



Article Optical and Geometrical Characterizations of Non-Linear Supramolecular Liquid Crystal Complexes

Hoda A. Ahmed ^{1,2}, Mohamed Hagar ^{2,3,*}, Omaima A. Alhaddad ⁴ and Ayman A. Zaki ^{5,6,*}

- ¹ Faculty of Science, Department of Chemistry, Cairo University, Cairo 12613, Egypt; ahoda@sci.cu.edu.eg
- ² College of Sciences, Chemistry Department, Taibah University, Yanbu 30799, Saudi Arabia
- ³ Faculty of Science, Chemistry Department, Alexandria University, Alexandria 21321, Egypt
- ⁴ College of Sciences, Chemistry Department, Madina Monawara, Taibah University, Al-Madina 30002, Saudi Arabia; alhaddad105@yahoo.com
- ⁵ College of Sciences, Physics Department, Taibah University, Yanbu 30799, Saudi Arabia
- ⁶ Faculty of Sciences, Physics Department, Banha University, Banha 13518, Egypt
- * Correspondence: mohamedhaggar@gmail.com (M.H.); ayman_a73@hotmail.com (A.A.Z.)

Received: 18 July 2020; Accepted: 5 August 2020; Published: 14 August 2020



Abstract: Nonlinear architecture liquid crystalline materials of supramolecular 1:1 H-bonded complexes (**I/II** and **I/III**) were prepared through a self-assembly intermolecular interaction between azopyridine (**I**) and 4-*n*-alkoxybenzoic acid (**II**) as well as 4-*n*-alkoxyphenylazo benzoic acid (**III**). The H-bond formation of the prepared supramolecular hydrogen bonded (SMHB) complexes was confirmed by Fourier-transform infrared spectroscopy (FT-IR) and differential scanning calorimetry (DSC). Optical and mesomorphic behaviors of the prepared complexes were studied by polarized optical microscopy (POM) as well as DSC. Theoretical calculations were performed by the density functional theory (DFT) and used to predict the molecular geometries of the synthesized complexes, and the results were used to explain the experimental mesomorphic and optical properties in terms of their estimated thermal parameters. Ordinary and extraordinary refractive indices as well as birefringence at different temperatures were investigated for each sample using an Abbe refractometer and modified spectrophotometer techniques. Microscopic and macroscopic order parameters were calculated for individual compounds and their supramolecular complexes.

Keywords: nonlinear supramolecular liquid crystal complexes; optical studies; refractive index; birefringence; DFT theoretical calculations

1. Introduction

Many liquid crystalline compounds display one or more distinct mesophases depending on the basis of the molecular arrangement such as nematic (N) and smectic phases [1–3]. Optical properties, such as absorbance, transmittance, refractive index and birefringence are very important for liquid crystal (LC) applications. Transmission with a long temperature range was measured for nematic LC [4]. Additionally, the index of refraction and birefringence were determined by wedge and Newton's rings techniques for LC in the N-Sm phase [5–8]. Yildiz et al. used Abbe refractometer and rotating-analyzer techniques for measuring ordinary (n_o) and extraordinary (n_e) refractive indices and birefringence (Δn) [5,9]. In addition, the dependence of birefringence on temperature was studied for LCs [10–18]. The factors of the birefringence, of thermal stability and order parameter were also reported [19,20]. Recently, supramolecular liquid crystals (SMLCs) intensively attracted the attention of many scientific research studies [21–31]. Among the self-assembly method LCs is H-bonding intermolecular interactions with noncovalent bonds [32–36]. Among the H-bond acceptors

and donors, pyridine derivatives and carboxylic acids were shown to be the best choice in many studies. Furthermore, the use of multifunctional compounds in the establishment of noncovalent interaction could produce good properties of SMLC network architectures [37,38]. The photoresponsive properties of azopyridines make them a good choice for liquid-crystal materials due to their aptitude for thermal and photo *trans-cis*-isomerisation [39,40]. Recently, the designing of new structures according to computational prediction attracts the attention of many researchers [39,41–50]. Studying the optical parameters of the LCs requires some information about the molecular geometries. The DFT method becomes an effective tool for its excellent performance and consistency with the experimental data [27,28,43,48,51–61].

The aim of the present work was to design angular H-bonded supramolecular complexes (Scheme 1) of new conformations and investigate their optical properties using different techniques. In addition, DFT theoretical calculations were carried out to estimate the molecular geometry of the prepared H-bonded complexes as well as to predict their thermal parameters. Ordinary and extraordinary refractive indices, birefringence and order parameters were measured and compared for all supramolecular H-bonded complexes.



