

Article

Experimental Study on Influence of Initial Relative Dry Density on K_0 of Coarse-Grained Soil

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Abstract: The coefficient of earth pressure at rest, K_0 , is a significant mechanical parameter, and the investigation of the K_0 of coarse-grained soil has important theoretical significance and applicational value in geotechnical engineering. However, there are few studies on the influence of the initial dry density (ρ_d) on the K_0 of coarse-grained soil due to the limitations of the related test instruments or methods. A series of K_0 tests for two types of coarse-grained soils (rockfill soil and sandy-gravel soil) were conducted based on a newly developed large-scale apparatus to reveal the relationship between the K_0 and ρ_d of coarse-grained soil. The test results showed that the K_0 of coarse-grained soil decreases with an increase in vertical stress, and this trend tends to be gentle with respect to the increase in vertical stress. The results also implied that there was a negative linear relationship between the K_0 of coarse-grained soil and ρ_d . Furthermore, a comparative analysis between rockfill soil and sandy-gravel soil indicated that the relative equation proposed by the authors was appropriate for any type of coarse-grained soil with any ρ_d . Moreover, an empirical equation that can accurately describe the effective relationship of σ_v and ρ_d with the K_0 for coarse-grained soil was proposed, and the accuracy of the empirical equations were verified by the K_0 test results concerning sand-gravel soil. Finally, based on the published research findings, the empirical equations' applicability to any coarse-grained soil was verified.

Keywords: coefficient of earth pressure at rest; coarse-grained soil; initial relative density; effective vertical stress; soil type



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1. Introduction

The coefficient of earth pressure at rest K_0 is a significant mechanical parameter of soil and is defined as the ratio of the effective horizontal stress σ'_h to the effective vertical stress σ'_v in the soil under conditions of no lateral strain [1]. The study of the K_0 has important theoretical significance and applicational value for practical geotechnical engineering projects, e.g., those related to slopes [2,3], foundation pits [4–7], and retaining walls [8–11]. However, this measure is not accurate enough for engineering purposes, especially with respect to coarse-grained soils, which are mainly defined as soil and rock mixtures with a particle size of 0.075 mm to 60 mm and a particle content of more than 50% [12]. In fact, using the existing test instruments, it is difficult to accurately measure the K_0 of coarse-grained soil due to its large particle size, and there are few research achievements in this regard [4]. Therefore, few studies on the K_0 of coarse-grained soil have been reported.

Unfortunately, it is necessary to accurately obtain the K_0 of coarse-grained soil in many geotechnical engineering applications. For example, coarse-grained soil is often used as a subgrade filling material in heavy haul railways, and its K_0 value plays a prominent role in predicting the deformation of roadbeds and the earth pressure of a structure. The

investigation of the K_0 of coarse-grained soil has important theoretical significance and applicational value in practical geotechnical engineering.

According to the research of Li et al. [13], the initial dry density ρ_d of soil has a significant influence on the effective internal friction angle (φ') of coarse-grained soil. With the increasing ρ_d , the φ' of coarse-grained soil increased linearly. Through testing, Gao et al. [14] found that remolded loess has a linear positive correlation with φ' and proposed an empirical formula for it. Li et al. [15] investigated the effect of ρ_d on the shear strength of coal gangue through experiments and found that the φ' of coal gangue also increased with ρ_d .

Previous studies have highlighted the fact that the φ' of soil increases linearly with an increase in ρ_d . Many scholars have focused on the relationship between the φ' and K_0 [16–18], and it has been determined that there is a negative correlation between soil φ' and K_0 . Therefore, with an increase in ρ_d , the K_0 of soil may decrease. However, some researchers have reported that the K_0 of sand and clay decreased with an increase in ρ_d [19–21]. Currently, the majority of studies about the relationship between ρ_d and K_0 have focused on the soil type of sand or clay [22], but still provided ambiguous results about the relationship between the ρ_d and K_0 for coarse-grained soil.

According to the research of Zhu et al. [23], stress state has a significant effect on the K_0 of coarse-grained soil. Moreover, the formula modelling the relationship between the K_0 of coarse-grained soil and its stress state was developed based on experimental results (refer to Equation (1)). However, Equation (1) was obtained on the basis of the test data of loose samples, thus raising the question of whether the equation is applicable for compacted coarse-grained soil. Additionally, the influence mechanism of stress state on the K_0 of coarse-grained soil also needs to be explored further.

$$K_{0oc} = \left[\frac{K_{0\max} + K_{0\min} \sqrt{\frac{\sigma_c/OCR}{P_a}}}{\sqrt{\frac{\sigma_c/OCR}{P_a}} + 1} \right] OCR^n \quad (1)$$

In the equation above, p_a is standard atmospheric pressure; $K_{0\max}$ and $K_{0\min}$ are material parameters, i.e., the K_0 values corresponding to the situation when the σ'_v is 0 and tends to ∞ , respectively; and σ'_c is the pre-consolidation pressure.

