

Figure S1. XRD patterns of P-modified ferrierite zeolites calcined at 500 °C.

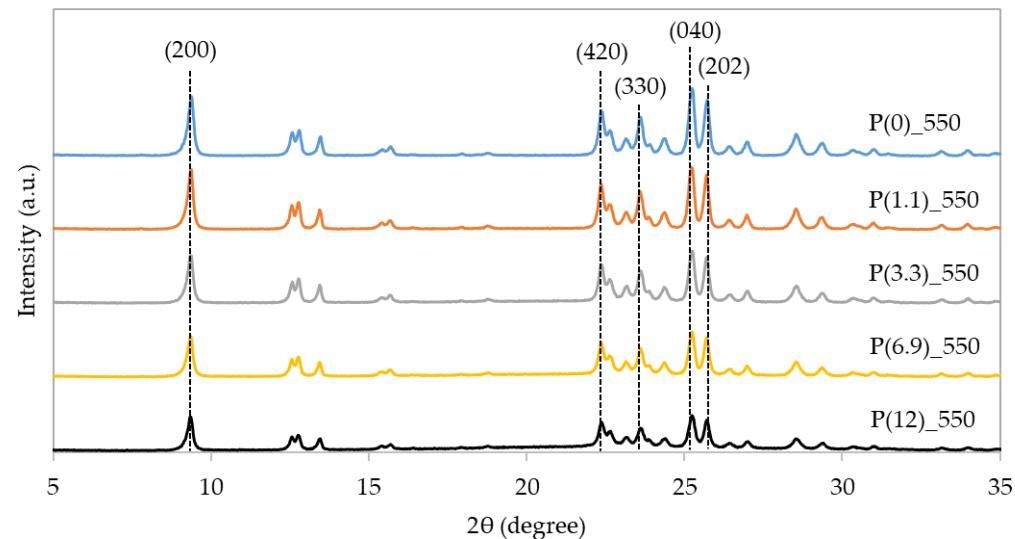


Figure S2. XRD patterns of P-modified ferrierite zeolites calcined at 550 °C.

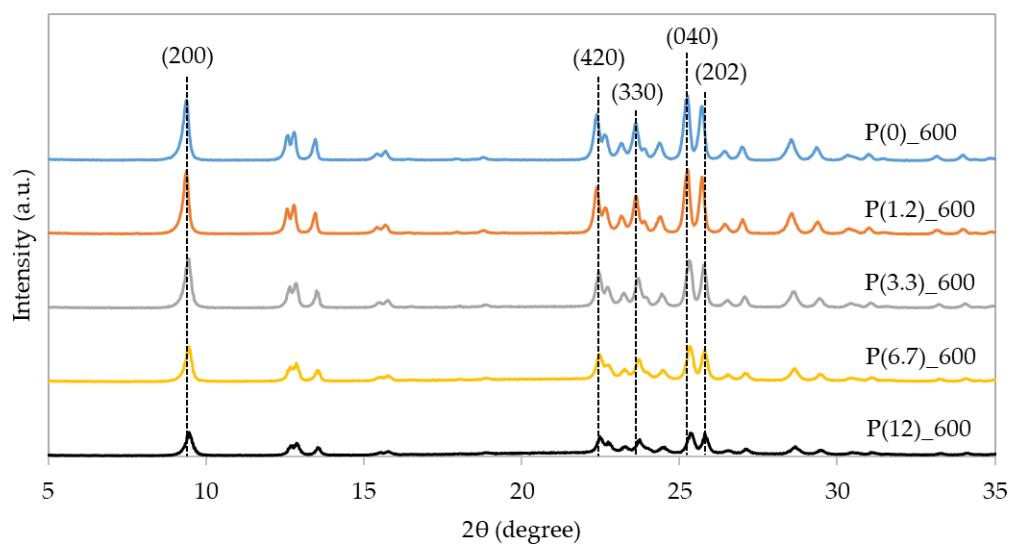


Figure S3. XRD patterns of P-modified ferrierite zeolites calcined at 600 °C.

