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Modifying SEBAL Model Based on the Trapezoidal Relationship between Land Surface Temperature and Vegetation Index for Actual Evapotranspiration Estimation

Xiao-Gang Wang ¹, Wen Wang ^{1,2,*}, Dui Huang ¹, Bin Yong ¹ and Xi Chen ¹

- State Key Laboratory of Hydrology-Water Resources and Hydraulic Engineering, Hohai University, Nanjing 210098, China; E-Mails: xiaogang05010@163.com (X.-G.W.); huangdui2004520@163.com (D.H.); yongbin hhu@126.com (B.Y.); xichen@hhu.edu.cn (X.C.)
- Water Resources Section, Faculty of Civil Engineering and Geosciences,
 Delft University of Technology, P.O. Box 5048, 2600 GA Delft, The Netherlands
- * Author to whom correspondence should be addressed; E-Mail: w.wang@126.com; Tel.: +86-25-8378-7331.

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Abstract: The Surface Energy Balance Algorithm for Land (SEBAL) is widely used to estimate actual evapotranspiration (ET_a). One major limitation of the SEBAL model is the subjectiveness in selecting extreme cold/hot pixels. In the present study, the SEBAL model is modified by determining the extreme cold/hot status, based on the theoretical trapezoidal relationship between land surface temperature (Ts) and Enhanced Vegetation Index (EVI), which is established for each pixel. In this way, the dependence of SEBAL model on the existence of extreme cold/hot status and the subjectiveness in selecting cold/hot pixels with SEBAL model are eliminated. The performance of the classical SEBAL model and the modified version, T-SEBAL, are compared for estimating ET_a for a semi-arid catchment, and the result showed that the accuracy of ET_a estimation is improved by the T-SEBAL model compared with the classical SEBAL model.

Keywords: evapotranspiration; SEBAL; Ts~VI trapezoidal space

1. Introduction

Evapotranspiration (ET) plays an important role in hydrological cycles. It is a complex process influenced by conditions of solar radiation, atmosphere, and land surface, which makes it difficult to estimate actual evapotranspiration (referred to as ET_a hereafter) accurately. The early research of ET_a mainly focuses on developing meteorological approaches on the local scale [1–5]. However, such methods can rarely be extended to large areas due to land surface heterogeneity and the dynamic nature of the heat transfer processes [6]. Following the development of multi-temporal and multi-spectral remote sensing databases which can provide key surface characteristic (e.g., albedo, land surface temperature, and vegetation index), models of spatially and temporally dynamic feedback mechanism based on the land surface energy balance are proposed. The models retrieving ET_a mainly relying on remotely sensed data can be roughly categorized into *residual methods*, which calculate latent heat flux as the residual of the surface energy balance (*i.e.*, net radiation R_n minus sensible heat flux H and soil heat flux H and soil heat flux H and potential H and

The most widely used residual method/model so far is the Surface Energy Balance Algorithm for Land (SEBAL) proposed by Bastiaanssen *et al.* [7,13], which estimates regional ET_a with remotely sensed land surface temperature, surface emissivity, NDVI, and minimum requirement of some routine ground meteorological observation data, *i.e.*, sunshine duration and wind speed. The core assumption in SEBAL is a linear relationship between near-surface vertical temperature gradient and land surface temperature, and the relationship is determined by two extreme hydrological pixels, *i.e.*, extreme wet/cold and extreme dry/hot pixels. Although SEBAL has been applied in more than 30 countries worldwide with considerable accuracy [13,14], there are still some deficiencies, including the requirement of the existence of extreme "cold" and "hot" pixels throughout the image scene, the dependence of extreme pixel selection on domain size, and the subjectiveness in selecting the extreme pixels by different users, especially in the context of complicated surfaces.

To mitigate the limitation resulted from the manual selection of cold and hot points with SEBAL model, Allen *et al.* [15] proposed the Mapping Evapotranspiration at high Resolution with Internalized Calibration (METRIC). METRIC departs from the SEBAL model in its use of weather-based reference ET to establish energy balance conditions at a "cold" pixel, and a value of 1.05 ET_r (reference ET for 0.5 m tall alfalfa) estimated by standardized ASCE Penman-Monteith equation is considered to be ET_a of the "cold" pixel. In addition, METRIC considers the effects of complicated topography. However, METRIC still need to select a "representative cold pixel" from the satellite scene, which has biophysical characteristics similar to the reference crop (alfalfa). Su [9] proposed the SEBS model to estimate the evaporative fraction based on energy balance of dry/wet limiting cases (*i.e.*, at the wet-limit, ET takes place at its potential rate, while at the dry-limit point, the sensible heat flux reaches its maximum value $R_n - G$) for each pixel. SEBS does not require the existence and the selection of extreme pixels, but it needs many required parameters and a relatively complex solution of the turbulent heat fluxes which may introduce considerable uncertainty when a priori knowledge about the research area is not sufficient.

Moran et al. (1994) [11] proposed a measured surface minus air temperatures $(T_s - T_a)$ vs. vegetation cover (V_c) trapezoidal space which defined the extreme vertices as well-watered vegetation,

water-stressed vegetation, saturated bare soil, and dry bare soil, respectively, and used measured T_a , R_n , and G to calculate the $T_s - T_a$ for four vertices. However, using measured values of R_n and G for four vertices of $(T_s - T_a) \sim V_c$ may distort the trapezoidal space significantly, because the deviation of R_n between bare soil and vegetation may be up to 20% [16], and deviation of G is even larger. In addition, $T_s - T_a$ measurements for the four extreme vertices of the $(T_s - T_a) \sim V_c$ are not available in real application. Therefore, Wang *et al.* (2011) [17] suggested a pixel-based $T_s \sim$ vegetation index (VI) trapezoidal model to simplify the $(T_s - T_a) \sim V_c$ trapezoidal space, which uses an iterative procedure to consider the interaction process between T_s with R_n and the difference of G at different vertices. The $T_s \sim VI$ trapezoidal space have been used in combination with the Priestley-Taylor equation to estimate ET_a [18]. Following the same line, Long *et al.* (2012) [19] proposed a vegetation fraction $V_c \sim T_s$ trapezoidal framework with different formulation, where the warm edge is determined by analytically deriving temperatures of the bare surface with the largest water stress and the fully vegetated surface with the largest water stress, and the cold edge is set to be the regional average T_a .

In the present study, we would like to develop a method to define the hot and cold pixels for the SEBAL model by calculating surface temperatures at dry bare soil points and well-watered vegetation points of the pixel-based T_s ~VI trapezoid formulated by Wang *et al.* (2011) [17], so as to eliminate the limitations with SEBAL model. The method is described in Section 2; and the application result is presented in Section 4.

2. Method of Modifying SEBAL Using the Trapezoidal Relationship between Land Surface Temperature and Vegetation Index

2.1. SEBAL Model

SEBAL model estimates the surface net radiation flux R_n (W·m⁻²), the soil heat flux G (W·m⁻²), and the sensible heat flux H (W·m⁻²) firstly, then estimates the latent heat flux LE (W·m⁻²) as an energy residual by:

$$LE = R_n - G - H \tag{1}$$

 R_n is given by:

$$R_n = (1 - \alpha)R_s + \varepsilon_a \sigma T_a^4 - \varepsilon_s \sigma T_s^4 - (1 - \varepsilon_s)\varepsilon_a \sigma T_a^4$$
 (2)

where, R_s is the solar shortwave radiation (W·m⁻²), which is estimated by the empirical parameterization of Zillman (1972) [20] in the present study; ε_s and ε_a are the surface emissivity and atmospheric emissivity respectively; α is albedo (dimensionless); σ is the Stefan-Bolzman constant (5.67 × 10⁻⁸ W·m⁻²·K⁻⁴); T_s and T_a are the land surface temperature (K) and air temperature (K) at satellite observation time.

G is calculated as a friction of R_n . The ratio G/R_n is usually defined as a function of leaf area index (LAI) or Normalized Difference Vegetation Index (NDVI). In SEBAL, G is given by:

$$\frac{G}{R_n} = \frac{(T_s - 273.15)}{\alpha} (0.0032\alpha_{avg} + 0.0062\alpha_{avg}^2) (1 - 0.978NDVI^4)$$
(3)

where, α_{avg} is the daily average albedo which cannot be obtained from remotely sensed images directly. As the variation in albedo under all clear sky presents a U-shape, high at the sunrise and sunset and low at the noon, therefore a linear algorithm was suggested to calculate α_{avg} using instantaneous α , *i.e.*, $\alpha_{avg} = 1.02\alpha + 0.01$ [14].

