current ( $I_{\text {full load }}$ ) by a certain value nominated as the over loading capacity (OLC). On the other hand, $I_{\text {pui,max }}$ shall be lower than the minimum fault current $\left(I_{f, \min }\right)$ by a certain value called the sensitivity factor $(S F)$. Moreover, the relay time dial shall be bounded between minimum ( $T_{D i, \min }$ ) and maximum ( $T_{D i, \max }$ ) value besides the TCC, as is also the case in digital relays. $T C C_{i, \min }$, and $T C C_{i, \max }$ are the lower and upper limits of the CCs' type that have discrete values rather than other settings that have continuous values.
The dependent constraints examined in this research lie in two types; the selectivity constraint and the minimum operating time constraint as dedicated in (8) and (9), respectively.

$$
\begin{gather*}
\text { CTM }_{\text {min }, j} \leq t_{b r i}-t_{p r i} \leq C T M_{\max , j}  \tag{8}\\
t_{p r i} \geq t_{\min , i} \tag{9}
\end{gather*}
$$

where: $t_{b r i}$, and $t_{p r i}$ are the operating time of the backup and primary relay, respectively, at the same fault point. $C T M_{\min , j}$, and $C T M_{m a x, j}$ are the minimum and maximum values of CTM, respectively, while $t_{\text {min, }, i}$ is the minimum possible operating time of the protection relay by activating its instantaneous CCs.
4. Extracting the optimal values of the decision variables in addition to plotting the convergence trend of FOF.

## 3. Procedures of the GTO

The metaheuristic algorithms are more significant in solving many sophisticated engineering problems due to their simple implementation and are more superior than other heuristic techniques to crop global optimal solution. The metaheuristic techniques can be classified as: natural, swarm, physical, and human based. One of the new, nature-inspired algorithms which is inspired by the gorilla group trait is developed by [60] and is called GTO. In the GTO, the exploration and exploitation processes are implemented using five methodologies: three in the exploration phase and two in the exploitation phase. In the exploration phase, all gorillas are considered as nominee solutions and the best one is considered as the silverback gorilla. The three methodologies of the exploration phase can be summarized as: the resettlement to an unknown position when rand $<$ controlled the variable ( $p$ ); then the transition to other different gorilla is decided if rand rand $\geq 0.5$; and lastly, the transition to a known position is selected when rand $<0.5$. These exploration processes can be depicted as:

$$
G X(k+1)=\left\{\begin{array}{cc}
(H L-L L) \times r_{1}+L L & \text { rand }<p  \tag{10}\\
\left(r_{2}-C_{1}\right) \times X_{r}(k)+S \times C_{2} & \text { rand } \geq 0.5 \\
X(k)-S \times\left[S \times\left(X(k)-G X_{r}(k)\right)+r_{3} \times\left(X(k)-G X_{r}(k)\right)\right] & \text { rand }<0.5
\end{array}\right.
$$

where: $G X(k+1)$ is the nominee location vector in the iteration of $(k+1)$ rank, $X(k)$ is the existing vector of the gorilla location, $r_{1}, r_{2}$ and $r_{3}$ and rand are the updated random values between 0 and 1 in each iteration, $H L$, and $L L$ are the higher and lower values of desired understudying problem variables, respectively, $X_{r}$ is a randomly selected member of the
gorilla group, $G X_{r}$ is the one vector of the random gorilla candidate's updated location in each phase. The parameters $C_{1}, C_{2}$ and $S$ are calculated using:

$$
\begin{gather*}
C_{1}=1+\cos \left(2 r_{4}\right)\left[1-\frac{i t}{i t_{\max }}\right]  \tag{11}\\
S=C_{1} \times r_{5}  \tag{12}\\
C_{2}=r_{6} \times X(k) \tag{13}
\end{gather*}
$$

where: $r_{4}$ are updated random variables between 0 and $1, i t, i t_{\max }$ are the current and maximum iteration, respectively, and $r_{5}$ is the random parameters between -1 and 1 . The behavior of the gorilla silverback is emulated by (12) and $r_{6}$ is a random variable between $-C_{1}$ and $C_{1}$ in the problem dimension.

The exploitation phase consists of two methodologies, the first one is the following of the silverback gorilla when the variable $C_{1} \geq W$ and can be emulated by (14). However, the second one is the competition for adult females when $C_{1}<W$ and can be simulated by (15).
where: $W$ is a set point before the optimization process.

$$
\begin{equation*}
G X(k+1)=S \times\left(\left|\frac{1}{N_{G}}\right| \sum_{m=1}^{N_{G}} G X_{m}(k)\right)^{\frac{1}{2^{S}}} \times\left(X(k)-X_{s}\right)+X(k) \tag{14}
\end{equation*}
$$

where: $X_{s}$ is the silverback gorilla location, which is the best solution, $G X_{m}(k)$ describes each nominee gorilla's vector location in iteration $k$, and $N_{G}$ is the gross number of gorillas.

$$
\begin{equation*}
G X(m)=X_{s}-\left(2 r_{6}-1\right)(\text { Beta } \times E)\left(X_{s}-X(k)\right. \tag{15}
\end{equation*}
$$

where: $r_{6}$ is a random value between 0 and 1, Beta is a set parameter before optimization start and $E$ is the variable that simulates the violence on the solution dimension based on the value of the rand variable

The $X(k)$ is replaced by $G X(k)$ when the FOF value of $G X(k)$ is lower than one of $X(k)$.
The procedures of minimizing the FOF (i.e., the TOT of the primary relays) based on the GTO algorithm are depicted in Figure 2.


Figure 2. GTO Flow chart procedures.

## 4. Study Cases and Results with Debates

The performance of the proposed GTO is evaluated in two various study cases with different topologies. The first one is the IEEE 15-bus system, which is deemed as a pure transmission network tackled many times before in the literature. The obtained results are compared to the latest powerful optimizers and manifest the superiority of the GTO over them for solving this highly constrained optimization problem. The second one is an isolated practical distribution network belonging to the Agiba petroleum company located in Egypt. Both networks are investigated using two scenarios; scenario one considers the fixed NI curve while scenario two optimizes the curve between the four standard IEC TCCs. Furthermore, the GTO control parameters are set as follows for better results: $p=0.000001$, Beta $=4, W=0.9, N_{G}=100$, and $i t_{\max }=500$.

### 4.1. Study Case 1: The IEEE 15-Bus Network

Figure 3 depicts the single-line diagram (SLD) of the IEEE 15-bus network and its system data obtained can be found in [12,14,40,45].


Figure 3. The SLD of the IEEE 15-bus network.
To validate the GTO results, the following assumptions are considered for a fair comparison with other algorithms: (i) an OLC between $100 \%$ to $150 \%$ of the full load current with no considerations on the minimum fault current conditions, the (ii) $T_{D i, \min }=0.05 \mathrm{~s}$
for scenario one and 0.01 s for scenario two while $T_{D i, \max }=1 \mathrm{~s}$ for both scenarios, (iii) $C T M_{\min , j}=0.2 \mathrm{~s}$ and $C T M_{\max , j}=0.4 \mathrm{~s}$, and (iv) $T C C_{i, \min }=1$ and $T C C_{i, \max }=4$.

Table 2 lists the optimized settings of DOCRs in the IEEE 15-bus network using the GTO for both scenarios. It is revealed that the GTO has been managed for selecting the EI curve for all relays in scenario two in the hope of achieving the best obtained FOF ever. The operating times of the primary/backup relays are recorded in Table 3 with no violations in the independent or dependent constraints. The entrenched fair comparison results in the obvious superiority of the GTO over other algorithms with various natures as announced in Table 4. The GTO achieves a TOT of 9.0775 s and 1.3962 s , attaining a $24.2 \%$ and a $43 \%$ reduction compared to SMA for scenarios one and two, respectively. Moreover, the FOF smooth convergence trend using the GTO for this highly penetrated DG network is shown in Figure 4.

Table 2. Optimum DOCRs settings of the IEEE 15-bus using GTO.

