

*Supplementary Materials*

# **Thin Electric Heating Membrane Constructed with a Three-Dimensional Nanofibrillated Cellulose—Graphene—Graphene Oxide System**

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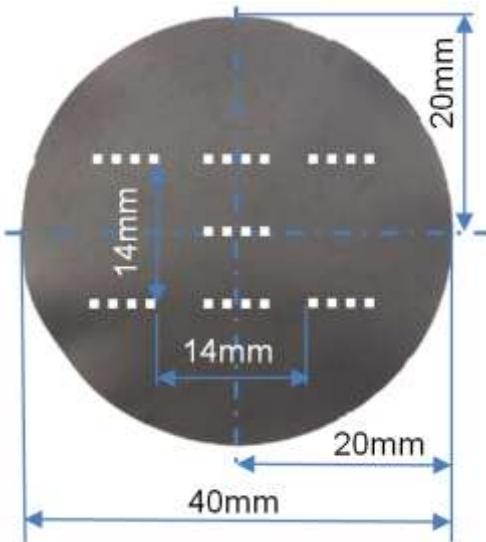
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Voltage ( $U$ ) applied on two electrodes under a given power density and resistance between the two electrodes on the electric heating membrane was calculated according to the equation (S1) and (S2).

$$U=(R^*P)^{1/2} \quad (S1)$$

$$P=p^*s \quad (S2)$$

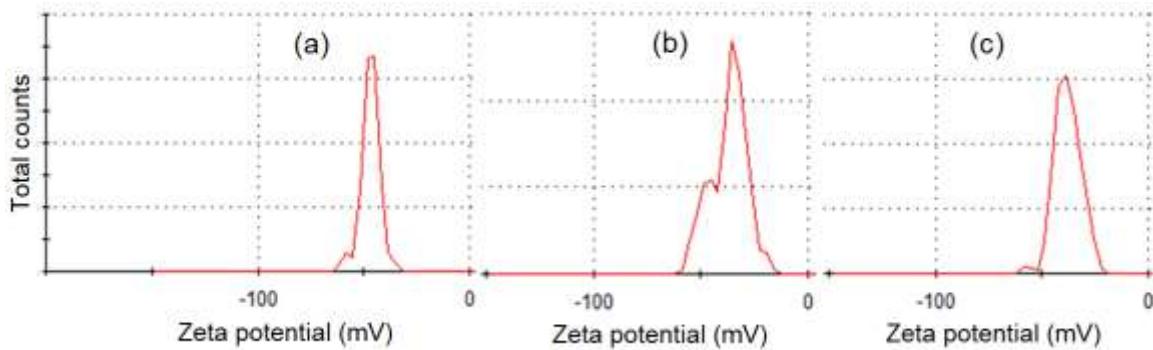
In which,  $U$ ,  $R$ ,  $P$ ,  $p$ ,  $s$  are voltage (V) applied on two electrodes of the membrane, resistance ( $\Omega$ ) between two electrodes, total power (W) applied on the electrodes, power density ( $\text{W}\cdot\text{m}^{-2}$ ), effective heating surface ( $\text{m}^2$ ,  $20\text{mm}\times30\text{mm}$ ), respectively.