Another method for estimating G is proposed by Su [9], given by:

$$G = R_n \times [\Gamma_c + (1 - V_c)(\Gamma_s - \Gamma_c)]$$
(4)

where, Γ_c and Γ_s denote the ratio of G/R_n for full vegetation canopy and bare soil, originally set as 0.05 and 0.315, respectively; V_c is the fractional canopy coverage, defined as $(\text{EVI} - \text{EVI}_{\text{min}})/(\text{EVI}_{\text{max}} - \text{EVI}_{\text{min}})$. It is found that, setting $\Gamma_s = 0.315$ will lead to serious overestimation of G compared with ground observations in our case study area, therefore, Γ_s is set to be 0.28 in the present study by a trial and error approach. As, globally, EVI mostly ranges from 0.07 for deserts to 0.7 for Amazon forests at 1-km resolution (MOD12A2) [21], and in our study area there are many pixels with EVI below 0.07, we set the value of EVI_{max} (maximum EVI) as 0.7 for full vegetation coverage, and EVI_{min} (minimum EVI) 0.05 for bare soil.

H is calculated by:

$$H = \rho C_p (T_0 - T_a) / r_a \tag{5}$$

where, ρ is the air density (kg·m⁻³), C_p is the air specific heat at constant pressure (1004 J·K⁻¹·kg⁻¹), T_0 is the aerodynamic temperature (K), r_a is the aerodynamic resistance (m·s⁻¹). As T_0 cannot be observed directly, whereas T_s could be retrieved from remotely sensed images, SEBAL establishes a linear relationship relating the vertical temperature gradient dT (= $T_0 - T_a$) to T_s , *i.e.*:

$$dT = a + bT_s (6)$$

where, a and b are coefficients of the linear relationship throughout a scene, estimated using T_s at two anchor points selected from the satellite image, i.e., a hot point where $H = R_n - G$ and a cold point where H = 0. At the cold point, dT = 0, whereas at the hot point, dT reaches its maximum dT_{hot} .

 r_a is given by:

$$r_a = \frac{1}{ku^*} \left[\ln(\frac{z_2}{z_1}) - \varphi_h(z_2, L) + \varphi_h(z_1, L) \right]$$
 (7)

where, k is the von Karman constant (=0.4); z_2 and z_1 are the upper and lower reference heights for aerodynamic resistance taken as 2 m and 0.1 m [13], respectively; u^* is the friction velocity obtained at the blending layer of 100 m to 200 m; φ_h is the stability correction of atmosphere for heat transport based on Monin-Obukhov length L (dimensionless, equals $\rho C_p u^{*3} T_s / (kgH)$); g is gravitational acceleration (=9.8 m·s⁻²). In fact, z_1 is equivalent to the roughness length for heat transfer z_{oh} . An alternative value of 0.01 for z_1 is also used in other studies [22,23]. Paul *et al.* (2014) [24] found that $z_{oh} = 0.1$ m and $z_{oh} = 0.01$ m led to the same estimate of ET_a. Thus, $z_{oh} = 0.01$ m is used in the present study for Equation (7), which is assumed to be more suitable to the vegetation sparse area.

The calculation of H is the core of the SEBAL model. With dT and r_a calculated, H could be estimated, and latent heat flux, LE, is immediately derived according to Equation (1).

2.2. Limitations of SEBAL Model

The existence and proper selection of cold and hot pixels in the image scene are crucial for the successful application of SEBAL, as they are essential for deriving variables a and b to estimate the temperature gradient dT.

The cold point is defined as the well-watered pixel with dense vegetation. Bastiaanssen *et al.* [13] chose water body as the cold point assuming that T_0 and T_a are approximately equal at such sites. The hot point is defined as bare soil pixels with the highest T_s [25], such as the dry bare agricultural field, but it is recommended that the hot point should not be treated as hot desert area, an asphalt floor, and biomass burning pixels [26], or other extreme hot areas which cannot represent natural surface, as the slope of the dT equation in such areas may be distorted.

However, it is cumbersome to find appropriate hot and cold pixels in some situations. For instance, water bodies does not always present in an image, especially for semi-arid areas when the image resolution is coarse. In that case, the average air temperature of the region may be used as cold point temperature [19]. In a catchment experienced a long-time drought or heavy rainfall, cold or hot points may do not exist at all. Furthermore, for mountainous areas, it is not possible to define a universal linear relationship between the temperature gradient dT and surface temperature T_s applicable to various topographic locations. In addition, the selection of dry and wet pixels over the area of interest (AOI) makes the SEBAL-estimated ET_a subject to the sizes of the AOI and the satellite image pixels [27].

On the other hand, the calculation of H is quite sensitive to the selection of extreme pixels. It was found that a 2 K increase in T_s for hot point may lead to 12% decrease in H, while for the cold point, a 2 K increase may result in 15% decrease in H in some cases [28]. Due to the importance and the complexity in defining the hot and cold pixels, it is suggested that experienced image processors are needed to correctly identify hot and cold pixels [29].

2.3. Modification of SEBAL Model Based on T_s~VI Trapezoidal Relationship

In the T_s ~VI trapezoidal space, the four vertices represent four extreme conditions, *i.e.*, well-watered vegetation, water-stressed vegetation, saturated bare soil, and dry bare soil (Figure 1). The dry bare soil vertex is defined for the case of bare surface with the largest water stress, which is equivalent to the definition of hot point in SEBAL; the well-watered vegetation vertex represents the situation with full vegetation coverage and no water stress, corresponding to the cold pixel in SEBAL. Therefore, the temperatures at hot and cold points can be calculated based on the T_s ~VI trapezoid pixel by pixel, and the determination of hot/cold pixels in SEBAL is modified from manual selection to physically-based calculation. The T_s ~VI trapezoid based modification of SEBAL model is referred to as T-SEBAL hereafter. The pixel-based procedure for estimating H with T-SEBAL is composed of the following two parts describe in Sections 2.3.1 and 2.3.2.

Point 4: dry bare soil

Warm edge

Point 2: water-stressed vegetation

Cold edge

Point 3: saturated bare soil

Point 1: well-watered vegetation

Figure 1. Structure of the T_s ~VI trapezoidal space.

2.3.1. Construct $T_s \sim VI$ Trapezoid and Calculate Temperatures of Hot and Cold Points

The core of constructing T_s VI trapezoidal space is the calculation of T_s for four extreme vertices with an iterative procedure considering the interaction among T_s , R_n , r_a , and u^* . The following formulas are used for calculating T_s for each vertex in the T_s VI trapezoidal space [11,19].

• Point 1, cold point. For full vegetation-covered and well-watered surface.

$$T_{s,1} = \left[r_a'(R_n - G) / C_v\right] \left\{ \gamma(1 + r_{cm} / r_a') / \left[\Delta + \gamma(1 + r_{cm} / r_a')\right] \right\} - VPD / \left[\Delta + \gamma(1 + r_{cm} / r_a')\right] + T_a$$
 (8a)

• Point 2. For full vegetation-covered surface with no available water.

$$T_{s,2} = \left[r_a'(R_n - G) / C_v\right] \left\{ \gamma(1 + r_{cx} / r_a') / \left[\Delta + \gamma(1 + r_{cx} / r_a')\right] \right\} - VPD / \left[\Delta + \gamma(1 + r_{cx} / r_a')\right] + T_a$$
 (8b)

• Point 3. For saturated bare soil, where canopy resistance $r_c = 0$.

$$T_{s,3} = \left[r_a'(R_n - G)/C_v\right] \left[\gamma(\Delta + \gamma)\right] - VPD/(\Delta + \gamma) + T_a$$
(8c)

• Point 4, hot point. For dry bare soil, where $r_c = \infty$ (analogous to complete stomatal closure).

$$T_{s,4} = r_a'(R_n - G)/C_v + T_a$$
 (8d)

where, the subscript n (1, 2, 3 and 4) of T_s refers to the nth vertex in Figure 1; r_a' is the aerodynamic resistance estimated with Equation (9), which is different from the formula Equation (7) used in SEBAL; r_c is the canopy resistance (m·s⁻¹); r_{cm} and r_{cx} are the minimum and maximum canopy resistance; Δ is the slope of saturated vapor pressure to air temperature; γ is the air humidity constant (hPa·C⁻¹); VPD is the vapor pressure deficit of the air (hPa); C_v is the volumetric heat capacity of air (1295.16 J·K⁻¹·m⁻³); G is estimated as a fraction of R_n . For full-cover vegetation edge, G/R_n is negligible, say 0.05, while for dry bare soil and wet bare soil, G can approximately reach up to 0.5 R_n and down to 0.15 R_n , respectively [30].