In addition, research [24,25] has shown that different soil types lead to the alteration of K_0 , even for different clays [26]. Many scholars have conducted a number of studies on the particle size of coarse-grained soils. Marachi used the rejection method to reduce the maximum particle size of all three coarse grains to 151, 51, and 12 mm, and ensured that all the specimens had the same initial dry density [27]. Ahad used the rejection method and a similar grading method to reduce the size of coarse grains and carried out large triaxial tests on the reduced-size specimens. However, most scholars have studied the shear expansion of particle size, the angle of internal friction, and shear expansion, while focusing to a lesser degree on analyzing the static pressure coefficient to determine the scaling effect [28]. Therefore, further studies on the influence of soil type on the K_0 of coarse-grained soil are particularly significant.

In this paper, to reveal the relationship between K_0 and ρ_d for coarse-grained soil, a series of K_0 tests for two types of soil (rockfill and sandy gravel) were conducted using a newly developed large-scale apparatus. Based on the experimental results of regarding gravel, a formula for the relationship between K_0 and D_{r0} and vertical stress σ_c was developed and then validated via the experimental results of the rockfill. Moreover, the influence of coarse-grained soil type was studied by comparing the experimental data of rockfill and sandy-gravel soil with the same initial conditions.

2. K_0 Experiment for Coarse-Grained Soil

A large-scale K_0 -test device developed by Hohai University was used in this study (Figure 1). Compression tests can be conducted on various types of soil (e.g., coarse-grained soil) under a high stress state. The employed test equipment mainly consists of a pressure

chamber, a loading system, and a measurement control system. The loading system consists of a loading frame provided by the top beam and a loading cylinder, which is connected to the base of the pressure chamber, with the pump pressure providing the jacking force from the bottom of the specimen through the piston. The testing system mainly consists of four Schein pull sensors (10), one load sensor, two displacement sensors (11), and weight sensors (12). The working principle of this device is as follows: The specimen in the barrel will adopt a lateral deformation tendency under the vertical compressive stress; thus, the semi-circular rigid barrel is squeezed. At this time, the normal stress acting on the AB section is equal to the lateral stress acting on the specimen, and the combined force of the normal stress on this section, which is the total pressure in the specimen along the direction of the diameter of the cross section, can be measured using a tensile force transducer. Accordingly, the lateral stress in the specimen can be obtained as

$$\sigma'_h = \frac{N_h}{(h - \Delta h)d} \quad (2)$$

where $(h - \Delta h)d$ is the area of the AB section, wherein h and d are the initial height and diameter of the specimen, respectively. Δh is the compression of the specimen after loading, measured by the displacement sensor. N_h is the total pressure in the specimen along the cross section in the direction of the diameter, which is measured by the tensile sensor.

During the test, as the soil tends to move downwards relative to the sidewall when vertically compressed, it is bound to generate a frictional force with respect to the sidewall. This friction gradually reduces the vertical stress on the specimen along the height of the specimen, resulting in the N_v measured by the vertical load cell not being equal to the actual vertical stress acting inside the specimen. It is, therefore, necessary to eliminate the effect of friction on the side walls and obtain test data that better reflect the actual stresses on the specimen.

To attenuate the effect of sidewall friction, in this study, we used the arithmetic mean of the vertical forces at the bottom and top of the specimen as the vertical force applied to the specimen to calculate the K_0 . During the test, four pressure weight sensors are arranged at the bottom of the specimen barrel, and the sensors are zeroed before loading to exclude the effect of the barrel with regard to the specimen's own weight, thereby allowing the sidewall friction force f to be measured during the test. Thus, the vertical pressure on the top surface of the specimen is N_v/A (A is the area of the specimen), and the vertical pressure on the bottom surface is $(N_v - f)/A$. Assuming that friction is uniformly distributed along the side walls, the average vertical stress in the specimen is as in Equation (3).

$$\sigma'_h = \frac{N_v - 0.5f}{0.25\pi d^2} \quad (3)$$

Therefore, the static lateral coefficient of pressure, K_0 , corrected for the effect of friction, can be calculated using Equation (4).

$$\sigma'_h = \frac{N_h}{(h - \Delta h)d} / \frac{N_v - 0.5f}{0.25\pi d^2} \quad (4)$$

Two types of coarse-grained soil from the Dashixia concrete face dam and the Rumei rockfill dam were tested. Then, the sandy-gravel soil materials were denoted as S1–S4, while the rockfill materials were denoted as R1–R4. The shares of each grain group of grades 60~40, 40~20, 20~10, 10~5, and <5 mm are 17.22%, 25.04%, 17.75%, 13.38%, and 26.6%, respectively. The particle size distribution of the sandy-gravel soil, which is the same as that for the rockfill, is depicted in Figure 2.

