

## Article

# Cost Minimizations and Performance Enhancements of Power Systems Using Spherical Prune Differential Evolution Algorithm Including Modal Analysis

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**Abstract:** A novel application of the spherical prune differential evolution algorithm (SpDEA) to solve optimal power flow (OPF) problems in electric power systems is presented. The SpDEA has several merits, such as its high convergence speed, low number of parameters to be designed, and low computational procedures. Four objectives, complete with their relevant operating constraints, are adopted to be optimized simultaneously. Various case studies of multiple objective scenarios are demonstrated under MATLAB environment. Static voltage stability index of lowest/weak bus using modal analysis is incorporated. The results generated by the SpDEA are investigated and compared to standard multi-objective differential evolution (MODE) to prove their viability. The best answer is chosen carefully among trade-off Pareto points by using the technique of fuzzy Pareto solution. Two power system networks such as IEEE 30-bus and 118-bus systems as large-scale optimization problems with 129 design control variables are utilized to point out the effectiveness of the SpDEA. The realized results among many independent runs indicate the robustness of the SpDEA-based approach on OPF methodology in optimizing the defined objectives simultaneously.

**Keywords:** optimal power flow; multi-objective optimization methodologies; pareto-set; stability; voltage analysis



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## 1. Introduction

Till this moment, power networks remain one of the most complicated systems in industry due to many reasons, such as variation of generation and load demand, the inclusion of renewable energy systems, and storage devices. These power systems are entirely nonlinear systems, where many components including synchronous generators, transformers, transmission lines, and induction motors have a deep nonlinearity. The optimal operation of such components to achieve a concise economic target, emission minimization possibility, power loss reduction and other objectives under the power system constraints plays an important role in the power system operation and is named optimal power flow (OPF) [1–5]. This problem, as mentioned earlier, is consequently considered a significant nonlinear optimization problem. In this issue, some fitness functions can be sequentially solved under the system operating conditions, including fuel consumption cost (FC), pollution release rate, active power loss, reactive power loss, bus voltage declines and many more.

Previously, several classical mathematical optimization approaches have been employed to solve the OPF problem [6–10]. Among the said traditional methods are: (i) moment-based relaxations [6], (ii) linear and quadratic programming [7], (iii) decomposition of the network graph into a spanning tree and closed cycles [8], (iv) safety barrier interior-point approach [9], and (v) a semi-definite method [10]. Nevertheless, these traditional approaches have many disadvantages, including their dependency on the values of the problem initial conditions, solver type, and accuracy. It shall be stuck into a local solution under the OPF problem's nonlinearity. For that reason, different heuristics-based optimization techniques have been developed for solving such problems. Principally, similar heuristic techniques are randomly initialed populations of their agents, and the suboptimal/optimal answer is based on their methodologies. Several optimization methods have been used to tackle the OPF problem whether the target is single or multiple objective functions, such as genetic procedures [11], particle swarm optimizer [12], imperialist competitive algorithm [13], chaotic invasive weed optimization algorithms [14], JAYA algorithm [15], shuffled-frog-leaping algorithm [16], social spider optimization algorithm [17], chaotic salp swarm optimizer [18], new adaptive partitioning flower pollination algorithm [19], and others [20–38].

Among these kinds of literature, as mentioned earlier, the reader can notice that an avalanche of articles is presented to solve OPF problems using differential evolution (DE) with various versions [23,34–38], in which the authors concluded the powerful features and advantages of DE in solving OPF problems. Few of these works are employed to solve simultaneous multiple conflicting objectives such as OPF problems. Principally, these reported studies indicate the great development of metaheuristic algorithms. Therefore, a novel spherical prune DE algorithm (SpDEA) is implemented to solve the multiple objective OPF problems in this study.

It is well-known that DE is considered a much-enhanced version of the genetic algorithm originally established by Storn and Price [39]. DE procedures have many variants for mutation schemes, such as DE/X/Y/Z, DE/best/2, DE/rand/1/bin, and so on; each variant has its own advantage, and its performance relies on the nature of the problem to be optimized [40,41]. DE has many key advantageous items e.g., (i) it's simple to apply with a very effective mutation process, (ii) DE has a comparatively smooth convergence at high speeds of processing, (iii) a smaller size of the population generally suffices for solving large-scale engineering problems, and (iv) accordingly, it can be confirmed that there are significant reductions in computation burdens placed on the computer processors. The SpDEA has the flexibility to select the best compromise Pareto within the search space, and this leads to obtaining the optimal point in a quick manner, representing good merit.

The problem defines the optimal settings of design variables of the network through optimizing various identified objectives under system operating and capacity constraints. The control variables involve the active power output, the generating units' voltage, tap-changer adjustments, and reactive compensating apparatuses. The control variables are continuous except for the transformer tap settings, which are discrete, and its step is chosen  $\pm 1.25\%$ . Many objective functions may be involved through the OPF formulation, such as FC of generating units, pollution rate released by these units, network real power loss, voltage deviation, etc.

In this article, a novel SpDEA is presented to solve different multiple objective OPF problems. The vector objective functions include the FC, network overall real power losses, voltage deviation index, and stability of power networks. Voltage stability analysis has attracted much interest. It relies on a modal analysis, which is represented as a fitness function. In this issue, the Jacobian matrix is reduced, and then eigenvalues and eigenvectors are determined. The amplitude of eigenvalues measures the system instability. When this amplitude increases, the incremental voltage decreases, indicating the system's strong voltage stability. The output (active power) of the units, their voltages, tap settings of power transformers, and compensating devices represent the design control variables of the problem. The SpDEA is employed to solve the OPF problem for two medium-size

systems: a 30-bus network and a large-scale system, for instance, 118-bus network under multiple objective functions. The value of the SpDEA is compared to that obtained by using other optimization techniques. The numerical results are performed on MATLAB software. The results achieved demonstrate a competition of the SpDEA with other competing methods to solve multi-objective OPF problems.

The paper is sectionalized and arranged as follows: Section 2 introduces OPF problem representations with the proposed objectives and their associated constraints. In Section 3, the SpDEA mathematical model and its general procedures are presented. Section 4 gives the simulation scenarios, numerical results, and discussions. In Section 5, final concluding remarks along with future trends are drawn.

## 2. OPF Mathematical Representations

In this study, the optimization problem is expressed with four objectives for simultaneous optimization. The adopted objectives are depicted in (1)–(4):

$$TFC = \sum_{i=1}^{N_g} a_i P_{Gi}^2 + b_i P_{Gi} + c_i \quad (1)$$

$$TPL = TGP - TPD \quad (2)$$

$$TVD_{PQ} = \sum_{i=1}^{N_{PQ}} \left| |V_i| - |V_{ref}| \right| \quad (3)$$

$$\lambda_i = \frac{\Delta Q_{mi}}{\Delta V_{mi}} \quad (4)$$

where  $TFC$  is the total FC of the generating units,  $P_{Gi}$  is the active output generating power at  $i$ th bus,  $a_i$ ,  $b_i$ ,  $c_i$  are FC coefficients of  $i$ th generating unit,  $N_g$  defines the number of generators,  $TPL$  is the system total active power loss,  $TGP$  is the total generated power,  $TPD$  is total power demand,  $TVD_{PQ}$  is the total voltage deviation of all PQ buses,  $|V_{ref}|$  is the reference voltage magnitude (typically,  $|V_{ref}|$  has a value of 1 per unit (pu)),  $N_{PQ}$  defines the number of PQ buses,  $\lambda_i$  specifies the magnitude of eigen value, and  $\Delta Q_{mi}$  and  $\Delta V_{mi}$  define the  $i$ th modal reactive power and voltage changes, respectively.