 R_n is estimated with Equation (2). For bare surface and full-covered vegetation, ε_s are set as 0.93 and 0.993, respectively, according to the result of Snyder *et al.* [31]. The albedo is a key parameter to estimate R_n . In the work of Wang *et al.* [17], the surface shortwave albedo derived from MODIS product MCD43A3 is used for all the four vertices, which is not physically reasonable. Hence, values of albedo at four extreme cases are defined separately in the present study. There are some suggestions

about the albedo values for different land surfaces [32–34]. In our application, considering those suggestions and by a trial-and-error procedure, albedos are set to be 0.1 and 0.25 for saturated bare soil (point 3) and dry bare soil (point 4), and 0.18 and 0.20 for well-watered vegetation (point 1) and water-stressed vegetation (point 2).

Aerodynamic resistance r_a is given by [35]:

$$r_a' = \left[ln \left(\frac{z - d}{z_{0m}} \right) - \psi_m \right] \left[ln \left(\frac{z - d}{z_{0h}} \right) - \psi_h \right] (k^2 u)^{-1}$$

$$\tag{9}$$

where, u is wind speed (m·s⁻¹); d is displacement height (m), given by 0.67h, with the height of vegetation h estimated from z_{0m} , i.e., $h = 8z_{0m}$; z_{0m} is the momentum roughness length, defined as a function of NDVI, i.e., $\exp(a + b \cdot \text{NDVI})$, where we set a = -5.2 and b = 5.3 [36]; z_{0h} is the heat roughness length; ψ_h and ψ_m are the stability correction for heat and momentum, calculated according to the value of Monin-Obukhov length L. The heat roughness length z_{0h} is estimated by $z_{0h} = z_{0m}/\exp(kB^{-1})$, where kB^{-1} is a dimensionless parameter.

Many formulas have been used for estimating kB^{-1} with different complexity. Verhoef *et al.* (1997) [37] evaluated several methods of kB^{-1} estimation for the bare soil site with the soil classified as silt loam and showed that the equation of Owen and Thomson (1963) [38] performed well, so it is used for the situation of bare soil, given by:

$$kB_s^{-1} = k\alpha (8Re^*)^m Pr^n \tag{10}$$

where, the subscript s refers to bare soil; α is a factor lying between 0.45 and 0.7 with an average of 0.52; Re^* is the roughness Reynolds number and equals to $z_{0m,s}$ u^*/v , with $z_{0m,s}$ and v being the momentum roughness length under bare soil circumstance and kinematic viscosity of the air; Pr is the Prandtl number (0.71); m and n are constants given by 0.45 and 0.8, respectively.

For full canopy coverage situations, the formula developed by Blümel (1999) [39] is used, given by:

$$kB_c^{-1} = C_k (\sigma_\alpha LSAI^3)^{-0.25} \left[\frac{D_f u}{\ln((z-d)/z_{om,c})} \right]$$
 (11)

where $C_k = 16.4 \text{ m}^{-1} \cdot \text{s}^{1/2}$; D_f is the leaf width, set to be 0.01 m (for open shrubland) as in NASA Global Land Data Assimilation System (GLDAS); $z_{0m,c}$ is the momentum roughness length of full canopy coverage; σ_{α} is the moentum partion factor relevant to LSAI (leaf and stem area index). If LSAI is not known, the factor $(\sigma_{\alpha}LSAI^3)^{-0.25}$ is approximately set as 0.4 provided that LSAI \geq 4.

Canopy resistance r_c is estimated as r_s/LAI_{max} , where r_s is the stomatal resistance (s·m⁻¹) and LAI_{max} is the maximum LAI in full-cover vegetation. In the paper of Wang *et al.* [17], the maximum r_s (r_{smax}) and minimum r_s (r_{smin}) are set as 1500 s·m⁻¹ and 100 s·m⁻¹, respectively. However, it was found that setting $r_{smax} = 1500$ cannot adequately consider the constraint of evapotranspiration under full water-stress condition, therefore, we set r_{smax} as 5000 s·m⁻¹ as suggested by Dickinson [40]. There are several schemes available for setting vegetation parameters, such as NASA GLDAS [41], and European Centre for Medium-Range Weather Forecasts (ECMWF) [42]. In our application, assuming that the vegetation for the semi-arid zone is closed shrubland, according to the vegetation parameter scheme of NLDAS, r_{smin} is set to be 175 s·m⁻¹ and LAI_{max} 5.

Combing Equation (2) with Equation (8a)–(8d), we get a quartic equation for T_s at each vertex.

Taking point 4 as an example, the quartic equation is given by:

$$T_{s,4} = \frac{r_a'(1-r_4)}{C_v} \Big[(1-\alpha)R_s + \varepsilon_a \sigma T_a^4 - \varepsilon_s \sigma T_{s,4}^4 - (1-\varepsilon_s)\varepsilon_a \sigma T_a^4 \Big] + T_a$$
 (12)

where, r_4 is the ratio of G to R_n at point 4. By solving these equations, we get T_s for each vertex of the T_s ~VI trapezoid.

The procedure for constructing the $T_s \sim VI$ trapezoid on a pixel basis is summarized in the dash line box of Figure 2, which may be divided into three major steps. (1) Estimate the initial value of r_a ' using meteorological data without considering the two stability corrections, *i.e.*, ψ_h and ψ_m ; (2) Iteratively solve the quartic equation for T_s (e.g., Equation (12)), and calculate H, L, and r_a ' sequentially for each vertex, after 10 iterations when the r_a ' is stable, *i.e.*, difference between two adjacent calculations of r_a ' is smaller than five percent; (3) Verify the reasonableness of $T_s \sim VI$ trapezoid by comparing the location of every pixel's (EVI, T_s) point with the hot/cold edges of the $T_s \sim VI$ trapezoid, considering that there are errors in T_a which is extrapolated from a few observation sites and uncertainties in the parameterization for the calculation of aerodynamic resistance, which could lead to errors in T_s at vertices of $T_s \sim VI$ trapezoids. If an observed (EVI, T_s) point falls outside the hot/cold edges, an adjustment is made to make the point be contained within the $T_s \sim VI$ trapezoid. Figure 3 gives an example for the adjustment when a (EVI, T_s) point falls above the warm edge.

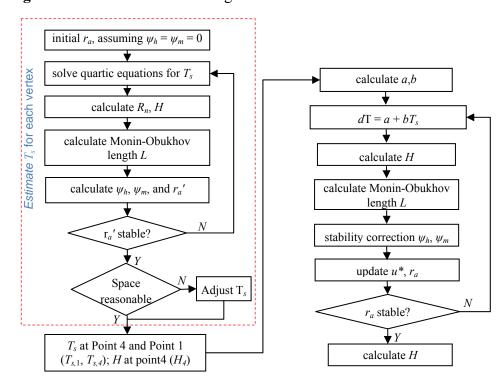
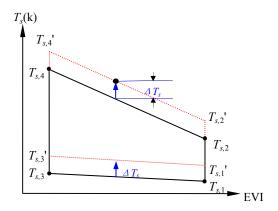


Figure 2. Procedure for estimating sensible heat flux H with T-SEBAL.

Figure 3. Adjustment of T_s when the (EVI, T_s) point is above the warm-edge of the calculated $T_s \sim VI$ trapezoid.



2.3.2. Estimate Sensible Heat Flux *H*

With the theoretical T_s ~VI trapezoid constructed for each pixel uniquely, the calculated values of $T_{s,l}$ at point 1 and $T_{s,4}$ at point 4 are used as the hot point temperature and cold point temperature respectively. $T_{s,l}$ and $T_{s,4}$, together with calculated R_n –G at point 4 (*i.e.*, $(R_n$ – $G)_4$), are used to estimate the coefficients a and b in Equation (6) for each pixel, given by:

$$b = \frac{(R_n - G)_4 r_{a, hot}}{\rho C p(T_{s, 4} - T_{s, 1})}$$
(13)

$$a = -b \times T_{s,1} \tag{14}$$

where, $(R_n-G)_4$ is the calculated sensible heat flux of point 4 (H_4) (Figure 1); $r_{a,hot}$ is the aerodynamic resistance at hot point calculated using Equation (7). Then dT and r_a for each pixel are estimated using Equations (6) and (7), respectively. Finally, H for each pixel could be estimated with Equation (5). The procedure for estimating H is described in the right part of Figure 2, following the procedure of standard SEBAL.

3. Case Study Area

The Walnut Gulch Experimental Watershed (WGEW) is located in southeastern Arizona, United States, with an area of 150 km² contained within the upper San Pedro River Basin (Figure 4). Climate at WGEW is classified as semiarid. The mean annual air temperature and precipitation are 17.7 °C and 312 mm respectively. Sixty percent of the precipitation concentrates in monsoon season between July and September. Desert shrubs dominate the lower two-thirds of WGEW and the remaining upper one third is desert grasses.

