



Article Lithium Polysulfide Interaction with Group III Atoms-Doped Graphene: A Computational Insight

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Received: 12 May 2020; Accepted: 7 September 2020; Published: 12 September 2020



Abstract: The development of long lifetime Li–S batteries requires new sulfur–carbon based composite materials that are able to suppress the shuttle effect—namely, The migration of soluble lithium polysulfides from the cathode to the anode of the cell. Graphene is one of the most promising carbon supports for sulfur, thanks to its excellent conductivity and to the possibility of tailoring its chemical–physical properties, introducing heteroatoms in its structure. By using first principle density functional theory simulations, this work aims at studying the effect of doping graphene with group III elements (B, Al, Ga) on its electronic properties and on its chemical affinity towards lithium polysulfides. Our results show that Al and Ga doping strongly modify the local structure of the lattice near heteroatom site and generate a charge transfer between the dopant and its nearest neighbor carbon atoms. This effect makes the substrate more polar and greatly enhances the adsorption energy of polysulfides. Our results suggest that Al- and Ga-doped graphene could be used to prepare cathodes for Li–S cells with improved performances and lifetime.

Keywords: Li-S battery; graphene doping; gallium; boron; aluminum; density functional theory

1. Introduction

Electrification of passenger vehicles is considered to be the most effective approach to reduce greenhouse and noxious emissions and to mitigate the oil dependence of modern society [1,2].

If light-weighting is yet a major innovation route to improve the electric vehicle efficiency, The key component to increase the kilometric range is certainly the battery package [3].

The key component of electric vehicles is the battery package, which determines the kilometric range. Lithium-ion secondary batteries represent the most mature and reliable technology currently applied to build the electrochemical energy storage system of electric vehicles. The specific energy of lithium ion batteries ranges between 150 and 240 Wh/kg [4] and it allows a driving range lower than 250–300 km on a single charge. To reach a driving range compatible with the market expectation, that is at least 600 km, an energy density higher than 500 Wh/kg is required.

Li–S battery has a theoretical specific energy of 2600 Wh/kg, while the practical one expected is 800 Wh/kg, a value much larger than the specific energy of lithium-ion battery [4–6]. A typical Li–S cell consists of a lithium metal anode and a sulfur–carbon composite cathode with an organic liquid electrolyte in between. The device converts electrochemical energy to electric energy and vice-versa via the breaking and formation of the S–S bond. During discharge, sulfur is reduced by a two-electron reduction process to form polysulfide intermediates (Li_2S_x , x = 2–8) until lithium sulfide (Li_2S) is formed at the end [7]. One of the main problems hindering the application of Li–S batteries is the low

conductivity of sulfur. Carbon materials are widely used to improve the electronic conductivity of the sulfur cathode, while the ionic conductivity is enhanced by using liquid electrolyte. However, high solubility of lithium polysulfides in the liquid electrolyte leads to the so-called polysulfide shuttle. This mechanism consists of the migration of soluble sulfur species from the cathode to the anode, where they react with the lithium anode to form a passivation layer on its surface. The polysulfide shuttle reduces the columbic efficiency of the cell due to the loss of active materials and to the degradation of lithium anode [7]. On the other hand, The shuttle mechanism protects the cell from overcharge [8] and improves thanks to the removal of the Li dendrites caused by the reaction with the polysulfides. For this reason, The shuttle mechanism should be limited to increase the coulombic efficiency of the cell but not completely suppressed.

Among the carbon-based materials used as a conductive support for the sulfur cathode, graphene has been gaining interest since its discovery in 2004 [9]. Graphene is a carbon-based material characterized by high electrical conductivity and exceptional mechanical properties. Moreover, its properties can be tailored, introducing heteroatoms in the structure [10]. Possible industrial applications of graphene include supercapacitors and batteries [11–13], lubricants [14,15], electronic devices [16,17] and catalysis [18–20]. Even if the blending of graphene with sulfur can mitigate the insulating nature of sulfur-based electrodes, it has been reported that the interaction between pure carbon-based materials and polysulfides (Li or S) is not strong enough for effective binding and for the reduction in the shuttle effect related to the dissolution and diffusion of polysulfides [21]. Thanks to its simple structure, graphene is a perfect model system for theoretical investigations and it was intensively studied using first principle calculations [22,23].