It is worth mentioning that the stability of the mode  $i$  is based on  $\lambda_i$ . The largest  $\lambda_i$  indicates slight variations of the modal voltage due to reactive power change. Therefore, the least value of  $\lambda_i$  is chosen as a fourth objective, which requires upgrading for a better power system voltage stability. A further derivation regarding eigenvalues and eigenvectors for the modal analysis can be found in [42].

The aforementioned optimization problem undergoes to set of equality/inequality limitations such as:

$$\left. \begin{aligned} P_{Gi} - P_{Di} &= |V_i| \sum_{j=1}^N |V_j| (G_{ij} \cos \delta_{ij} + B_{ij} \sin \delta_{ij}) \\ Q_{Gi} - Q_{Di} &= |V_i| \sum_{j=1}^N |V_j| (G_{ij} \sin \delta_{ij} - B_{ij} \cos \delta_{ij}) \end{aligned} \right\}, \quad \forall i \in N \quad (5)$$

$$\left. \begin{aligned} P_{Gi}^{min} &\leq P_{Gi} \leq P_{Gi}^{max} \\ Q_{Gi}^{min} &\leq Q_{Gi} \leq Q_{Gi}^{max} \end{aligned} \right\}, \quad \forall i \in N_g \quad (6)$$

$$|V_i^{min}| \leq |V_i| \leq |V_i^{max}|, \quad \forall i \in N \quad (7)$$

$$t_k^{min} \leq t_k \leq t_k^{max}, \quad \forall k \in N_t \quad (8)$$

$$S_{li} \leq S_{li}^{rated}, \quad \forall i \in n_{br} \quad (9)$$

$$Q_{ci}^{min} \leq Q_{ci} \leq Q_{ci}^{max}, \quad \forall i \in N_c \quad (10)$$

where  $P_{Di}$  is the active demand power at bus  $i$ ;  $G_{ij}$  and  $B_{ij}$  are the conductance and susceptance between bus  $i$  and  $j$ , respectively;  $\delta_{ij}$  is the power angle between bus  $i$  and  $j$ ;  $Q_{Gi}$  is the reactive power generation at bus  $i$ ;  $Q_{Di}$  is the load reactive demand power at bus  $i$ ;  $P_{Gi}^{min}, P_{Gi}^{max}$  are the lower and higher limits of  $P_{Gi}$ , respectively;  $Q_{Gi}^{min}, Q_{Gi}^{max}$  are the min/max limits of  $Q_{Gi}$ , respectively;  $|V_i^{min}|, |V_i^{max}|$  are the min/max limits of  $|V_i|$ , respectively;  $t_k^{min}, t_k^{max}$  are the min/max limits of tap settings of the  $k$ th transformer, respectively;  $N_t$  defines the number of power transformers;  $S_{li}$  is apparent power flow in  $i$ th line;  $S_{li}^{rated}$  specifies the rated line maximum transfer capacity;  $nbr$  defines the number of network branches;  $Q_{ci}^{min}, Q_{ci}^{max}$  are the min/max limits of  $Q_{ci}$ , respectively; and  $N_c$  defines the number of nominated buses for capacitive devices.

In this study, the vector-defined objectives are solved using the SpDEA and are based on the fuzzification of Pareto fuzzy optimal (PFO) solutions. In this issue, the objective function  $OF_i$  is expressed by a fuzzy membership function  $\mu_i$  to normalize the values between 0 and 1 as expressed in (11) [23]:

$$\mu_i = \frac{OF_i - OF_i^{min}}{OF_i^{max} - OF_i^{min}} \tag{11}$$

In addition, for each  $k$ -th Pareto solution, the normalized membership  $\mu^k$  is estimated by the formula depicted in (12):

$$\mu^k = \frac{\sum_{i=1}^{Noj} \mu_i^k}{\sum_{k=1}^M \sum_{i=1}^{Noj} \mu_i^k}, \quad \forall k \in M \tag{12}$$

where  $Noj$  and  $M$  define the number of objectives and the number of PFO solutions, respectively. The best compromise solution is chosen for the minimum value of  $\mu^k$ .

### 3. Mathematical Model of SpDEA

The main three strategies for the DE procedure include mutation, crossover, and selection stage. Similar to other challenging optimization methods, at initial stage, a vector of random positions  $(x_{j,i}^{(0)})$  for the population is created within the predefined boundaries, which can be expressed in (13):

$$x_{j,i}^{(0)} = x_{j, min} + r(\dots) \cdot (x_{j, max} - x_{j, min}), \forall i \in PS, \quad \forall j \in dim \tag{13}$$

where  $dim$  defines the number of decision variables,  $PS$  is the population-size,  $r(\dots)$  is a uniform random distribution function  $\in [0, 1]$ , and  $x_{j, min}$  and  $x_{j, max}$  are min/max limits of the  $j$ th decision control variable, respectively.

At this moment, the DE starts to mutate and to recombine the population to generate trial vectors  $x'_i$ . Then, DE implements a uniform crossover procedure to produce trial vectors  $x''_i$ . This is made by mixing  $x'_i$  and the target vector  $x_i$  based on the crossover probability  $CR \in [0, 1]$ , which is combined in a single formula as depicted in (14):

$$x''_{j,i}^{(g)} = \begin{cases} x_a^{(g)} + \alpha \cdot (x_b^{(g)} - x_c^{(g)}), & \forall i \in PS \text{ if } r_j(\dots) \leq CR \\ x_{j,i}^{(g)} & \text{else} \end{cases} \tag{14}$$

where  $g$  is the iteration counter,  $x_a$  is a base-vector and  $x_b$  and  $x_c$  are the difference trial vectors that are picked up randomly, factors of  $a, b, c$ , and  $i$  are unequal and  $\alpha$  defines the scaling factor  $\in [0, 1]$ .

Then, a move is made to the new position, and as a final point, the collection occurs where a tournament is seized between the target and trial vectors, and the one with the best fitness value is endorsed to pass to the next generation. Through this, agents of a new generation are better than that of the previous ones.

The controlling parameters of the DE required for appropriate adaption by the users include  $\alpha$  and  $CR$ , along with those used with all other competing methods, such as the maximum iterations and PS. In common practice, the tuning of the DE-controlling factors is carried out by trial and error procedures to achieve a satisfactory performance of the DE algorithm.

This work cares by solving multiple objective optimization problems, such as the defined four objectives of OPF as stated in (1)–(4). SpDEA is applied to deal with such anticipated simultaneous objectives. Spherical pruning has been proposed by Reynoso-Meza [43,44] to improve diversity in the approximated PFO. Spherical coordinates are employed to partition the search space, and a selection of one solution is chosen in each spherical sector, evading congestion regions. SpDEA comprises actions to expand relevance applicability and to look effectively for a PFO approximation within the pertinency boundaries [45,46].

