

Article



# **Comparison between Simulation and Analytical Methods in Reliability Data Analysis: A Case Study on Face Drilling Rigs**

## Seyed Hadi Hoseinie <sup>1,\*</sup>, Hussan Al-Chalabi <sup>2</sup>, and Behzad Ghodrati <sup>2</sup>

- <sup>1</sup> Department of Mining Engineering, Isfahan University of Technology, Isfahan 84156-83111, Iran
- <sup>2</sup> Division of Operation & Maintenance Engineering, Lulea University of Technology, 97187 Lulea, Sweden; hussan.hamodi@ltu.se (H.A.-C.); Behzad.ghodrati@ltu.se (B.G.)
- \* Correspondence: hadi.hoseinie@ltu.se; Tel.: +98-914-316-1688

Received: 16 December 2017; Accepted: 22 March 2018; Published: 10 April 2018



Abstract: Collecting the failure data and reliability analysis in an underground mining operation is challenging due to the harsh environment and high level of production pressure. Therefore, achieving an accurate, fast, and applicable analysis in a fleet of underground equipment is usually difficult and time consuming. This paper aims to discuss the main reliability analysis challenges in mining machinery by comparing three main approaches: two analytical methods (white-box and black-box modeling), and a simulation approach. For this purpose, the maintenance data from a fleet of face drilling rigs in a Swedish underground metal mine were extracted by the MAXIMO system over a period of two years and were applied for analysis. The investigations reveal that the performance of these approaches in ranking and the reliability of the studies of the machines is different. However, all mentioned methods provide similar outputs but, in general, the simulation estimates the reliability of the studied machines at a higher level. The simulation and white-box method sometimes provide exactly the same results, which are caused by their similar structure of analysis. On average, 9% of the data are missed in the white-box analysis due to a lack of sufficient data in some of the subsystems of the studies' rigs.

Keywords: modeling; simulation; black-box; white-box; Pareto analysis

## 1. Introduction

During the last three decades different drilling techniques, from pneumatic to electro-hydraulic, have been developed. Nowadays, drilling rigs have high capacities and are equipped with different advanced monitoring and control systems. The focus of development in this machinery has not just been on speed, but also on the quality of drilling, operation costs, and safety [1]. Face drilling rigs are powerful machines, manufactured with a wide range of capabilities and are applied either in the mines or in construction projects. They are important machines with a critical role in the mine production rate and a construction project's duration. Therefore, their reliability and availability are very crucial for whole excavation operation. Collecting a wide range of data, getting the deep information from machine and well-established maintenance process are required to achieve a reliable drilling operation. Drilling machines are complex and compactly-designed, making their maintenance challenging, which suggests the need for an in-depth study of their failure behavior [2]. Reliability studies in underground mining machinery have been carried out by many researchers and in different types of mines, varying from coal to hard rock metal mines. A review of the related outstanding literature has been presented by Hoseinie et al. [3]. It has been emphasized in the past that reliability studies in mines, specifically in underground mining, are particularly difficult due to their harsh

operation and maintenance environment, as well as work pressures [4]. Considering the importance of mobile underground machinery for mine production, the complexity of the machinery and the harsh mining environment, a reliability analysis of the drilling rig must meet rigorous requirements and come up with clear results.

In this paper, the reliability of a fleet of face drilling rigs in a Swedish mine is analyzed using three different approaches: two analytical methods (white-box and black-box modeling) and simulation. Finally, the results of each approach are discussed and compered.

#### 2. Face Drilling Rigs: A Case Study

Face drilling rigs are used for the drilling of blasting holes in construction and mining tunnels/galleries. Many international companies manufacture drilling rigs that are composed of similar operational units and have similar structures, however, they have variable technical characteristics, especially in capacity and power. This study examined a fleet of three rigs, called Machine A, B, and C in a Swedish underground metal mine. All of the rigs in this study are the same model and are manufactured by the Atlas Copco Company. Each rig has four retractable stabilizer legs and an articulated four-wheel drive chassis. They are operated electrically by a maximum power capacity of 158 kW. Figure 1 shows the schematic view of the studied rigs and their different parts. According to the operation manuals, field observations, and maintenance reports from the case study mine, the drilling rig is considered a system that consists of 12 operational subsystems working simultaneously to achieve the desired function and is connected in a series of configuration, as shown in Figure 2.