The introduction of dopants is a well-used strategy for tuning the properties of host materials. Heteroatom-functionalized graphene with high affinity for lithium sulfide has been recently reported as a promising material enabling high cycling stability, long life and high specific energy density [24,25]. Many theoretical investigations were devoted to the doping of graphene with different heteroatoms to tune the physical properties and modify the reactivity [26–30]. In particular, intense research activity was devoted to the simulation of the interaction of lithium polysulfides with graphene functionalized with different dopants. Nitrogen doping is effective in increasing the adsorption energy of polysulfide when nitrogen is in pyridinic or pyrrolic positions; when nitrogen is in the graphitic position, The interaction with polysulfides is comparable to that of pristine graphene [31,32]. P. Velez et al. simulated the interaction of lithium polysulfides with graphene [31,32]. P. Velez et al. simulated the interaction of lithium polysulfides with graphene monolayers doped with different heteroatoms (B, O, N, F, S, P, Si, Al, Cl) [33]: their conclusions suggest that the B-, Al- and Si-doped systems are the most promising for applications in Li–S batteries. Little work was devoted till now on the Ga-doped graphene [34–36] and to the best of our knowledge no computational studies concentrate on the interaction with polysulfides.

For this reason, in the present work, we present density functional theory (DFT) calculations of doped graphene structures with group III atoms (B, Al and Ga) with the aim of comparing their capability of trapping long-chain polysulfides. The initial screening to determine the best doping element was performed simulating the uncharged graphene substrate in vacuum. This is an oversimplified model since the polysulfides interact with a charged electrode and with the components of the electrolyte (solvent and ions). The influence of cations and of the electrolyte components on the polysulfides was recently studied by Bieker et al. [37,38]. They demonstrated that the electrolyte components have a mutual interaction in stabilizing different polysulfides species. For this reason, after selecting the most promising material, The Al-doped graphene, we included in our calculations also the effect of solvation and of the polarization of the surface.

Since we are interested in increasing the interaction of soluble long-chain polysulfides (Li_2S_n , n = 4, 6, 8) with the graphene electrode in liquid electrolytes, we selected Li_2S_6 as the probe molecule. The same choice was made in other studies [39] since Li_2S_6 plays a key role in the shuttle mechanism. To verify that our assumption is acceptable, we performed additional calculations using Li_2S_4 and Li_2S_8 (see Supplementary Materials).

Our results are reported to shed light onto the understanding of the chemical interaction between graphene doped with group III elements and polysulfides, and to stimulate the development of new electrode materials for suppressing the shuttle mechanism.

2. Computational Method

First principle density functional theory (DFT) calculations were performed using the Quantum Espresso ab initio simulation package [40,41]. The exchange–correlation interaction between electrons was described using the generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof exchange–correlation functional optimized for solids (PBEsol) [42]. Frozen-core all-electron calculations were made possible by using the projector augmented wave (PAW) method [43]. The dispersion interactions were included in the simulations adopting the dispersion-corrected density functional theory by Grimme as implemented in the DFT-D3 method [44]. The Brillouin zone was sampled by using a $3 \times 3 \times 1$ irreducible Monkhorst-Pack k point grid [45] during structural optimizations. A finer $11 \times 11 \times 1$ grid was used instead for the calculation of density of states (DOS). The electron wavefunctions were expanded in a plane wave basis with an energy cutoff of 50 Rydberg and a Marzari–Vanderbilt smearing [46] of 0.02 Ry was applied to improve the convergence of the self-consistent field procedure.

A monoclinic supercell of 14.75 Å × 14.75 Å with 72 carbon atoms (6 × 6) was built for the pristine graphene monolayer. The cell size was kept constant during optimization. A 20 Å vacuum space was used in the z direction, to avoid interaction amongst graphene monolayers. Figure 1 shows the computational cell projected along the *z*-axis. All representations of the molecular and crystal structures and of the differential charge densities were obtained using the VESTA visualization program [47].



Figure 1. The 6×6 supercell used for the simulations of the doped graphene and of its interaction with Li_2S_6 . Brown = carbon atoms; red = the heteroatom.

The geometry of the free Li₂S₆ molecule in vacuum was optimized in a simple cubic cell with a lattice parameter of 20 Å. The same computational parameters used for the doped graphene were adopted, except for the selection of the Γ point alone for the k-space sampling. All the atomic positions of the graphene supercell and of the polysulfide molecule were fully relaxed using the Broyden–Fletcher–Goldfarb–Shanno algorithm [48–51]. The convergence criteria of maximum force less than 1×10^{-4} Ry/Bohr and energy change less than 5×10^{-4} Ry were used throughout all the structural optimizations. To analyze the interaction of the polysulfide with the graphene surface two types of starting configurations were considered: one with the lithium atoms of the polysulfide pointing to the heteroatom of the modified graphene surface and another one with the sulfur atoms pointing to the functionalized surface.