| Relay ID. | Scenario 1 |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $I_{p}(\mathrm{~A})$ | $T_{D}(\mathrm{~s})$ | $I_{p}(\mathrm{~A})$ | $T_{D}(\mathrm{~s})$ | Curve |
| R1 | 274.3358 | 0.0675 | 293.9991 | 0.0215 | EI |
| R2 | 313.9608 | 0.0681 | 307.6176 | 0.0244 | EI |
| R3 | 478.9256 | 0.0654 | 477.1756 | 0.0221 | EI |
| R4 | 440.9214 | 0.0663 | 442.4978 | 0.0294 | EI |
| R5 | 489.9721 | 0.0662 | 431.7093 | 0.0297 | EI |
| R6 | 373.4484 | 0.0661 | 374.9995 | 0.0264 | EI |
| R7 | 345.0252 | 0.0685 | 367.4998 | 0.0270 | EI |
| R8 | 556.5137 | 0.0668 | 559.5983 | 0.0205 | EI |
| R9 | 432.7932 | 0.0658 | 433.3580 | 0.0184 | EI |
| R10 | 403.1725 | 0.0634 | 403.8370 | 0.0199 | EI |
| R11 | 449.1812 | 0.0677 | 449.9982 | 0.0269 | EI |
| R12 | 483.8421 | 0.0666 | 502.4489 | 0.0210 | EI |
| R13 | 509.7451 | 0.0500 | 516.4943 | 0.0131 | EI |
| R14 | 394.2057 | 0.0649 | 323.7574 | 0.0338 | EI |
| R15 | 344.3698 | 0.0663 | 367.4998 | 0.0251 | EI |
| R16 | 253.7067 | 0.0639 | 245.1271 | 0.0232 | EI |
| R17 | 179.5477 | 0.0667 | 187.4989 | 0.0351 | EI |
| R18 | 457.3094 | 0.0678 | 487.9445 | 0.0204 | EI |
| R19 | 425.2535 | 0.0672 | 425.6398 | 0.0251 | EI |
| R20 | 620.0474 | 0.0641 | 622.3204 | 0.0213 | EI |
| R21 | 539.9664 | 0.0612 | 539.9992 | 0.0166 | EI |
| R22 | 202.2495 | 0.0639 | 201.8658 | 0.0244 | EI |
| R23 | 395.0120 | 0.0644 | 393.4877 | 0.0243 | EI |
| R24 | 251.1717 | 0.0653 | 224.4215 | 0.0314 | EI |
| R25 | 348.8178 | 0.0629 | 286.8513 | 0.0287 | EI |
| R26 | 304.9423 | 0.0685 | 307.2427 | 0.0383 | EI |
| R27 | 352.4827 | 0.0653 | 320.5883 | 0.0275 | EI |
| R28 | 447.8116 | 0.0667 | 389.5427 | 0.0293 | EI |
| R29 | 671.0048 | 0.0673 | 674.2527 | 0.0263 | EI |
| R30 | 201.8216 | 0.0658 | 192.8832 | 0.0310 | EI |
| R31 | 300.5795 | 0.0671 | 263.0405 | 0.0283 | EI |
| R32 | 278.9333 | 0.0661 | 284.9837 | 0.0161 | EI |
| R33 | 351.3740 | 0.0745 | 405.0106 | 0.0227 | EI |
| R34 | 298.8261 | 0.0685 | 280.2785 | 0.0308 | EI |
| R35 | 364.0380 | 0.0603 | 296.5395 | 0.0290 | EI |
| R36 | 433.7195 | 0.0676 | 382.2169 | 0.0261 | EI |
| R37 | 553.7038 | 0.0666 | 599.9994 | 0.0276 | EI |
| R38 | 299.4094 | 0.0672 | 248.6752 | 0.0331 | EI |
| R39 | 285.5946 | 0.0667 | 294.4203 | 0.0225 | EI |
| R40 | 560.6371 | 0.0670 | 490.9930 | 0.0293 | EI |
| R41 | 297.1019 | 0.0635 | 299.9973 | 0.0268 | EI |
| R42 | 337.1191 | 0.0674 | 374.1360 | 0.0164 | EI |
| TOT (s) |  |  |  | 1.3962 |  |

Table 3. Operating times of M/B relay pairs with their associated CTM values of the IEEE 15-bus based on GTO.

| Relay Pairs |  | Scenario 1 |  |  | Scenario 2 |  |  | Relay Pairs |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 1 | 6 | 0.1783 | 0.3830 | 0.2047 | 0.0114 | 0.2154 | 0.2039 | 20 | 30 | 0.1742 | 0.3743 | 0.2002 | 0.0113 | 0.2162 | 0.2049 |
| 2 | 4 | 0.1730 | 0.3795 | 0.2065 | 0.0088 | 0.2320 | 0.2232 | 21 | 17 | 0.1519 | 0.3828 | 0.2309 | 0.0055 | 0.3053 | 0.2998 |
| 2 | 16 | 0.1730 | 0.4115 | 0.2385 | 0.0088 | 0.2271 | 0.2183 | 21 | 19 | 0.1519 | 0.3970 | 0.2451 | 0.0055 | 0.2135 | 0.2080 |
| 3 | 1 | 0.2115 | 0.4116 | 0.2000 | 0.0257 | 0.2319 | 0.2061 | 21 | 30 | 0.1519 | 0.3743 | 0.2224 | 0.0055 | 0.2162 | 0.2107 |
| 3 | 16 | 0.2115 | 0.4115 | 0.2000 | 0.0257 | 0.2271 | 0.2013 | 22 | 23 | 0.1930 | 0.4921 | 0.2991 | 0.0211 | 0.3744 | 0.3533 |
| 4 | 7 | 0.1976 | 0.4056 | 0.2080 | 0.0242 | 0.2655 | 0.2412 | 22 | 34 | 0.1930 | 0.4027 | 0.2097 | 0.0211 | 0.2242 | 0.2031 |
| 4 | 12 | 0.1976 | 0.4167 | 0.2191 | 0.0242 | 0.2249 | 0.2006 | 23 | 11 | 0.1744 | 0.3939 | 0.2195 | 0.0126 | 0.2212 | 0.2086 |
| 4 | 20 | 0.1976 | 0.4151 | 0.2175 | 0.0242 | 0.2287 | 0.2045 | 23 | 13 | 0.1744 | 0.4789 | 0.3046 | 0.0126 | 0.3325 | 0.3200 |
| 5 | 2 | 0.2375 | 0.4380 | 0.2005 | 0.0408 | 0.2440 | 0.2032 | 24 | 21 | 0.2021 | 0.4723 | 0.2702 | 0.0243 | 0.2634 | 0.2391 |
| 6 | 8 | 0.2318 | 0.4525 | 0.2207 | 0.0433 | 0.2467 | 0.2034 | 24 | 34 | 0.2021 | 0.4027 | 0.2006 | 0.0243 | 0.2242 | 0.2000 |
| 6 | 10 | 0.2318 | 0.4381 | 0.2063 | 0.0433 | 0.2474 | 0.2041 | 25 | 15 | 0.2295 | 0.4442 | 0.2148 | 0.0366 | 0.3377 | 0.3012 |
| 7 | 5 | 0.2377 | 0.4375 | 0.1998 | 0.0478 | 0.2506 | 0.2028 | 25 | 18 | 0.2295 | 0.4429 | 0.2134 | 0.0366 | 0.2582 | 0.2216 |
| 7 | 10 | 0.2377 | 0.4381 | 0.2004 | 0.0478 | 0.2474 | 0.1995 | 26 | 28 | 0.2325 | 0.4724 | 0.2399 | 0.0557 | 0.2799 | 0.2242 |
| 8 | 3 | 0.2147 | 0.4155 | 0.2008 | 0.0236 | 0.2237 | 0.2001 | 26 | 36 | 0.2325 | 0.4993 | 0.2668 | 0.0557 | 0.2809 | 0.2252 |
| 8 | 12 | 0.2147 | 0.4167 | 0.2020 | 0.0236 | 0.2249 | 0.2012 | 27 | 25 | 0.2580 | 0.4581 | 0.2001 | 0.0575 | 0.2573 | 0.1999 |
| 8 | 20 | 0.2147 | 0.4151 | 0.2005 | 0.0236 | 0.2287 | 0.2050 | 27 | 36 | 0.2580 | 0.4993 | 0.2413 | 0.0575 | 0.2809 | 0.2235 |
| 9 | 5 | 0.2357 | 0.4375 | 0.2018 | 0.0326 | 0.2506 | 0.2180 | 28 | 29 | 0.2654 | 0.4651 | 0.1997 | 0.0571 | 0.3316 | 0.2745 |
| 9 | 8 | 0.2357 | 0.4525 | 0.2168 | 0.0326 | 0.2467 | 0.2140 | 28 | 32 | 0.2654 | 0.5005 | 0.2352 | 0.0571 | 0.2589 | 0.2018 |
| 10 | 14 | 0.1993 | 0.4117 | 0.2124 | 0.0206 | 0.2224 | 0.2018 | 29 | 17 | 0.1821 | 0.3828 | 0.2007 | 0.0138 | 0.3053 | 0.2914 |
| 11 | 3 | 0.2042 | 0.4155 | 0.2113 | 0.0234 | 0.2237 | 0.2003 | 29 | 19 | 0.1821 | 0.3970 | 0.2149 | 0.0138 | 0.2135 | 0.1997 |
| 11 | 7 | 0.2042 | 0.4056 | 0.2014 | 0.0234 | 0.2655 | 0.2421 | 29 | 22 | 0.1821 | 0.3828 | 0.2007 | 0.0138 | 0.2139 | 0.2001 |
| 11 | 20 | 0.2042 | 0.4151 | 0.2109 | 0.0234 | 0.2287 | 0.2053 | 30 | 27 | 0.2096 | 0.4184 | 0.2089 | 0.0310 | 0.2318 | 0.2008 |
| 12 | 13 | 0.2112 | 0.4789 | 0.2677 | 0.0245 | 0.3325 | 0.3080 | 30 | 32 | 0.2096 | 0.5005 | 0.2910 | 0.0310 | 0.2589 | 0.2279 |
| 12 | 24 | 0.2112 | 0.4119 | 0.2007 | 0.0245 | 0.2452 | 0.2207 | 31 | 27 | 0.2037 | 0.4184 | 0.2147 | 0.0192 | 0.2318 | 0.2126 |
| 13 | 9 | 0.1809 | 0.5396 | 0.3587 | 0.0248 | 0.3331 | 0.3084 | 31 | 29 | 0.2037 | 0.4651 | 0.2614 | 0.0192 | 0.3316 | 0.3124 |
| 14 | 11 | 0.1804 | 0.3939 | 0.2134 | 0.0134 | 0.2212 | 0.2077 | 32 | 33 | 0.2263 | 0.4307 | 0.2044 | 0.0249 | 0.2510 | 0.2261 |
| 14 | 24 | 0.1804 | 0.4119 | 0.2315 | 0.0134 | 0.2452 | 0.2318 | 32 | 42 | 0.2263 | 0.4719 | 0.2456 | 0.0249 | 0.2697 | 0.2447 |
| 15 | 1 | 0.1729 | 0.4116 | 0.2387 | 0.0123 | 0.2319 | 0.2196 | 33 | 21 | 0.2720 | 0.4723 | 0.2003 | 0.0578 | 0.2634 | 0.2056 |
| 15 | 4 | 0.1729 | 0.3795 | 0.2065 | 0.0123 | 0.2320 | 0.2197 | 33 | 23 | 0.2720 | 0.4921 | 0.2201 | 0.0578 | 0.3744 | 0.3166 |
| 16 | 18 | 0.2014 | 0.4429 | 0.2415 | 0.0228 | 0.2582 | 0.2353 | 34 | 31 | 0.2698 | 0.4699 | 0.2001 | 0.0676 | 0.2674 | 0.1998 |
| 16 | 26 | 0.2014 | 0.4360 | 0.2345 | 0.0228 | 0.3996 | 0.3767 | 34 | 42 | 0.2698 | 0.4719 | 0.2021 | 0.0676 | 0.2697 | 0.2021 |
| 17 | 15 | 0.1944 | 0.4442 | 0.2499 | 0.0284 | 0.3377 | 0.3094 | 35 | 25 | 0.2369 | 0.4581 | 0.2212 | 0.0475 | 0.2573 | 0.2099 |
| 17 | 26 | 0.1944 | 0.4360 | 0.2416 | 0.0284 | 0.3996 | 0.3712 | 35 | 28 | 0.2369 | 0.4724 | 0.2355 | 0.0475 | 0.2799 | 0.2324 |
| 18 | 19 | 0.1581 | 0.3970 | 0.2389 | 0.0055 | 0.2135 | 0.2080 | 36 | 38 | 0.2291 | 0.4309 | 0.2018 | 0.0286 | 0.2285 | 0.1998 |
| 18 | 22 | 0.1581 | 0.3828 | 0.2247 | 0.0055 | 0.2139 | 0.2084 | 37 | 35 | 0.2564 | 0.4564 | 0.1999 | 0.0754 | 0.2759 | 0.2006 |
| 18 | 30 | 0.1581 | 0.3743 | 0.2162 | 0.0055 | 0.2162 | 0.2107 | 38 | 40 | 0.3000 | 0.5066 | 0.2066 | 0.0858 | 0.3276 | 0.2418 |
| 19 | 3 | 0.2053 | 0.4155 | 0.2102 | 0.0230 | 0.2237 | 0.2008 | 39 | 37 | 0.2847 | 0.4851 | 0.2005 | 0.0790 | 0.4681 | 0.3890 |
| 19 | 7 | 0.2053 | 0.4056 | 0.2002 | 0.0230 | 0.2655 | 0.2425 | 40 | 41 | 0.2676 | 0.4789 | 0.2113 | 0.0588 | 0.4148 | 0.3560 |
| 19 | 12 | 0.2053 | 0.4167 | 0.2114 | 0.0230 | 0.2249 | 0.2019 | 41 | 31 | 0.2304 | 0.4699 | 0.2395 | 0.0508 | 0.2674 | 0.2165 |
| 20 | 17 | 0.1742 | 0.3828 | 0.2087 | 0.0113 | 0.3053 | 0.2940 | 41 | 33 | 0.2304 | 0.4307 | 0.2003 | 0.0508 | 0.2510 | 0.2002 |
| 20 | 22 | 0.1742 | 0.3828 | 0.2087 | 0.0113 | 0.2139 | 0.2026 | 42 | 39 | 0.2022 | 0.4036 | 0.2014 | 0.0172 | 0.2174 | 0.2002 |