**Figure S1.** Specific position for the test of sheet resistance on the membranes.

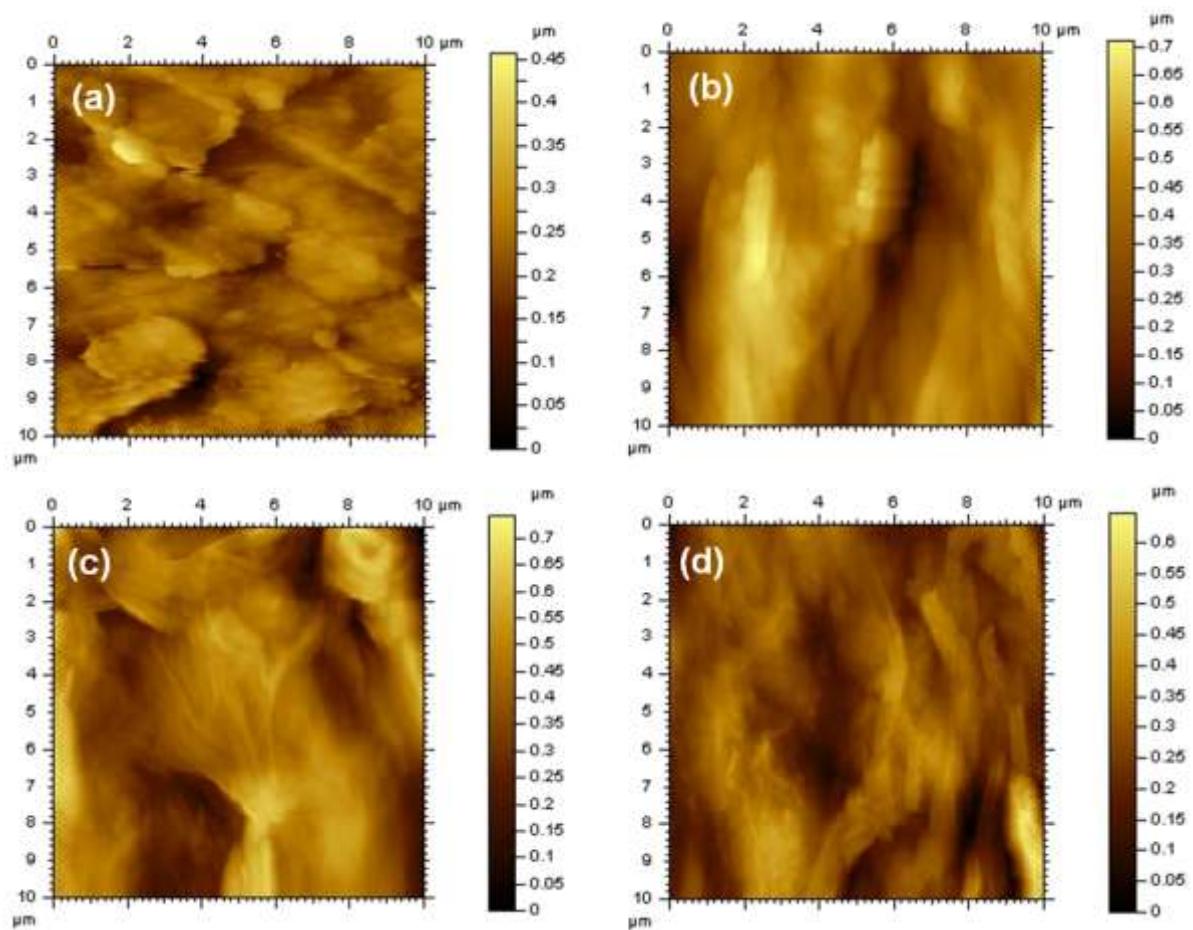


**Figure S2.** Installation of electrodes and temperature senor on the membrane. In which, heat and electrically resisting tape was used for the installation of temperature senor.