The adsorption energy between the doped graphene monolayers and the lithium–polysulfide was calculated using the following formula:

$$E_{ads} = E_{Gr+LPS} - E_{Gr} - E_{LPS},$$
(1)

where $E_{Gr + LPS}$, E_{LPS} and E_{Gr} are, respectively, The total energy of the graphene layer (pristine or doped) with lithium–polysulfide adsorbed, The energy of the optimized lithium–polysulfide molecule and the energy of graphene substrates (pristine or doped). A negative sign of E_{ads} means a favorable attractive interaction.

The differential charge density was used to highlight regions of charge accumulation and depletion associated with the adsorption of Li_2S_6 on the graphene monolayer. The differential charge density is defined as:

$$\Delta \rho = \rho_{\rm Gr+LPS} - \rho_{\rm Gr} - \rho_{\rm LPS},\tag{2}$$

where $\rho_{Gr + LPS}$, ρ_G and ρ_{LPS} represent the charge densities of the graphene layer (pristine or doped) with lithium–polysulfide adsorbed of the graphene substrate (doped or pristine) and of the polysulfide. Löwdin's [52] charge population analysis was applied to study the charge transfer between different atoms.

The effect of solvation and of polarization of the graphene electrode was evaluated on most of the material showing the higher binding energy for the polysulfide, The Al-doped graphene. To include in our calculations the effect of the solvent and of electrode polarization, we used the Environ software [40,53], integrated with Quantum Espresso density functional theory code. Since our system is characterized by 2D periodic boundary conditions, we addressed the periodic-image errors arising from the use of periodic boundary conditions using the real-space method proposed by Dabo et al. [54]. The presence of solvent molecules was treated implicitly using a homogeneously polarizable medium with dielectric constant equal to 7. That value of the dielectric constant corresponds to the most common solvents, e.g., 1,3-dioxalane or 1,2-dimethoxyethane, used in the formulation of the electrolytes for Li–S cells. The electrolyte cavity was treated using the soft-sphere continuum solvation (SSCS) model recently proposed by Fisicaro et al. [55]. To treat the electrode polarization and the presence of ionic countercharges of opposite signs in the electrolyte, we adopted the planar countercharge model described in [56]. This corresponds to the well-known Helmholtz's model of the electrode-electrolyte interface. The countercharge planes were symmetrically placed at a distance of 7 A from the graphene substrate simulating in this way the presence of a layer of solvent molecules adsorbed on the electrode. The electrode potential was calculated with the grand-canonical approach described by Andreussi et al. [57]. The electrostatic potential of an electrode can be defined with respect to different reference potentials. In DFT calculations on electrochemical interfaces, The absolute potential scale [58], measuring the potential with respect to the potential of a point in the vacuum above the solution-vacuum interface, is the most convenient. In the absolute scale, The potential of the standard hydrogen electrode is 4.44 eV, so the reduction potential of lithium is 1.4 V. We obtained the absolute potential \emptyset^{abs} of the graphene electrode using the expression:

$$\tilde{\mu}_e^{abs} = -e \varnothing^{abs} = WF \tag{3}$$

where $\tilde{\mu}_e^{abs}$ is the electrochemical potential of electrons and *WF* is the work function obtained as the difference between the Fermi level and the flat Hartree potential inside the bulk implicit solvent.

3. Results and Discussion

3.1. Lithium Polysulfide

The atomic positions of the Li_2S_6 molecule were taken from the supporting information of [32] and optimized with Quantum Espresso. Figure 2 shows the geometry of Li_2S_6 . The molecule presents a C2 point group symmetry. Our results are consistent with previous studies [31,32], although small

differences are acknowledged and attributed to the different implementation of the calculation codes adopted and to the choice of computational parameters (e.g., exchange and correlation functional, treatment of dispersion interactions).



Figure 2. Optimized geometry of the Li_2S_6 molecule. Li and S atoms are represented, respectively, in green and yellow.

The charge population analysis (see Table 1) denotes the transfer of electronic charge from the Li atoms to nearest sulfur atoms (S_1 and S_6). As better explained in the next section, The doping of graphene generates charge redistribution and the polarization of bonds, The partial ionic nature of the Li–S bond can enhance the interaction of the polysulfide with the doped substrates.

Table 1. Excess charges with respect to isolated atoms calculated according to Löwdin's approach.