Figure 4. FOF convergence of the IEEE 15-bus network using GTO.

Table 4. GTO TOT comparison with other algorithms of the IEEE 15-bus.

| Scenario 1 |  |  |  |  | Scenario 2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GTO | SMA [12] | EGWO [57] | MEFO [25] | MWCA [13] | GTO | SMA [12] | SFSA [44] | FPA [45] |
| 9.0775 | 11.9761 | 12.2282 | 13.953 | 13.282 | 1.3962 | 2.4504 | 3.21 | 2.95 |

### 4.2. Study Case II: The Agiba Power Network

This network is an isolated practical one consisting of three DGs, five distribution transformers, five medium voltage motors, four MCCs, fourteen cables, and seventeen OCRs. The network SLD is designed using the Microsoft Visio platform as shown in Figure 5, while the system data regarding the equipment ratings and fault currents are announced in Appendix A (see Tables A1-A8). The upcoming conditions are assumed during the optimization process which are summarized as follows:

1. Transformer OCRs are fitted with the inrush inhibitor feature (2nd harmonic blocking) to transcend the inrush current during the energizing.
2. Motors are started using Variable Frequency Drives (VFDs) which limit the starting current to one per unit.
3. Equipment damage curves are not included in the study and considered as future works.
4. Only phase OC protection coordination considering the transformers connection is performed.
5. Bus coupler one and two are assumed to be closed.
6. The maximum fault current condition is examined when the three DGs are in service.
7. The minimum fault current condition is examined when only DG1 and DG2 are in service.
Since most of the distribution transformers are rated as the Dy11 vector group, a two-phase fault shall be theorized in addition to the three-phase fault. Figure 6 shows the two-phase fault currents distribution due to a two-phase fault (between band c) at the star side, as it is clarified that the fault current at line $C$ of the delta side is multiplied by two. Therefore, this network should be investigated using various test models of combinations between the three-phase and two-phase faults in addition to the maximum and minimum fault conditions. The following four test models are listed and a further analysis is performed to characterize each one.
8. Test Model One: Maximum three-phase fault current condition;
9. Test Model Two: Maximum general fault current condition;
10. Test Model Three: Minimum two-phase fault current condition; and
11. Test Model Four: Minimum general fault current condition.

The OCRs' optimum settings tabulated in Tables 5 and 6 are generated using the first two test models, respectively. The GTO accomplishes TOT of 1.2509 s and 0.8368 s for test model one while 1.2614 s and 0.7607 s for test model two using scenarios one and two, respectively. In addition, the $M / B$ operating times and their associated CTM values are listed in Tables 7 and 8 for the first two test models also. It can be observed that scenario two in test model two achieves the least possible TOT. In this context, the optimal settings for OCRs are also generated using the minimum fault current condition as announced in Tables 9 and 10, whereas the operating times are collected in Tables 11 and 12, respectively, respectively. The output TOTs of test model three are 1.3385 s for scenario one and 0.7875 s for scenario two, while in test model four they are 1.325 s for scenario one and 0.7589 s for scenario two.


Figure 5. The SLD of Agiba test network.


Figure 6. The 2-phase fault currents distribution over Dy11 distribution transformer.

Table 5. OCRs optimum settings of Agiba network using Test Model 1.

| Relay ID. | Scenario 1 |  |  | Scenario 2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | Curve |
| R1 | 331.6117 | 0.0644 | 340.3342 | 0.0470 | VI |
| R2 | 330.5366 | 0.0604 | 341.1965 | 0.0314 | EI |
| R3 | 331.2808 | 0.0627 | 341.0609 | 0.0304 | EI |
| R4 | 167.7614 | 0.0639 | 135.9965 | 0.1137 | VI |
| R5 | 199.1274 | 0.0205 | 152.1001 | 0.2837 | EI |
| R6 | 20.3363 | 0.0370 | 15.2550 | 0.8794 | VI |
| R7 | 156.3881 | 0.0723 | 150.7917 | 0.1205 | VI |
| R8 | 226.3209 | 0.0207 | 248.9035 | 0.1443 | EI |
| R9 | 10.1672 | 0.0425 | 10.3708 | 0.9998 | VI |
| R10 | 164.7615 | 0.0646 | 167.8963 | 0.0889 | VI |
| R11 | 152.1286 | 0.0226 | 202.3552 | 0.1596 | EI |
| R12 | 40.5282 | 0.0316 | 37.4771 | 0.2736 | VI |
| R13 | 167.2944 | 0.0639 | 167.9290 | 0.1754 | EI |
| R14 | 196.5018 | 0.0206 | 202.7059 | 0.0556 | VI |
| R15 | 15.2566 | 0.0503 | 19.4621 | 0.5316 | VI |
| R16 | 163.7832 | 0.0639 | 160.8550 | 0.0909 | VI |
| R17 | 243.5889 | 0.0188 | 238.0619 | 0.1101 | EI |
| TOT (s) |  | 1.2509 |  |  | 0.8368 |

Table 6. OCRs optimum settings of Agiba network using Test Model 2.

| Relay ID. | Scenario 1 |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | Curve |
| R1 | 300.7964 | 0.0688 | 341.1739 | 0.0300 | EI |
| R2 | 303.7651 | 0.0674 | 341.1994 | 0.0276 | EI |
| R3 | 290.8823 | 0.0688 | 341.0980 | 0.0287 | EI |
| R4 | 154.0312 | 0.0678 | 167.8909 | 0.0909 | VI |
| R5 | 164.0629 | 0.0220 | 201.7282 | 0.1612 | EI |
| R6 | 16.5401 | 0.0387 | 20.3211 | 0.0572 | LI |
| R7 | 146.5419 | 0.0755 | 136.0492 | 0.2656 | EI |
| R8 | 251.0151 | 0.0200 | 188.4000 | 0.2519 | EI |
| R9 | 10.2956 | 0.0424 | 10.3699 | 0.9998 | VI |
| R10 | 167.5220 | 0.0647 | 166.6866 | 0.1765 | EI |
| R11 | 152.1000 | 0.0226 | 152.1013 | 0.2835 | EI |
| R12 | 40.0069 | 0.0317 | 40.6304 | 0.0284 | LI |
| R13 | 151.1998 | 0.0685 | 138.6302 | 0.1137 | VI |
| R14 | 152.1035 | 0.0226 | 167.4478 | 0.2337 | EI |
| R15 | 17.9116 | 0.0381 | 20.3392 | 0.0572 | LI |
| R16 | 125.9700 | 0.0745 | 167.6305 | 0.1751 | EI |
| R17 | 185.1458 | 0.0209 | 185.1000 | 0.1923 | EI |
| TOT (s) |  | 1.2614 |  |  | 0.7607 |