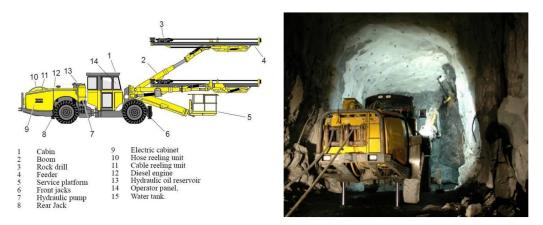


Figure 1. One of case study drilling rigs; (left) basic units [5]; (right) drilling rig in mine [6].

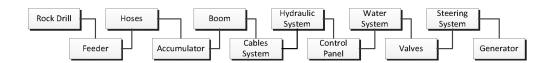


Figure 2. The defined reliability block diagram for face drilling rig.

#### 2.1. Data Collection

The required data for this study was collected from available operation and maintenance reports extracted from a computerized maintenance management system (CMMS) called "MAXIMO" and some field observations over a period of two years. After refining and filtering the data, the failures of each subsystem were assigned to its data-log and the failure frequency was analyzed. As can be seen in Figure 3, the Pareto analysis shows that hoses, rock, drills and feeders are the top three subsystems/units view point of failure frequency. On average, 63.3% of all recorded failures in this

fleet are related to these subsystems. All of the defined subsystems for the face drilling rigs do not appear in the Pareto analysis in all machines. This means that some subsystems had no failures during the study period or had fewer than five failures and were not analyzed (the figure's "others" column represents these subsystems).

#### 2.2. Reliability Analysis

Collecting data, analyzing, and making a decision are time consuming processes that must be done during any reliability study. In general, there are three main approaches for the reliability analysis of the systems [7,8];

- (a) White-box modeling: the white-box (or structural) approach explicitly takes the structure of the system into account [9,10]. In other words, in this method, the state of the system is modeled in terms of the states of the various components [8]. In order to model the reliability of the system, the reliability of all subsystems are calculated and combined based on the reliability network and overall system configuration.
- (b) Black-box modeling: black-box analysis is a system-based analytical method, referring to the technique of testing a system with no knowledge of its internal workings [11]. When the system is treated as a black-box, there is no concern about how the system "looks inside" [12]. In this approach, the system is described either in terms of two states (working/failed) or more than two states (allowing for one or more partially failed states) without explicitly linking them to components of the system [8].
- (c) Simulation: stochastic simulation is a suitable technique to assess the reliability of a system and can be applied in two ways [8,9,12]: (1) Sequential approach: by examining each basic interval of the simulated period in chronological order; and (2) Random approach: by examining randomly chosen basic intervals of the system lifetime.

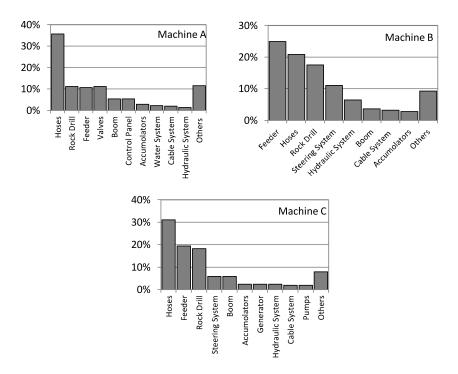


Figure 3. Pareto analysis on studied face drilling rigs.