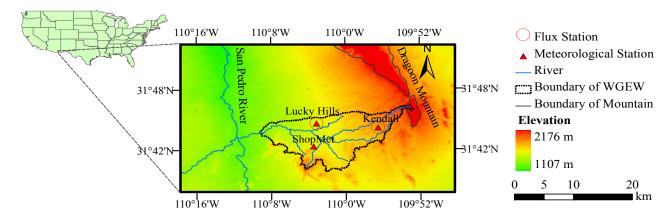


Figure 4. Location of the study area, flux stations and meteorological stations.

Two flux towers, *i.e.*, Lucky Hills and Kendall, were operating in WGEW. Lucky Hills (elevation 1372 m) is shrub-dominated. The fraction of vegetation (creosote bush, whitethorn Acacia, tarbush) at this site is 26% with the average vegetation height maintained at almost 1 m constantly. Kendall (elevation 1526 m) is grass-dominated. The vegetation height at this site ranges from 0.4 to 0.7 m, and the vegetation covers about 40% of land surface during the growing season [43].

The fluxes of the two sites are measured by the Bowen Ratio Energy Balance System (BREB) (model 023/CO₂, Campbell Scientific Inc., Logan, UT, USA) every 2 s and automatically recorded at a 20-min time step. The datasets include net radiation from a net radiometer calibrated yearly at 3 m height (model Q*7, REBS, Seattle, WA, USA), and soil heat flux data from five soil heat flux plates at 8 cm depth (model HFT3, REBS). The theory and formulations used to calculate sensitive heat flux and latent heat flux were presented in detail by Emmerich *et al.* [43].

There is a very dense rain gauge network with 88 weighing rain gauges within the WGEW. The meteorological dataset of air temperature, relative humidity and wind speed, *etc.*, are measured at three sites, *i.e.*, Lucky Hills, Kendall and ShopMet (Figure 4), recorded at the same frequency of 20 min. Air temperature is extrapolated to the whole study area by the method described in Wang *et al.* [17], considering the leaf area index (LAI), elevation and topography feature. Other meteorological variables at the three observation sites are averaged and applied to the whole study area.

Products of the moderate resolution imaging spectroradiometer (MODIS) are used in the present study as remotely sensed input data for the model (Table 1). Data with 1 km and 250 m resolution are resampled to 500 m using the nearest neighbor method. Fifteen dates with clear-sky and complete meteorological observations in 2004 were selected to estimate the fluxes with the T-SEBAL and SEBAL model. To ensure a better chance that the cold/hot points can be reliably selected for each date with SEBAL model and subsequently make a fair comparison between SEBAL and T-SEBAL model, images covering an area much larger than the WGEW (as shown in Figure 4) are used in the present study.

In summary, major data used in the present study include:

- (1) Ground based meteorological observations: air temperature T_a , wind speed u, and relative humidity U;
- (2) MODIS products: land surface temperature T_s , satellite overpass time, surface emissivity ε_s , vegetation index *NDVI* and *EVI*, albedo, and latitude (radian).
- (3) DEM from the Shuttle Radar Topography Mission (SRTM).

Product ID	Contents	Spatial Resolution	Temporal Resolution		
MOD03	Geo-location data	1 km	Daily		
MOD11A1	Surface temperature and emissivity, overpass time, Quality control	1 km	Daily		
MCD12Q1	Land cover type	500 m	Yearly		
MOD13A1	Vegetation indices	250 m	8 days		
MCD43A3	Surface reflectance BRDF/Albedo	500 m	16 days		

Table 1. MODIS product data used.

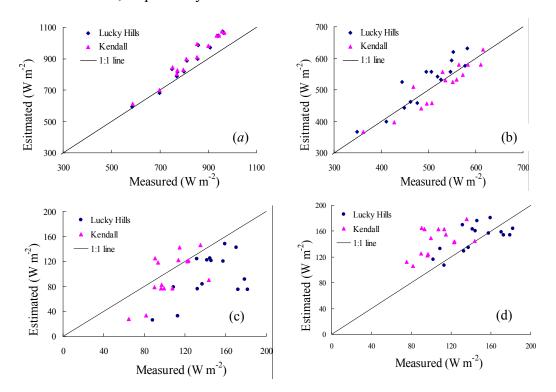
4. Application of T-SEBAL Model

4.1. Surface Net Radiation Flux and Soil Heat Flux

The calculations for surface net radiation flux and soil heat flux are the same for both T-SEBAL and SEBAL.

Net radiation flux is estimated using Equation (2), and the intermediate variable—solar shortwave radiation—is calculated with the empirical parameterization by Zillman (1972) [20]. Ground soil heat flux G is estimated with two equations, *i.e.*, Equations (3) and (4). Comparison between calculated net radiation flux and soil heat flux with observations in 15 dates are shown in Figure 5.

Figure 5. Estimated (a) R_s , (b) R_n , (c) G with Equation (3), and (d) G with Equation (4) vs. ground observations, respectively.



By visual inspection of Figure 5 we see that, the estimates of R_s are generally in good agreement with the observations, just slightly overestimated, mostly in the part of high values. The root mean squared error (RMSE) of R_s estimates for Lucky Hills and Kendall are 77 W·m⁻² and 84 W·m⁻², respectively.

 R_n estimates are also in good agreement with the observations. By fitting the simple linear regression between estimated R_n and the observations at Lucky Hills and Kendall, we found that the coefficient of determination r^2 is up to 0.79. The RMSE of estimated R_n at Lucky Hills and Kendall are 39.5 W·m⁻² and 29 W·m⁻² respectively. As shown in Figure 5, there is generally no obvious bias between the estimated and the observed, however, R_n is overestimated at Lucky Hills, while underestimated at Kendall.

Compared with ground observations, G estimates with Equation (3) poorly agree with the observations (Figure 5c), with a RMSE of 44.86 W·m⁻². Comparatively, G estimates with Equation (4) are better (Figure 5d), just slightly overestimated, with RMSE = 33 W·m⁻² and average relative error 21.6% (max relative error 74%). Therefore the Equation (4) is used in the calculation of H for both T-SEBAL and SEBAL in later procedures.

4.2. Sensible Heat Flux and Latent Heat Flux

H is calculated differently with SEBAL and T-SEBAL because of their different ways of defining extreme cold/hot points, as described in Sections 2.1 and 2.3.

For the SEBAL model, a subjective selection procedure is conducted for selecting cold/hot points. Candidates of hot points are defined as those pixels in the satellite image scene with their surface temperatures above the 95 percentile of all pixels, NDVI less than 0.2, the slope less than 10%, and none urban and built-up land-cover. Then, the pixel with the highest albedo was chosen as the hot point from the candidates, which have similar pixels around them. As no water body exists in this semi-arid region, the lower one between the minimum T_s throughout the scene and the average T_a of the whole area is defined as the temperature of the cold pixel. It is found that, among the 15 dates investigated, the minimum T_s is mostly larger than the average T_a except for DOY345.

For the T-SEBAL model, the values of T_s at the four vertices of T_s ~EVI trapezoid for each pixel are estimated using the method described in Section 2.3. The calculated T_s at T_s ~EVI trapezoid vertices for all the pixels of the study area are plotted in the form of box-and-whisker plot in Figure 6 to illustrate the reasonability of the trapezoids for four exemplary dates in different seasons. As illustrated in Figure 6, the points in DOY183 and DOY 267 are closer to the warm edge (the line between point 4 and point 2) than in DOY75 and DOY345, indicating more intense water scarcity in DOY183 and DOY 267 than in DOY75 and DOY345.

The hot and cold point temperatures (*i.e.*, $T_{s,hot}$ and $T_{s,cold}$) determined by T-SEBAL and SEBAL in 15 dates for the study area are illustrated in Figure 7 and presented in Table 2. The values of $T_{s,hot}$ and $T_{s,cold}$ of T-SEBAL shown in Figure 7 are the average of the whole image, because T-SEBAL computes $T_{s,hot}$ and $T_{s,cold}$ on a pixel basis. It is shown that, $T_{s,hot}$ given by T-SEBAL is higher than that by SEBAL about 1.6 K on average, and $T_{s,cold}$ by T-SEBAL is significantly lower than by SEBAL with about 2.9 K. Consequently, T-SEBAL retrieves larger difference between hot point and cold point temperatures.

Figure 6. Box-and-whisker plots of calculated T_s at four vertices of T_s ~EVI trapezoids of four dates in 2004: (a) DOY75; (b) DOY183; (c) DOY267; (d) DOY345. (For each boxplot, the bottom and top of the box are the first and third quartiles, the band inside the box is the median, the lower whisker is the lowest datum still within 1.5 IQR (interquartile range) of the lower quartile, and the upper whisker is the highest datum still within 1.5 IQR of the upper quartile).