Table 7. Operating times of M/B relay pairs with their associated CTM values of the Agiba Network using Test Model 1.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 5 | 4 | 0.0501 | 0.2500 | 0.1999 | 0.0500 | 0.2494 | 0.1994 |
| 4 | 1 | 0.1543 | 0.4295 | 0.2753 | 0.0781 | 0.3620 | 0.2839 |
| 4 | 2 | 0.1543 | 0.4015 | 0.2472 | 0.0781 | 0.3841 | 0.3061 |
| 4 | 3 | 0.1543 | 0.4176 | 0.2634 | 0.0781 | 0.3708 | 0.2928 |
| 6 | 1 | 0.0501 | 0.4295 | 0.3794 | 0.0648 | 0.3620 | 0.2972 |
| 6 | 2 | 0.0501 | 0.4015 | 0.3514 | 0.0648 | 0.3841 | 0.3193 |
| 6 | 3 | 0.0501 | 0.4176 | 0.3676 | 0.0648 | 0.3708 | 0.3060 |
| 8 | 7 | 0.0499 | 0.2501 | 0.2002 | 0.0501 | 0.2490 | 0.1989 |
| 7 | 1 | 0.1701 | 0.4295 | 0.2594 | 0.0922 | 0.3620 | 0.2697 |
| 7 | 2 | 0.1701 | 0.4015 | 0.2313 | 0.0922 | 0.3841 | 0.2919 |

Table 7. Cont.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 7 | 3 | 0.1701 | 0.4176 | 0.2475 | 0.0922 | 0.3708 | 0.2786 |
| 9 | 1 | 0.0500 | 0.4295 | 0.3795 | 0.0500 | 0.3620 | 0.3120 |
| 9 | 2 | 0.0500 | 0.4015 | 0.3515 | 0.0500 | 0.3841 | 0.3341 |
| 9 | 3 | 0.0500 | 0.4176 | 0.3677 | 0.0500 | 0.3708 | 0.3208 |
| 11 | 10 | 0.0501 | 0.2500 | 0.1999 | 0.0499 | 0.2502 | 0.2003 |
| 10 | 1 | 0.1549 | 0.4295 | 0.2746 | 0.0762 | 0.3620 | 0.2858 |
| 10 | 2 | 0.1549 | 0.4015 | 0.2466 | 0.0762 | 0.3841 | 0.3079 |
| 10 | 3 | 0.1549 | 0.4176 | 0.2628 | 0.0762 | 0.3708 | 0.2946 |
| 12 | 1 | 0.0500 | 0.4295 | 0.3795 | 0.0499 | 0.3620 | 0.3121 |
| 12 | 2 | 0.0500 | 0.4015 | 0.3515 | 0.0499 | 0.3841 | 0.3342 |
| 12 | 3 | 0.0500 | 0.4176 | 0.3676 | 0.0499 | 0.3708 | 0.3209 |
| 14 | 13 | 0.0501 | 0.2498 | 0.1997 | 0.0501 | 0.4308 | 0.3807 |
| 13 | 1 | 0.1542 | 0.4295 | 0.2753 | 0.0503 | 0.3620 | 0.3117 |
| 13 | 2 | 0.1542 | 0.4015 | 0.2473 | 0.0503 | 0.3841 | 0.3338 |
| 13 | 3 | 0.1542 | 0.4176 | 0.2634 | 0.0503 | 0.3708 | 0.3205 |
| 15 | 1 | 0.0641 | 0.4295 | 0.3654 | 0.0501 | 0.3620 | 0.3119 |
| 15 | 2 | 0.0641 | 0.4015 | 0.3374 | 0.0501 | 0.3841 | 0.3341 |
| 15 | 3 | 0.0641 | 0.4176 | 0.3536 | 0.0501 | 0.3708 | 0.3208 |
| 17 | 16 | 0.0500 | 0.2500 | 0.2000 | 0.0501 | 0.2502 | 0.2001 |
| 16 | 1 | 0.1529 | 0.4295 | 0.2766 | 0.0745 | 0.3620 | 0.2875 |
| 16 | 2 | $0.1529$ | $0.4015$ | $0.2486$ | $0.0745$ | 0.3841 | 0.3096 |
| 16 | 3 | 0.1529 | 0.4176 | 0.2647 | 0.0745 | 0.3708 | 0.2963 |

Table 8. Operating times of $\mathrm{M} / \mathrm{B}$ relay pairs with their associated CTM values of the Agiba Network using Test Model 2.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 5 | 4 | 0.0500 | 0.2501 | 0.2000 | 0.2501 | 0.0501 | 0.2000 |
| 4 | 1 | 0.1587 | 0.4191 | 0.2603 | 0.3665 | 0.0780 | 0.2884 |
| 4 | 2 | 0.1587 | 0.4143 | 0.2556 | 0.3372 | 0.0780 | 0.2592 |
| 4 | 3 | 0.1587 | 0.4071 | 0.2484 | 0.3510 | 0.0780 | 0.2730 |
| 6 | 1 | 0.0501 | 0.4191 | 0.3690 | 0.3665 | 0.0500 | 0.3164 |
| 6 | 2 | 0.0501 | 0.4143 | 0.3642 | 0.3372 | 0.0500 | 0.2871 |
| 6 | 3 | 0.0501 | 0.4071 | 0.3570 | 0.3510 | 0.0500 | 0.3009 |
| 8 | 7 | 0.0503 | 0.2503 | 0.2000 | 0.2964 | 0.0500 | 0.2463 |
| 7 | 1 | 0.1737 | 0.4191 | 0.2453 | 0.3665 | 0.0499 | 0.3165 |
| 7 | 2 | 0.1737 | 0.4143 | 0.2406 | 0.3372 | 0.0499 | 0.2872 |
| 7 | 3 | 0.1737 | 0.4071 | 0.2333 | 0.3510 | 0.0499 | 0.3011 |
| 9 | 1 | 0.0500 | 0.4191 | 0.3691 | 0.3665 | 0.0500 | 0.3165 |
| 9 | 2 | 0.0500 | 0.4143 | 0.3643 | 0.3372 | 0.0500 | 0.2872 |
| 9 | 3 | 0.0500 | 0.4071 | 0.3571 | 0.3510 | 0.0500 | 0.3010 |
| 11 | 10 | 0.0501 | 0.2502 | 0.2001 | 0.4103 | 0.0500 | 0.3603 |
| 10 | 1 | 0.1562 | 0.4191 | 0.2629 | 0.3665 | 0.0499 | 0.3166 |
| 10 | 2 | 0.1562 | 0.4143 | 0.2582 | 0.3372 | 0.0499 | 0.2873 |
| 10 | 3 | 0.1562 | 0.4071 | 0.2509 | 0.3510 | 0.0499 | 0.3011 |
| 12 | 1 | 0.0500 | 0.4191 | 0.3691 | 0.3665 | 0.0500 | 0.3164 |
| 12 | 2 | 0.0500 | 0.4143 | 0.3643 | 0.3372 | 0.0500 | 0.2871 |
| 12 | 3 | 0.0500 | 0.4071 | 0.3571 | 0.3510 | 0.0500 | 0.3010 |
| 14 | 13 | 0.0500 | 0.2503 | 0.2003 | 0.2494 | 0.0499 | 0.1994 |
| 13 | 1 | 0.1594 | 0.4191 | 0.2596 | 0.3665 | 0.0797 | 0.2868 |
| 13 | 2 | 0.1594 | 0.4143 | 0.2549 | 0.3372 | 0.0797 | 0.2575 |
| 13 | 3 | $0.1594$ | 0.4071 | 0.2476 | 0.3510 | 0.0797 | 0.2713 |
| 15 | 1 | 0.0501 | 0.4191 | 0.3690 | 0.3665 | 0.0500 | 0.3164 |
| 15 | 2 | 0.0501 | 0.4143 | 0.3643 | 0.3372 | 0.0500 | 0.2871 |
| 15 | 3 | 0.0501 | 0.4071 | 0.3570 | 0.3510 | 0.0500 | 0.3009 |
| 17 | 16 | 0.0501 | 0.2507 | 0.2005 | 0.4331 | 0.0527 | 0.3803 |
| 16 | 1 | 0.1629 | 0.4191 | 0.2562 | 0.3665 | 0.0500 | 0.3164 |
| 16 | 2 | 0.1629 | 0.4143 | 0.2515 | 0.3372 | 0.0500 | 0.2871 |
| 16 | 3 | 0.1629 | 0.4071 | 0.2442 | 0.3510 | 0.0500 | 0.3010 |

Table 9. OCRs optimum settings of Agiba network using Test Model 3.

| Relay ID. | Scenario $\mathbf{1}$ |  |  |  | Scenario 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{I} \boldsymbol{p}(\mathbf{A})$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | $\boldsymbol{I}_{\boldsymbol{p}}(\mathrm{A})$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | Curve |
|  | 319.6939 | 0.0505 | 311.2207 | 0.0208 | EI |
| R2 | 341.1941 | 0.0491 | 340.4273 | 0.0181 | EI |
| R4 | 165.7031 | 0.0558 | 154.7975 | 0.0744 | EI |
| R5 | 200.7996 | 0.0176 | 196.5116 | 0.0795 | EI |
| R6 | 15.2550 | 0.0345 | 16.0424 | 0.0394 | LI |
| R7 | 125.9700 | 0.0712 | 131.2142 | 0.1403 | EI |
| R8 | 188.4000 | 0.0192 | 217.2035 | 0.0864 | EI |
| R9 | 7.7850 | 0.0398 | 10.3080 | 0.0616 | LI |
| R10 | 161.5779 | 0.0567 | 151.4155 | 0.0779 | EI |
| R11 | 152.1000 | 0.0197 | 183.5210 | 0.0412 | VI |
| R12 | 30.5400 | 0.0291 | 30.5400 | 0.0249 | LI |
| R13 | 125.9701 | 0.0659 | 146.6947 | 0.0832 | EI |
| R14 | 152.1000 | 0.0197 | 171.1541 | 0.1047 | EI |
| R15 | 15.2550 | 0.0345 | 20.0760 | 0.0314 | LI |
| R16 | 163.2165 | 0.0555 | 125.9700 | 0.1105 | EI |
| R17 | 201.7820 | 0.0174 | 234.5884 | 0.0532 | EI |
| TOT (s) |  | 1.3385 |  |  | 0.7875 |