The random approach, usually known as the "Monte Carlo" method, is a numerical method that allows for the solution to mathematical and technical problems by means of a system of probabilistic

models and the simulation of random variables. In this method the stochastic failure occurrence of the system is analyzed and the probability of the failure and success of the system operation are calculated. The failure behavior of each subsystem is considered in this method.

Every mentioned reliability analysis approach has special and different inputs, advantages, disadvantages, limitations and outputs. Sometimes when the white-box approach is applied there are some statistical-based restrictions. For example, it is very difficult to fit a failure density function on the available data in subsystems that have less than five numbers of failures [13]. Therefore, all these failures are missed in the calculations and analysis. However, they actually exist. In the black-box approach the all of the failure data is put in one set. The main disadvantage of this method is that we are not able to study the failure behavior of each subsystem and detailed information about the failure modes of the system is missed. As for its advantages, the calculation time is very low and the complete failure data is used in this approach. The simulation method stands in line with white-box modeling, nevertheless, the final reliability analysis of the whole system is performed stochastically. The main disadvantages of this method include high calculation time and missing failure data during the distribution fitting.

Within this article, the available failure data is analyzed by the above mentioned methods and the resulting reliability plots and the applications of each approach are compared and discussed.

#### 2.2.1. Reliability Analysis Using the White-Box Modeling Approach

As discussed, in the white-box method the reliability of the whole machine is calculated based on the reliability of its subsystems. Therefore, all of the data analysis is performed during the time between failures (TBF) of the subsystems. Since the subsystems of a face drilling rig have a series of configurations, the reliability of the whole machine in time *t* is calculated by multiplying the reliability of all subsystems at time *t*.

In the CMMS, the failure data are recorded based on calendar time. Since drilling is not a continuous process, the TBFs were estimated by considering the utilization of each rig. Reliability and maintainability data analysis is usually done based on the assumption that the TBF and TTR data are independent and identically distributed (iid) in the time domain. It was critical to conduct a formal verification analysis of the assumption, otherwise, completely wrong conclusions could be drawn [14,15]. In this study, statistical analysis could not find trends in the failure and repair data. The failure data were tested for trends with the Laplace trend test, which is used to determine whether a data set is identically distributed or not [14]. If such a trend is observed, classical statistical techniques for reliability analysis may not be appropriate, and a non-stationary model such as the non-homogenous Poisson process (NHPP) must be fitted [15,16]. Otherwise, the serial correlation test can be used to test the dependence of the failure data. A dependence test determines whether successive failures are dependent in data without a long-term trend or not [15]. If dependence is not observed, the iid assumption is valid.

In this study, after testing and confirming the validity of the iid assumption, different types of statistical distributions were examined on the data and their parameters were estimated using Easyfit Professional software version 5.6 [17] and Minitab software [18]. The goodness of a fit of the distributions was tested by using the Kolmogorov–Smirnov (K-S) test. All of the statistical tests used a significance level of 0.05. The best fitted failure density functions are presented in Table 1.

The reliability plots of the subsystems of the studied machines and the reliability of the whole machines based on the white-box modeling are presented in Figures 4–6. As can be seen in these figures, the accumulator, cable, water, and generator subsystems have the highest reliability, while the feeder and hose subsystems have the lowest reliability level. The figures show that the reliability behaviors of the all subsystems are more or less similar in all studied machines, possibly because they are all in the same working environment, are the same model, come from the same manufacturer, have the same maintenance crew, and are used by operators with similar skills.