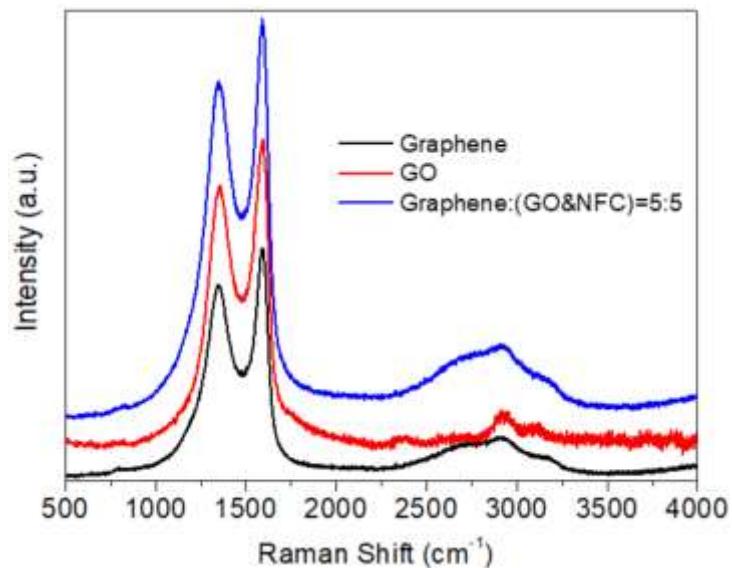


**Figure S3.** Zeta potential distribution of (a) NFC, (b) GO, and (c) NFC–GO

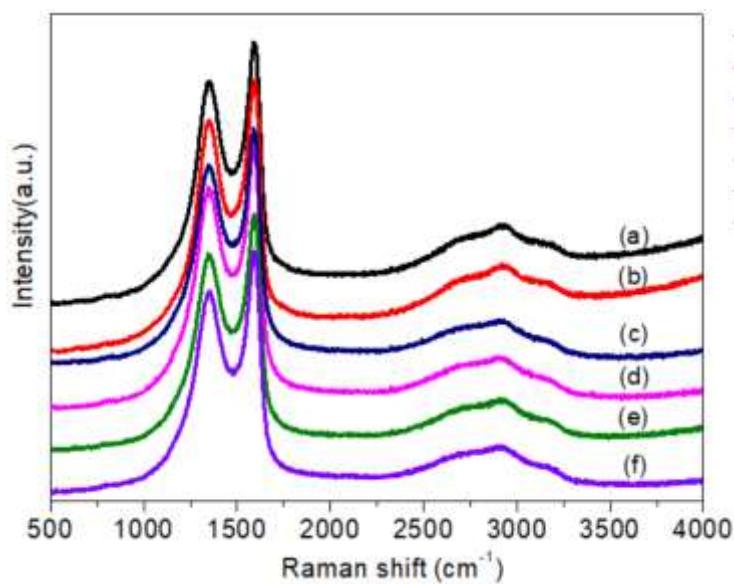
dispersions.



**Figure S4.** Two-dimension AFM analysis on  $16 \text{ g} \cdot \text{m}^{-2}$  membranes with (a) 30 or (b) 50 wt.% graphene, (c)  $8 \text{ g} \cdot \text{m}^{-2}$  membrane with 50 wt.% graphene, all GO:NFC = 1:1, and (d)  $16 \text{ g} \cdot \text{m}^{-2}$  membrane with 50 wt.% graphene, GO:NFC = 1:9.



**Figure S5.** Raman spectra of graphene, GO, and the membrane.

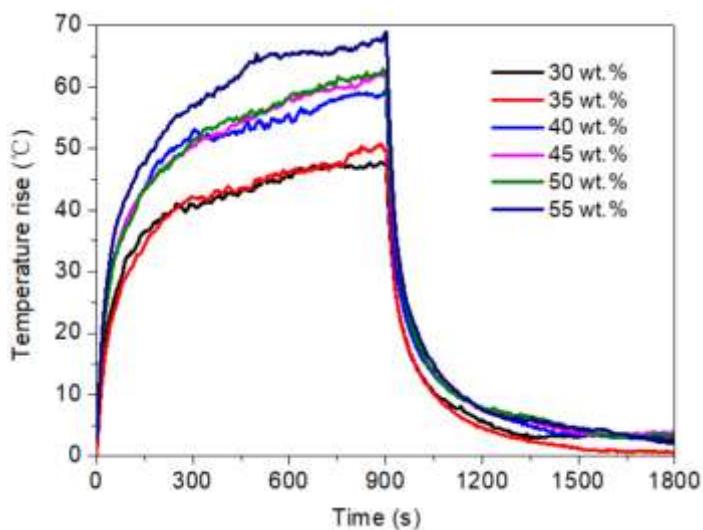


**Figure S6.** Raman spectra of membranes with GO:NFC = 1:1 and (a) 20, (b) 30, and (c) 50 wt.% graphene, and with 50 wt.% graphene and (d) 5, (e) 15, and (f) 30 wt.% GO.

**Table S1.** Electrical parameters in the heating test for the membrane with various amount of graphene with grammage of  $16 \text{ g}\cdot\text{m}^{-2}$  and the ratio between GO and NFC as 1:1 (under the power density of  $1500 \text{ W}\cdot\text{m}^{-2}$ ).

| Membrane with<br>different amount of<br>graphene | First heating test  |                    | Second heating test |                    |
|--|---------------------|--------------------|---------------------|--------------------|
|  | parameters          | parameters         | parameters          | parameters         |
|  | R <sub>1</sub> (KΩ) | U <sub>1</sub> (V) | R <sub>2</sub> (KΩ) | U <sub>2</sub> (V) |
| 30 wt.%  | 23.550              | 146                | 22.260              | 142                |
| 35 wt.%  | 14.610              | 115                | 12.995              | 108                |
| 40 wt.%  | 7.535               | 82                 | 6.685               | 78                 |
| 45 wt.%  | 5.580               | 71                 | 4.765               | 65                 |
| 50 wt.%  | 3.750               | 58                 | 3.274               | 54                 |
| 55 wt.%  | 2.326               | 46                 | 2.004               | 43                 |

R<sub>1</sub>: resistance between two electrodes of the membrane before the first electric heating test; R<sub>2</sub>: resistance between two electrodes of the membrane before the second electric heating test. U<sub>1</sub>: voltage applied in the first test; U<sub>2</sub>: voltage applied in the second test.

