Supplementary Information

Dependence of Eu²⁺ Emission Energy on the Host Structure c/a Ratio

The Eu²⁺ emission wavelength offset was observed in the row of ternary sulfides with common chemical formulae ALnS₂:Eu (A = Na, K, Rb; Ln = La, Gd, Y, Lu). The wavelengths were converted to the emission energy and its dependence on c/a ratio for each the material (c, a are the dimensions of the unit cell) is shown in Figure S1.



Figure S1. Dependence of Eu²⁺ emission energy on the host structure *c/a* ratio for each material studied.

The Eu²⁺ emission energy is given by [S1]

$$E_{\rm em} = E_{\rm free} - D - \Delta S \tag{S1}$$

where E_{free} is the free ion energy, D and ΔS are the redshift and Stokes shift in chosen compound.

For Ce³⁺ the redshift would be [S2–S5]:

$$D^{Ce} = E_c^{Ce} + mE_{cfs}^{Ce} - 0.234 \text{ eV}$$
 (S2)

where E_c and E_{cfs} are the centroid shift and crystal field splitting of the 5d excited state, *m* is the constant, representing a contribution of the crystal field splitting to the redshift. Since the Ce³⁺ redshift, Stokes shift, centroid shift and crystal field splitting must be linearly related to those of Eu²⁺ [S1], Equation (S2) could be slightly modified by inserting some proportionality constant *b*. Taking this into account and expressing the centroid shift in the first approximation after [S2,S6,S7], the emission energy in Equation (S1) for Eu²⁺ in sixfold coordination of S²⁻ (*D*_{3d} point symmetry group) becomes:

$$E_{\rm em} = E_{\rm free} + 0.234b - \Delta S - \frac{e^2}{4\pi\varepsilon_0} \frac{\left(\left\langle r^2 \right\rangle_{\rm 5d} - \left\langle r^2 \right\rangle_{\rm 4f}\right)}{R^6} \sum_{i=1}^6 \alpha_i - mE_{\rm cfs}$$
(S3)

where *r* is the coordinate of an electron in either the 5d or 4f orbital, α_i is the polarizability of the *i*-th ligand at a distance *R* from the Eu²⁺ ions, *e* is the elementary charge, and ε_0 is the permittivity of vacuum.

The splitting of the excited state $4f^{6}5d^{1}(^{2}D)$ by the local crystal field is schematically shown in Figure S2.

The local symmetry of either M or Ln perturbed octahedra in the materials is D_{3d} (Figure S2a). Using the method of descending symmetry [S8], one can find the Eu²⁺ ion excited state splitting due to ligand field. Initially undistorted octahedron has the O_h local symmetry, which splits the nd¹ outer shell into T_{2g} (ground level, triply degenerated) and E_g (doubly degenerated) (see e.g., [S2]). When the local symmetry is reduced, additional splitting of the levels appears. The T_{2g} and E_g levels are decomposed, as it is shown in Figure S2b, into irreducible representations of the D_{3d} point group [S8]. The electric dipole transition 5d-4f occurs between the lowest level ($E_g(d_{xz}, d_{yz})$) of the excited state 4f⁶5d¹(²D) after removing degeneracy by the crystal field and the ground state 4f⁷(⁸S_{7/2}). Due to variation of the local crystal field strength depending on the lattice type, the quantity δ (the energy separation between the ²D state shifted by the centroid shift, and the $E_g(d_{xz}, d_{yz})$ additionally lowered by the Stokes shift) also changes accordingly. There might also be additional weak splitting of the lowest $E_g(d_{xz}, d_{yz})$ level caused by slight local distortions of the crystal field and/or influence of more distant ligands, having hexagonal symmetry (see Figure 1 in the main text). Using the crystal field theory (for details see e.g., [S9]), with some simplifications, the energy E_{cfs} of the lowest $E_g(d_{xz}, d_{yz})$ (Figure S2) could be the following:

$$E_{\rm cfs} = \left(\frac{A}{\left(1 + \left(\xi \frac{c}{a}\right)^2\right)^{3/2}} - \frac{B}{\left(1 + \left(\xi \frac{c}{a}\right)^2\right)^{5/2}}\right)$$
(S4)

where the M,Ln-S distance is $R = \left(\left(\frac{c}{12} \right)^2 + \frac{a^2}{3} \right)^{1/2}$, assuming for simplicity $c_{M,Ln} = \frac{(c_M + c_{Ln})}{2} = \frac{c}{6}$ (see Figure 1 in the main text), $\xi^2 = \frac{1}{48} \approx 0.0208$. *A* and *B* are the coefficients accounting for the Ln ion charge and expectation values of the *r* electron coordinates $\langle r^2 \rangle$ and $\langle r^4 \rangle$ in the Eu²⁺5d orbital, respectively.