Subcyctome	Best Fitted Function				
Subsystems	Machine A	Machine B	Machine C		
Hoses	Weibull 2P $\alpha = 0.92, \beta = 20.75$	Weibull 3P $\alpha = 0.95, \beta = 55.53, \gamma = 0.6$	Lognormal 3P σ = 1.07, μ = 3.12, γ = -1.19		
K-S goodness of fit	0.067	0.121	0.094		
Rock Drill	Weibull 2P $\alpha = 0.98, \beta = 69.1$	Lognormal $\sigma = 1.26, \mu = 3,27$	Gamma 3P $\alpha = 1.13, \beta = 52.61$		
K-S goodness of fit	0.115	0.084	0.173		
Feeder	Lognormal 3P $\sigma = 1.26, \mu = 3.4, \gamma = -0.14$	Weibull 2P $\alpha = 0.82, \beta = 42.47$	Exponential $\lambda = 0.018$		
K-S goodness of fit	0.089	0.115	0.109		
Boom	Weibull 2P $\alpha = 1.04, \beta = 146.28$	Exponential $\lambda = 0.006$	Weibull 3P $\alpha = 0.58, \beta = 122.7, \gamma = 19.0$		
K-S goodness of fit	0.023	0.159	0.063		
Accumulators	Normal σ = 197.41, μ = 256.16	Normal $\sigma = 214.1, \mu = 300.5$	Weibull 2P $\alpha = 1.48, \beta = 502.1$		
K-S goodness of fit	0.095	0.118	0.159		
Cable System	Less than 5 failures	Weibull 2P $\alpha = 1.09, \beta = 339.7$	Exponential $\lambda = 0.002$		
K-S goodness of fit		0.039	0.047		
Hydraulic System	Gamma $\alpha = 0,336, \ \beta = 1047$	Weibull 3P $\alpha = 0.6, \beta = 148.3, \gamma = 16.92$	Lognormal 3P $\sigma = 0.77, \mu = 5.45, \gamma = -66.7$		
K-S goodness of fit	0.152	0.089 0.096			
Valves	Lognormal $\sigma = 1.17, \mu = 4.36$	Less than 5 failures Less than 5 failu			
K-S goodness of fit	0.117				
Control Panel	Exponential $\lambda = 0.008$	Less than 5 failures Less than 5 failu			
K-S goodness of fit	0.053				
Water System	Lognormal $\sigma = 1.27, \mu = 5.17$	Less than 5 failures Less than 5 failu			
K-S goodness of fit	0.071				
Steering System	Less than 5 failures	Weibull 3P $\alpha = 1.15, \beta = 112.9, \gamma = 4.27$	Lognormal 3P $\sigma = 0.62, \mu = 5.22, \gamma = -37.$		
K-S goodness of fit		0.108 0.113			
Generator	Less than 5 failures	Less than 5 failures	Weibull 2P $\alpha = 0.999, \beta = 299.82$		
K-S goodness of fit			0.021		
otal number of failures	313	196	231		

Table 1. Fa	ilure data	analysis	of subsyste	ms of studied	machines.
-------------	------------	----------	-------------	---------------	-----------

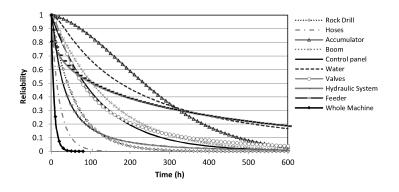


Figure 4. Reliability plots of the subsystems of Machine A using white-box approach.

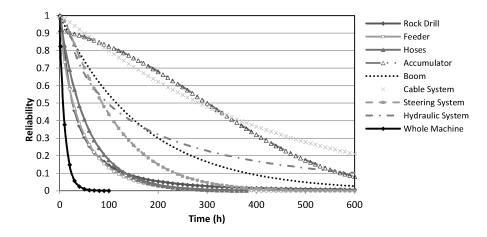


Figure 5. Reliability plots of the subsystems of Machine B using white-box approach.

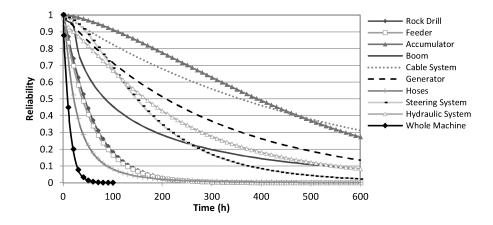


Figure 6. Reliability plots of the subsystems of Machine C using white-box approach.