The principle motivation of the Sp is to investigate the offered solutions in the current PFO approximation using normalized spherical coordinates from a reference solution in the spherical sector. The general procedures of SpDEA are depicted in the flowchart shown in Figure 1. On the other hand, the detailed procedures of Sp mechanism are shown in Figure 2.

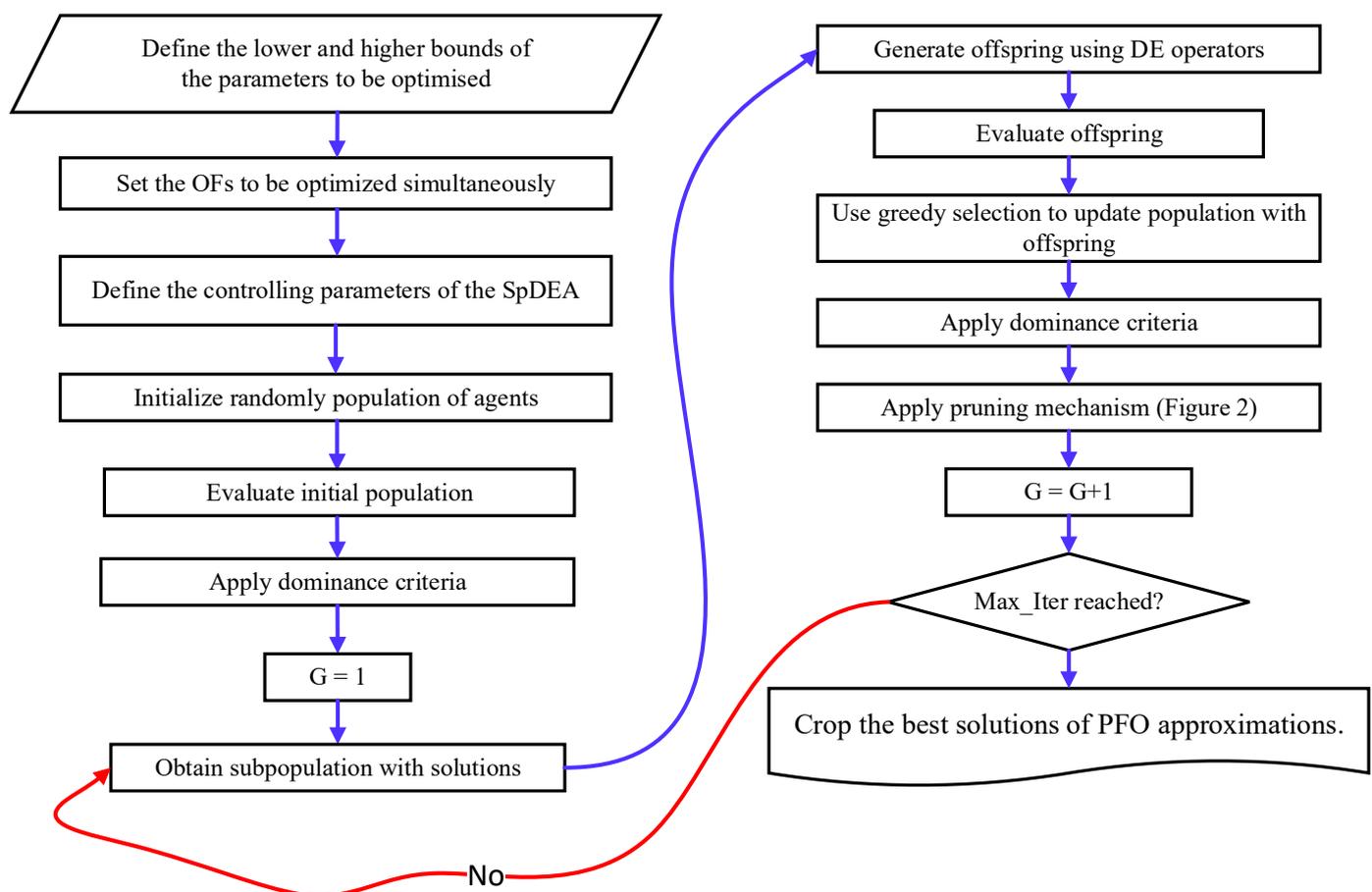


Figure 1. General procedures of SpDEA.

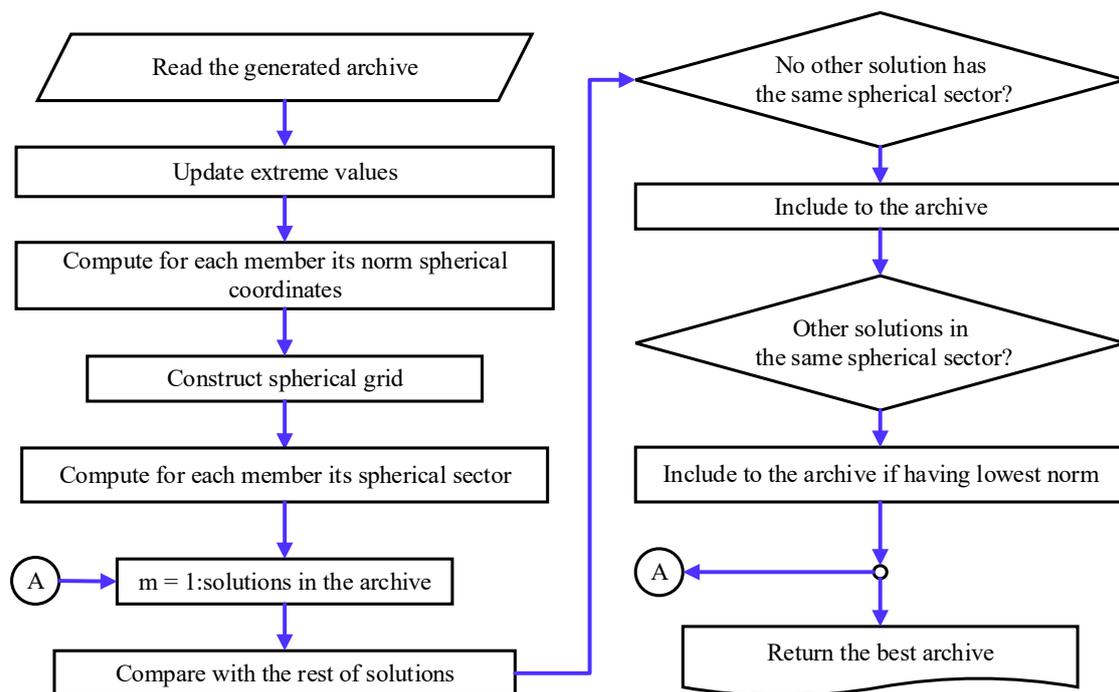


Figure 2. Procedures of Sp mechanism.