Figure S2. (a) Local sulphur surrounding (six S²⁻ ions) of either mono or trivalent cation site (in the center), having the trigonal symmetry of bipyramidal antiprism (D_{3d} symmetry group). (b) Schematic energy level diagram (ground and first excited states) of the Eu²⁺ ion; the splitting of the excited level 4f⁶5d¹(²D) due to the local crystal field (a) is shown. Δ_0 is the energy separation between the ²D excited state after the centroid shift and ground state; δ accounts for the Stokes shift of the lowest $E_g(d_{xz}, d_{yz})$ level as well.

The emission energy (Equation (S3)) then transforms as:

$$E_{\rm em} = \Delta - \frac{A'}{\left(1 + \left(\xi \frac{c}{a}\right)^2\right)^{3/2}} + \frac{B'}{\left(1 + \left(\xi \frac{c}{a}\right)^2\right)^{5/2}}$$

$$A' = mA$$

$$B' = mB - C / \langle R \rangle$$

$$C = \frac{e^2}{4\pi\varepsilon_0} \left(\langle r^2 \rangle_{\rm 5d} - \langle r^2 \rangle_{\rm 4f}\right) \sum_{i=1}^6 \alpha_i$$
(S5)

here $\Delta = E_{\text{free}} + 0.234b - \langle \Delta S \rangle$, we assume the Stokes shift on average to be constant for the row of materials studied; $\langle R \rangle = \sum_{i=1}^{N} R_i / N$, N = 11 is the number of studied compounds (Figure S1).

Instead of four parameters Δ , *A*, *B* and *C* to vary, in the first approximation we thus obtain only three Δ , *A*' and *B*'. It does not much influence the precision of the fit, since the more the parameters vary in the linear combination, the less accurate are the values they get.

Fitting the curve calculated from Equation (S5) to the experimental dependence in Figure S1, the following parameters were obtained: $\Delta = 4.7 \pm 0.2 \text{ eV}$, $A' = -4.4 \pm 1$, $B' = -14.4 \pm 2$. Due to simplifications introduced by algebraic manipulations the uncertainties of determined A' and B' constants may be quite large. However, the important question about the Eu²⁺ emission wavelength shift has been semi-quantitatively solved.

Luminescence and EPR Experiment-Additional Data

As an example, four normalized decay curves of KLnS₂:Eu (Ln = Lu, Y, Gd, La; 0.05% Eu) are shown in Figure S3. Interestingly, their signal-to-background ratio improves in the KLuS₂:Eu-KYS₂:Eu-KGdS₂:Eu-KLaS₂:Eu series, which may be related to processes of the excited state ionization of the Eu²⁺ activator, at least in the KGdS₂, KLaS₂ hosts, see the main document.



Figure S3. RT Normalized decay curves related to the Eu²⁺ 5d-4f transition in KLnS₂:Eu (Ln = Lu, Y, Gd, La); Excitation and emission wavelengths taken from Table 3 in the main document; data of KLuS₂:Eu after [S10].

In order to obtain the spin-Hamiltonian parameters (see main body of the article) for the Eu²⁺ and Gd³⁺ ions (uncontrolled impurity) in the KLaS₂:Eu, the simulated in "Easyspin 4.5.5 toolbox" program [S11] curves were fitted to the angular variations of the corresponding resonance magnetic fields obtained by the $\mathbf{B} || \mathbf{c} \rightarrow \mathbf{B} \perp \mathbf{c}$ rotation of a sample (see Figures S4 and S5).



Figure S4. Angular dependence of the resonance lines produced by the Eu²⁺ ions measured in KLaS₂:Eu single crystal. Dots represent experimental data and solid lines are the fitting curves simulated in "Esyspin 4.5.5 toolbox" program [S11]. f is the microwave frequency.