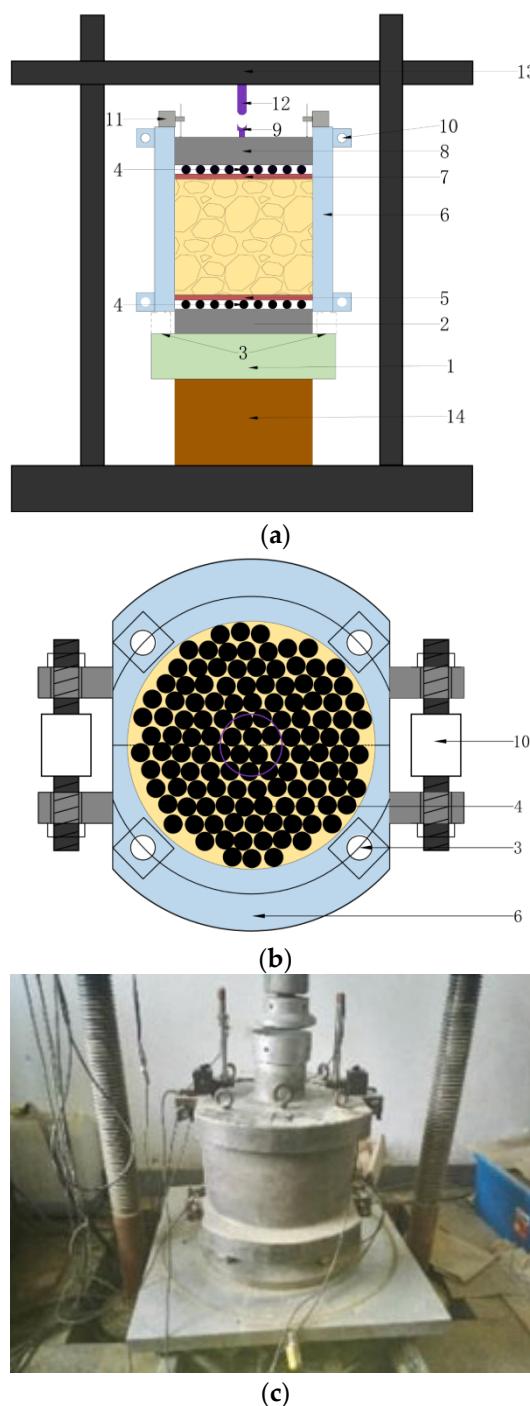


Figure 1. Test equipment (Note: 1—pedestal, 2—base, 3—load sensor, 4—steel ball, 5—the bottom force transmission plate, 6—semicircular rigid cylinders, 7—the top force transmission plate, 8—pressure plate, 10—tension sensors, 11—displacement sensor, 12—load sensor, 13—loading frame, and 14—loading device). (a) Sketch map of test equipment, (b) top view of the apparatus, and (c) physical view of the instrument.

The diameter and height of all specimens are 40 cm and 30 cm, respectively. The specimens of coarse-grained soil were produced as follows: first, specimens were air-dried and divided into three equal parts by weight, which were then filled into a pressure chamber. Then, specimens of each layer were compacted using a vibrating compactor to obtain the designed initial dry density, ρ_d . The ρ_d of every specimen is shown in Table 1.

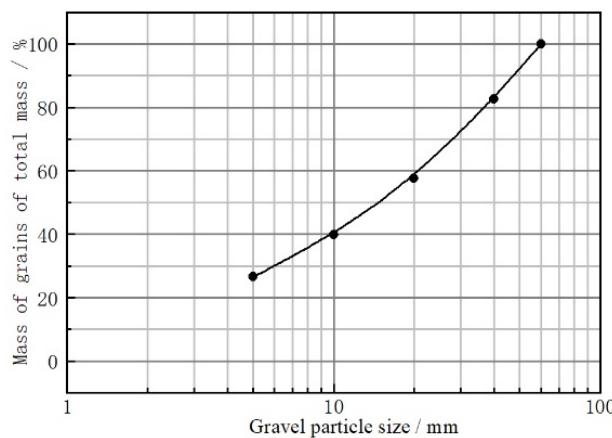


Figure 2. Particle Size Distribution (PSD) curves of test specimens.

Table 1. Basic property of tested soil and specimens.

Sand	Specimen	Density (g/cm ³)
Rockfill	R1	2.003
	R2	1.948
	R3	1.896
	R4	1.847
Sand gravel	S1	2.043
	S2	1.989
	S3	1.938
	S4	1.844

3. Test Results and Discussion

3.1. Relationship between K_0 and σ'_v for Coarse-Grained Soil

Based on the experimental results, the relationship between K_0 and vertical stress σ'_v for S1–S4 is illustrated in Figure 3. It can be observed that σ'_v has a significant influence on the K_0 of coarse-grained soil and that K_0 decreases as σ'_v increases. Elsewhere, similar results were found in the test results for loose coarse-grained soil [26], sand [29,30], municipal solid waste, and sand gravel [31]. Hence, it is of great theoretical importance to obtain a formula that describes the relationship between K_0 and σ'_v . According to the K_0 test of coarse-grained soil, Zhu et al. [26] determined a relationship between $K_0-\sigma'_v$, as shown in Equation (1). However, Equation (1) was obtained based on loose specimens. Therefore, further studies are required to determine whether it is applicable for dense coarse-grained soil.

