## **Supporting Information**



Figure S1. Comparison of catalytic performances of our catalyst 0.04Sr-Ho<sub>2</sub>O<sub>3</sub> and three reference catalysts at different temperatures: (a) CH<sub>4</sub> conversion and (b) C<sub>2</sub>-C<sub>3</sub> selectivity.
(▼) 0.04Sr-Ho<sub>2</sub>O<sub>3</sub>-NS, (▲) 0.04Sr-La<sub>2</sub>O<sub>3</sub>, (●) 3%Li/MgO, (■) 0.04Sr-CeO<sub>2</sub>.



**Figure S2.** TEM image of Ho<sub>2</sub>O<sub>3</sub>-NP.



Figure S3. XPS spectra of O 1s on  $Ho_2O_3$ -NP (a),  $Ho_2O_3$ -NS (b),  $0.02Sr-Ho_2O_3$ -NS (c),  $0.04Sr-Ho_2O_3$ -NS (d) and  $0.06Sr-Ho_2O_3$ -NS (e).



Figure S4. The typical GC chromatograms detected by a FID (a) and a TCD (b).



Scheme S1. Proposed reaction mechanism of methane transformation to ethane, ethylene, propane and propylene.