Figure S5. Angular dependence of the resonance lines produced by the Gd³⁺ ions measured in KLaS₂:Eu single crystal. Dots represent experimental data and solid lines are the simulated fitting curves [S11].

The simulated curves show good agreement with experimental data. However, the broadening of the Eu²⁺ hyperfine lines and intermixing of spectral components originating from both the ions are, mostly, responsible for the local worsening of the fit. Besides, as the sample was of a platelet shape, one can expect some slight inhomogenity of its structure on the edges and surface of the sample (gradual tensions could exist). The rather indented edges do not allow precise determination of the direction in the rotational plane (0001), to take it as a reference point when measuring the angular variations in a perpendicular plane. The scarce deviation from axial symmetry in the (0001) plane (Figure S6) may cause unexpected shifts of the resonance lines as well.



Figure S6. EPR spectra measured in KLaS₂:Eu single crystal at the specific magnetic field orientations (assigned with the angle of rotation) in the (0001) rotational plane.

By analogy to the KLaS₂:Eu, the same procedure of finding spin-Hamiltonian parameters (Table 5 in the main document) is suitable for KYS₂:Eu. Angular dependences of the Eu²⁺ and Gd³⁺ ions are presented in Figures S7 and S8. The general discrepancy between the materials is that in KYS₂ the EPR lines from four Eu²⁺ centers could be resloved in spectra and only three of them could be treated separately in the angular dependence. In contrast to the KYS₂, in the previous work [S12] we reported the presence of three Eu²⁺ centers created by the substitution of the Eu²⁺ ions for both K and Lu regular lattice cations and the perturbed one.



Figure S7. Angular dependencies of the resonance lines produced by the Eu²⁺ centers measured in KYS₂:Eu single crystal. Dots represent experimental data and solid lines are the simulated fitting curves [S11].



Figure S8. Angular dependence of the resonance lines produced by the Gd³⁺ ions measured in KYS₂:Eu single crystal. Dots represent experimental data and solid lines are the simulated fitting curves [S11].

Although the fit is not perfect (see Figures S7 and S8), the slight disagreement between the fitting curves and experimental data most probably is due to the same reasons as in the case of KLaS₂:Eu (see above). The angular dependence in the (0001) plane is in Figure S9. It shows almost axial symmetry similarly to the KLaS₂.



Figure S9. EPR spectra measured in KYS₂:Eu single crystal at the chosen magnetic field directions (spectra assigned with the angle of rotation) in the (0001) rotational plane.

Below 160 K, the light emission from the Eu³⁺ ions occurred in all the sulfides studied except the KLaS₂ (see main text of the article). Since they are not paramagnetic, the direct EPR observation is impossible. However, to clarify if some charge transformation (Eu²⁺ \rightarrow Eu³⁺) when lowering the sample temperature indeed took place is possible. With this aim the temperature dependencies of the Eu²⁺ EPR spectra in the KYS₂ (Figure S10, for better visualization, the Gd³⁺ resonances were mostly extracted from the spectra) and KLuS₂ (Figure S11) were performed. It is noteworthy that the spectra do not demonstrate signal intensity fading with decreasing temperature. Obversely, the signal-to-noise ratio increases due to elongation of the spin-relaxation time till saturation (approximately at 20 and 50 K for the KYS₂ and KLuS₂, respectively). No changes to the intensity distribution between spectral components originating from different Eu²⁺ centers in both the materials was observed as well. This indicates that the Eu²⁺ \rightarrow Eu³⁺ charge transformation does not exist, but the Eu³⁺ ions are initially presented in the materials.



Figure S10. EPR spectra measured in KYS₂:Eu single crystal at the chosen temperatures, distinguished by color accordingly. Blue and red vertical line segments are associated with two clearly visible fine transitions, originating from the two Eu²⁺ centers.



Figure S11. EPR spectra measured in KLuS₂:Eu single crystal at the chosen temperatures, distinguished by color accordingly. Blue and red vertical line segments are associated with two clearly visible fine transitions, originating from the two Eu²⁺ centers.

Figure S12 gives EPR and luminescence results together showing that emission intensity released by Eu^{2+} occupying both K⁺ and Lu^{3+} sites in KLuS₂ is temperature independent.



Figure S12. Temperature dependence of the products of amplitudes and band widths of Gaussians components for emission spectra of Eu²⁺-doped KLuS₂ (see the main document for details).

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