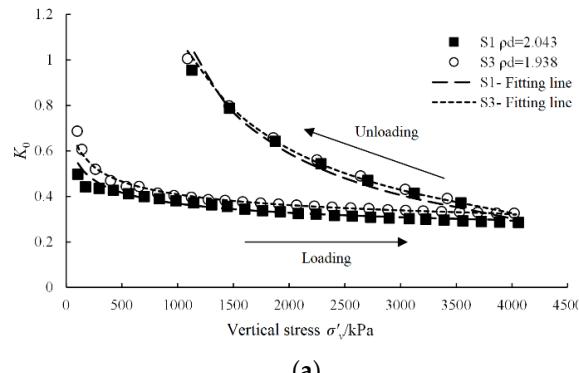


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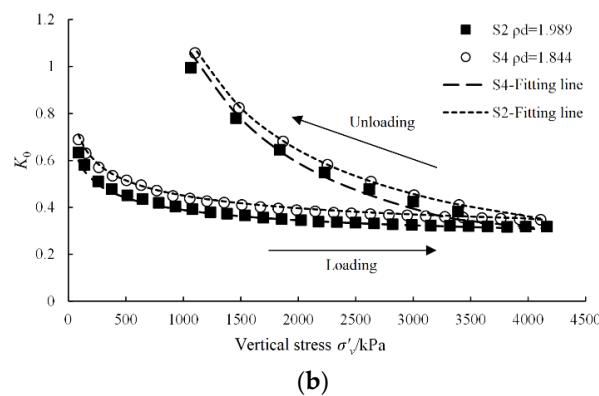


Figure 3. $K_0-\sigma_1$ curves with different p_d : (a) S1 and S3; (b) S2 and S4.

To verify the applicability of Equation (1) for dense coarse-grained soil, Equation (1) was adapted to fit the test results of S1~S4, for which the fitting parameters are listed in Table 2, while the fitting curves are given in Figure 4. Figure 4 shows that the fitting curve and experimental results are in good agreement. Specifically, compared to the corresponding test data, the average error of the fitting data for Equation (1) is less than 5%, while the maximum error is less than 14%. As discussed above, it is clear that Equation (1) can also be adopted to describe the K_0 behavior of compacted coarse-grained soil.

Table 2. $K_{0\max}$ and $K_{0\min}$ of the tested specimens.

Fitting Parameters	Specimen			
	D1	D2	D3	D4
$K_{0\max}$	0.872	0.894	0.922	0.968
$K_{0\min}$	0.212	0.234	0.246	0.268
n	0.747	0.704	0.684	0.678
R^2	0.98	0.99	0.99	0.99

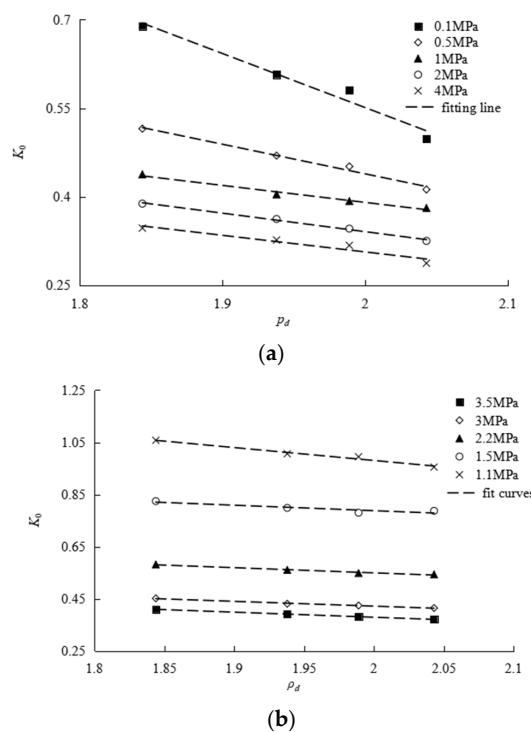


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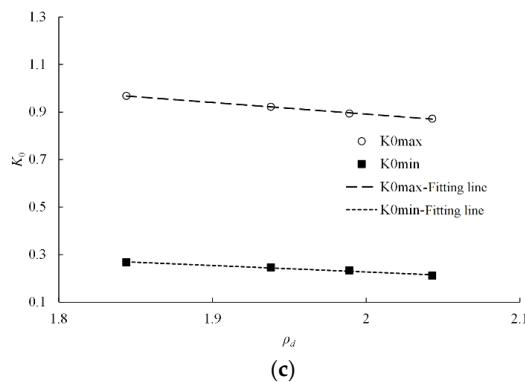


Figure 4. $K_{0\max}/K_{0\min}-p_d$ fitting curves: (a) loading stage; (b) unloading stage. (c) $K_{0\max}/K_{0\min}-D_{r0}$ fitting curves.

3.2. Influence of Initial Dry Density (ρ_d) on K_0

To analyze the effect of the initial dry density (ρ_d) on the K_0 for coarse-grained soil, the test results of different values of ρ_d are given in Figure 3a,b. From Figure 3a,b, it can be seen that there are evident differences in the K_0 of different ρ_d under the same σ'_v . More specifically, the K_0 of the specimens tend to decrease with an increasing ρ_d . A similar variation law of K_0 was reported in the study of silt-bearing sand [19], pure sand [22], and muddy sand [23]. Obviously, there is important theoretical significance to obtaining a formula that can describe the relationship between K_0 and ρ_d .