(b) I/III

Scheme 1. 1:1 SMHB complexes (a) I/II and (b) I/III.

2. Experimental

Preparation of 1:1 Supramolecular Complexes

4-*n*-Octyloxybenzoic acid (II) was purchased from Merck Company (Germany). The transition temperature of the azopyridine-based derivative (I) was checked with the previously reported one [62,63].

Equal molar amounts of the individual components of the target SMHBLCs complex (I/II and I/III) was melted with stirring till an intimate blend then cooled to room temperature (Scheme 2) [64,65].



(b) I/III

Scheme 2. Preparation of 1:1 SMHB complexes (a) I/II and (b) I/III.

3. Results and Discussion

3.1. FT-IR Spectroscopic Confirmation of SMHB Complex Formation

The spectral data of the FT-IR were recorded in order to prove the H-bonded supramolecular complex formation. The spectra were measured for individual components as well as their supramolecular complexes I/II and I/III (Figure 1). The C=O stretching vibration is well known to be at 1681 cm⁻¹ [66–68]. The formation of the H-bonding between the proton acceptor nitrogen atom and the COOH group of the H-donor of acid exchanged the dimeric H-bonds of carboxylic acid.

The sharing of the hydroxyl group of the COOH in H-bonding decreased its vibrational strength. As shown from Table 1, theoretically, the length of OH-bond increased from 0.97573 Å with H-bonding to 1.032 and 1.038 Å for complexes I/II and I/III, respectively. Moreover, its stretching vibration decreased to 2561.3 cm⁻¹ instead of 3662.6 cm⁻¹ of the free acid for the complex I/II. Experimental FT-IR spectra illustrated that there was no considerable impact of the H-bonding on the C=O strength vibration, where, there was only a 4 cm⁻¹ decrease ($v_{C=O} = 1681.7 \text{ cm}^{-1}$). However, the ester linkage of the azopyridine base C=O group influenced the stretching vibration; the wavenumber of C=O of the complex I/II increased from 1724.4 to 1728.1 cm⁻¹ and 1734.0 cm⁻¹ for the other, I/III. Furthermore, an important provident of the H-bonding in the supramolecular complexes (SMCs) is the existence of three Fermi resonating frequencies of the OH group, A-, B- and C-types [50,69–74]. The Fermi band of the A type existed in the range of 2912 to 2835 cm⁻¹ under the C-H stretching vibrations. Furthermore, the important vibrational frequency of the O-H (B-type) at 2352 cm⁻¹ could be assigned to the in-plane bending stretching vibration. However, the Fermi band of the C-type of the interaction of the stretching vibration of the OH and the overtone of the torsional effect was in the range of 1901.3 and 1902.8 cm⁻¹.

Compound	^Ú ОН (ст ⁻¹)	О-Н (Å)	ύ _{C=0} (cm ⁻¹)	C=O (Å)	^Ú C=NPyr (cm ^{−1})	C=N _{Pyr} (Å)	^Ú Nr=NPyr (cm ^{−1})	N=N _{Pyr} (Å)	${}^{\acute{ u}_{ ext{H-bond}}}$ (cm $^{-1}$)	H-Bond (Å)
Ι	-	-	-	-	1615.9	1.347	1475.6	1.211	-	-
II	3662.6	0.976	1691.9	1.238	-	-	-	-	-	-
III	3660.7	0.976	1691.1	1.237	-	-	1475.8	1.282	-	-
I/II	2561.3	1.032	1668.5	1.251	1617.7	1.348	1475.5	1.281	2561.3	1.619
I/III	2469.9	1.038	1669.1	1.250	1618.2	1.348	1475.4	1.282	2469.9	1.597

Table 1. The calculated bond length (Å) wave numbers (cm⁻¹) of characteristic groups of the base **I**, acids **II** and **III** and their supramolecular complex **I**/**II** and **I**/**III**.



Figure 1. FT-IR spectrum of azopyridine base I, acids II and III, as well as their 1:1 supramolecular H-bonded complex I/II and I/III.

3.2. Mesomorphic Properties

Differential scanning calorimetry (DSC) measurements were recorded to study the mesomorphic transition behavior of 1:1 SMHB complexes I/II and I/III, and the type of mesophases was proved by measuring the polarized optical microscopy (POM). Thermal analyses of these complexes were recorded from the second heating scan and the DSC profiles upon heating/cooling cycles for I/II and I/III SMHB complexes (Figure S1, Supplementary Materials). Illustrative textures of the investigated mesophases from the POM are shown in Figure 2. The 1:1 molar supramolecular complex formation can also be confirmed from the crystallization peak symmetry (Figure S1).