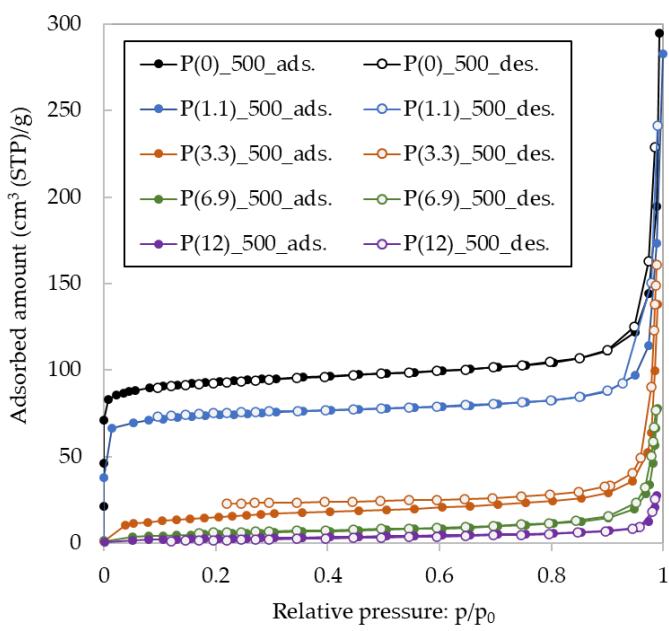


Figure S4. N₂ adsorption-desorption isotherms for P-modified ferrierite zeolites calcined at 500 °C.

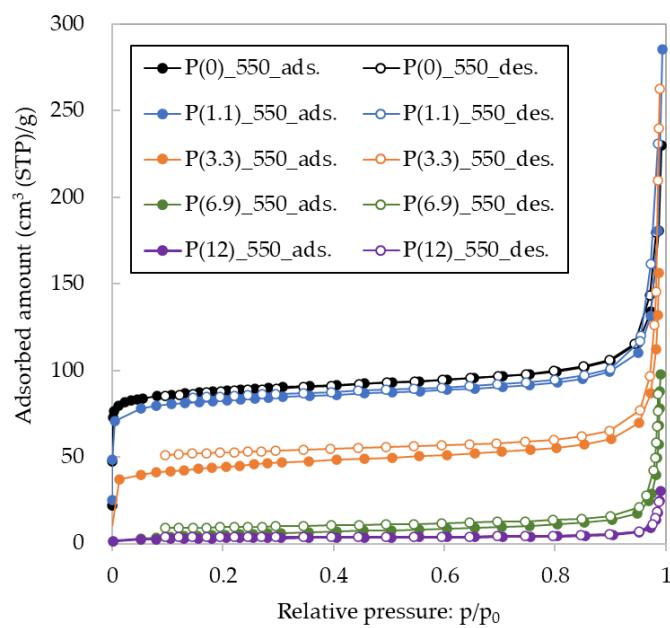


Figure S5. N₂ adsorption-desorption isotherms for P-modified ferrierite zeolites calcined at 550 °C.

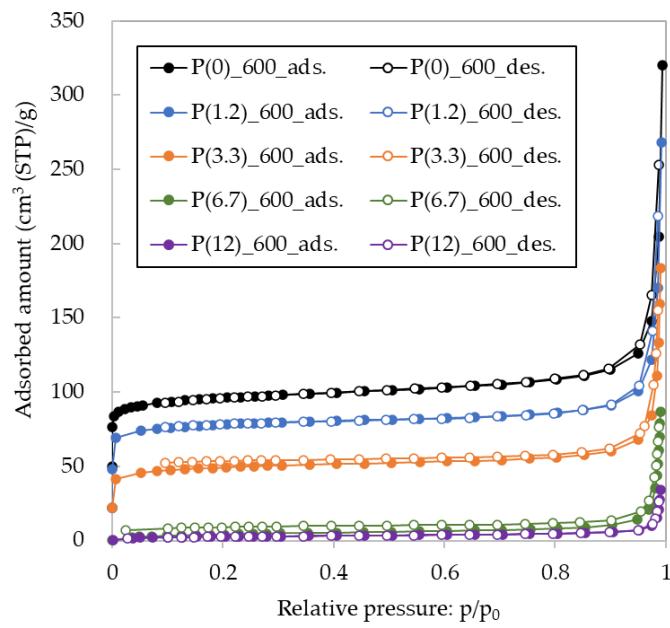


Figure S6. N₂ adsorption-desorption isotherms for P-modified ferrierite zeolites calcined at 600 °C.