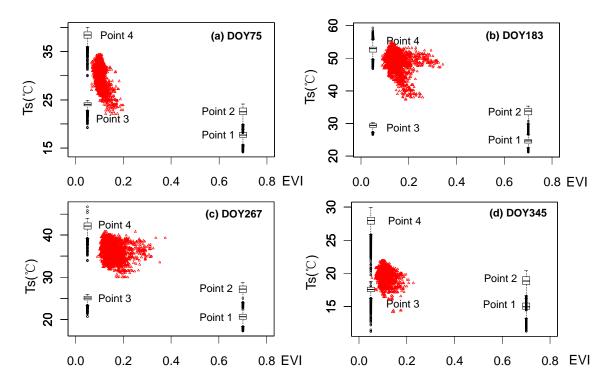


Figure 7. Comparison of the land surface temperature at hot points and cold points for SEBAL and T-SEBAL.

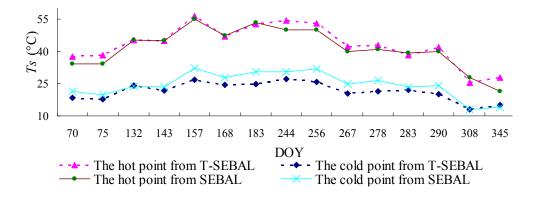


 Table 2. Variables and parameters at extreme points given by Surface Energy Balance Algorithm for Land (SEBAL) and T-SEBAL for 15 dates.

	T-SEBAL				SEBAL							
DOY	$T_{s,4}$	$T_{s,1}$	$(R_n-G)_4$	а	b	dT_{hot}	$T_{s,hot}$	$T_{s,cold}$	$(R_n-G)_{hot}$	a	b	dT_{hot}
	(°C)	(°C)	$(\mathbf{W} \cdot \mathbf{m}^{-2})$	(°C)	(-)	(°C)	(°C)	(°C)	$(\mathbf{W} \cdot \mathbf{m}^{-2})$	(°C)	(-)	(°C)
70	37.60	18.37	261.57	-6.89	0.38	5.28	34.21	21.54	322.21	-12.71	0.59	7.53
75	38.33	17.68	281.04	-7.15	0.40	4.84	34.17	19.74	349.69	-12.04	0.61	8.81
132	45.33	23.98	344.73	-8.95	0.37	7.11	45.07	23.89	377.51	-8.36	0.35	7.44
143	44.99	21.62	333.59	-7.99	0.37	7.73	44.75	23.43	348.11	-8.43	0.36	7.77
157	56.20	26.77	318.91	-9.68	0.36	9.35	54.93	32.07	342.36	-13.79	0.43	9.82
168	47.02	24.41	335.06	-8.26	0.34	6.91	47.31	27.69	343.26	-9.14	0.33	6.56
183	52.77	24.68	351.16	-8.54	0.35	8.53	53.43	30.59	380.05	-12.24	0.40	9.12
244	54.14	27.08	287.78	-10.72	0.40	7.73	50.01	30.61	359.16	-17.45	0.57	11.13
256	52.90	25.67	286.65	-9.01	0.35	7.30	50.01	31.95	324.91	-15.98	0.50	8.98
267	42.05	20.53	281.19	-7.49	0.36	5.79	39.87	24.61	314.95	-12.31	0.50	7.58
278	42.92	21.43	242.46	-7.50	0.35	6.03	41.01	26.36	295.87	-12.65	0.48	6.98
283	38.25	22.12	256.27	-7.58	0.34	4.97	39.23	23.44	273.95	-7.27	0.31	4.92
290	41.89	20.15	228.47	-7.58	0.38	6.25	39.77	23.98	273.69	-12.47	0.52	8.24
308	25.30	13.11	214.09	-4.92	0.38	4.16	27.73	13.04	228.29	-3.52	0.27	4.01
345	27.84	14.95	174.30	-5.47	0.37	1.64	21.29	14.13	257.16	-10.88	0.77	5.54

Besides the differences in the estimation for hot and cold point temperatures, from Table 2, we can also see significant differences in the values of $(R_n - G)$ at hot points calculated by T-SEBAL and SEBAL (denoted by $(R_n - G)_4$ and $(R_n - G)_{hot}$, respectively). The values of $(R_n - G)_4$ given by T-SEBAL are on average smaller than $(R_n - G)_{hot}$ given by SEBAL. The differences in not only hot and cold point temperatures, but also the values of $(R_n - G)$, together lead to the significant difference in establishing the linear relationship between dT to T_s in Equation (6), which is reflected in different estimates of a and b by T-SEBAL and SEBAL according to Equations (13) and (14), shown in Table 2. That means, T-SEBAL and SEBAL differ not only in their ways of determining $T_{s,hot}$ and $T_{s,cold}$, but also in the calculation of $(R_n - G)$.

With the linear relationship determined, we can further estimate H for each pixel. Figure 8 shows the difference between SEBAL estimates and T-SEBAL estimates over the whole study area, and the scatter plots of SEBAL estimates versus T-SEBAL estimates for DOY75, DOY83, DOY267, and DOY345, respectively. The scatter plots show that the H estimates by T-SEBAL are generally well correlated with those by SEBAL, and the correlation coefficients between the two are 0.85, 0.6, 0.71, and 0.73 in DOY75, DOY183, DOY267, and DOY345, respectively. However, there are some biases between the two, that is, H estimates by T-SEBAL are on average ~117 W·m⁻², ~3 W·m⁻² and ~52 W·m⁻² lower in DOY345, DOY267 and DOY75, and 53 W·m⁻² higher in DOY 183, than those by SEBAL. Such biases can be explained by the differences in the calculation of dT. In DOY345, b estimated by T-SEBAL is significantly lower than that by SEBAL while values of T_s at the cold point given by two models have slight differences, which leads to significantly higher dT estimates by SEBAL than by T-SEBAL, especially in the areas with high T_s values. As a consequence, H estimated by SEBAL is significantly larger than by T-SEBAL in DOY345. The situations are more or less similar for DOY 267 and DOY75. As to DOY 183, both $T_{s,1}$ and b by T-SEBAL are smaller than SEBAL, leading to overall larger dT and consequently larger H by T-SEBAL than by SEBAL.

With *H* estimated for each pixel, we can easily derive *LE* as an energy residual with Equation (1). The scatter plots of *H* and *LE* estimates with T-SEBAL and SEBAL against observations at Lucky Hills and Kendall for 15 dates are displayed in Figure 9. From Figure 9 we see that *H* is underestimated by both T-SEBAL and SEBAL in general. However, in terms of RMSE (Root mean square error), MAE (Mean absolute error), MBE (Mean bias error), T-SEBAL generally performs better than SEBAL in the estimation of LE, as shown in Table 3 [8,44–48].

Besides the results of LE estimation with T-SEBAL and SEBAL in the present study, Table 3 also lists some published results in the literature for Walnut Gulch watershed for comparison. It is shown that, compared with other published results, the T-SEBAL results in the present study are better in general, especially considering the fact that in T-SEBAL all energy-related variables are estimated whereas observational data are used in many published results, e.g., Norman *et al.* (1995) [8] and Moran *et al.* (1996) [44] used observed R_n , Anderson *et al.* (1997) [45], Kustas *et al.* (1998) [46], and Li *et al.* (2008) [47] used observed R_s to estimate LE.

Figure 8. Differences between *H* estimated by T-SEBAL and *H* estimated by SEBAL (T-SEBAL estimates minus SEBAL estimates) (**left panels**) and the scatter plots T-SEBAL estimates *versus* SEBAL estimates (**right panels**) in four dates.

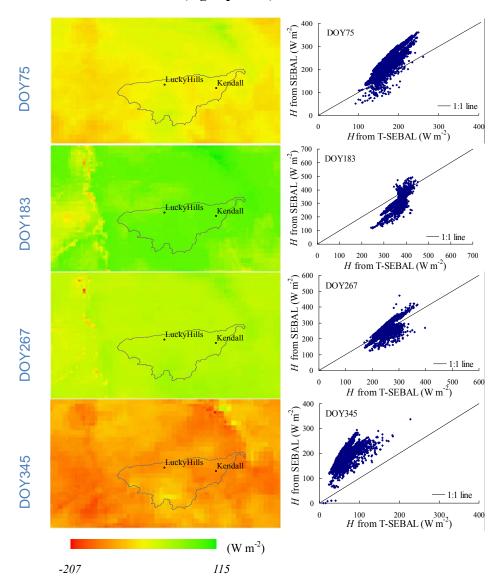


Figure 9. Comparison of T-SEBAL and SEBAL estimated (a) H and (b) LE versus observations.