Table 10. OCRs optimum settings of Agiba network using Test Model 4.

| Relay ID. | Scenario 1 |  | Scenario 2 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | $\boldsymbol{I}_{\boldsymbol{p}} \mathbf{( A )}$ | $\boldsymbol{T}_{\boldsymbol{D}} \mathbf{( s )}$ | Curve |  |  |  |  |  |
| R1 | 300.9234 | 0.0570 | 341.1827 | 0.0197 | EI |  |  |  |  |  |
| R2 | 302.8060 | 0.0529 | 341.1986 | 0.0307 | VI |  |  |  |  |  |
| R4 | 167.5252 | 0.0544 | 125.9700 | 0.1075 | EI |  |  |  |  |  |
| R5 | 152.1000 | 0.0197 | 199.3379 | 0.0774 | EI |  |  |  |  |  |
| R6 | 15.2550 | 0.0345 | 16.4287 | 0.3422 | VI |  |  |  |  |  |
| R7 | 125.9701 | 0.0703 | 126.0366 | 0.1436 | EI |  |  |  |  |  |
| R8 | 188.4000 | 0.0193 | 188.4171 | 0.1158 | EI |  |  |  |  |  |
| R9 | 7.7850 | 0.0398 | 7.7872 | 0.7265 | VI |  |  |  |  |  |
| R10 | 125.9700 | 0.0653 | 167.3015 | 0.0599 | EI |  |  |  |  |  |
| R11 | 152.1003 | 0.0201 | 153.7081 | 0.0501 | VI |  |  |  |  |  |
| R12 | 40.6146 | 0.0269 | 40.7084 | 0.1364 | VI |  |  |  |  |  |
| R13 | 167.7060 | 0.0544 | 167.9591 | 0.0594 | EI |  |  |  |  |  |
| R14 | 202.7896 | 0.0176 | 152.1852 | 0.1332 | EI |  |  |  |  |  |
| R15 | 20.2051 | 0.0323 | 15.2761 | 0.3681 | VI |  |  |  |  |  |
| R16 | 166.9924 | 0.0538 | 165.3569 | 0.0588 | EI |  |  |  |  |  |
| R17 | 185.1000 | 0.0181 | 221.1283 | 0.0328 | VI |  |  |  |  |  |
| TOT (s) | 1.3250 |  |  |  |  |  |  |  | 0.7589 |  |

Table 11. Operating times of M/B relay pairs of the Agiba Network using Test Model 3.

| M/B Relay Pair |  |  | Scenario 1 |  |  |  |  |  |  | Scenario 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{M}$ | $\mathbf{B}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ |  |  |  |
| 5 | 4 | 0.0499 | 0.2502 | 0.2002 | 0.0500 | 0.2499 | 0.1999 |  |  |  |
| 4 | 1 | 0.1717 | 0.4003 | 0.2286 | 0.0613 | 0.3273 | 0.2660 |  |  |  |
| 4 | 2 | 0.1717 | 0.4205 | 0.2488 | 0.0613 | 0.3554 | 0.2941 |  |  |  |
| 6 | 1 | 0.0500 | 0.4003 | 0.3503 | 0.0500 | 0.3273 | 0.2773 |  |  |  |
| 6 | 2 | 0.0500 | 0.4205 | 0.3705 | 0.0500 | 0.3554 | 0.3054 |  |  |  |
| 8 | 7 | 0.0502 | 0.2501 | 0.1999 | 0.0500 | 0.2505 | 0.2005 |  |  |  |

Table 11. Cont.

| M/B Relay Pair |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{M}$ | $\mathbf{B}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( \mathbf { s } )}$ | $\mathbf{C T M} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( \mathbf { s } )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | Scenario $\mathbf{C T M} \mathbf{( s )}$ |
| 7 | 1 | 0.1944 | 0.4003 | 0.2060 | 0.0828 | 0.3273 | 0.2445 |
| 7 | 2 | 0.1944 | 0.4205 | 0.2262 | 0.0828 | 0.3554 | 0.2726 |
| 9 | 1 | 0.0500 | 0.4003 | 0.3503 | 0.0500 | 0.3273 | 0.2773 |
| 9 | 2 | 0.0500 | 0.4205 | 0.3705 | 0.0500 | 0.3554 | 0.3054 |
| 11 | 10 | 0.0500 | 0.2502 | 0.2002 | 0.0500 | 0.2499 | 0.1999 |
| 10 | 1 | 0.1726 | 0.4003 | 0.2278 | 0.0614 | 0.3273 | 0.2660 |
| 10 | 2 | 0.1726 | 0.4205 | 0.2480 | 0.0614 | 0.3554 | 0.2941 |
| 12 | 1 | 0.0500 | 0.4003 | 0.3503 | 0.0607 | 0.3273 | 0.2666 |
| 12 | 2 | 0.0500 | 0.4205 | 0.3705 | 0.0607 | 0.3554 | 0.2947 |
| 14 | 13 | 0.0500 | 0.2500 | 0.2000 | 0.0499 | 0.2500 | 0.2001 |
| 13 | 1 | 0.1800 | 0.4003 | 0.2204 | 0.0615 | 0.3273 | 0.2658 |
| 13 | 2 | 0.1800 | 0.4205 | 0.2406 | 0.0615 | 0.3554 | 0.2939 |
| 15 | 1 | 0.0501 | 0.4003 | 0.3503 | 0.0501 | 0.3273 | 0.2773 |
| 15 | 2 | 0.0501 | 0.4205 | 0.3705 | 0.0501 | 0.3554 | 0.3053 |
| 17 | 16 | 0.0499 | 0.2501 | 0.2002 | 0.0500 | 0.2538 | 0.2038 |
| 16 | 1 | 0.1697 | 0.4003 | 0.2307 | 0.0601 | 0.3273 | 0.2672 |
| 16 | 2 | 0.1697 | 0.4205 | 0.2509 | 0.0601 | 0.3554 | 0.2953 |

Table 12. Operating times of M/B relay pairs for Agiba Network using Test Model 4.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 5 | 4 | 0.0501 | 0.2502 | 0.2000 | 0.0501 | 0.2490 | 0.1989 |
| 4 | 1 | 0.1683 | 0.4224 | 0.2541 | 0.0585 | 0.3892 | 0.3307 |
| 4 | 2 | 0.1683 | 0.3945 | 0.2262 | 0.0585 | 0.3321 | 0.2736 |
| 6 | 1 | 0.0499 | 0.4224 | 0.3725 | 0.0500 | 0.3892 | 0.3391 |
| 6 | 2 | 0.0499 | 0.3945 | 0.3446 | 0.0500 | 0.3321 | 0.2821 |
| 8 | 7 | 0.0505 | 0.2508 | 0.2003 | 0.0503 | 0.2498 | 0.1994 |
| 7 | 1 | 0.1922 | 0.4224 | 0.2302 | 0.0782 | 0.3892 | 0.3110 |
| 7 | 2 | 0.1922 | 0.3945 | 0.2024 | 0.0782 | 0.3321 | 0.2539 |
| 9 | 1 | 0.0500 | 0.4224 | 0.3724 | 0.0501 | 0.3892 | 0.3391 |
| 9 | 2 | 0.0500 | 0.3945 | 0.3445 | 0.0501 | 0.3321 | 0.2820 |
| 11 | 10 | 0.0511 | 0.2514 | 0.2003 | 0.0502 | 0.2502 | 0.2000 |
| 10 | 1 | 0.1783 | 0.4224 | 0.2441 | 0.0578 | 0.3892 | 0.3314 |
| 10 | 2 | 0.1783 | 0.3945 | 0.2162 | 0.0578 | 0.3321 | 0.2744 |
| 12 | 1 | 0.0501 | 0.4224 | 0.3723 | 0.0502 | 0.3892 | 0.3389 |
| 12 | 2 | 0.0501 | 0.3945 | 0.3445 | 0.0502 | 0.3321 | 0.2819 |
| 14 | 13 | 0.0504 | 0.2502 | 0.1998 | 0.0501 | 0.2503 | 0.2002 |
| 13 | 1 | 0.1683 | 0.4224 | 0.2541 | 0.0578 | 0.3892 | 0.3314 |
| 13 | 2 | 0.1683 | 0.3945 | 0.2262 | 0.0578 | 0.3321 | 0.2743 |
| 15 | 1 | 0.0501 | 0.4224 | 0.3723 | 0.0500 | 0.3892 | 0.3391 |
| 15 | 2 | 0.0501 | 0.3945 | 0.3445 | 0.0500 | 0.3321 | 0.2821 |
| 17 | 16 | 0.0500 | 0.2503 | 0.2003 | 0.0501 | 0.2500 | 0.1999 |
| 16 | 1 | 0.1662 | 0.4224 | 0.2562 | 0.0554 | 0.3892 | 0.3338 |
| 16 | 2 | 0.1662 | 0.3945 | 0.2283 | 0.0554 | 0.3321 | 0.2767 |

Figures 7 and 8 depict the FOF convergence of the Agiba power network using scenarios one and two, respectively. Moreover, statistical measures are analyzed in Table 13 to evaluate the GTO performance using parametric and non-parametric tests. The $p$-value is produced from the $t$-test using thirty independent runs and by being rounded to four decimals. It is worth to mention that the smaller the $p$-value, the stronger the evidence to reject the null hypothesis. Consequently, the output conclusions from the studied case with DGs considering the transformer phase shift are as follows:

1. The GTO succeeds in obtaining the optimal solutions without any violations in practical isolated networks with DGs using various test models.
2. The OCRs' coordination using the minimum two-phase fault current guarantees the fast convergence rate. Therefore, it is the suitable choice in online applications.
3. The output $p$-value is minimum in test models one and two, which assures that the attained results at each run are more correlated. Accordingly, the maximum fault current coordination using the fixed NI curve is the best suitable framework in the case of a radial DG network with distribution transformers.
4. The distribution of the EF currents with their optimal coordination in the case of Dy11 transformers will be a future study.