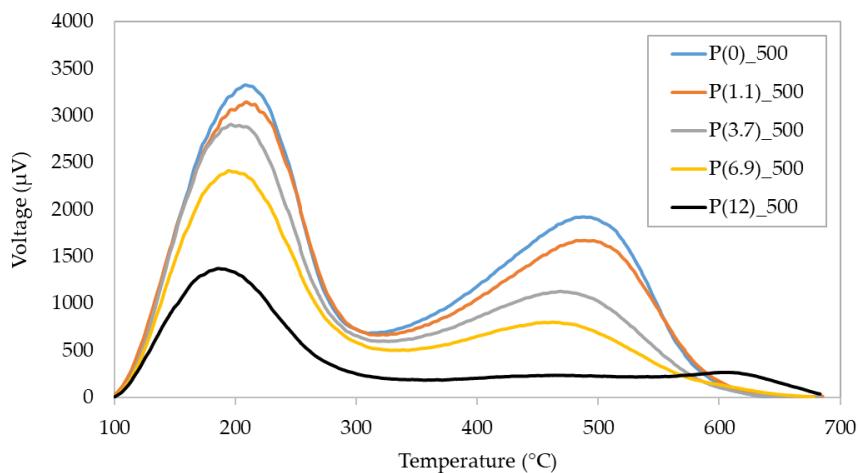


Figure S7. NH₃-TPD profiles for P-modified ferrierite zeolites calcined at 500 °C.

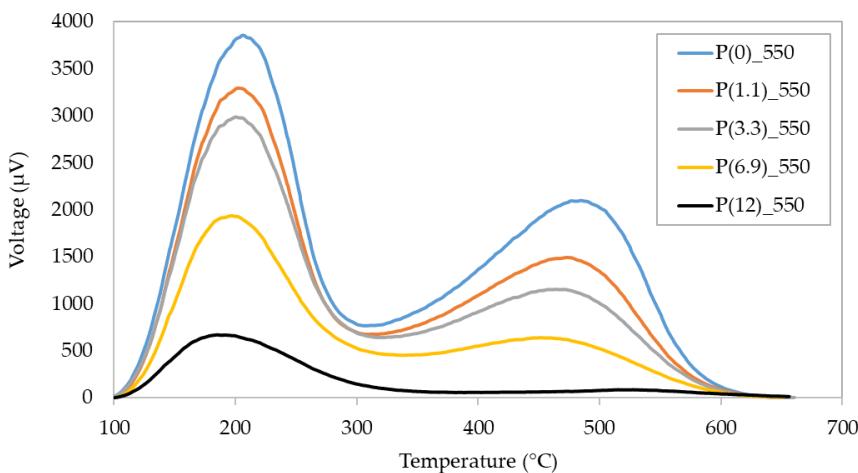


Figure S8. NH₃-TPD profiles for P-modified ferrierite zeolites calcined at 550 °C.

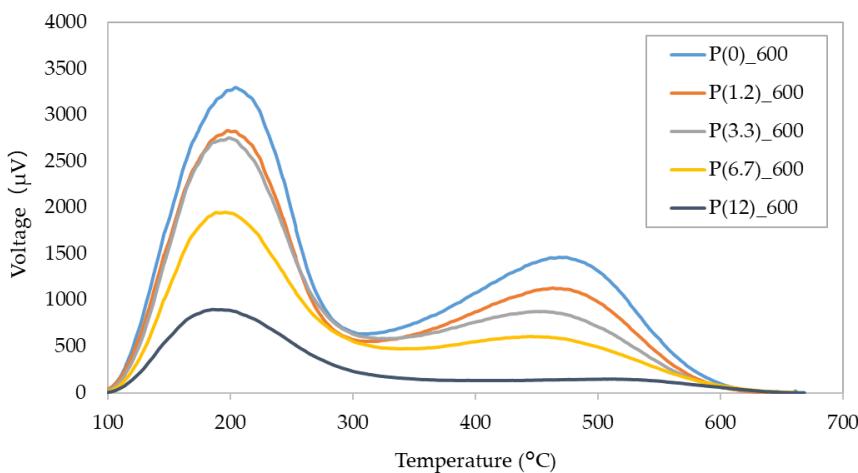


Figure S9. NH₃-TPD profiles for P-modified ferrierite zeolites calcined at 600 °C.