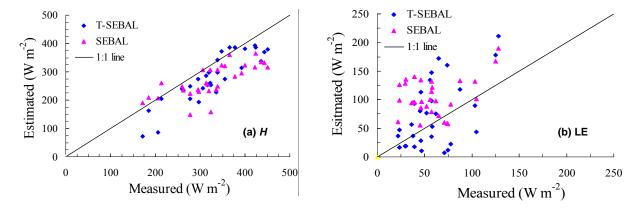


Table 3. Comparison of different LE estimation accuracies for Walnut Gulch watershed (W·m⁻²).

Authors	I	nputs	M - J -1/M - 41 J	MAE ^a		MBE ^b		RMSE °	
Authors	Remote sensing	Ground observation	Model/Method	LH	KD	LH	KD	LH	KD
Present study	MODIS in 15 dates	wind speed u , T_a , relative humidity	T-SEBAL SEBAL	45.8 59.2	35.0 38.5	27.2 57.8	1.6 33.8	56.4 66.0	41.8 47.0
Norman <i>et al.</i> (1995) [8]	directional brightness temperature $T_b(\theta)$ and its angle of view θ	R_n , u , T_a and f_c or LAI, vegetation height and leaf size.	TSM	45	31				
Moran <i>et al</i> . (1996) [44]	TM in 8 dates, radar in 6 dates	R_n , G , VPD, and T_a , etc.	Combing T _s -T _a vs. SAVI trapezoidal space and P-M equation	45					29
Zhan <i>et al.</i> (2001) [48]	radiometric surface temperature T_r	$u, T_a, etc.$	CECM			-22	-5	50	39
Anderson <i>et al.</i> (1997) [45]	24 dates of $T_b(\theta)$	R_s , u , etc.	TSTIM	3	36			42	
Kustas <i>et al.</i> (1998) [46]	TM in 6 dates	R_s , u , T_a , T_b , h_c , leaf width, roughness parameters, etc .	dual-source model			-15		65	
Li <i>et al</i> . (2008) [47]	MODIS and TM in 3 dates	R_s , u , T_a , vapor pressure e_a , etc .	TSM				69 (MODIS) 34 (TM 30 m) 32 (TM 120 m)		

Note: LH and KD represent the two flux stations Lucky Hills and Kendall in Walnut Gulch watershed, respectively. a. MAE is given by $\frac{1}{n}\sum_{t=1}^{n}|P_t-Q_t|$; b. MBE is given by $\frac{1}{n}\sum_{t=1}^{n}(P_t-Q_t)$; c. RMSE is given by $\left[\frac{1}{n}\sum_{t=1}^{n}(P_t-Q_t)^2\right]^{1/2}$, where P and Q are the estimation and the observation respectively.

4.3. Daily Actual ET

As the residual energy, LE is calculated according to the Equation (1) after estimated H, and it could be converted to instantaneous ET (ET_{inst}) by the latent heat of vaporization.

$$ET_{inst} = \frac{LE}{l_e \rho_w} \tag{15}$$

where ET_{inst} is the instantaneous ET_a (m·s⁻¹). ρ_w is density of water (~1000 kg·m⁻³). l_e is the latent heat of vaporization(J·kg⁻¹) calculated as:

$$l_e = [2.501 - 0.00236(T_s - 273.15)] \times 10^6$$
 (16)

Jackson *et al.* (1983) [49] related diurnal trend of the ratio of ET_{inst} to daily value (ET_d) to a sine function:

$$ET_d/ET_{inst} = 2N/\left[\pi \sin(\pi t/N)\right] \tag{17}$$

where t is the time in the day (beginning at sunrise). N is the time period between sunrise and sunset, which is calculated by the equation suggested by Jackson [49].

For the 15 dates studied in the present study, in comparison with the observations, the MAE, MBE and RMSE of daily ET_a estimates with T-SEBAL are 0.42 mm, 0.1 mm, and 0.52 mm, respectively, which are all smaller than the results with SEBAL, that is, 0.58 mm, 0.49 mm, and 0.68 mm, respectively.

Distribution of daily actual ET given by both T-SEBAL and SEBAL in DOY75, DOY 183, DOY 345, and DOY 267 are plotted in Figure 10 (left and middle columns). In addition, the differences between the T-SEBAL estimates and SEBAL estimates are also plotted in Figure 10 (right column). We may find that, as expected, ET_a estimates with T-SEBAL and those with SEBAL have similar spatial pattern. However, there are also some quite significant differences. Firstly, ET_a estimates by T-SEBAL has an overall negative bias compared with those given by SEBAL in DOY183, and overall positive biases in DOY 75 and DOY345. Secondly, there exist clear differences in ET_a estimates in the Dragoon Mountain area (on the upper right side). SEBAL gives high ET_a estimates (higher than the average throughout the scene) in the mountain area in DOY75, DOY183, and DOY267, whereas T-SEBAL shows lower ET_a estimates. As we know, the Dragoon Mountain area is generally rocky and poorly vegetated, thereby should have lower ET than surrounding areas, we believe that ET_a estimates by T-SEBAL are more acceptable than those by SEBAL.

We further compared the average ET_a estimate over the WGEW by the two models with average antecedent precipitation in the previous 10 days in the 15 dates we studied, shown in Figure 11. Clearly, ET_a estimates by T-SEBAL have a better relationship with antecedent precipitation than those by SEBAL, indicating that ET_a estimates by T-SEBAL are physically sounder.

Figure 10. Spatial distribution of daily ET_a (mm) estimated by T-SEBAL (**left column**) and SEBAL (**middle column**) and their differences (T-SEBAL estimates minus SEBAL estimates) (**right column**) in four dates.

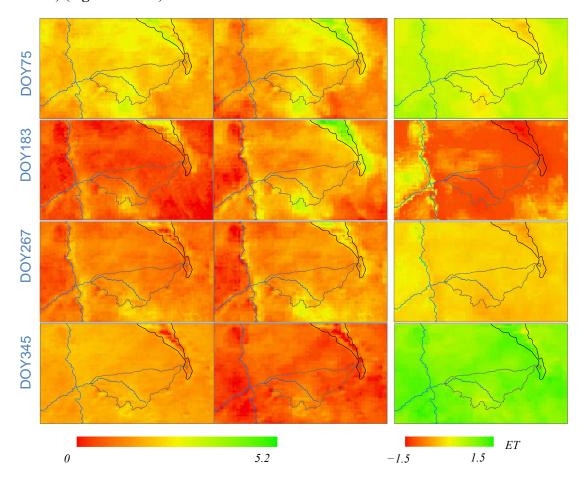
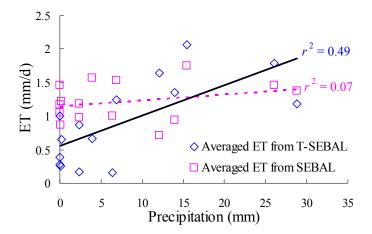


Figure 11. Comparison of the average ET_a estimated by T-SEBAL and SEBAL vs. 10-day antecedent precipitation over the WGEW.



5. Sensitivity Analysis

To assess the robustness of the T-SEBAL model, sensitivity analysis is conducted to investigate model sensitivity to variations of several important parameters and variables, including: land surface

temperature T_s that is derived from MODIS product; air temperature T_a , relative humidity U, and wind speed u that are observed on the ground; minimum canopy resistance r_{cm} , the ratio of G/R_n , and albedos of four vertices that are set empirically or by calibration.

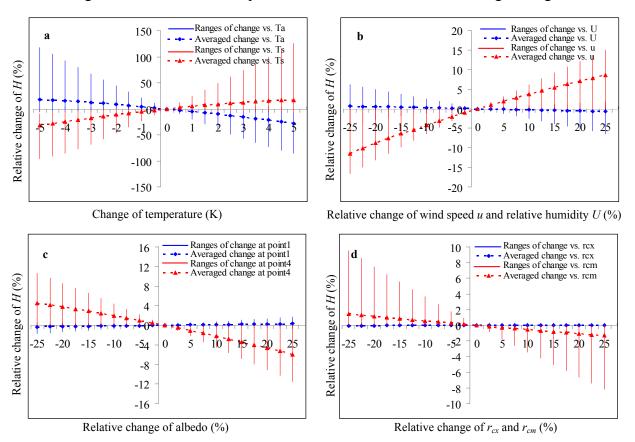
As sensible heat flux H is the essential output of the T-SEBAL model, the sensitivity analysis is conducted based on the change of H estimates in response of input changes. The sensitivity S_i of T-SEBAL to an input i is defined as [25]:

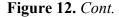
$$S_i = (\frac{H_{\pm} - H_0}{H_0}) \times 100\% \tag{18}$$

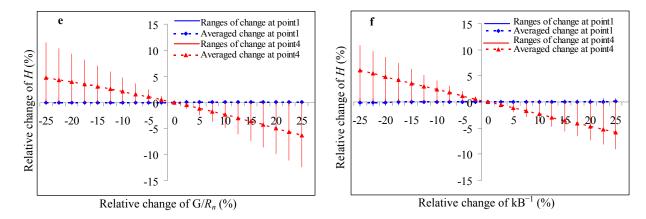
where, H_0 , H_+ and H_- are the sensible heat flux estimated by T-SEBAL when the input equals its reference value i_0 , is increased and is decreased, respectively, with reference values used for all other inputs.