Figure 7 shows the reliability plots of all three machines using the white-box method in one area. As the figure indicates, machine C has the highest reliability among the studied machines, while machine A has the lowest level. The maximum difference value is 20% at almost 15 h. An obvious result of these plots is that the studied machines are almost equal in reliability during the period of high reliability operation (from time 0 to 5 h) and also during the period of very low reliability (after 35 h). The reliability of all machines decreases to almost zero after 50 h of operation.

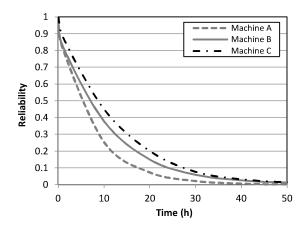


Figure 7. Reliability plots of all machines using white-box modeling.

#### 2.2.2. Reliability Analysis Using Black-Box Modelling Approach

In this approach, no subsystems were considered for the machines and all of the failure data were analyzed as one statistical population per one machine. The iid testing procedures and data analysis were performed on the whole failure data of each machine. Reliability models and calculated plots are drawn from these data. The results of the data analysis using the black-box method are presented in Table 2.

Machine	Number of Failures	<b>Best-Fitted Function</b>	Parameters
A	347	Weibull (3P)	$\begin{aligned} \alpha &= 0.93\\ \beta &= 7.11\\ \gamma &= 0.11 \end{aligned}$
В	216	Weibull (2P)	$\alpha = 0.91$ $\beta = 11.04$
С	251	Weibull (3P)	$\alpha = 0.94$ $\beta = 10.69$ $\gamma = 0.33$

Table 2. Parameters of best-fitted distributions on failure data using the black-box approach.

Using the parameters of the best-fit functions given in Table 2, the reliability plots of the machines are drawn in Figure 8. As shown in this figure, the reliability of all the machines reaches almost zero after 50 h of operation. The reliability of machine A is the lowest. In total, the black-box method finds very close, almost similar values for machines B and C.

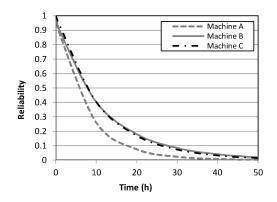


Figure 8. Reliability plots of all studied machines using black-box modeling.

#### 2.2.3. Reliability Analysis Using Simulation Approach

The Monte Carlo simulation is a powerful approach for the reliability analysis of large-scale complex networks that has been developed in several stages and different application guidelines have been recommended so far. During the simulation process, subsystems may have random failures and repair distributions, and failure data of the subsystems are sometimes not sufficient and smaller in sample size [19]. These two phenomena cause some challenges in the simulation, nevertheless, they have not been able to restrict the applications or reduce its profit.

According to the available literature, the Monte Carlo reliability simulation is carried out by different algorithms that are mainly built up on the Kamat and Raily (K–M) [20] algorithm. It is considered the most general reliability simulation method, and other methods, such as Rice and Moore (R–M) [21], Chao and Huang (C–H) [22], Lin et al. (L–D–L) [23], and Lin and Donagh (L–D) [24] are known as the modifications or specializations of this method [25]. Therefore, in this paper the K–R method is applied for the reliability simulation of face drilling rigs.

In the Kamat and Raily method the random failure times for each subsystem are generated based on defined failure distribution functions, which are then applied to assess the success or the failure of the system. Figure 9 presents the flowchart of the K–M simulation method. More details of this method are presented by Wang and Pham [19] and Hoseinie et al. [25,26].

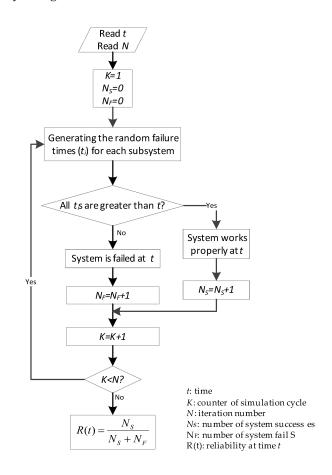


Figure 9. The flowchart of the K-R Monte Carlo reliability simulation method (adopted from [25]).