Further detailed explanation concerning the Sp definitions such as normalized spherical coordinates, sight range, spherical grid and sector, and so on, along with mathematical representations, can be obtained from [43,46]. The overall controlling parameters of SpDEA are  $\alpha$ , CR, PS, and the number of arcs that should be tuned sufficiently for better performance. Fuzzy-based decision-making methodology [23] is used to choose the best compromise among trade-off PFO points for various scenarios.

#### 4. Numerical Simulations, Scenarios, and Discussions

This current study focuses on solving the OPF problem in power systems from the multi-objective function perspective using the proposed SpDEA. The problem codes are built with MATLAB software [47]. The OPF problem is solved by different IEEE standard systems such as 30 and 118-bus systems. The main features of these two systems are depicted in Table 1, extracted from [1,15,23].

Table 1. Main features of the systems under study.

Parameter	30-Bus	118-Bus
Generators	6	54
Load bus	21	99
Branches	41	186
Tap settings transformers	4	9
Capacitive shunt compensators	9	12
Total Connected loads, MVA	283.4 + j126.2	4242 + j1438
Number of control variables	25	129

The aforementioned four objective functions are combined to form different multi-objective functions through the OPF problem. The summary of various vector objectives of the OPF problem is demonstrated in Table 2. The computer simulations are performed using a PC (Intel(R) Core(TM) i7 2.4 GHz  $\mu$ P, 16 GB RAM, and Windows 10 system). The controlling parameters that adjust the performance of the SpDEA are specified in Table 3.

**Table 2.** Scenarios of multiple objective representation of the OPF problem.

Formulation	Case #	TFC	TPL	TVD <sub>PQ</sub>	1/λ <sub>i</sub>
Two objectives	1	✓	✓	✗	✗
	2	✓	✗	✓	✗
	3	✓	✗	✗	✓
Three objectives	4	✓	✓	✓	✗
	5	✓	✓	✗	✓
	6	✓	✗	✓	✓
Four objectives	7	✓	✓	✓	✓

**Table 3.** Optimal characteristics of the proposed SpDEA for various systems under study.

Controlling Parameter	Best Settings	
	30-Bus	118-Bus
PS	50	50
α	0.5	0.7
CR	0.9	0.9
Number of arcs	10 <sup>Noj</sup>	10 <sup>Noj</sup>
Maximum Pareto solutions	1500	5000
No. of iterations	1000	5000

It is well-meaning to state that the power/load flow of the two systems under study is carried out using the full Newton–Raphson method implemented under MATPOWER [48]. It may be useful to state here some penalties added to the objective function (s) to produce a feasible solution. Among these penalties, the magnitude of bus voltages, power line flow, and reactive power of generating units are proposed. The typical MATLAB code to fulfill the condition of bus voltage and line flow limits is shown in Figure 3. The limitations of generating units' reactive power are controlled through N-R LF, as illustrated in the next subsections. The studied cases of the OPF problem for these IEEE standard power systems are demonstrated in the following subsections comprising necessary validations, comparisons, and discussions. It might be worth mentioning that all runs are performed on a Laptop with Intel® Core™ i7-7700HQ CPU with 16 GB installed memory.

```

% Penalize for line flows
line_rated_flows = mpc.branch(:, RATE_A);
Penalty_line_flows = max(0, (Line_Flow-line_rated_flows));
Penalty_line_flows = sum(max(0, (Line_Flow-line_rated_flows)));
% Penalize for bus voltage
Vm = results.bus(:, VM); Vmax = mpc.bus(:, VMAX);
Vmin = mpc.bus(:, VMIN);
Penalty_bus_voltages = sum(max(0, Vm-Vmax)) + ...
sum(max(0, Vmin-Vm));
%Total Penalties
Penalties = 1e6*Penalty_line_flows + 1e5*Penalty_bus_voltages;

```

**Figure 3.** Check line flows and bus voltage limits.

#### 4.1. IEEE 30-Bus System

In this system, nine buses are nominated for capacitive shunt compensators at bus numbers of {10, 12, 15, 17, 20, 21, 23, 24, and 29} [15,23]. The network data are demonstrated in detail in [1,48]. The voltage magnitude of buses changes in the range 90–110%, the transformer taps settings lie in the range 90%–110% with a step of ±1.25%, and the reactive power of the shunt compensator is 5 MVar. The SpDEA solves the different multiple objectives that are formulated in Table 2. The optimal characteristics of the SpDEA are

revealed in Table 3. Many independent runs have been carried out to determine the optimal values of control variables. The optimal values of control variables and their corresponding fitness values are pointed out in Table 4.