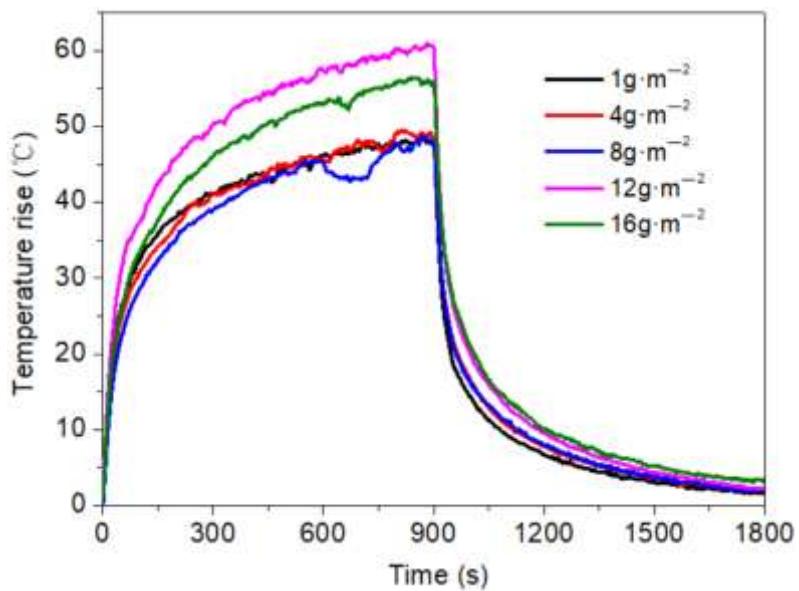


**Figure S7.** Temperature rise on the membrane with different amount of graphene in the first heating test under the power density of  $1500 \text{ W}\cdot\text{m}^{-2}$ .

**Table S2.** Electrical parameters in the heating test for the membrane with various grammages under the power density of  $1500 \text{ W} \cdot \text{m}^{-2}$ .

| Membrane with various<br>grammages ( $\text{g} \cdot \text{m}^{-2}$ ) | First heating test     |                  | Second heating test    |                  |
|---|------------------------|------------------|------------------------|------------------|
|   | parameters             |                  | parameters             |                  |
|   | $R_1 (\text{K}\Omega)$ | $U_1 (\text{V})$ | $R_2 (\text{K}\Omega)$ | $U_2 (\text{V})$ |
| 1   | 20.925                 | 137              | 20.000                 | 134              |
| 4   | 16.545                 | 122              | 15.360                 | 118              |
| 8   | 6.215                  | 75               | 5.920                  | 73               |
| 12  | 4.420                  | 63               | 3.729                  | 58               |
| 16  | 3.667                  | 57               | 3.181                  | 54               |

$R_1$ : resistance between two electrodes of the membrane before the first electric heating test;  $R_2$ : resistance between two electrodes of the membrane before the second electric heating test.  $U_1$ : voltage applied in the first test;  $U_2$ : voltage applied in the second test.



**Figure S8.** Temperature rise on the membrane with various grammages in the first heating test under the power density of  $1500 \text{ W}\cdot\text{m}^{-2}$ .

**Table S3.** Electrical parameters in the heating test of the membrane (grammage of 8 g·m<sup>-2</sup>) inputted with different power density.

| Power density (W·m <sup>-2</sup> ) | Heating test parameters |       |
|------------------------------------|-------------------------|-------|
|                                    | R (KΩ)                  | U (V) |
| 500                                | 6.400                   | 44    |
| 1000                               | 6.290                   | 61    |
| 1500                               | 5.920                   | 73    |
| 2000                               | 6.150                   | 86    |
| 2500                               | 5.765                   | 93    |

R: resistance between two electrodes of the membrane before the electric heating test; U: voltage applied in the test.