According to the presented algorithm in Figure 9, a computer code was developed in MATLAB software. For each machine, the program was run in different operation times and with the iteration number of 10,000. The simulated reliability plots of the studied machines are presented in Figure 10. As can be seen in this figure, the reliability of Machine A is the lowest value as well as in the other two methods. Also, the difference between the reliability of Machine B and C are a maximum 10%.

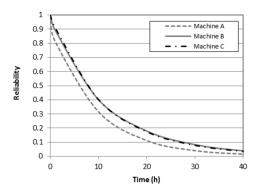
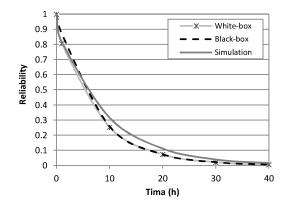


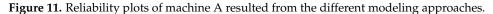
Figure 10. Reliability plots of all three studied machines achieved from the simulation method.

#### 3. Comparison and Discussion

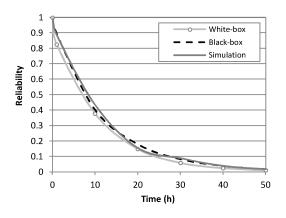
As discussed earlier, the reliabilities of the face drilling rigs were analyzed using three methods and the resulted reliability plots for each machine are presented in Figures 11–13. As seen in these figures, the resulted reliability plots are very similar and sometimes have the same values in each machine.

In Machine A (Figure 11), during the initial eight hours, the results of all methods are very similar to each other. After this period, the reliability plots of the white-box and black-box modeling become almost the same, but the simulation plot comes over them. At the end, after 30 h of operation, the reliability plots of all the methods show almost the same values. Finally, all reach zero after 40 h.





In Machine B (Figure 12), the reliability plot of simulation is almost the same values as the black-box modeling. Both of them are higher than the white-box approach. In total, the reliability of this machine reaches almost zero after 50 h, which is 10 h more than Machine A.





In Machine C (Figure 13), the results are complicated. Before 5 h, the simulation plot is close to the black-box method and is higher than the white-box. After 5 h, the simulation result separates from the black-box and is closer to the white-box. In passing 25 h, all plots show the same values and they join each other.

In general, the simulation method determines the higher values with greater accuracy than the other methods or are very similar in reliability values to the white-box method. It is caused by the process of simulation method, which is based on the failure distribution functions of the machines' subsystems.

In more or less the whole time period in all of the studied machines, the black-box and white-box methods reveal a reasonable difference in values (except at times after 10 h in machine A). Because

when the white-box method is used, the frequencies of the failures in some of the subsystems are less than five and therefore, the related subsystems and their failures are eliminated from the analysis process. Nevertheless, in the black-box approach all of the failures are counted and the analysis is performed using a complete set of failure data. In detail, according to Tables 1 and 2, the number of missing data can be summarized as shown in Table 3. On average, 9.3% of the data has been missed within the white-box analysis, which accounts for the differences in the resulted values of this method. However, even without considering the missed data, the combination of different failure modes and failure distributions in the black-box method results in a different description of system reliability, which presents a holistic and general view of system reliability.

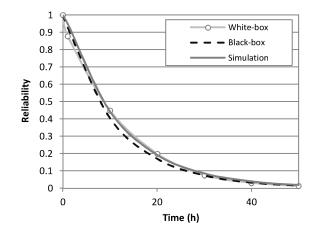


Figure 13. Reliability plots of machine C resulted from of different modeling approaches.

Machine	Number of Failures Used in Analysis		Missed Failure Data (%)
	Black-Box	White-Box	Niisseu Fuiture Dum (76)
А	347	313	9.8
В	216	196	9.3
С	251	231	8

Table 3. Number of analyzed and missed data view point of different modeling approaches.