**Table 4.** Optimal design settings for various multiple objectives using the SpDEA.

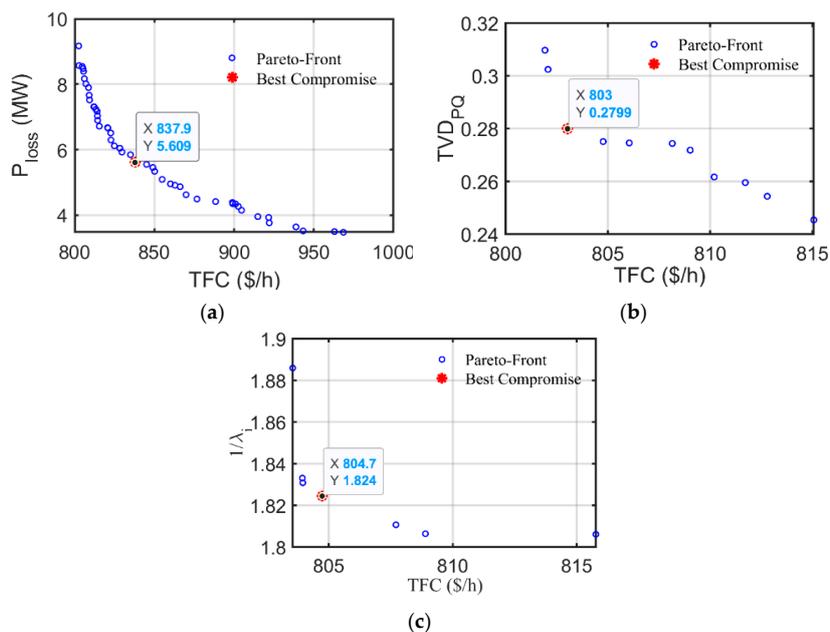
Control Variable	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6	Case 7
P <sub>G1</sub> (MW)	113.1667	177.6982	166.9543	108.0535	118.6186	166.5374	133.9738
P <sub>G2</sub> (MW)	64.0182	41.8139	51.7267	64.7741	57.7370	47.3021	34.8274
P <sub>G5</sub> (MW)	31.3178	22.9850	24.3110	34.0394	38.7262	26.7118	37.8803
P <sub>G8</sub> (MW)	32.9767	21.8647	25.7964	34.6170	35.0000	10.0000	33.6451
P <sub>G11</sub> (MW)	22.3965	15.6356	11.7609	20.4313	26.8753	11.5664	27.0341
P <sub>G13</sub> (MW)	25.1334	12.4976	12.0000	26.9377	12.0000	30.3921	21.9287
V <sub>G1</sub> (pu)	1.1000	1.0566	0.9810	0.9434	1.0317	1.0474	1.0249
V <sub>G2</sub> (pu)	1.0444	0.9258	0.9875	1.0753	1.0577	0.9959	0.9991
V <sub>G5</sub> (pu)	1.0249	0.9957	0.9246	0.9395	1.0307	0.9808	0.9570
V <sub>G8</sub> (pu)	1.0062	0.9361	0.9098	0.9000	1.0432	0.9560	0.9915
V <sub>G11</sub> (pu)	0.9223	1.0808	1.0308	1.0922	1.0185	1.0441	0.9951
V <sub>G13</sub> (pu)	1.0238	1.0617	1.0963	0.9601	1.0344	0.9483	0.9026
T <sub>6-9</sub>	90.00%	101.25%	110.00%	110.00%	97.50%	103.75%	97.50%
T <sub>6-10</sub>	105.00%	101.25%	101.25%	96.25%	92.50%	103.75%	107.50%
T <sub>4-12</sub>	98.75%	105.00%	102.50%	110.00%	90.00%	108.75%	105.00%
T <sub>27-28</sub>	93.75%	96.25%	110.00%	96.25%	90.00%	90.00%	102.50%
Q <sub>C10</sub> (MVar)	0.0000	3.3390	1.8112	1.7133	1.2975	0.0000	1.6315
Q <sub>C12</sub> (MVar)	2.6816	1.8507	3.3804	0.6132	4.0053	5.0000	2.9783
Q <sub>C15</sub> (MVar)	2.5428	4.2656	1.7458	4.6312	2.8315	2.7412	1.4480
Q <sub>C17</sub> (MVar)	2.1897	4.6759	2.0146	1.7066	1.5406	5.0000	3.5829
Q <sub>C20</sub> (MVar)	5.0000	0.0000	0.0000	5.0000	2.3553	0.7706	0.0000
Q <sub>C21</sub> (MVar)	1.6192	0.0000	3.9538	3.7275	2.6113	0.0000	4.2438
Q <sub>C23</sub> (MVar)	5.0000	0.5253	2.8481	2.1642	0.8609	0.1956	3.9938
Q <sub>C24</sub> (MVar)	1.5333	3.5208	0.0000	4.3222	5.0000	2.1634	1.4571
Q <sub>C29</sub> (MVar)	2.8376	0.7658	2.9261	0.9703	5.0000	4.6769	0.8602
TFC (\$/h)	<b>837.8510</b>	<b>803.0290</b>	<b>804.7330</b>	<b>846.2620</b>	<b>844.0380</b>	<b>815.9640</b>	<b>840.9170</b>
TPL (MW)	<b>5.6093</b>	9.0949	9.1493	<b>5.4530</b>	<b>5.5572</b>	9.1098	<b>5.8894</b>
TVD <sub>PQ</sub> (pu)	0.8106	<b>0.2799</b>	0.7761	<b>0.2498</b>	1.3021	<b>0.4916</b>	<b>0.4575</b>
1/λ <sub>i</sub>	2.0447	1.9569	<b>1.8245</b>	1.9681	<b>2.1704</b>	<b>2.1167</b>	<b>1.8790</b>
Elapsed time (s)	59.0	58.0	57.0	58.4	58.1	58.6	55.50

It may be noted that in the N-R LF using MATPOWER, the option of “pf.enforce\_q\_lims” is set to 1. As a result of activating this option, any generator’s reactive power exceeds the min/max limits after running the N-R LF, and the corresponding bus is converted to a PQ-bus, with Q<sub>g</sub>. If the reference bus is converted to PQ-bus, the first remaining PV-bus will be used as the slack bus for the next iteration at the limit, and the case is re-run. The voltage magnitude at the bus will deviate from the specified value to satisfy the reactive power limit. In other words, the relevant operating constraints of the reactive power output from the generators are maintained within practical operating points. The corresponding generator’s reactive power outputs are arranged in Table 5 of design settings for various objectives using the SpDEA.

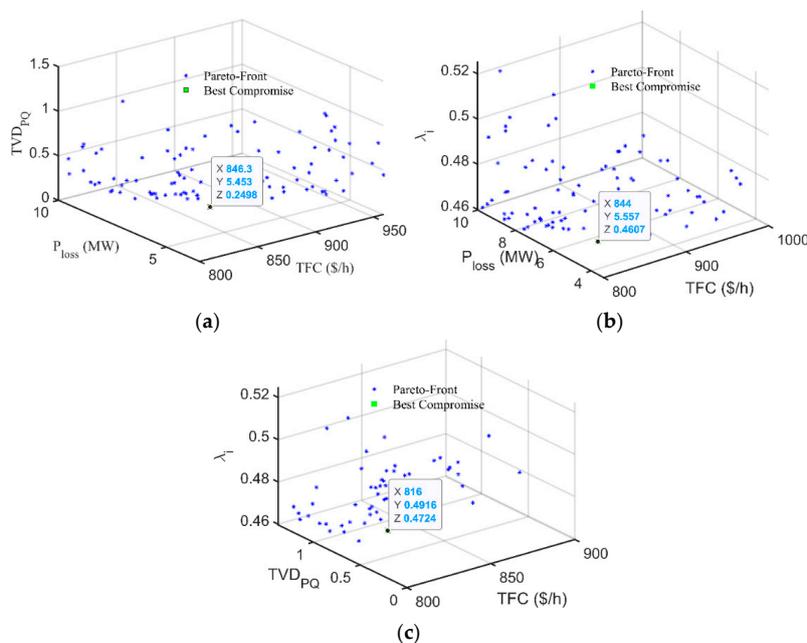
Figure 4a–c illustrate PFO solutions and best compromise value for cases 1–3, representing the anticipated bi-objective cases. On the other hand, Figure 5a–c illustrate PFO solutions and best compromise value for cases 4–6, representing the anticipated tri-objective cases. It is worthy of note here that these Pareto optimal solutions lie in an acceptable range of minimization of each simultaneous objective function. Moreover, the best compromise value is located at a proper value within the suggested PFO solutions.

**Table 5.** The related generator’s reactive power for optimal design settings for various multiple objectives using the SpDEA.

$Q_g$	$Q_{g, min}$	$Q_{g, max}$	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6	Case 7
$Q_{G1}$ (MVar)	−200	200	8.0712	−10.9857	−7.5976	2.6806	11.2260	−10.8816	−1.3888
$Q_{G2}$ (MVar)	−20	100	22.5222	28.7441	23.9599	7.5863	29.6632	21.4916	23.6488
$Q_{G5}$ (MVar)	−15	80	22.5225	22.6871	20.7621	16.0374	20.0417	19.9615	16.8297
$Q_{G8}$ (MVar)	−15	60	20.1239	8.8863	−2.1677	−9.2505	20.9694	6.7302	1.0296
$Q_{G11}$ (MVar)	−10	50	5.0564	28.4858	45.5612	40.5390	12.3456	34.1309	24.7763
$Q_{G13}$ (MVar)	−15	60	15.3335	34.9163	37.1135	42.7452	−6.0118	39.9768	35.7466



**Figure 4.** PFO solutions and best compromise value for cases 1–3 (a–c) for bi-objectives. (a) Case 1, (b) Case 2, (c) Case 3.