To study the influence law of ρ_d on K_0 , the K_0 values of rockfill at different ρ_d values corresponding to σ'_v at 0.1 to 4 MPa during loading and at 3.5 to 1.1 MPa during unloading were obtained using the results of S1–S4, as shown in Figure 3. K_0 and ρ_d are approximately linearly negatively correlated under the same σ'_v .

$$K_0 = b - a\rho_d \quad (5)$$

In the above equation, a and b are material parameters. The rockfill parameters a and b and the determination coefficient R^2 obtained via fitting under each vertical stress during loading and unloading are listed in Table 3, and the fitting curve is depicted in Figure 4.

Table 3. a and b under different vertical stress for specimens.

Value	During Loading (MPa)						During Unloading (MPa)			
	0.1	0.5	1	2	4	3.4	3	2.5	1.5	1.1
a	0.92	0.5	0.29	0.31	0.28	0.19	0.18	0.2	0.21	0.49
b	2.4	1.4	0.97	0.97	0.87	0.77	0.79	0.95	1.21	1.97
R^2	0.94	0.88	0.85	0.84	0.95	0.94	0.91	0.97	0.88	0.94

It can be seen from Figure 4 that the fitting curve of Equation (5) agrees well with the test data. More specifically, the error of prediction value in Equation (5) is small, the maximum error is less than 10.2%, and the minimum value of determination coefficient R^2 is 0.83. Obviously, under the same σ'_v , the relationship between the K_0 and the initial dry density (ρ_d) of rockfill can be approximately expressed by a linear equation. In Equation (1), $K_{0\max}$ and $K_{0\min}$ represent the K_0 of soil when $\sigma'_v \rightarrow \infty$ and $\sigma'_v = 0$, respectively; thus, $K_{0\max}$ and $K_{0\min}$ may have a linear relationship with ρ_d .

Based on Tables 1 and 2, the relationship between the $K_{0\max}/K_{0\min}$ and the ρ_d of rockfill is plotted in Figure 4. Figure 4 shows that the $K_{0\max}$ and $K_{0\min}$ of rockfill decrease linearly with an increase in ρ_d . Therefore, the relationship between $K_{0\max}/K_{0\min}$ and ρ_d can be expressed as follows:

$$\begin{cases} K_{0\max} = K_{0\max 0} - cp_d \\ K_{0\min} = K_{0\min 0} - dp_d \end{cases} \quad (6)$$

where $K_{0\max 0}$, $K_{0\min 0}$, c , and d are the material parameters, and $K_{0\max 0}$ and $K_{0\min 0}$ are the K_0 of the soil with $\rho_d \rightarrow 0$ when σ'_v is 0 and tends to be ∞ , respectively.

The test data of S1–S4 were fitted using Equation (6), and the rockfill parameters $K_{0\max 0}$, $K_{0\min 0}$, c , and d used in the test are 1.8685, 0.4886, 0.7741, and 0.2724, respectively. The fitting curves are shown in Figure 4. It can be seen from Figure 4 that the fitting curve agrees well with the test results. Specifically, the error of the predicted value in Equation (6) is less than 1%, and the maximum error is less than 2%. Hence, it can be considered that Equation (6) accurately describes the relationship between K_0 and ρ_d .

By combining Equations (1) and (6), the relationship between the K_0 and ρ_d of coarse-grained soil can be obtained.

$$K_0 = \left[\frac{K_{0\max 0} - c\rho_d + (K_{0\min 0} - d\rho_d)\sqrt{\frac{\sigma'_v/OCR}{P_a}}}{\sqrt{\frac{\sigma'_v/OCR}{P_a}} + 1} \right] OCR^n \quad (7)$$

From Equation (7), under the known material parameters (i.e., $K_{0\max 0}$, $K_{0\min 0}$, c , and d) conditions, the K_0 of coarse-grained soil can be estimated based on the OCR and σ'_v .

To validate Equation (7), the test results of R1–R4 were fitted, for which the sand gravel parameters $K_{0\max 0}$, $K_{0\min 0}$, c , and d are 1.3408, 0.2064, 0.7075, and 0.2596, respectively. The fitting curve and corresponding test data are plotted in Figure 5. In Figure 5, it is evident that the fitting curve of Equation (7) is in good agreement with the test data. The error of the predicted value in Equation (6) is less than 5%, and the maximum error is less than 11.3%. Obviously, Equation (7) can describe the relationship between K_0 and ρ_d as well as σ'_v for coarse-grained soil.