Atom	q _{Löwdin} (a.u.)
Li ₂	0.165
Li ₂	0.165
S_1	-0.205
S_2	0.185
S_3	0.116
S_4	0.116
S_5	0.185
S_6	-0.205

3.2. Doped Graphene

In the following, pristine graphene, boron, aluminum and gallium-doped graphene are referenced as PG, BG, AG and GG, respectively. The structural modification associated with the heteroatom doping of graphene can be characterized by using the z-distance between the heteroatom, $\Delta z(X)$, and the x–y plane where the graphene layer lies and the bond length d_{X-C} between the heteroatom and the nearest carbon atoms (C₁, C₂ and C₃ in Figure 1). An important distortion of the planar geometry of pristine graphene with the insertion of Al and Ga is observed due to the larger size of the heteroatoms compared to carbon: the dopants protrude out of the graphene layer. On the other hand, since boron has an atomic radius similar to carbon, $\Delta z(B)$ and $\Delta z(C)$ are zero and only the bond length is modified by the doping. Our results, reported in Table 2, are comparable with those obtained by Varghese et al. [34].

Table 2. Structural properties of doped graphene monolayers. PG = pristine graphene, BG, AG, GG respectively boron, aluminum and gallium doped graphene. $\Delta z(X)$ vertical displacement of heteroatom X from graphene layer, $\Delta z(C)$ vertical displacement from the graphene layer of the 3 carbon atoms nearest to X, dX-C bond length between the heteroatom and the nearest carbon atoms.

Substrate	$\Delta z(X)$	Δz(C)	d _{X-C}
PG	0	0	1.42
BG	0	0	1.49
AG	1.65	0.87	1.85
GG	1.59	0.88	1.83

The doping of the graphene sheet with a heteroatom generates a redistribution of charge and a modification in its chemical properties. Table 3 reports the excess charge on B, Al and Ga and on the three neighboring carbon atoms (C_1 , C_2 and C_3) according to Löwdin's method.

Table 3. Excess charges on heteroatom X and on its first neighbor carbon atoms calculated according to Löwdin's approach.

Charge (a.u.)	PG	BG	AG	GG
q _X	_	0.104	0.805	0.465
q _{C1}	0.000	-0.124	-0.287	-0.188
q _{C2}	0.000	-0.123	-0.300	-0.196
q _{C3}	0.000	-0.123	-0.300	-0.196

Charge analysis shows that the doped systems exhibit an excess of positive charge on the heteroatom and an excess of negative charge on the neighboring carbon atoms. In addition, one can note that the Al produces the most remarkable redistribution of charge in comparison with the pristine graphene. Our results are in partial disagreement with previous literature by Vélez et al. [33] that predicted a negative excess charge on boron and positive charges on aluminum and gallium. On the other hand, Varghese et al. [34] found positive excess charge on boron and aluminum but negative on gallium. Wang et al., in their study of dissociation of N₂O on doped graphene, found a positive excess charge on Ga and Al. The differences between the research results mentioned here can be explained on the basis of the different computational approaches and selected parameters used and, in particular, as the methods followed to calculate the partial charges [59,60]. On the other hand, we consider our results reliable and realistic since they are in accordance with the commonly accepted concept of electronegativity of the chemical elements: the electronegativity of group III atoms is much lower than that of the carbon atom; the dopant atoms lose electronic charge in favor of carbon, and generate a polarized zone possibly strengthening the binding of the polysulfide to the graphene sheet.

The peculiar electronic structure of graphene is due to the sp² hybridization of the electronic orbitals of carbon atoms and to the symmetry of the structure. The density of states (DOS) presents a zero-band gap, so the material can be considered as a semimetal. Figure 3 shows the density of states of the different systems (DOS) considered here, where the DOS of the G-pristine system is given for comparison in grey.



Figure 3. Density of states (DOS) of the three doped systems. In each graph, The blue curve represents the DOS corresponding to the doped substrate and the grey area indicates the DOS of PG. The inset contains in red the projected DOS of the heteroatom. The diagrams were shifted in order to place the Fermi level at zero in all cases.

We can observe that the presence of all heteroatoms shifts the DOS to higher energy values, thereby enhancing the density of states at the Fermi level and the metallic character of the system. Our results are coherent with those obtained in previous studies [33,34] and can be explained on the basis of the different electronegativity levels of the heteroatoms with respect to the carbon that generates a polarization of the X–C bond. Moreover, in AG and GG, The structural distortion of the graphene layer from its original planar structure, induced by the difference in size between the heteroatoms and carbon, suggests a change in the nature of the hybridization state from sp² to sp³ for the C–X covalent bond.