In other view, according to Figures 7–9, the ranking of the studied machines in the white-box method is different with the other two methods. In the white-box (Figure 7), the reliability of machine C is obviously higher than machine B and A, nevertheless, in the black-box and simulation approaches the reliability of machine C and B are almost the same values. The reliability of machine A is the lowest value in all methods.

Finally, according to the presented results, it could be concluded that, even though the results of the three mentioned reliability analysis methods are clearly different, this is sometimes negligible. Therefore, in fleet level analysis, considering the required time for analysis the black-box method could be helpful in finding the reliability of each machine or detecting the weakest machine (lowest reliability) in the fleet. In further analysis, the white-box method can be used, but only on the weakest machine to do the subsystem and component level analysis.

Since the working environment is so harsh in mining, the machinery must be analyzed and the reliability view point monitored in regular time periods. Therefore, considering the time consuming nature of the simulation method, it is not suggested that it be applied in normal mining machineries.

## 4. Conclusions

In this paper the reliability of face drilling machines in a Swedish underground mine were analyzed using white-box, black-box, and simulation methods. The overall findings could be listed as followings:

- 1. Applied reliability analysis methods obviously reveal different results, where the difference varies from almost zero to 20 percent. It is recommended to apply the black-box method in fleet level analysis, the white-box in machine level and simulation only in complex systems or in the case of a lack of available failure data.
- 2. Comparative analysis shows that the applied reliability analysis approaches present different rankings of machines within the fleet, nevertheless, in finding the last-ranked machine they present the same result.
- 3. According to all findings of this study, when our aim is to analyze the machine's reliability itself and to investigate the production stoppages and production reliability, the black-box method is the best method of modeling. All failure data are included in this method, and it is the shortest and easiest way when compared to the other methods.

**Acknowledgments:** The authors are grateful to the employees and managers of Boliden Mineral AB for their kind cooperation during the data collection. The financial support of the Center of Advanced Mining and Metallurgy (CAAM) of Lulea University of Technology is also acknowledged.

**Author Contributions:** Study conception and design were carried out by all authors (A, B, C); B collected the data; A, B and C analyzed the data; A made the simulations; A, B, C wrote the article.

Conflicts of Interest: The authors declare no conflict of interest.

### References

- 1. Atlas Copco. *Face Drilling*, 2nd ed.; The Friday Press: Dorchester, UK, 2013.
- 2. Al-Chalabi, H. Reliability and Life Cycle Cost Modelling of Mining Drilling Rigs. Ph.D. Thesis, Luleå University of Technology, Luleå, Sweden, 2015.
- 3. Hoseinie, S.H.; Ataie, M.; Khalokakaie, R.; Ghodrati, B.; Kumar, U. Reliability Analysis of Drum Shearer Machine at Mechanized Longwall Mines. *J. Qual. Maint. Eng.* **2012**, *18*, 98–119. [CrossRef]
- 4. Dhillon, B.S. *Mining Equipment Reliability, Maintainability and Safety;* Springer: New York, NY, USA, 2008.
- 5. Atlas Copco Rock Drills AB. *Atlas Copco Boomer L1C, L2C Mk 7B Operator's Instructions;* Manual Edition; Atlas Copco Rock Drills AB: Orebro, Sweden, 2010.
- 6. Stedt, M. We Have a Very Stable Future. Available online: http://www.regiondalarna.se/leva-i-dalarna/garpenberg-framtid (accessed on 9 April 2018).
- 7. Kececiyoglu, D.B. *Reliability Engineering Handbook*; Destech Publication: Lancaster, PA, USA, 2002; Volume 1, p. 721.
- 8. Misra, K.B. *Principles of Reliability Engineering*; RAMS Consultants: Bangalore, India, 2011; p. 456.
- 9. Cheung, R.C. A user-oriented software reliability model. *IEEE Trans. Softw. Eng.* **1980**, *SE-6*, 118–125. [CrossRef]
- 10. Littlewood, B. Software reliability model for modular program structure. *IEEE Trans. Reliab.* **1979**, *28*, 241–246. [CrossRef]
- 11. Krishna, M.K.; Verma, A.K.; Srividya, A.; Ljubisa, P. Integration of black-box and white-box modeling approaches for software reliability estimation. *Int. J. Reliab. Qual. Saf. Eng.* **2010**, *17*, 261–273. [CrossRef]
- 12. Rausand, M.; Høyland, A. System Reliability Theory: Models, Statistical Methods and Applications; John Wiley: Hoboken, NJ, USA, 2014.
- 13. ReliaSoft. Weibull<sup>++</sup>—Reliability Life Data Analysis. Available online: http://reliawiki.org/index.php/ Weibull%2B%2B\_Examples (accessed on 9 April 2018).
- 14. Kumar, U.; Klefsjö, B. Reliability analysis of hydraulic systems of LHD machines using the power law process model. *Reliab. Eng. Syst. Saf.* **1992**, *35*, 217–224. [CrossRef]
- 15. Birolini, A. *Reliability Engineering: Theory and Practice*, 5th ed.; Springer: Heidelberg, Germany; New York, NY, USA, 2007.