**Figure 5.** PFO solutions and best compromise value for cases 4–6 (a–c) for triple-objectives. (a) Case 4, (b) Case 5, (c) Case 6.

For a rational comparison, the SpDEA-based OPF results are compared with MODE and others, summarized in Table 6. It can be noted from this comparison that the best compromise values of OPF solutions using the SpDEA are very competitive, even though the TFC and TNL functions are contradictory. It reflects the proper design of the SpDEA to solve the multi-objective OPF problem in power systems. In addition to that, the average elapsed CPU times for various objectives' scenarios are mentioned in the last row of Table 4. It may be noted that bold font indicates the best results obtained so far.

**Table 6.** Comparison of optimal values for various cases.

Method	Case 1		Case 2		Case 3		Case 4			
	TFC (\$/h)	TPL (MW)	TFC (\$/h)	TVD <sub>PQ</sub> (pu)	TFC (\$/h)	1/λ <sub>i</sub>	TFC (\$/h)	TPL (MW)	TVD <sub>PQ</sub> (pu)	
SpDEA	<b>837.85</b>	<b>5.61</b>	<b>803.03</b>	<b>0.279</b>	<b>804.73</b>	<b>1.83</b>	<b>846.26</b>	<b>5.45</b>	<b>0.250</b>	
MODE	821.18	6.08	801.59	0.222	802.061	1.97	818.28	6.58	0.261	
MJaya [49]	827.91	5.80	×	×	×	×	×	×	×	
MOALO [50]	826.46	5.77	803.06	0.379	×	×	×	×	×	
Method	Case 5			Case 6			Case 7			
	TFC (\$/h)	TPL (MW)	1/λ <sub>i</sub>	TFC (\$/h)	TVD <sub>PQ</sub> (pu)	1/λ <sub>i</sub>	TFC (\$/h)	TPL (MW)	TVD <sub>PQ</sub> (pu)	1/λ <sub>i</sub>
SpDEA	<b>844.04</b>	<b>5.56</b>	<b>2.170</b>	<b>815.96</b>	<b>0.492</b>	<b>2.117</b>	<b>840.92</b>	<b>5.89</b>	<b>0.458</b>	<b>1.879</b>
MODE	818.001	7.24	1.822	811.78	0.300	1.911	819.02	6.90	0.297	1.932

×: not covered in this paper.

#### 4.2. IEEE 118-Bus System

In this scenario, the SpDEA is applied to solve different vector objectives of the OPF problem for the standard 118-bus IEEE system [48] with the main features stated in Table 1. The capacitive compensating devices are installed on the bus numbers of {34, 44, 45, 46, 48, 74, 79, 82, 83, 105, 107, and 110} and its maximum rated capacity is 30 MVar [19,22,23]. The data are demonstrated in detail in Table 2. The generating voltage magnitude of buses changes in the range 90–110%, the tap settings lie in the range 90%–110%. This optimization problem involves 129 control variables, posing a large challenge to the proposed algorithm. The optimal characteristics of the proposed SpDEA for this test case are demonstrated in Table 7 (last column). The various multiple objectives that are formulated in Table 2 are solved using the proposed SpDEA. The best values of control variables and their best compromise settings are recorded. However, the data of all cases are huge, and it is incredibly difficult to write in a paper. Therefore, only one case (case 1) is proposed, as illustrated in Table 7. The best compromise Pareto records 140,700 \$/h and 30.339 MW to the TFC and TNL of the network. Figure 6a illustrates PFO solutions and best compromise value for case 1. It can be noted here that the SPDEA selects the best compromise Pareto within the search space. It is worthy to note here that these PFO solutions lie in an acceptable range of minimization of each simultaneous objective function.

Moreover, Figure 6b,c point out the PFO solutions and their corresponding best compromise for the other cases that include bi-objective functions (cases 2–3). On the other hand, Figure 7a–c indicate the PFO solutions and their corresponding best compromise for three simultaneous objective functions (cases 4–6). The best compromise values for all these cases lie in acceptable ranges that can be confirmed. In addition, the SpDEA is applied to case 7 for solving the multi-objective function that contains all four objectives. In this issue, the best compromise Pareto records 150,718 \$/h, 33.69 MW, 1.415 pu, and 0.2525 to the TFC, TNL of the system, TVD for PQ buses, and voltage stability index, respectively. Therefore, it is successfully applied to various multiple adopted scenarios of the OPF problem regarding spot-on large-scale power systems.