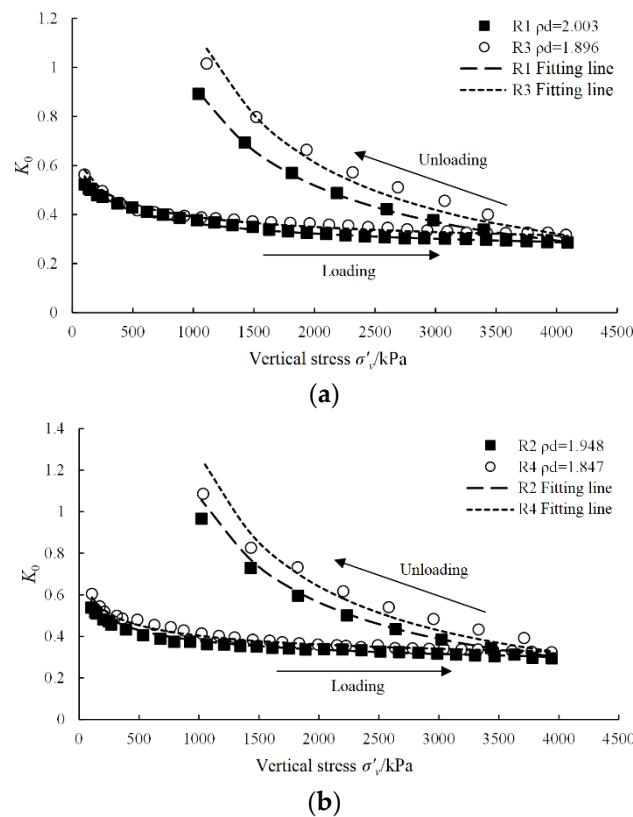


Figure 5. K_0-d_M curves. (a) S1 and S3. (b) S2 and S4.

4. Empirical Formula Verification

In this paper, K_0 tests were carried out on piles of sand, pebble material, and gravel, resulting in empirical equations for K_0 and ρ_d . In order to further verify that the above

empirical Equation (7) for determining the K_0 , ρ_d , and for coarse-grained soils are applicable to dry density coarse-grained soils at any gradation and to non-ground coarse-grained soils, the above conclusions need to be supported by more test data. In one study, the maximum particle sizes d_{\max} of the original graded soil material were determined to be 600 and 100 mm for piled stone and sand-cobble, respectively. In order to meet the test size requirements, a series of large triaxial tests with different particle sizes and grading structures were carried out on the sand-cobble by using three different grading reduction methods, namely, a scalping technique, a replacement technique, and a parallel gradation technique [23]. The effect of different loading conditions on the K_0 of sand pebbles was detailed by studying the static earth pressure coefficient of sand pebbles under different loading conditions, which was derived as K_0 increases significantly with an increasing over consolidation ratio (OCR), yielding an empirical equation that can well describe the relationship between OCR and K_0 . The test results are shown in Table 4. The empirical Equation (7) derived above was further validated using the values obtained from the cited paper.

Table 4. Different dry densities, $K_{0\max}$, and $K_{0\min}$.

Soils	Density (g/cm^3)	$K_{0\max}$	$K_{0\min}$
S ₆₀	2.051	0.953	0.291
S ₄₀	2.034	0.972	0.296
S ₂₀	1.962	1.006	0.304
S ₁₀	1.904	1.042	0.312
R ₆₀	2.010	0.880	0.227
R ₄₀	2.009	0.892	0.284
R ₂₀	1.942	0.914	0.297
R ₁₀	1.907	0.935	0.311
P ₆₀	2.012	0.861	0.296
P ₄₀	1.950	0.885	0.302
P ₂₀	1.892	0.926	0.313
P ₁₀	1.818	0.970	0.324

In Table 4, the relationships between the $K_{0\max}$ and $K_{0\min}$ and ρ_d for sand and pebbles are plotted, as shown in Figure 6, which shows that the $K_{0\max}$ and $K_{0\min}$ for sand and pebbles decrease linearly with an increasing density. The material parameters c and d of the sand and pebbles under this condition can be calculated by taking Equation (6) into account and then using Equation (7) to estimate the soil K_0 equation under vertical stress.