Figure 7. FOF convergence of Agiba test network using scenario 1 settings.


Figure 8. FOF convergence of Agiba test network using scenario 2 settings.

Table 13. Statistical measures of GTO performance in Agiba power network over 30 independent runs.

| Test Model |  | Parametric Tests |  |  |  |  | Non-Parametric Tests | Elapsed <br> Time (s) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Min | Max | Mean | Median | SD | $p$-Value |  |
|  | Scenario 1 | 1.2509 | 1.4947 | 1.3043 | 1.2839 | 0.0546 | 0 | 101.3520 |
| Model 1 | Scenario 2 | 0.8368 | 316.0821 | 41.4577 | 1.0940 | 91.2971 | 0.0106 | 96.4464 |
|  | Scenario 1 | 1.2614 | 1.5560 | 1.3321 | 1.3204 | 0.0612 | 0 | 89.0859 |
| Model 2 | Scenario 2 | 0.7607 | 51.9367 | 4.9727 | 1.0817 | 12.1945 | 0.0343 | 99.9674 |
|  | Scenario 1 | 1.3385 | 1.7845 | 1.4123 | 1.3814 | 0.1057 | 0.0003 | 78.1487 |
| Model 3 | Scenario 2 | 0.7875 | 261.3888 | 9.8377 | 1.1547 | 47.5108 | 0.1527 | 73.4870 |
|  | Scenario 1 | 1.3250 | 1.8892 | 1.3953 | 1.3587 | 0.1082 | 0.0007 | 78.1213 |
| Model 4 | Scenario 2 | 0.7589 | 109.7749 | 5.5243 | 1.2019 | 20.0733 | 0.1019 | 76.3707 |

Finally, these results demonstrate the efficacy of selecting the best suitable optimization test model in distribution networks. However, the validity of GTO results is examined over a well-known algorithm (WCA) that proves its superiority in all test models, as shown in Table 14.

Table 14. GTO defense regarding the TOT in Agiba power network.

| Test Model | Scenario | GTO | WCA |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1.2509 | 1.6962 |
|  | 2 | 0.8368 | 1.7862 |
| 2 | 1 | 1.2614 | 1.6556 |
|  | 2 | 0.7607 | 1.4319 |
| 3 | 1 | 1.3385 | 1.7049 |
|  | 2 | 0.7875 | 1.3996 |
| 4 | 1 | 1.3250 | 1.9487 |
|  | 2 | 0.7589 | 1.4550 |

Moreover, further analysis is performed in each test model to manifest which of them will achieve the best smooth coordination between M/B relay pairs. This has been concluded by checking the coordination in the minimum fault condition when the opposite maximum fault condition is optimized and vice versa. The checked operating times and CTM values for the four test models are arranged in Tables 15-19. It can be notified that the best strategy for fulfilling the smoothest coordination is using test model four. That is because it achieves the minimum possible value of the summation of CTMs, average of CTMs, and standard deviation.

Table 15. Coordination check of Test Model 1.

| M/B Relay Pair |  |  | Scenario $\mathbf{1}$ |  |  |  |  |  |  | Scenario 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{M}$ | $\mathbf{B}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ |  |  |  |
| 5 | 4 | 0.0552 | 0.2940 | 0.2387 | 0.0840 | 0.3394 | 0.2554 |  |  |  |
| 4 | 1 | 0.1903 | 0.4837 | 0.2934 | 0.1362 | 0.4365 | 0.3004 |  |  |  |
| 4 | 2 | 0.1903 | 0.4520 | 0.2618 | 0.1362 | 0.5035 | 0.3673 |  |  |  |
| 6 | 1 | 0.0562 | 0.4837 | 0.4275 | 0.1095 | 0.4365 | 0.3270 |  |  |  |
| 6 | 2 | 0.0562 | 0.4520 | 0.3958 | 0.1095 | 0.5035 | 0.3940 |  |  |  |
| 8 | 7 | 0.0555 | 0.2911 | 0.2355 | 0.0869 | 0.3439 | 0.2570 |  |  |  |
| 7 | 1 | 0.2087 | 0.4837 | 0.2749 | 0.1616 | 0.4365 | 0.2750 |  |  |  |
| 7 | 2 | 0.2087 | 0.4520 | 0.2433 | 0.1616 | 0.5035 | 0.3419 |  |  |  |
| 9 | 1 | 0.0554 | 0.4837 | 0.4283 | 0.0844 | 0.4365 | 0.3521 |  |  |  |
| 9 | 2 | 0.0554 | 0.4520 | 0.3966 | 0.0844 | 0.5035 | 0.4191 |  |  |  |
| 11 | 10 | 0.0549 | 0.2936 | 0.2387 | 0.0839 | 0.3456 | 0.2617 |  |  |  |

Table 15. Cont.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathbf{s})$ | CTM (s) |
| 10 | 1 | 0.1908 | 0.4837 | 0.2929 | 0.1342 | 0.4365 | 0.3023 |
| 10 | 2 | 0.1908 | 0.4520 | 0.2612 | 0.1342 | 0.5035 | 0.3693 |
| 12 | 1 | 0.0573 | 0.4837 | 0.4264 | 0.0848 | 0.4365 | 0.3517 |
| 12 | 2 | 0.0573 | 0.4520 | 0.3947 | 0.0848 | 0.5035 | 0.4187 |
| 14 | 13 | 0.0552 | 0.2934 | 0.2382 | 0.0661 | 0.7385 | 0.6724 |
| 13 | 1 | 0.1900 | 0.4837 | 0.2936 | 0.1435 | 0.4365 | 0.2930 |
| 13 | 2 | 0.1900 | 0.4520 | 0.2620 | 0.1435 | 0.5035 | 0.3600 |
| 15 | 1 | 0.0715 | 0.4837 | 0.4121 | 0.0847 | 0.4365 | 0.3519 |
| 15 | 2 | 0.0715 | 0.4520 | 0.3805 | 0.0847 | 0.5035 | 0.4188 |
| 17 | 16 | 0.0557 | 0.2932 | 0.2375 | 0.0838 | 0.3432 | 0.2594 |
| 16 | 1 | 0.1882 | 0.4837 | 0.2954 | 0.1309 | 0.4365 | 0.3057 |
| 16 | 2 | 0.1882 | 0.4520 | 0.2638 | 0.1309 | 0.5035 | 0.3726 |

Table 16. Coordination check of Test Model 2.

| M/B Relay Pair |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{M}$ | $\mathbf{B}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | Scenario $\mathbf{1}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | Scenario 2 |
| 5 | 4 | 0.0575 | 0.2949 | 0.2373 | 0.1069 | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | 0.3533 |
| 4 | 1 | 0.2018 | 0.5097 | 0.3079 | 0.1509 | 0.5920 | 0.2464 |
| 4 | 2 | 0.2018 | 0.5047 | 0.3028 | 0.1509 | 0.5447 | 0.4411 |
| 6 | 1 | 0.0571 | 0.5097 | 0.4526 | 0.0922 | 0.5920 | 0.3998 |
| 6 | 2 | 0.0571 | 0.5047 | 0.4475 | 0.0922 | 0.5447 | 0.4525 |
| 8 | 7 | 0.0589 | 0.2926 | 0.2337 | 0.1095 | 0.5402 | 0.4308 |
| 7 | 1 | 0.2199 | 0.5097 | 0.2898 | 0.1687 | 0.5920 | 0.4233 |
| 7 | 2 | 0.2199 | 0.5047 | 0.2848 | 0.1687 | 0.5447 | 0.3761 |
| 9 | 1 | 0.0564 | 0.5097 | 0.4533 | 0.0919 | 0.5920 | 0.5001 |
| 9 | 2 | 0.0564 | 0.5047 | 0.4483 | 0.0919 | 0.5447 | 0.4528 |
| 11 | 10 | 0.0574 | 0.2974 | 0.2400 | 0.1065 | 0.7316 | 0.6252 |
| 10 | 1 | 0.2001 | 0.5097 | 0.3096 | 0.1689 | 0.5920 | 0.4231 |
| 10 | 2 | 0.2001 | 0.5047 | 0.3046 | 0.1689 | 0.5447 | 0.3758 |
| 12 | 1 | 0.0587 | 0.5097 | 0.4510 | 0.0928 | 0.5920 | 0.4992 |
| 12 | 2 | 0.0587 | 0.5047 | 0.4460 | 0.0928 | 0.5447 | 0.4520 |
| 14 | 13 | 0.0574 | 0.2944 | 0.2370 | 0.1065 | 0.3475 | 0.2410 |
| 13 | 1 | 0.2022 | 0.5097 | 0.3075 | 0.1526 | 0.5920 | 0.4394 |
| 13 | 2 | 0.2022 | 0.5047 | 0.3024 | 0.1526 | 0.5447 | 0.3921 |
| 15 | 1 | 0.0573 | 0.5097 | 0.4524 | 0.0923 | 0.5920 | 0.4997 |
| 15 | 2 | 0.0573 | 0.5047 | 0.4474 | 0.0923 | 0.5447 | 0.4524 |
| 17 | 16 | 0.0579 | 0.2903 | 0.2323 | 0.1120 | 0.7664 | 0.6544 |
| 16 | 1 | 0.2035 | 0.5097 | 0.3062 | 0.1695 | 0.5920 | 0.4225 |
| 16 | 2 | 0.2035 | 0.5047 | 0.3012 | 0.1695 | 0.5447 | 0.3752 |