3.3. Structures of Polysulfide on Doped Graphene

Figure 4 shows the optimized geometries for Li_2S_6 adsorbed on the graphenic substrates. The interaction strongly modifies the bond length and angles of the polysulfide, but no chemical bonds are broken, and the molecule preserves its integrity.



Figure 4. Structures of Li_2S_6 adsorbed on graphene substrates. Carbon atoms in brown, heteroatoms (B, Ga, Al) in the graphene layer in red, lithium atoms in green, sulfur atoms in yellow. Li_2S_6 suffers an important distortion of its structure interacting with doped graphene.

Table 4 reports the adsorption energies for the configurations depicted in Figure 4. As is apparent, The strength of the interaction follows the order PG < BG < GG < AG.

Substrate	Adsorption Energy (eV)
PG	-0.75
BG	-0.97
AG	-2.32
GG	-1.97

Table 4. Adsorption energy of Li₂S₆ on doped graphene substrates.

The polysulfide interacts with pristine graphene through one of the lithium atoms (Figure 4a). The most stable configuration is reached when one of the lithium atoms is placed over one of the carbon atoms of the graphene monolayer, at a distance of 2.502 Å. The interaction is not strong and mainly due to dispersion forces as expected.

The presence of boron in the substrate does not significantly modify the result: the interaction is stronger and the polysulfide orients one of the lithium atoms towards the surface. In this specific case, The most stable configuration is with the lithium atom located on the center of the graphenic ring containing the boron atom (Figure 4b). The medium distance between lithium and the five carbon atoms of the ring is 2.466 Å and the distance between lithium and boron is 2.431.

In the case of aluminum and gallium doping, The most stable configurations apply to the formation of a chemical bond between the heteroatom on graphene and one of the sulfur atoms linked to lithium of the polysulfides to form a bridge Li–S-X (X = Al, Ga). The interaction of the heteroatom with the other sulfur atoms of Li₂S₆ leads to less stable configurations with lower binding energy. In addition to the formation of the Li–S-X bridge, Li₂S₆ rotates and orients one of its lithium atoms to point towards a carbon atom on the substrate (Figure 4c,d). This configuration, found also by Vélez et al. [33] for aluminum-doped graphene, maximizes the adsorption energy since, in addition to the formation of the chemical bond between sulfur and the heteroatom, there is a contribution of the dispersion interactions between lithium and carbon. In the case of the aluminum-doped system the Al–S bond length is 2.316 Å and the distance between lithium and the nearest carbon on the monolayer is 2.182 Å. The same figures for the gallium-doped system are: Ga–S bond length 2.375 Å, Li–C distance 2.241 Å.

Our results show that the introduction of III group elements in the graphene structure can be used to tailor the interaction with Li_2S_6 and, especially in the case of aluminum and gallium, it can improve the binding of the polysulfide on the substrate, limiting in this way the shuttling mechanism associated to the polysulfide diffusion in the electrolyte solvents.

3.4. Electronic Structure of Polysulfide on Doped Graphene

3.4.1. Li₂S₆ on Pristine Graphene

Charge population analysis in Table 5 shows that the adsorption of Li_2S_6 on pristine graphene involves a charge transfer of electrons from the substrate to the polysulfide. In particular, The charge is transferred to the lithium atom. A total of about 0.37 electrons are gained by Li_2S_6 . This implies a redistribution of charge density in Li_2S_6 ; as highlighted by Figure 5a: charge accumulates on lithium atoms and on the sulfur atoms attached to them. On the other hand, a charge depletion region (cyan color in the picture) is formed on the sulfur atoms not bonded to lithium atoms. No accumulation of charge is evident between the polysulfide and the substrate. This confirms that the adsorption does not involve the formation of chemical bonds and that it is generated by the action of dispersion forces. The analysis of the projected density of states (DOS) in Figure 5b shows the interaction between the $2p_z$ orbital of the carbon atom nearest to the lithium atom with the s and p orbitals of the lithium atom. The bonding states are located below and near the Fermi energy. The figure does not report the p_x and p_y orbitals of carbon that are situated at much lower energies and are hybridized with s states to form sp₂ orbitals, responsible for the formation of the covalent σ bond in graphene. It is well known that delocalized π states in graphene are mainly contributed by electrons from C 2p_z orbitals. So, the interaction of the lithium atom of the polysulfide with pristine graphene is due essentially to the π electrons, but the small overlap of the DOS peaks in Figure 5b reveals a very weak interaction.