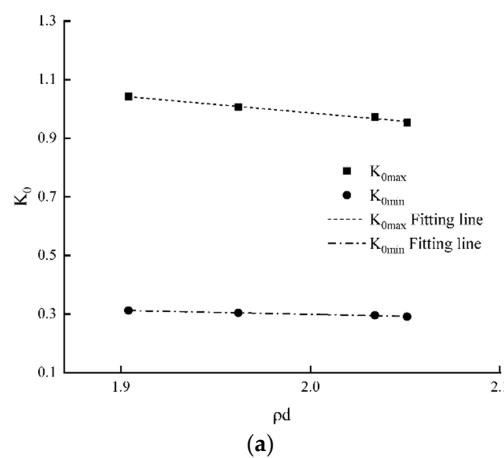


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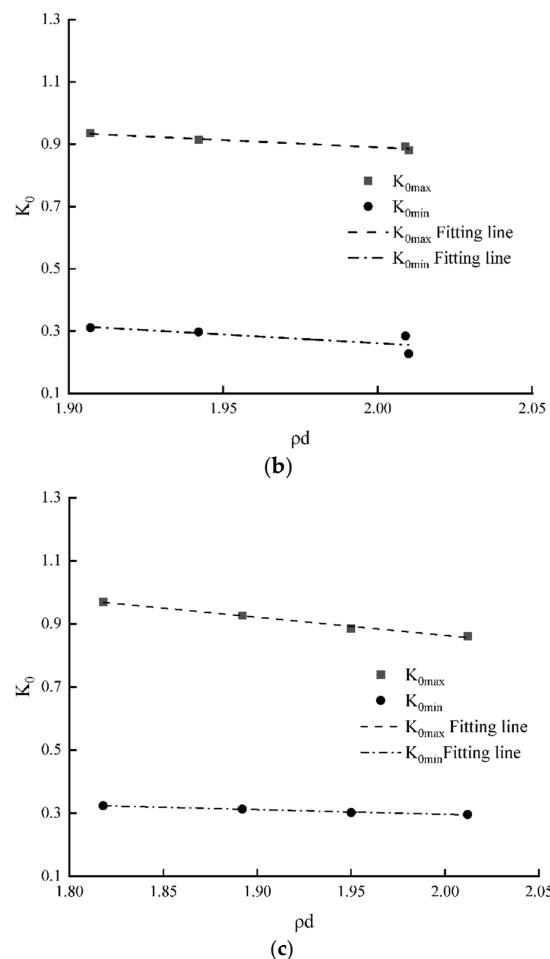


Figure 6. $K_{0\max}/K_{0\min}-\rho_d$ fitting curves of the specimens for different techniques: (a) scalping technique, (b) replacement technique, and (c) parallel gradation technique.

Using Equation (7) to fit the sand and gravel K_0 test results above, for which the fitting curve is in accordance with Figure 7, causes the K_0 -fitted value and the test to yield a very good match error, which is less than 5%; thus, the fitting effect is good. This result shows the reliability of the empirical formula and its applicability to different dry density coarse-grained soils. Therefore, the static lateral pressure coefficient test was carried out for different dry densities of sand and pebbles, for which the parameters presented in (7) were obtained, so that the relationship between the static lateral pressure coefficient and the initial dry density and vertical stress can be better described by Equation (7).

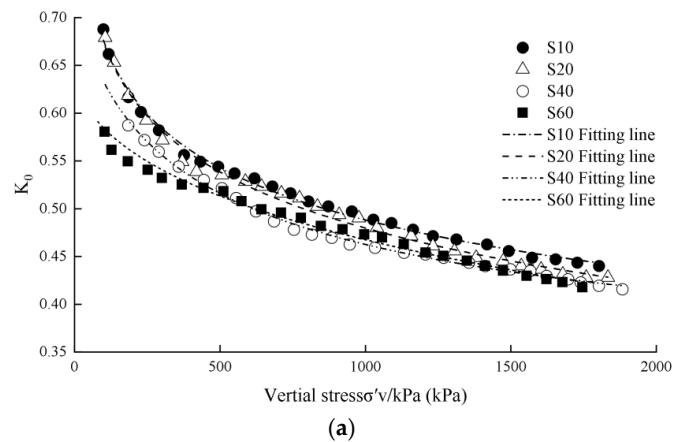


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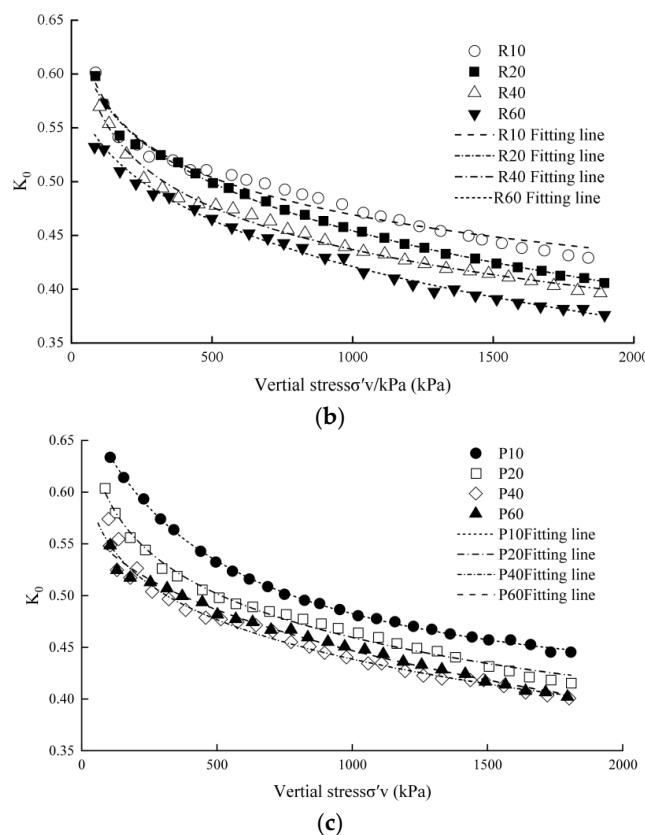
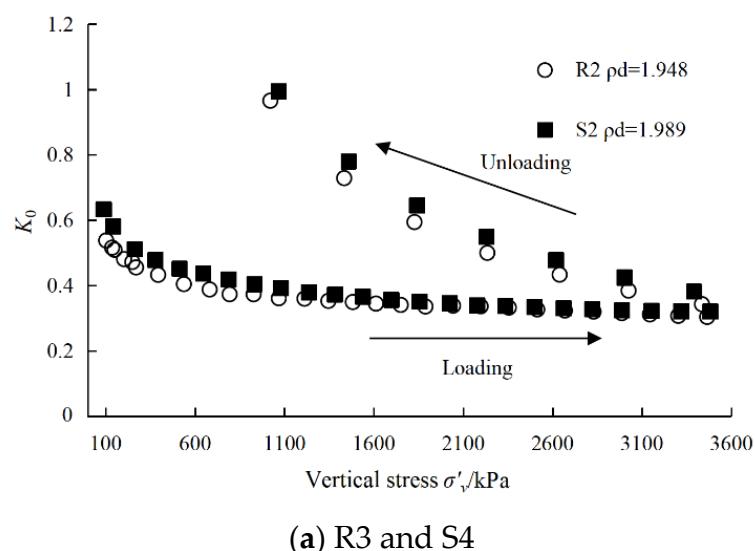