Table 17. Coordination check of Test Model 3.

| M/B Relay Pair |  | Scenario 1 |  |  |  | Scenario 2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{M}$ | $\mathbf{B}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( \mathbf { s } )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( \mathbf { s } )}$ | $\mathbf{C T M} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{M}} \mathbf{( s )}$ | $\boldsymbol{t}_{\boldsymbol{B}} \mathbf{( s )}$ | $\mathbf{C T M} \mathbf{( s )}$ |
| 5 | 4 | 0.0451 | 0.2144 | 0.1693 | 0.0301 | 0.1486 | 0.1185 |
| 4 | 1 | 0.1334 | 0.3537 | 0.2203 | 0.0176 | 0.2508 | 0.2331 |
| 4 | 2 | 0.1334 | 0.3683 | 0.2349 | 0.0176 | 0.2691 | 0.2514 |
| 6 | 1 | 0.0438 | 0.3537 | 0.3099 | 0.0268 | 0.2508 | 0.2240 |
| 6 | 2 | 0.0438 | 0.3683 | 0.3245 | 0.0268 | 0.2691 | 0.2423 |
| 8 | 7 | 0.0454 | 0.2195 | 0.1742 | 0.0292 | 0.1455 | 0.1163 |
| 7 | 1 | 0.1549 | 0.3537 | 0.1988 | 0.0238 | 0.2508 | 0.2269 |

Table 17. Cont.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathrm{~s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 7 | 2 | 0.1549 | 0.3683 | 0.2135 | 0.0238 | 0.2691 | 0.2452 |
| 9 | 1 | 0.0445 | 0.3537 | 0.3092 | 0.0268 | 0.2508 | 0.2239 |
| 9 | 2 | 0.0445 | 0.3683 | 0.3239 | 0.0268 | 0.2691 | 0.2422 |
| 11 | 10 | 0.0456 | 0.2148 | 0.1692 | 0.0381 | 0.1487 | 0.1106 |
| 10 | 1 | 0.1344 | 0.3537 | 0.2193 | 0.0176 | 0.2508 | 0.2331 |
| 10 | 2 | 0.1344 | 0.3683 | 0.2340 | 0.0176 | 0.2691 | 0.2514 |
| 12 | 1 | 0.0429 | 0.3537 | 0.3108 | 0.0324 | 0.2508 | 0.2184 |
| 12 | 2 | 0.0429 | 0.3683 | 0.3254 | 0.0324 | 0.2691 | 0.2367 |
| 14 | 13 | 0.0456 | 0.2190 | 0.1733 | 0.0300 | 0.1488 | 0.1188 |
| 13 | 1 | 0.1433 | 0.3537 | 0.2104 | 0.0177 | 0.2508 | 0.2331 |
| 13 | 2 | 0.1433 | 0.3683 | 0.2250 | 0.0177 | 0.2691 | 0.2514 |
| 15 | 1 | 0.0438 | 0.3537 | 0.3099 | 0.0267 | 0.2508 | 0.2240 |
| 15 | 2 | 0.0438 | 0.3683 | 0.3245 | 0.0267 | 0.2691 | 0.2423 |
| 17 | 16 | 0.0451 | 0.2144 | 0.1692 | 0.0302 | 0.1523 | 0.1221 |
| 16 | 1 | 0.1320 | 0.3537 | 0.2217 | 0.0173 | 0.2508 | 0.2335 |
| 16 | 2 | 0.1320 | 0.3683 | 0.2364 | 0.0173 | 0.2691 | 0.2517 |

Table 18. Coordination check of Test Model 4.

| M/B Relay Pair |  | Scenario 1 |  |  | Scenario 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | B | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) | $t_{M}(\mathbf{s})$ | $t_{B}(\mathrm{~s})$ | CTM (s) |
| 5 | 4 | 0.0437 | 0.2103 | 0.1666 | 0.0235 | 0.1410 | 0.1175 |
| 4 | 1 | 0.1313 | 0.3473 | 0.2160 | 0.0173 | 0.2409 | 0.2236 |
| 4 | 2 | 0.1313 | 0.3241 | 0.1929 | 0.0173 | 0.2373 | 0.2200 |
| 6 | 1 | 0.0439 | 0.3473 | 0.3034 | 0.0272 | 0.2409 | 0.2137 |
| 6 | 2 | 0.0439 | 0.3241 | 0.2802 | 0.0272 | 0.2373 | 0.2102 |
| 8 | 7 | 0.0437 | 0.2168 | 0.1731 | 0.0230 | 0.1372 | 0.1142 |
| 7 | 1 | 0.1536 | 0.3473 | 0.1937 | 0.0232 | 0.2409 | 0.2177 |
| 7 | 2 | 0.1536 | 0.3241 | 0.1705 | 0.0232 | 0.2373 | 0.2142 |
| 9 | 1 | 0.0446 | 0.3473 | 0.3027 | 0.0273 | 0.2409 | 0.2136 |
| 9 | 2 | 0.0446 | 0.3241 | 0.2795 | 0.0273 | 0.2373 | 0.2101 |
| 11 | 10 | 0.0446 | 0.2170 | 0.1724 | 0.0336 | 0.1403 | 0.1066 |
| 10 | 1 | 0.1427 | 0.3473 | 0.2046 | 0.0170 | 0.2409 | 0.2238 |
| 10 | 2 | 0.1427 | 0.3241 | 0.1814 | 0.0170 | 0.2373 | 0.2203 |
| 12 | 1 | 0.0426 | 0.3473 | 0.3047 | 0.0271 | 0.2409 | 0.2138 |
| 12 | 2 | 0.0426 | 0.3241 | 0.2815 | 0.0271 | 0.2373 | 0.2103 |
| 14 | 13 | 0.0432 | 0.2104 | 0.1672 | 0.0235 | 0.1402 | 0.1167 |
| 13 | 1 | 0.1313 | 0.3473 | 0.2160 | 0.0170 | 0.2409 | 0.2239 |
| 13 | 2 | 0.1313 | 0.3241 | 0.1928 | 0.0170 | 0.2373 | 0.2203 |
| 15 | 1 | 0.0436 | 0.3473 | 0.3037 | 0.0272 | 0.2409 | 0.2137 |
| 15 | 2 | 0.0436 | 0.3241 | 0.2805 | 0.0272 | 0.2373 | 0.2102 |
| 17 | 16 | 0.0434 | 0.2106 | 0.1672 | 0.0332 | 0.1414 | 0.1082 |
| 16 | 1 | 0.1297 | 0.3473 | 0.2176 | 0.0163 | 0.2409 | 0.2245 |
| 16 | 2 | 0.1297 | 0.3241 | 0.1945 | 0.0163 | 0.2373 | 0.2210 |

Table 19. CTM comparison of the various test models.

| Test Model No | Scenario No | Sum of CTMs | Average of <br> CTMs | Standard <br> Deviation |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 7.1928 | 0.3127 | 0.0740 |
|  | 2 | 8.0267 | 0.3490 | 0.0882 |
| 2 | 1 | 7.7956 | 0.3389 | 0.0868 |
|  | 2 | 10.0687 | 0.4378 | 0.0929 |
| 3 | 1 | 5.6077 | 0.2438 | 0.0589 |
|  | 2 | 4.8509 | 0.2109 | 0.0514 |
| 4 | 1 | 5.1629 | 0.2245 | 0.0531 |
|  | 2 | 4.4683 | 0.1943 | 0.0443 |

Eventually, this paper aims at proving the best strategy for achieving the smoothest coordination of OCRs in practical, isolated distribution networks. The conclusion is that using the general minimum fault condition is the best trend in this practical network., not only due to its achieving of the minimum TOT, but also because it preserves the smoothest coordination at the maximum fault points with the least obtained value of the CTM summation.

## 5. Conclusions

A new methodology based on GTO procedures have been proposed to produce the best settings of OCRs across two test cases under numerous scenarios in an automated manner, tests in which the practical constraints including the transformer phase shift and other scenarios for min/max fault conditions are considered with minimal interferences from protection engineers. The first case is a 15-bus network with DGs which is widely used in the literature to validate and signify the cropped results of GTOs when they are compared to others. The second test case is for an isolated real distribution network with DGs for the Agiba Petroleum company which is located in the West Desert of Egypt. The relay coordination problem is adapted as an optimization problem subject to a set of predefined constraints and is solved using the GTO including the fixed and varied inverse IEC curves. For this test case, the best strategy for achieving the smoothest coordination of OCRs in practical isolated distribution networks has been indicated considering the transformer phase shifting. The conclusion is that using the general minimum fault condition is the best trend in this practical network, not only due to achieving the minimum total operating time, but also since it preserves the smoothest coordination at the maximum fault points with the least obtained value of CTMs for the studied cases.

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## Appendix A AGIBA Test Network Data

The following tables announces the typical date of AGIBA test network.