Table 5. Charge population analysis for the PG + Li_2S_6 system. Excess charges are reported for the Li atom, for the carbon atom interacting with lithium (C_0) and for its three nearest neighbor carbons (C_1 , C_2 and C_3) in the graphene monolayer.

Atomic Site	Charge (a.u.)
Li	-0.17
C ₀	-0.03
C1	0.00
C ₂	0.00
C_3	-0.01



Figure 5. (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configuration of the PG + Li_2S_6 system. The plotted iso-level is 1.5×10^{-2} e/Bohr³. (b) Partial density of states projected on selected atoms. The densities were shifted to align the Fermi level to zero.

3.4.2. Li₂S₆ on Boron-Doped Graphene

As we have seen in Section 3.2, The presence of boron in the graphene structure determines a charge transfer from boron to its nearest carbon neighours, this affects the adsorption of the polysulfide on the substrate. Table 6 reports Löwdin's charge analysis for the BG + Li_2S_6 system. Since the lithium atom is located at the center of the graphenic ring containing the boron atom, we report the excess charges of all the atoms of the ring calculated, taking as reference the charges of the same atoms for the system with no polysulfide adsorbed. In total, about 0.14 electrons are transferred to the sulfide, mainly to the lithium atom nearest to the substrate. The variation of charge on each atom of the substrate atoms is very limited.

Table 6. (Charge population	analysis for the B	$G + Li_2S_6$ system.	Excess of	charges are	reported f	or the Li
atom, for	the boron atom an	d for the five carb	ons interacting w	ith lithiu	ım.		

Atomic Site	Charge (a.u.)
Li	-0.14
В	-0.06
C1	0.00
C ₂	-0.01
C ₃	-0.02
C_4	-0.02
C ₅	-0.02

The differential charge density in Figure 6a gives further insight on the nature of the adsorption process of the polysulfide. A charge accumulation between the lithium atom and the substrate and

a depletion of charge, especially between the lithium and sulfur atoms, are evident. The increased charge density on carbon atoms induced by the presence of the boron atom makes the substrate more polar and strengthens the interaction with the polysulfide. This is confirmed by the analysis of partial densities of states in Figure 6b. The states from boron and carbon overlap in the region between the Fermi level and -2 eV: this indicates the formation of the π C–B bond. Lithium s and p orbitals overlap with p_z orbitals of boron and carbon associated with the π bonding. This explains the increased adsorption energy of Li₂S₆ on the boron-doped system with respect to pristine graphene.



Figure 6. (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configuration of the BG + Li_2S_6 system. The plotted iso-level is 1.5×10^{-2} e/Bohr³. (b) Partial density of states projected on selected atoms. The densities were shifted to align the Fermi level to zero.

3.4.3. Li₂S₆ on Aluminum-Doped Graphene

Based on the modification of energetic, structural and electronic properties induced by Al doping, we expect a stronger modification of the electronic properties of the AG + Li_2S_6 system with respect to the pristine and boron-doped counterparts. In fact, The doping with aluminum determines a charge transfer from the heteroatom to its nearest carbon neighbours much stronger than in the case of boron. Table 7 reports Löwdin's charge analysis for the AG + Li_2S_6 system. Now, in contrast to the previous cases, 0.13 electrons are transferred from the sulfide to the substrate. Essentially all the charge is accumulated by the aluminum atom.

Table 7. Charge population analysis for the AG + Li_2S_6 system. Excess charges are reported for the lithium atom near the substrate, for the sulfur atom bonded to aluminum, for the aluminum atom and for the three carbons (C_1 , C_2 , and C_3) bonded to aluminum. C_1 is also the atom interacting with lithium.

Atomic Site	Charge (a.u.)
Li	-0.06
S	0.10
Al	-0.11
C ₁	-0.02
C ₂	0.05
C ₃	0.05

The differential charge density in Figure 7a shows an accumulation of charge between one of the lithium atoms of the polysulfide and the carbon atoms of the substrate. Moreover, charge is accumulated in the region between sulfur and aluminum (Al–S bond). Even more than in the case of boron doping, The increased charge density on carbon atoms induced by the presence of the heteroatom

and aluminum. That peak appears in the doped substrate (see Figure 3 for AG system and its inset) and is further populated in the AG + Li_2S_6 system. Figure 7c shows the overlap between sulfur and aluminum states below the Fermi level that can be intepreted as the formation of bonding states. So, The formation of a bond between sulfur and aluminum and the increased interaction of lithium with carbon due to the polarization induced by aluminum explains the high adsorption energy of Li_2S_6 on the aluminum-doped graphene.