Figure 7. $K_0-\sigma'_v$ curves of the specimens for different techniques: (a) scalping technique, (b) replacement technique, and (c) parallel gradation technique.

5. Influence Mechanism of Vertical Stress on K_0

According to the research of Landva et al. [24] and Levenberg et al. [25], soil type has some influence on K_0 . Thus, to investigate the influence of soil type on the K_0 of coarse-grained soil, experimental data (R2 and S3 as well as R3 and S4 with similar initial dry density values) were plotted in Figure 8. In Figure 8, it is evident that the K_0 of sand gravel is larger than that of rockfill under the same σ'_v . Therefore, it is obvious that the coarse-grained soil type precipitates the difference in K_0 .



(a) R3 and S4

Figure 8. Cont.

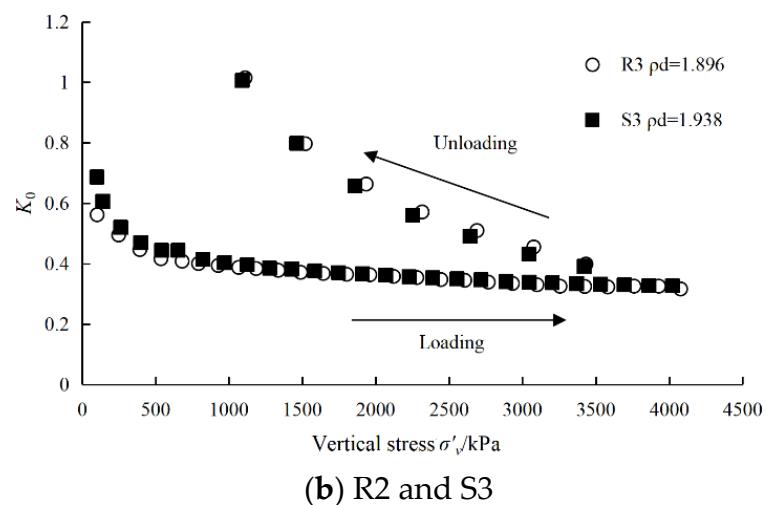


Figure 8. K_0 behavior of sandy gravel and rockfill under loading and unloading conditions.

To further study the effect of the coarse-grained soil type on K_0 , the average values of K_0 under different σ'_v values of R2, S3, R3, and S4 were listed in Table 5. According to Table 5, under the same conditions of initial relative density and gradation, the K_0 of sand gravel is over 10% larger than that of rockfill. Under the unloaded condition, the K_0 of sand gravel is over 14% larger than that of rockfill. From the above results, the soil type has a certain influence on the coarse-grained soil, and the K_0 of sand gravel is larger than that of rockfill under the same initial conditions. Moreover, the influence of soil type on coarse-grained soil needs to be further studied.

Table 5. The average value of K_0 during loading/unloading for test specimens.

	Sand and Gravel		Rockfill	
	S3	S4	R2	R3
Loading phase	0.397	0.427	0.367	0.372
Unloading phase	0.62	0.646	0.54	0.565

6. Conclusions

A series of K_0 tests for two types of soil (rockfill and sandy gravel) were conducted by a newly developed large-scale apparatus. The relationship between the K_0 , initial relative density (ρ_d), and vertical stress (σ'_v) of coarse-grained soil was studied, and an empirical formula was proposed based on the test results. The following results were obtained:

- (1) σ'_v has a significant influence on the K_0 of coarse-grained soil, while K_0 decreases as σ'_v increases, and this decreasing trend will be remarkably weakened under the influence of higher pressure. It was verified that the $K_0-\sigma'_v$ relationship proposed is applicable to compacted coarse-grained soil.
- (2) According to the test results concerning rockfill, the K_0 of the specimens tended to decrease with an increasing ρ_d . Furthermore, a formula for describing $K_0-\sigma'_v$ was obtained, which can describe the relationship between the K_0 , ρ_d , and σ'_v of coarse-grained soil. The reliability of the formula was verified by the test results regarding sand gravel. Finally, according to the published test results, further evidence has been obtained that this formula can accurately describe the relationship between K_0 , ρ_d , and σ'_v for any coarse-grained soil.
- (3) The type of coarse-grained soil in question has a certain influence on the K_0 of coarse-grained soil. The K_0 of sand gravel is larger than that of rockfill without other influencing factors.

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