Table A1. Distributed Generator Data.

| ID | $S_{\text {rated }}(\mathbf{k V A})$ | $\boldsymbol{V}_{\text {rated }}(\mathbf{k V})$ | $\boldsymbol{X} \boldsymbol{d}^{\prime \prime}(\%)$ | $\boldsymbol{X} \boldsymbol{d}^{\prime}(\%)$ | $\boldsymbol{X d}(\%)$ | $\boldsymbol{P} \boldsymbol{F}_{\text {rated }}(\%)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DG1 | 3250 | 11 | 20.4 | 25.3 | 189 | 80 |
| DG2 | 3250 | 11 | 20.4 | 25.3 | 189 | 80 |
| DG3 | 3250 | 11 | 20.4 | 25.3 | 189 | 80 |

Table A2. Distribution Transformer Data.

| ID | Voltage Ratio <br> $\mathbf{( k V )}$ | $S_{\text {rated }} \mathbf{( k V A )}$ | Impedance <br> $\mathbf{( \% )}$ | $\mathbf{X} / \mathbf{R}$ | Vector Group |
| :---: | :---: | :---: | :---: | :---: | :---: |
| TR1 | $11 / 3.3$ | 1600 | 6.13 | 5.76 | Dy11 |
| TR2 | $11 / 3.3$ | 1600 | 5.12 | 5.76 | Dy11 |
| TR3 | $11 / 3.3$ | 1600 | 6.13 | 5.76 | Dy11 |
| TR4 | $11 / 3.3$ | 1600 | 6.13 | 5.76 | Dy11 |
| TR5 | $11 / 3.3$ | 1600 | 6.37 | 5.76 | Dy11 |

Table A3. Motor Data.

| ID | Designation | $\boldsymbol{V}_{\text {rated }} \mathbf{( k V )}$ | $\boldsymbol{P}_{\text {rated }}(\mathbf{k W})$ | $\boldsymbol{I}_{\text {rated }}(\mathbf{A})$ | $\boldsymbol{P F}_{\text {rated }} \mathbf{( \% )}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MOPA | Oil Line Pump | 3.3 | 490 | 101.4 | 90.5 |
| MOPB | Oil Line Pump | 3.3 | 490 | 101.4 | 90.5 |
| MOPC | Oil Line Pump | 3.3 | 490 | 101.4 | 90.5 |
| MOPD | Oil Line Pump | 3.3 | 610 | 123.4 | 92.29 |
| WIP | Water Injection | 3.3 | 607 | 125.6 | 90.5 |

Table A4. Feeder Data.

| ID | Length (m) | Area (mm ${ }^{2}$ ) | Conductor/Insulation |
| :---: | :---: | :---: | :---: |
| F_TR1 | 10 | 25 | CU/XPLE |
| F_MCC-1 | 25 | 25 | CU/XPLE |
| F_TR2 | 10 | 25 | CU/XPLE |
| F_MCC-2 | 25 | 25 | CU/XPLE |
| F_TR3 | 10 | 25 | CU/XPLE |
| F_MCC-3 | 25 | 25 | CU/XPLE |
| F_TR4 | 10 | 25 | CU/XPLE |
| F_MCC-4 | 25 | 25 | CU/XPLE |
| F_TR5 | 10 | 25 | CU/XPLE |
| F_MOPA | 15 | 35 | CU/XPLE |
| F_MOPB | 15 | 35 | CU/XPLE |
| F_MOPC | 15 | 35 | CU/XPLE |
| F_MOPD | 15 | 35 | CU/XPLE |
| F_WIP | 15 | 35 | CU/XPLE |

Table A5. MCC Data

| ID | $\boldsymbol{V}_{\text {rated }} \mathbf{( k V )}$ | $\boldsymbol{P} \mathbf{( k W )}$ | $\boldsymbol{Q} \mathbf{( k V A r )}$ | $\boldsymbol{P} \boldsymbol{F}_{\text {rated }} \mathbf{( \% )}$ |
| :---: | :---: | :---: | :---: | :---: |
| MCC-1 | 11 | 177.8 | 77.2 | 91.73 |
| MCC-2 | 11 | 90.8 | 39.2 | 91.81 |
| MCC-3 | 11 | 355.7 | 154.6 | 91.71 |
| MCC-4 | 11 | 177.8 | 77.2 | 91.73 |

Table A6. Full Load Current and Current Transformer Ratio.

| Relay ID | $\boldsymbol{I}_{\boldsymbol{f l}}(\mathbf{A})$ | CTR |
| :---: | :---: | :---: |
| R1 | 170.6 | $250 / 5$ |
| R2 | 170.6 | $250 / 5$ |
| R3 | 170.6 | $250 / 5$ |
| R4 | 83.98 | $100 / 5$ |
| R5 | 101.4 | $150 / 5$ |
| R6 | 10.17 | $25 / 5$ |
| R7 | 83.98 | $100 / 5$ |
| R8 | 125.6 | $150 / 5$ |
| R9 | 5.19 | $25 / 5$ |
| R10 | 83.98 | $100 / 5$ |
| R11 | 101.4 | $150 / 5$ |
| R12 | 20.36 | $50 / 5$ |
| R13 | 83.98 | $100 / 5$ |
| R14 | 101.4 | $150 / 5$ |
| R15 | 10.17 | $25 / 5$ |
| R16 | 83.98 | $100 / 5$ |
| R17 | 123.4 | $150 / 5$ |

Table A7. Max-Fault Conditions (3 DGs are in service with Bus Coupler 1 and Bus Coupler 2 closed).

| Relay Pair ID | Primary | Backup | 3-Phase |  | 2-Phase |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $I_{f p}(\mathrm{~A})$ | $I_{f b}$ (A) | $I_{f p}(\mathrm{~A})$ | $I_{f b}$ ( A$)$ |
| 1 | R5 | R4 | 3244 | 973 | 2864 | 992 |
| 2 | R4 | R1 | 2810 | 937 | 2580 | 860 |
| 3 | R4 | R2 | 2810 | 937 | 2580 | 860 |
| 4 | R4 | R3 | 2810 | 937 | 2580 | 860 |
| 5 | R6 | R1 | 2810 | 937 | 2580 | 860 |
| 6 | R6 | R2 | 2810 | 937 | 2580 | 860 |
| 7 | R6 | R3 | 2810 | 937 | 2580 | 860 |
| 8 | R8 | R7 | 3786 | 1136 | 3350 | 1160 |
| 9 | R7 | R1 | 2810 | 937 | 2580 | 860 |
| 10 | R7 | R2 | 2810 | 937 | 2580 | 860 |
| 11 | R7 | R3 | 2810 | 937 | 2580 | 860 |
| 12 | R9 | R1 | 2810 | 937 | 2580 | 860 |
| 13 | R9 | R2 | 2810 | 937 | 2580 | 860 |
| 14 | R9 | R3 | 2810 | 937 | 2580 | 860 |
| 15 | R11 | R10 | 3244 | 973 | 2864 | 992 |
| 16 | R10 | R1 | 2810 | 937 | 2580 | 860 |
| 17 | R10 | R2 | 2810 | 937 | 2580 | 860 |
| 18 | R10 | R3 | 2810 | 937 | 2580 | 860 |
| 19 | R12 | R1 | 2810 | 937 | 2580 | 860 |
| 20 | R12 | R2 | 2810 | 937 | 2580 | 860 |
| 21 | R12 | R3 | 2810 | 937 | 2580 | 860 |
| 22 | R14 | R13 | 3244 | 973 | 2864 | 992 |
| 23 | R13 | R1 | 2810 | 937 | 2580 | 860 |
| 24 | R13 | R2 | 2810 | 937 | 2580 | 860 |
| 25 | R13 | R3 | 2810 | 937 | 2580 | 860 |
| 26 | R15 | R1 | 2810 | 937 | 2580 | 860 |
| 27 | R15 | R2 | 2810 | 937 | 2580 | 860 |
| 28 | R15 | R3 | 2810 | 937 | 2580 | 860 |
| 29 | R17 | R16 | 3167 | 950 | 2794 | 968 |
| 30 | R16 | R1 | 2810 | 937 | 2580 | 860 |
| 31 | R16 | R2 | 2810 | 937 | 2580 | 860 |
| 32 | R16 | R3 | 2810 | 937 | 2580 | 860 |

Table A8. Min-Fault Conditions (2 DGs are in service with Bus Coupler 1 and Bus Coupler 2 closed).

| Relay Pair | Primary | Backup | 3-Phase |  | 2-Phase |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\boldsymbol{I}_{f p}(\mathbf{A})$ | $\boldsymbol{I}_{f b}(\mathbf{A})$ | $\boldsymbol{I}_{f p}(\mathbf{A})$ | $\boldsymbol{I}_{f b} \mathbf{( A )}$ |
| 1 | R5 | R4 | 2505 | 751 | 2225 | 771 |
| 2 | R4 | R1 | 1669 | 835 | 1533 | 767 |
| 3 | R4 | R2 | 1669 | 835 | 1533 | 767 |
| 4 | R6 | R1 | 1669 | 835 | 1533 | 767 |
| 5 | R6 | R2 | 1669 | 835 | 1533 | 767 |
| 6 | R8 | R7 | 2879 | 864 | 2563 | 888 |
| 7 | R7 | R1 | 1669 | 835 | 1533 | 767 |
| 8 | R7 | R2 | 1669 | 835 | 1533 | 767 |
| 9 | R9 | R1 | 1669 | 835 | 1533 | 767 |
| 10 | R9 | R2 | 1669 | 835 | 1533 | 767 |
| 11 | R11 | R10 | 2505 | 751 | 2225 | 771 |
| 12 | R10 | R1 | 1669 | 835 | 1533 | 767 |
| 13 | R10 | R2 | 1669 | 835 | 1533 | 767 |
| 14 | R12 | R1 | 1669 | 835 | 1533 | 767 |
| 15 | R12 | R2 | 1669 | 835 | 1533 | 767 |
| 16 | R14 | R13 | 2505 | 751 | 2225 | 771 |
| 17 | R13 | R1 | 1669 | 835 | 1533 | 767 |
| 18 | R13 | R2 | 1669 | 835 | 1533 | 767 |
| 19 | R15 | R1 | 1669 | 835 | 1533 | 767 |
| 20 | R15 | R2 | 1669 | 835 | 1533 | 767 |
| 21 | R17 | R16 | 2452 | 736 | 2177 | 754 |
| 22 | R16 | R1 | 1669 | 835 | 1533 | 767 |
| 23 | R16 | R2 | 1669 | 835 | 1533 | 767 |

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