Figure 7. (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configuration of the AG + Li_2S_6 system. The plotted iso-level is 1.5×10^{-3} e/Bohr³. (b,c) Partial density of states projected on selected atoms. The densities were shifted to align the Fermi level to zero.

3.4.4. Li₂S₆ on Gallium-Doped Graphene

The GG + Li_2S_6 system is very similar to the AG + Li_2S_6 . As for aluminum, gallium doping determines a charge transfer to carbon atoms near the heteroatom and, as a consequence, a polarization of the substrate. Table 8 reports Löwdin's charge analysis for the GG + Li_2S_6 system. The sulfide transfer to the substrate is 0.19 electrons (not reported in the table). Essentially all the charge is accumulated by the gallium atom.

Atomic Site	Charge (a.u.)
Li	-0.06
S	0.17
Ga	-0.16
C ₁	-0.03
C ₂	0.04
C ₃	0.05

The differential charge density in Figure 8a shows an accumulation of charge between one of the lithium atoms of the polysulfide and the carbon atoms of the substrate. In addition, charge is accumulated in the region between sulfur and gallium (Ga–S bond). The partial densities of states in Figure 8b show an increased overlap, with respect to the pristine system, between lithium s and p orbitals and p_z orbitals of carbon, probably due to the augmented population of p_z states on carbon induced by gallium. This is confirmed by the presence in the density of states of carbon of a sharp peak at the Fermi level that can be ascribed to the bond between carbon and gallium. That peak appears in the doped substrate (see Figure 3 for GG system and its inset) and is further populated in the GG + Li₂S₆ system. Figure 8c shows the overlap between sulfur and aluminum orbitals below the Fermi level that can be intepreted as the formation of bonding states. As in the case of aluminum doping, The formation of a bond between sulfur and the heteroatom and the increased interaction of lithium with carbon due to the polarization of the substrate explain the high adsorption energy of Li₂S₆ on the gallium-doped graphene with respect to the born-doped and pristine systems.



Figure 8. Cont.



Figure 8. (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configuration of the GG + Li_2S_6 system. The plotted iso-level is 1.5×10^{-3} e/Bohr³. (b,c) Partial density of states projected on selected atoms. The densities were shifted to align the Fermi level to zero.

3.5. Solvent and Polarization Effects

With the AG system being the most promising substrate considered in the present study, we performed additional calculations on it to evaluate the effect of the presence of the electrochemical interface between the electrode and a liquid electrolyte. We adopted an implicit solvent characterized by a dielectric constant equal to that of typical solvents used in Li–S cells (e.g., 1,3-DOL or 1,2-DME). Moreover, a negative polarization of the system, mimicking the effect of electron transfer coming from the anode and associated to the oxidation of lithium, was applied. In this condition, we were able to calculate the potential of the electrode–electrolyte interface.

Figure 9 reports the behavior of the electrode potential as a function of the negative polarization: it is evident that the potential of zero charge (PZC), that is the potential of the not charged interface, is about 3.4 V vs. Li/Li ⁺. On the other hand, The potential of the electrode is 2.3 V vs. Li/Li + when the electron excess is about 0.4 electrons per sulfur atom. This is in agreement with the analogous experimental curve for the cathode of Li–S cell (see for example [4], page 27.6).



Figure 9. Electrode potential vs. Li/Li+ as a function of the polarization of the electrode expressed as excess electrons per sulfur atom.

The variation of the binding energy of Li_2S_6 to the aluminum-doped graphene as a function of the substrate polarization is reported in Figure 10. At the PZC, The binding energy is modified just by the presence of the implicit solvent. In that condition the binding energy is -1.34 eV and has

to be compared with the corresponding value in vacuum, -2.31 eV. So the presence of the solvent, as expected, weakens the interaction between the polysulfide and the AG substrate. The binding energy is further decreased by polarization of the surface and the curve, with respect to the total charge of the system, has a maximum at about 0.21 electrons per S atom.



Figure 10. Binding energy of the polysulfide on the AG substrate as a function of the charge per sulfur atom.

In the following we report Löwdin's charge analysis, The differential charge density plot and the partial densities of states for the AG + Li_2S_6 system in contact with the implicit solvent and at the potential of 2.3 V vs. Li/Li⁺.

Table 9 contains Löwdin's charge analysis: the data have to be compared with those reported inTable 7. In this case we obtain more negative charge accumulated on the Al atom. On the other hand, The complete analysis of the charge accumulated on the sulfide shows that 1.37 electrons are transferred to Li_2S_6 . Essentially, all the charge is accumulated on the lithium and sulfur atoms far from the substrate. So the effect of charging the substrate is to induce a strong charge separation on the polysulfide that may result in a possible decomposition of the molecule or in a chemical reaction with the substrate. This possibility will be further investigated in a following study.