Table S1. Supplementary table for multiple regression analysis.

| P-loaded zeolite | Micropore surface area $\text{m}^2 \text{ g}^{-1}$ | External surface area $\text{m}^2 \text{ g}^{-1}$ | Total pore volume $\text{cm}^3 \text{ g}^{-1}$ | Micropore volume $\text{cm}^3 \text{ g}^{-1}$ | Weak acid mmol g^{-1} | Strong acid mmol g^{-1} | <i>n</i> -butene yield C-mol% |
|-----------------------|--|---|--|---|--------------------------------------|--|-------------------------------------|
| | X1 | X2 | X3 | X4 | X5 | X6 | y |
| P(0)_450 | 352 | 28 | 0.37 | 0.11 | 1.446 | 1.428 | 31.2 |
| P(1.4)_450 | 339 | 22 | 0.27 | 0.11 | 1.388 | 1.303 | 4.6 |
| P(3.3)_450 | 168 | 21 | 0.20 | 0.06 | 1.083 | 1.02 | 0.2 |
| P(6.9)_450 | 13 | 12 | 0.11 | 0.01 | 0.735 | 0.833 | 0.0 |
| P(12)_450 | 5 | 5 | 0.04 | 0.00 | 0.536 | 0.6 | 0.2 |
| P(0)_500 | 460 | 27 | 0.37 | 0.14 | 1.397 | 1.305 | 27.8 |
| P(1.1)_500 | 361 | 21 | 0.29 | 0.11 | 1.340 | 1.153 | 4.5 |
| P(3.7)_500 | 34 | 20 | 0.23 | 0.02 | 1.121 | 0.831 | 0.3 |
| P(6.9)_500 | 6 | 14 | 0.14 | 0.00 | 0.894 | 0.658 | 0.0 |
| P(12)_500 | 4 | 6 | 0.05 | 0.00 | 0.504 | 0.379 | 0.0 |
| P(0)_550 | 436 | 27 | 0.33 | 0.13 | 1.449 | 1.368 | 29.8 |
| P(1.1)_550 | 392 | 25 | 0.37 | 0.12 | 1.235 | 1.059 | 2.5 |
| P(3.3)_550 | 189 | 24 | 0.32 | 0.06 | 1.097 | 0.859 | 0.2 |
| P(6.9)_550 | 8 | 11 | 0.15 | 0.01 | 0.633 | 0.538 | 0.0 |
| P(12)_550 | 9 | 3 | 0.04 | 0.00 | 0.256 | 0.115 | 0.0 |
| P(0)_600 | 474 | 29 | 0.38 | 0.14 | 1.324 | 1.027 | 19.8 |
| P(1.2)_600 | 383 | 19 | 0.35 | 0.11 | 1.189 | 0.893 | 3.9 |
| P(3.3)_600 | 229 | 16 | 0.28 | 0.07 | 1.009 | 0.733 | 0.3 |
| P(6.7)_600 | 6 | 9 | 0.13 | 0.03 | 0.698 | 0.592 | 0.0 |
| P(12)_600 | 5 | 4 | 0.05 | 0.03 | 0.328 | 0.201 | 0.3 |
| Average | 194 | 17 | 0.22 | 0.06 | 0.983 | 0.845 | 6.3 |
| Standard deviation | 187 | 9 | 0.13 | 0.05 | 0.385 | 0.375 | 11.0 |

Correlation coefficients (r_{ij})

| $x_i \backslash x_j$ | x_1 | x_2 | x_3 | x_4 | x_5 | x_6 | y |
|----------------------|-------|-------|-------|-------|-------|-------|-------|
| x_1 | 1.000 | | | | | | 0.706 |
| x_2 | 0.860 | 1.000 | | | | | 0.666 |
| x_3 | 0.915 | 0.946 | 1.000 | | | | 0.621 |
| x_4 | 0.988 | 0.847 | 0.909 | 1.000 | | | 0.700 |
| x_5 | 0.869 | 0.960 | 0.923 | 0.856 | 1.000 | | 0.636 |
| x_6 | 0.818 | 0.906 | 0.828 | 0.805 | 0.956 | 1.000 | 0.690 |
| y | 0.706 | 0.666 | 0.621 | 0.700 | 0.636 | 1.000 | 1.000 |