In the present study, H_{\pm} and H_0 are the mean values of the whole region as shown in Figure 4. The following sensitivity analysis results are based on the estimation of H for 15 dates. A deviation of 5 K with a step of 0.5 K is used to test the sensitivity to T_s and T_a , whereas a 25% deviation with a step of 2.5% change is used to test the sensitivity to other parameters. The results are presented in Figure 12.

igure 12. Sensitivity of sensible heat flux H to changes of some variables/parameters for 15 dates: (a) land surface and sir temperature; (b) wind speed and relative humidity; (c) albedo; (d) maximum and minimum canopy resistance; (e) ratio of G to R_n ; (f) kB-1. Vertical lines in each plot represent the range of percentage changes of H corresponding to the changes of different variables/parameters. Dashed lines are the average changes.







5.1. Sensitivity to T_s and T_a

Figure 12a shows that T_s is positively correlated with H, while T_a is negatively correlated, and both correlations are approximately linear. Precisely, a 5 K increase in T_s and T_a result in a 16.9% increase and 27.8% decrease in the estimate of H averagely, whereas a 5 K decrease in T_s and T_a lead to 31.4% decrease and 17.9% increase in the estimate of H. In comparison, for SEBAL in a semi-humid region [28], a 5 K decrease or increase in T_s can cause 59.8% decrease or 72.8% increase in the H estimate, which indicates more sensitivity of SEBAL than T-SEBAL.

Because the calculation of the land surface temperature of extreme points (*i.e.*, $T_{s,n}$, n = 1, 2, 3, 4) are calculated by solving quartic equations of surface temperature at extreme conditions, therefore, the changes of pixel T_s do not affect the calculation of $T_{s,hot}$ and $T_{s,cold}$, but affect the distance to hot point which could increase or decrease dT of pixels, and subsequently affect the estimation of H.

In contrast, T_a is positively correlated with $T_{s,n}$ as shown in Equation (8a-8d). Therefore, an increase in T_a would lead to the increase of $T_{s,n}$ and $(R_n-G)_4$, and consequently put the pixel in the constructed trapezoid toward the cold edge, thereby decrease the estimate of H.

5.2. Sensitivity to Wind Speed and Relative Humidity

Wind speed u is positively related to the H estimate, because the increase in u could result in the increase in friction velocity and the decrease in r_a and $T_{s,n}$, consequently put the T_s -EVI data points to the warm edge, resulting in the increase in H estimate. As shown in Figure 12b, a 25% increase or decrease in u could lead to 8.6% increase or 11.5% decrease in the H estimate on average.

Relative humidity (*U*) has smaller impacts on *H* estimation than wind speed. A 25% increase in *U* would result in only 0.7% decrease in *H*. Such an effect happens because the increase in *U* leads to the increase in ε_a and the decrease in *VPD*, which results in the increase in $T_{s,I}$ and $T_{s,4}$, consequently decrease the dT and H.

5.3. Sensitivity to Albedos at Four Vertices of $T_s \sim VI$ Trapezoid

As the albedos of four vertices are set differently, thereby, the sensitivity to albedo at each point is investigated separately. As shown in Figure 12c, in comparison with other points, the *H* estimation at

point 4 is more sensitive to the change of albedo, with a 25% increase or decrease causing -5.9% or 4.6% deviation in the H estimate. A 25% perturbation at point 1 only causes ~0.3% variation in H. Meanwhile, H is free of any influence by albedo variations at point 2 and point 3.

5.4. Sensitivity to Minimum and Maximum Canopy Resistance

The sensitivity to minimum canopy resistance (r_{cm}) is illustrated in Figure 10d, which indicates the negative correlation between r_{cm} and H estimates. That is, a 25% increase or decrease in r_{cm} could cause 1.3% decrease or 1.5% increase in the H estimate. The cause of such an effect is that, an increase in r_{cm} could result in an increase in the $T_{s,1}$ estimate according to the Equation (8a), which would reduce the temperature difference dT, thereby, reduce the estimate of H.

The maximum canopy resistance (r_{cx}) barely influences H estimation on average as shown in Figure 12d. r_{cx} is a parameter used to calculate $T_{s,2}$, which slightly affects the slope of hot edge and cause marginal influence on H estimation.

5.5. Sensitivity to G/R_n at Four Vertices of $T_s \sim VI$ Trapezoid

The $(G/R_n)_n$ ratio r_n (n = 1, 2, 3, 4, representing 4 vertices in Figure 1) are important parameters for estimating the $T_{s,n}$ of the trapezoidal space. Figure 12e illustrates that, for point 4 (dry bare soil), a 25% increase or decrease in $(G/R_n)_4$ could result in 6.3% decrease or 4.7% increase in the estimate of H. For point 1 (wet full vegetation), H estimation is insensitive to $(G/R_n)_1$, only 0.1% deviation with a 25% perturbation. Meanwhile, H is not influenced by the variation of $(G/R_n)_2$ and $(G/R_n)_3$.

5.6. Sensitivity to kB^{-1} for Canopy and Bare Soil Surface

 kB^{-1} is the crucial variable for the estimation of z_{0h} . In Figure 12f, it is demonstrated that values of kB^{-1} at point 4 (dry bare soil) are negatively related to H estimates, that is, a 25% increase in kB^{-1} for dry bare soil surface causes 5.8% decrease in the estimate of H. While the kB^{-1} for wet full vegetation surface shows little inference on H estimation.

6. Discussions

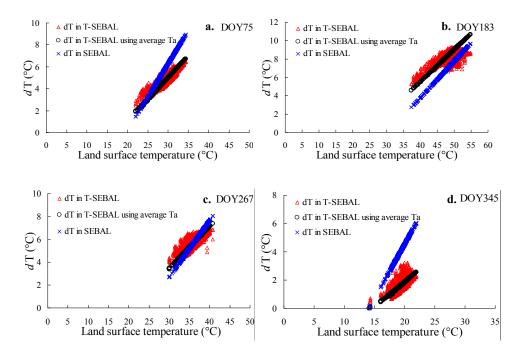
6.1. Comparison between T-SEBAL and SEBAL

T-SEBAL is designed to mitigate the subjectiveness and uncertainty in determining the extreme pixels in SEBAL. It intended to improve the performance of the standard SEBAL in the following two major aspects:

- (1) Avoid the subjective selection of hot point and cold point by calculating hot/cold point temperatures theoretically for the $T_s \sim VI$ trapezoid based on energy balance for the extreme dry/wet cases and replacing hot point with the dry soil vertex and cold point with the wet full vegetation vertex of the $T_s \sim VI$ trapezoid.
- (2) Avoid the requirement of the existence of extreme cold and hot pixels throughout the image scene and consequently avoid the dependence on domain size, by constructing the $T_s \sim VI$ trapezoid on a pixel basis.

According to the design of T-SEBAL model, $T_{s,4}$, $T_{s,1}$, and $(R_n-G)_4$ are unique for each pixel with T-SEBAL, whereas $T_{s,hot}$, $T_{s,cold}$, and $(R_n-G)_{hot}$ are constant throughout the whole image scene with SEBAL. Therefore, the forms of relationships between dT and T_s are different between T-SEBAL and SEBAL (see Figure 13), *i.e.*, T-SEBAL sets up a unique linear relationship for each pixel and consequently the same T_s in different pixels may correspond to different dT, whereas SEBAL builds a unified linear relationship for the whole image and therefore T_s and dT have a linear one-to-one relationship. The major reason that linear relationships between dT and T_s of different pixels are not consistent throughout the image scene with T-SEBAL is the spatial variation in T_a . If we use the average T_a of whole image to simulate the linear relationship, we can see that all pixels have similar linear relationships between dT and T_s , as shown in Figure 13 (dT in T-SEBAL using average T_a).

Figure 13. Comparison of the relationships between dT and land surface temperature (T_s) in T-SEBAL and SEBAL for four dates (a) DOY75; (b) DOY 183; (c) DOy 267; (d) DOY345.