Table 9. Charge population analysis for the charged AG + Li_2S_6 system in contact with the solvent. Excess charges are reported for the lithium atom near the substrate, for the sulfur atom bonded to aluminum, for the aluminum atom and for the three carbons (C_1 , C_2 , and C_3) bonded to aluminum. C_1 is also the atom interacting with lithium.

Atomic Site	Charge (a.u.)
Li	0.05
S	0.09
Al	-0.16
C ₁	0.09
C ₂	-0.05
C ₃	0.05

As for the uncharged system in vacuum, The differential charge density in Figure 11a shows an accumulation of charge between one of the lithium atoms of the polysulfide and the carbon atoms of the substrate. An accumulation of charge is evident in the region between sulfur and aluminum (Al–S bond) but is less intense than the corresponding system in vacuum and with no polarization. Moreover, The charge deplation region around the Al and S atoms is here larger than in Figure 7. The analysis of partial densities of states in Figure 11b shows that the energy levels of carbon are shifted towards higher energies and that there is a good overlap between the lithium s and p orbitals and

the p_z orbital of carbon as in the case of the uncharged system in vacuum. Here the most important overlap is observed at about -2 eV with respect to the Fermi level.



Figure 11. (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configuration of the charged AG + Li_2S_6 system in solvent. The plotted iso-level is 1.5×10^{-3} e/Bohr³. (b,c) Partial density of states projected on selected atoms. The densities were shifted to align the Fermi level to zero.

Figure 11c reports the overlap between sulfur and aluminum states below the Fermi level that can be intepreted as the formation of bonding states. With respect to the uncharged and isolated system, we note here an increased population of the states below the Fermi level as a consequence of the polarization of the substrate and of the charge transfer to the sulfide.

Since the structure and the electronic properties of the GG system are very similar to those of the Al-doped graphene, we expect that the solvation and the polarization of the substrate will modify the binding energy of Li₂S₆ to the Ga-doped substrate in a very similar way.

4. Conclusions

DFT calculations were performed to determine the adsorption behavior of Li_2S_6 on graphene substrates doped with III group elements. The sequence of adsorption binding energies is AG > GG > BG > pristine. The interaction between the polysulfide and pristine or boron-doped graphene is due to the interaction of the s and p states of lithium with delocalized π electrons of carbon (or boron). On the other hand, Al- and Ga-doped graphene interact with the polysulfide in two points: the heteroatom forms a chemical bond with one of the sulphur atoms. Moreover, as a consequence of

the polarization of the carbon atom of the substrate induced by the heteroatom, The interaction of one of the lithium atoms of the polysulfide with carbon is enhanced with respect to pristine graphene. Thus, according to our results, aluminum- and gallium-doped graphene could be used as the substrate of sulphur-based composite electrodes for Li–S cells since according to our calculations they could mitigate the shuttle effect and prolong the cell lifetime.

The presence of the solvent and of the polarization of the surface does not alter our findings: the simulation of the Al-doped system showed that the binding energy of the polysulfide is decreased but it is still higher than that of the polysulfide with the uncharged pristine graphene in vacuum. To increase the predictive power of our calculations, additional work could be devoted to study the effect of the inclusion of an explicit treatment of the solvent and to realize proper electrochemical experiments that are able to verify the accuracy of our simplified model of the electrochemical interface.

Supplementary Materials: The following are available online at http://www.mdpi.com/2313-0105/6/3/46/s1, Table S1: Adsorption energy of long chain polysulfides (Li_2S_x , x = 4, 6, 8) on the Al-doped graphene substrate. Figure S1: (a) Iso-surface (yellow color: negative, charge accumulation; cyan color: positive, charge depletion) of differential charge density for the most stable configurations of Li_2S_4 (a) and Li_2S_8 (b) on the Al-doped graphene. The plotted iso-level is 1.5×10^{-3} e/Bohr³. These densities have to be compared to Figure 7 in the main text: no relevant modification of the differential electron densities is observed as a function of the polysulfide length.

Author Contributions: Conceptualization, methodology, software, investigation, writing—original draft preparation M.F.S. Validation, writing—review and editing, D.P., A.I.P. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Acknowledgments: We would like to thank Oliviero Andreussi of University of North Texas for the fruitful discussion on electrochemical interfaces and for the support on the use of the Environ code.

Conflicts of Interest: The authors declare no conflict of interest.

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