**Table 7.** Optimal design settings and best data of case 1 of 118-bus network using the SpDEA.

Variable	Setting	Max	Variable	Setting	Max	Variable	Setting	Max
P <sub>G01</sub> (MW)	98.5129	100.0	P <sub>G104</sub> (MW)	18.4023	100.0	V <sub>G87</sub> (pu)	1.0611	1.10
P <sub>G04</sub> (MW)	0.0000	100.0	P <sub>G105</sub> (MW)	54.8394	100.0	V <sub>G89</sub> (pu)	0.9841	1.10
P <sub>G06</sub> (MW)	100.0000	100.0	P <sub>G107</sub> (MW)	0.0000	100.0	V <sub>G90</sub> (pu)	1.0121	1.10
P <sub>G08</sub> (MW)	23.0988	100.0	P <sub>G110</sub> (MW)	68.9143	100.0	V <sub>G91</sub> (pu)	1.0157	1.10
P <sub>G10</sub> (MW)	177.6589	550.0	P <sub>G111</sub> (MW)	0.0000	136.0	V <sub>G92</sub> (pu)	1.0678	1.10
P <sub>G12</sub> (MW)	42.8185	185.0	P <sub>G112</sub> (MW)	69.3657	100.0	V <sub>G99</sub> (pu)	0.9941	1.10
P <sub>G15</sub> (MW)	28.2670	100.0	P <sub>G113</sub> (MW)	67.3342	100.0	V <sub>G100</sub> (pu)	0.9000	1.10
P <sub>G18</sub> (MW)	83.6450	100.0	P <sub>G116</sub> (MW)	0.0000	100.0	V <sub>G103</sub> (pu)	1.0543	1.10
P <sub>G19</sub> (MW)	27.0238	100.0	V <sub>G01</sub> (pu)	1.0463	1.10	V <sub>G104</sub> (pu)	0.9646	1.10
P <sub>G24</sub> (MW)	17.0881	100.0	V <sub>G04</sub> (pu)	1.0600	1.10	V <sub>G105</sub> (pu)	0.9433	1.10
P <sub>G25</sub> (MW)	138.4995	320.0	V <sub>G06</sub> (pu)	1.0589	1.10	V <sub>G107</sub> (pu)	1.0516	1.10
P <sub>G26</sub> (MW)	38.1873	414.0	V <sub>G08</sub> (pu)	0.9462	1.10	V <sub>G110</sub> (pu)	0.9853	1.10
P <sub>G27</sub> (MW)	79.6290	100.0	V <sub>G10</sub> (pu)	1.1000	1.10	V <sub>G111</sub> (pu)	1.0258	1.10
P <sub>G31</sub> (MW)	14.7774	107.0	V <sub>G12</sub> (pu)	0.9113	1.10	V <sub>G112</sub> (pu)	0.9119	1.10
P <sub>G32</sub> (MW)	64.7293	100.0	V <sub>G15</sub> (pu)	0.9419	1.10	V <sub>G113</sub> (pu)	0.9721	1.10
P <sub>G34</sub> (MW)	66.3123	100.0	V <sub>G18</sub> (pu)	0.9341	1.10	V <sub>G116</sub> (pu)	0.9759	1.10
P <sub>G36</sub> (MW)	30.3050	100.0	V <sub>G19</sub> (pu)	1.0307	1.10	T <sub>5–8</sub>	110.00%	110%
P <sub>G40</sub> (MW)	100.0000	100.0	V <sub>G24</sub> (pu)	1.0146	1.10	T <sub>25–26</sub>	103.75%	110%
P <sub>G42</sub> (MW)	53.8052	100.0	V <sub>G25</sub> (pu)	0.9731	1.10	T <sub>17–30</sub>	102.50%	110%
P <sub>G46</sub> (MW)	43.0222	119.0	V <sub>G26</sub> (pu)	0.9711	1.10	T <sub>37–38</sub>	93.75%	110%
P <sub>G49</sub> (MW)	251.9802	304.0	V <sub>G27</sub> (pu)	1.0389	1.10	T <sub>59–63</sub>	102.50%	110%
P <sub>G54</sub> (MW)	71.3719	148.0	V <sub>G31</sub> (pu)	1.0407	1.10	T <sub>61–64</sub>	105.00%	110%
P <sub>G55</sub> (MW)	56.2296	100.0	V <sub>G32</sub> (pu)	1.0353	1.10	T <sub>65–66</sub>	90.00%	110%
P <sub>G56</sub> (MW)	86.2878	100.0	V <sub>G34</sub> (pu)	0.9687	1.10	T <sub>68–69</sub>	90.00%	110%
P <sub>G59</sub> (MW)	146.3078	255.0	V <sub>G36</sub> (pu)	0.9392	1.10	T <sub>80–81</sub>	106.25%	110%
P <sub>G61</sub> (MW)	190.7961	260.0	V <sub>G40</sub> (pu)	1.0458	1.10	Q <sub>C34</sub> (MVar)	4.4232	30
P <sub>G62</sub> (MW)	0.0000	100.0	V <sub>G42</sub> (pu)	0.9000	1.10	Q <sub>C44</sub> (MVar)	12.7388	30
P <sub>G65</sub> (MW)	388.9586	491.0	V <sub>G46</sub> (pu)	0.9019	1.10	Q <sub>C45</sub> (MVar)	11.0013	30
P <sub>G66</sub> (MW)	107.9369	492.0	V <sub>G49</sub> (pu)	0.9919	1.10	Q <sub>C46</sub> (MVar)	4.0472	30
P <sub>G69</sub> (MW)	250.5058	805.2	V <sub>G54</sub> (pu)	0.9883	1.10	Q <sub>C48</sub> (MVar)	15.6773	30
P <sub>G70</sub> (MW)	62.3974	100.0	V <sub>G55</sub> (pu)	1.0700	1.10	Q <sub>C74</sub> (MVar)	2.9030	30
P <sub>G72</sub> (MW)	46.3690	100.0	V <sub>G56</sub> (pu)	0.9721	1.10	Q <sub>C79</sub> (MVar)	15.9493	30
P <sub>G73</sub> (MW)	19.6229	100.0	V <sub>G59</sub> (pu)	0.9482	1.10	Q <sub>C82</sub> (MVar)	25.4304	30
P <sub>G74</sub> (MW)	47.0583	100.0	V <sub>G61</sub> (pu)	0.9289	1.10	Q <sub>C83</sub> (MVar)	23.0731	30
P <sub>G76</sub> (MW)	64.7490	100.0	V <sub>G62</sub> (pu)	0.9536	1.10	Q <sub>C105</sub> (MVar)	10.7369	30
P <sub>G77</sub> (MW)	54.1489	100.0	V <sub>G65</sub> (pu)	0.9628	1.10	Q <sub>C107</sub> (MVar)	8.8431	30
P <sub>G80</sub> (MW)	308.8801	577.0	V <sub>G66</sub> (pu)	1.0304	1.10	Q <sub>C110</sub> (MVar)	0.0000	30
P <sub>G85</sub> (MW)	4.4758	100.0	V <sub>G69</sub> (pu)	1.0550	1.10	Elapsed time (min)	<b>4.5</b>	
P <sub>G87</sub> (MW)	12.2678	104.0	V <sub>G70</sub> (pu)	0.9344	1.10	<b>TFC (\$/h)</b>	<b>140,700</b>	
P <sub>G89</sub> (MW)	255.0659	707.0	V <sub>G72</sub> (pu)	0.9000	1.10	<b>TPL (MW)</b>	<b>30.339</b>	
P <sub>G90</sub> (MW)	74.3701	100.0	V <sub>G73</sub> (pu)	0.9506	1.10	<b>TVD<sub>PQ</sub> (pu)</b>	<b>1.44273</b>	
P <sub>G91</sub> (MW)	39.3204	100.0	V <sub>G74</sub> (pu)	1.0810	1.10	1/λ <sub>i</sub>	0.252525	
P <sub>G92</sub> (MW)	31.5990	100.0	V <sub>G76</sub> (pu)	1.0081	1.10			
P <sub>G99</sub> (MW)	30.0157	100.0	V <sub>G77</sub> (pu)	1.0907	1.10			
P <sub>G100</sub> (MW)	130.2287	352.0	V <sub>G80</sub> (pu)	0.9479	1.10			
P <sub>G103</sub> (MW)	35.1592	140.0	V <sub>G85</sub> (pu)	0.9526	1.10			

Indeed, a fair comparison should be made between the proposed SpDEA-based OPF results and the MODE-based results to point out the flexibility, availability, and strength of the SpDEA-based OPF methodology. In this regard, Table 8 points out this detailed comparison for all seven cases. It is well-meaning here to say that the numerical results of the OPF problem using the SpDEA-based on OPF methodology are very similar to those obtained by the conventional MODE. The main merit of the proposed SpDEA is that it selects the best compromise among PFO solutions from several hundred Paretos within the search space. Moreover, the best compromise Paretos are within acceptable ranges. This property gives it a high possibility of reaching the optimal point in a quick way. This desired property is obviously illustrated in Figure 5. This reflects the proper design of the

SpDEA to solve the multiple vector simultaneous objectives of the OPF problem in electric power networks.