- 16. Louit, D.M.; Pascual, R.; Jardine, A.K. A practical procedure for the selection of time-to-failure models based on the assessment of trends in maintenance data. *Reliab. Eng. Syst. Saf.* **2009**, *94*, 1618–1628. [CrossRef]
- 17. MathWave Technologies, Easyfit Distribution Fitting Software. Available online: http://www.mathwave. com/easyfit-distribution-fitting.html,%202017 (accessed on 9 April 2018).
- 18. Minitab Ltd. Available online: http://www.minitab.com (accessed on 9 April 2018).
- Wang, H.; Pham, H. Survey of Reliability and Availability Evaluation of Complex Networks Using Monte Carlo Techniques. *Microelectron. Reliab.* 1997, 31, 187–209. [CrossRef]
- 20. Kamat, S.J.; Riley, M.W. Determination of Reliability Using Event-Based Monte Carlo Simulation. *IEEE Trans. Reliab.* **1975**, 24, 73–75. [CrossRef]
- 21. Rice, R.E.; Moore, A.H. A Monte Carlo Technique for Estimating Lower Confidence Limits on System Reliability Using Pass-Fail Data. *IEEE Trans. Reliab.* **1983**, *R*-32, 366–369. [CrossRef]
- 22. Chao, A.; Huang, L.C. A Modified Monte Carlo Technique for Confidence Limits of System Reliability Using Pass-Fail Data. *IEEE Trans. Reliab.* **1987**, *R-36*, 109–112. [CrossRef]
- 23. Lin, C.T.; Duran, B.S.; Lewis, T.O. Estimating Lower Confidence Limits on System Reliability Using a Monte Carlo Technique on Binomial Data. *Microelectron. Reliab.* **1988**, *28*, 487–493. [CrossRef]
- Lin, J.Y.; Donaghey, C.E. A Monte Carlo Simulation to Determine Minimal Cut Sets and System Reliability. In Proceedings of the Annual Reliability and Maintainability Symposium, Atlanta, GA, USA, 26–28 January 1993; pp. 246–249.
- 25. Hoseinie, S.H.; Khalokakaie, R.; Ataie, M.; Ghodrati, B.; Kumar, U. Monte Carlo Reliability Simulation of Coal Shearer Machine. *Int. J. Perform. Eng.* **2013**, *9*, 487–494.
- 26. Hoseinie, S.H.; Ghodrati, B.; Kumar, U. Monte Carlo reliability simulation of water system of longwall shearer machine. *Int. J. Reliab. Qual. Saf. Eng.* **2013**, *20*, 1350023. [CrossRef]



© 2018 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).