In addition, the spatial variation in T_a affect not only the linear relationship between dT and T_s , but also the correlation between H estimates by T-SEBAL and those by SEBAL. The correlation between H estimation by T-SEBAL when average T_a is used and H estimates by SEBAL is much higher than the results presented in Figure 8, with r up to 1.0, 0.99, 0.98, and 1.0 for DOY75, DOY183, DOY267, and DOY345, respectively. Therefore, considering the spatial variation in T_a when defining temperatures at hot/cold points has significant impact on the estimation of H and subsequently ET_a , and the capability of doing so in T-SEBAL at a pixel basis is one of the reasons that lead to the difference in H estimation by T-SEBAL and SEBAL.

6.2. Comparison with Other Modifications of SEBAL

Considerable efforts have been made in the hydrology remote sensing community on improving the SEBAL model. One important variant of SEBAL is the METRIC model which departs from the SEBAL

model in its use of weather-based reference ET to establish energy balance conditions at a "cold" pixel, but its application still depends on the manual selection of appropriate hot and cold pixels, which is quite different from the approach taken in the present study. A modification of SEBAL quite similar to T-SEBAL is M-SEBAL [19]. However, besides the difference in the formulation for constructing $T_s \sim VI$ trapezoid, there are significant differences in the way of defining the hot point temperature and the way of constructing the cold edge.

The hot point temperature in M-SEBAL is set on the warm edge at the point where the vegetation fraction (f_c) equals that of the pixel ($f_{c,i}$). That means, instead of setting up the linear relationship relating the vertical temperature gradient dT to T_s on the basis of the entire image scene as in SEBAL, the $dT \sim T_s$ relationship is set on the basis of a section of the $T_s \sim f_c$ trapezoid (equivalent to the $T_s \sim VI$ trapezoid) in M-SEBAL. The underlying assumption for setting $dT \sim T_s$ relationship in this way is that, LE is zero on the warm edge and H is zero on the cold edge. In T-SEBAL, however, we assume that LE is zero only on the point of bare soil with the largest water stress, but not on the point of full vegetation with the largest water stress, as it is known that the stomatal transpiration accounts for $\sim 90\%$ of total transpiration [50], which means that even in the case of full stomatal closure there would still be some water loss. Therefore, in the T-SEBAL, the temperature at the hot point is set the same as the temperate at the point of bare soil with the largest water stress, and the $dT \sim T_s$ relationship is set on the basis of the whole $T_s \sim VI$ trapezoid.

The cold edge in M-SEBAL is taken as the air temperature at the image time. But as shown in Figure 7, where the air temperature is used as the cold point temperature mostly (14 out of 15 dates) in SEBAL, the air temperature is consistently higher than the calculated cold point temperatures in T-SEBAL, just contrary to the statement of Long *et al.*, who argued that the use of T_a to substitute for the theoretical cold edge would underestimate the surface temperatures over sparsely vegetated surfaces without water stress [19]. Such a temperature difference at the cold edge would result in the overestimation of LE for the SEBAL model, as shown in Figure 9.

6.3. Limitations of T-SEBAL

There are several aspects of T-SEBAL needed to be worked on further, including:

- (1) The process of extrapolating/interpolating meteorological variables based on data at a limited number of observation sites may introduce some errors. As shown in the sensitivity analysis, the model is sensitive to air temperature and wind speed. However, only the extrapolation of air temperature is treated considering the effects of topography and LAI, whereas the wind speed is simply taken as an average of the three meteorological observation sites in our cased study area. Furthermore, although the effects of topography and LAI are considered, the accuracy of air temperature extrapolation/interpolation is still not always satisfying.
- (2) The parameterization under extreme conditions for constructing the T_s ~VI trapezoid need to be improved, such as ratios of G/R_n at extreme conditions. Compared with the G estimation with Equation (3), the method suggested by Equation (4) shows better fitness, therefore, the Equation (4) is used to estimate G in both SEBAL and T-SEBAL in this paper, and the G/R_n at full vegetation and bare soil surface are set as 0.05 and 0.28, respectively. However, those rates do not consider the effect of soil moisture, whereas many experiments have shown the differences in G/R_n for dry

and wet conditions (e.g., [30]), therefore, at point 3 (wet bare soil) and point 4 (dry bare soil) we set the ratio of G/R_n to be 0.15 and 0.35, respectively. In addition, several other intermediate parameters (e.g., albedo, ε_s , r_{cx} and r_{cm}) are also set using empirical values. The parameterization of the model for other types of ecosystems need to be further evaluated.

(3) There are many formulas available for calculating aerodynamic resistance r_a with different assumptions and complexity, as well as for the estimation of the dimensionless parameter kB⁻¹ which is used to define the relationship between momentum and heat roughness length. We found that different choice of the formula for either r_a or kB⁻¹ may have significant impacts on ET_a estimation results. In addition, as the land surface radiometric temperature T_s, instead of the aerodynamic temperature T_{aero} , is used in the process of constructing $T_s \sim VI$ trapezoid, the kB⁻¹ has to be adjusted, and actually has little to do with the kB^{-1} parameter when T_{aero} is used [51]. To avoid any confusion, Troufleau et al. (1997) even suggested using the term "radiometric kB⁻¹" as a contrast to the theoretical aerodynamic kB⁻¹ [51]. Norman and Becker (1995) also recommended the use of a different notation to avoid unnecessary confusion between the theoretical and empirically adjusted excess resistance [52]. Verhoef et al. (1997) [37] even conclude that the concept of kB^{-1} is questionable, but on the other hand, using the bulk transfer equation to calculate sensible heat from remotely sensed surface temperature requires the use of kB⁻¹ [35]. As a consequence of using the adjusted "radiometric kB⁻¹", the calculation of aerodynamic resistance r_a is different from the theoretical aerodynamic resistance r_a . That is why we used two formulas for calculating aerodynamic resistance However, the theoretical basis of doing so need further investigation.

7. Conclusions

The surface energy balance algorithm for Land (SEBAL) is widely used to estimate actual evapotranspiration (ET_a). Two major disadvantages of SEBAL model are its requirement of the existence of extreme cold and hot pixels in the study area, and the subjectiveness in selecting the two extreme pixels. A modified version of SEBAL model, T-SEBAL, is proposed in the present study to determine the extreme cold/hot points using a parameterized procedure based on the theoretical trapezoidal relationship between land surface temperature (T_s) and Enhanced vegetation index (EVI), so as to reduce the uncertainty in selecting hot and cold pixels and make the SEBAL model more robust.

The T-SEBAL model avoids the subjective selection of hot point and cold point in SEBAL model, does not need the existence of extreme cold and hot pixels throughout the image scene, and therefore has no dependence on domain size. In addition, as T-SEBAL sets up a unique linear relationship between dT (difference between aerodynamic temperature and air temperature) and T_s on a pixel basis, whereas SEBAL builds a unified linear relationship for the whole image, therefore T-SEBAL model has better capability to characterize the spatial variability of complex landscapes. The performances of the classical SEBAL model and T-SEBAL are compared for estimating ET_a for a semi-arid area, the Walnut Gulch Experimental Watershed, in USA, for 15 dates in 2004. The results of latent heat flux LE estimation demonstrate that, T-SEBAL model outperformed the classical SEBAL model in terms of root mean square error (RMSE), mean absolute error (MAE) and mean bias error (MBE), that is, $49.6 \text{ W} \cdot \text{m}^{-2}$, $40.4 \text{ W} \cdot \text{m}^{-2}$ and $14.4 \text{ W} \cdot \text{m}^{-2}$ with T-SEBAL vs, $57.3 \text{W} \cdot \text{m}^{-2}$, $48.9 \text{ W} \cdot \text{m}^{-2}$ and $45.8 \text{ W} \cdot \text{m}^{-2}$

with SEBAL, respectively. Additionally, for the 15 dates studied in the present study, the MAE, MBE, and RMSE of daily ET_a estimates with T-SEBAL are 0.42 mm, 0.1 mm, and 0.52 mm, respectively, which are all smaller than the results of SEBAL, that is, 0.58 mm, 0.49 mm, and 0.68 mm, respectively. In addition, ET_a estimates with T-SEBAL have better physical soundness than with SEBAL in the terms of the relationship between ET_a values with geomorphologic locations and the antecedent precipitation. The results indicate that, with the advantage of calculating hot/cold point temperatures theoretically on a pixel basis, T-SEBAL has better applicability for complex landscapes than standard SEBAL model.

There are several aspects of T-SEBAL needed to be worked on further, including the way of extrapolating meteorological variables based on data at a limited number of observation sites, the parameterization under extreme conditions for constructing the T_s -VI trapezoid, and the formulation of kB^{-1} and the aerodynamic resistance r_a .

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Author Contributions

Xiaogang Wang implemented the algorithm, Wen Wang designed the algorithm, Dui Huang conducted the sensitivity analysis, Bin Yong made the comparison with the results in the literature, Xi Chen checked the algorithm code and application results.

Conflicts of Interest

The authors declare no conflict of interest.

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