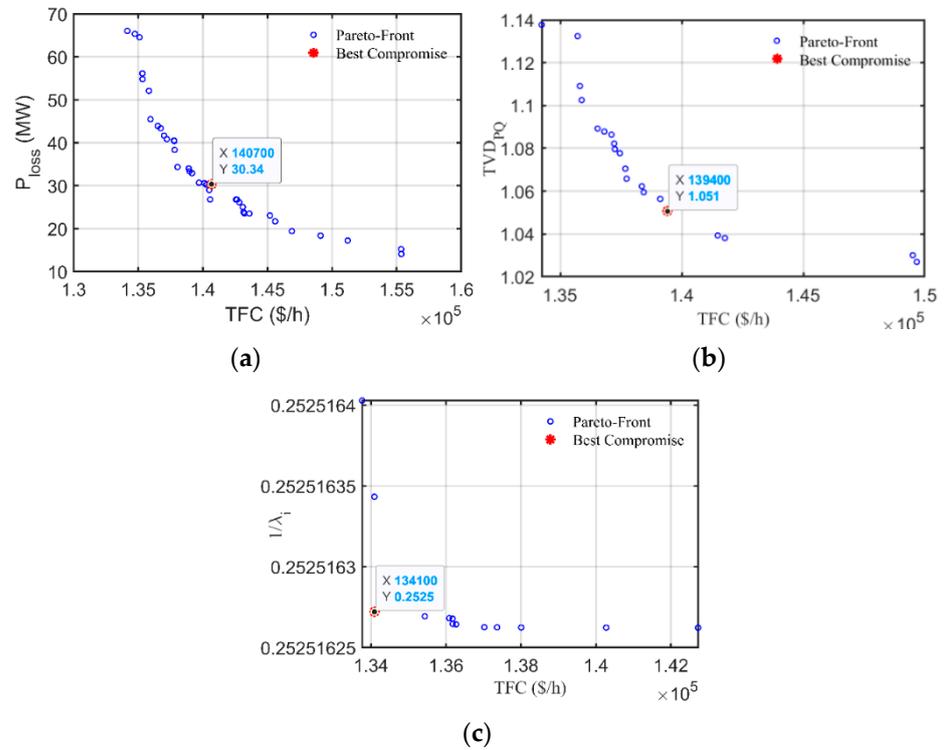


Figure 6. PFO solutions for the cases 1–3 (a–c) for the 118-bus system (bi-objective functions).

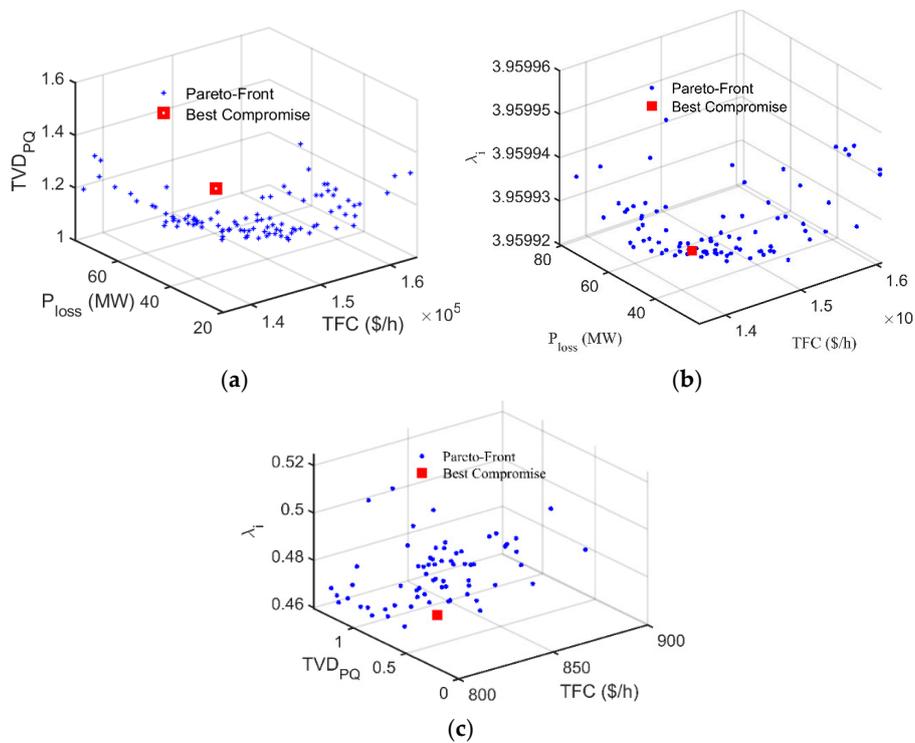


Figure 7. PFO solutions for the cases 4–6 (a–c) for the 118-bus system with three simultaneous objectives.

**Table 8.** Final cropped results of all cases 1–7 for the 118-bus network by SpMEA compared with MOALO [50].

Item	Case 1		Case 2		Case 3		Case 4		Case 5	Case 6	Case 7
	SpMEA	MOALO	SpMEA	MOALO	SpMEA	SpMEA	MOALO		SpDEA		
TFC (\$/h)	140,700	156,745	139,400	154,570	134,100	142,100	157,453	139,380	141,686	150,718	
TPL (MW)	30.339	90.659	50.0982	×	66.3373	38.8512	77,496	37.1432	56.9677	33.6933	
TVD (pu)	1.4427	×	1.051	3.887	1.4763	1.161	2.5864	1.52995	1.37546	1.41465	
$1/\lambda_i$	0.252525	×	0.252519	×	0.252516	0.252519	×	0.25253	0.252529	0.252516	
$\lambda_i$	3.96001	×	3.9601	×	3.96014	3.9601	×	3.95993	3.95994	3.96014	

×: not reported in the paper.

At last, it can be concluded that the SpDEA proves its viability in solving a large-scale conventional power system such as a standard IEEE 118-bus network. It is well-known strategically that many countries worldwide have planned to increase their shares of renewable energy generation from sources such as solar, wind, tidal, and many more, including energy storage facilities [51–53]. As a result, such penetrations to conventional power systems increase uncertainty. Therefore, it is important to extend the existing frameworks/methodologies to address this challenge. The later mentioned defines the future trend of our current work by incorporating system uncertainties and the variability of different types of renewable power sources and loads.

## 5. Conclusions

A novel application of the spherical prune differential evolution algorithm has been demonstrated to solve the OPF problem in electric power schemes to achieve simultaneous objectives under various scenarios. The OPF problem has been investigated with the well-known IEEE standard 30-bus and 118-bus networks as a large-scale optimization problem with 129 design control variables. All constraints have been respected with no violations. MATPOWER has been used to implement the full load flow analysis of the networks under study using full Newton–Raphson method. PFO solutions are generated, and the best settings are carefully selected by using the technique of normalized fuzzifications. The best results for the IEEE 30-bus system with quad objectives of TFC, TPL, TVD<sub>PQ</sub> and  $1/\lambda_i$  are equal to 840.92 \$/h, 5.89 MW, 9458 PU and 1.879, respectively. On the other hand, for the best results for the IEEE 118-bus system are equal to 150,718 (\$/h), 33.6933 MW, 1.41465 PU and 0.252516 for the same quad objectives, respectively. The demonstrated numerical simulations using the proposed SpDEA-based OPF methodology have proved their high performance, effectiveness, and robustness for solving the OPF problem of power systems in comparison to others reported in the literature.

Since the shares of renewable power sources including energy storage facilities are booming, uncertainty is increasing. Therefore, it is important to extend the existing frameworks/methodologies to address this challenge. The later mentioned defines the future trend of our current work by incorporating system uncertainties and the variability of different types of renewable power sources and loads.

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