Figure 2. Optical photomicrographs of compounds I and II and their complexes I/II and I/III upon heating.

The azopyridine (I) mesophase behavior was observed to have a smectic A (SmA) phase with a stability of 121.5 °C [65,75], while the 4-octyloxybenzoic acid (II) was dimorphic, exhibiting smectic C (SmC) and nematic (N) phases with a mesomorphic stability of 147 °C [62,63], and 4-octyloxy phenylazobenzoic acid (III) exhibited a SmC phase with a wide range of stability and an N phase with a very small stability range [75]. Therefore, the investigation of the mesophase behavior of the supramolecular complexes resulted from mixing the compounds with different mesogenic lengths (I/II and I/III) is an interesting study. Transition temperatures and associated enthalpies of transitions for the individual base and acids moiety as well as their corresponding 1:1 molar supramolecular complexes (I/II and I/III) are listed in Table 2. As can be seen from Table 2, upon heating, the complex I/II indicated an endothermic peak with 27.4 kJ/mol followed by a small endothermic smectogenic peak with 1.5 kJ/mol. The complex I/III illustrated a strong endothermic peak with 46.0 kJ/mol ascribed to the melting process, and an endothermic peak with 7.2 kJ/mol was assigned to the SmA-N transition followed by a small peak of nematic transition with 3.5 kJ/mol. Thus, the variation of peak enthalpy changed between the individual compounds and their SMHB complexes, which may be attributed to the different molecular geometries of each component. Data in Table 2 show that the I/II complex exhibited a monomorphic smectic A phase (SmA) with a thermal stability of 104.6 °C, while the second complex I/III possessed a dimorphic phase of enantiotropic SmC and N meophases with a higher thermal stability (198.7 °C). It can be concluded that the incorporation of azophenyl moiety in the acid component III leads to an enhancement of the thermal stability (i.e., the mesogenic core length is influenced by the mesophase stability) of their supramolecular complex I/III rather than I/II.

Sample	T_{Cr-SmC}	ΔH_{Cr-SmC}	T _{Cr-SmA}	ΔH_{Cr-SmA}	T _{SmC-N}	$\Delta H_{\rm SmC-N}$	T _{SmA-I}	$\Delta H_{\rm SmA-I}$	T_{N-I}	ΔH_{N-I}
Ι	-	-	96.1	23.5	-	-	121.5	1.6	-	-
Π	101.0	47.0	-	-	108.0	4.7	-	-	147.0	1.9
III	147.0	55.6	-	-	241.0	7.9	-	-	262.5	3.2
I/II	-		76.4	27.4	-		104.6	1.5	-	-
I/III	91.8	46.0	-	-	137.0	7.2	-	-	198.7	3.5

Table 2. Phase transition temperatures (T, $^{\circ}$ C) and enthalpy of transition (ΔH , kJ/mol) for the individual compounds (I, II and III) and their supramolecular complexes (I/II and I/III).

Cr = solid crystal; N = nematic; SmA = smectic A; SmC = smectic C; I = isotropic.

3.3. DFT Calculations

The DFT calculations were performed on a B3LYP 6-31G (d,p) basis set in the gas phase set out by Gaussian 09 software; see supplementary data. Due to the presence of many conformers of the base (I), the thermal parameters of two conformers (Ia and Ib) of less sterically hindered structures were investigated. The results of the theoretical calculations showed that the complexes could be forming a U-shaped geometry. However, the DFT calculations were performed for the isolated molecules in the gas phase at 0 K, and the thermotropic liquid crystals were enhanced in a molten state at a certain temperature range; conformational disorder could appear and strong deviations from the U-shape deduced from calculations could be impacted. Moreover, the actual confirmations in condensed phases could be very different, where the interaction as well as the electronic nature of the surrounding molecules could affect the geometrical structure. The geometry of the complexes was planar, where phenyl rings of the base and the acids were in the same plane. Recently, our group reported that [76] the molecular geometry of the H-bonded complexes might highly influence a certain mesophase behavior. The terminal intermolecular aggregations resulted from the change of the conformation by introduction of the terminal alkoxy chains, which play an important role for mesophase enhancement. The competitive effect of this interaction due to the terminal chain aggregation and the carbonyl ester, in addition to the lateral cohesive interactions, was highly impacted by the length of the terminal alkoxy chain. Moreover, increasing the core length (especially for complex I/III) and the number of side chains helped to induce mesophase formation. Furthermore, it widened the temperature range of the observed mesophase; this was clear in the phase transitions of I/III (Table 2). In our present work, these supramolecular complexes showed a nonlinear (U-shape) geometry which estimated DFT theoretical calculations. The calculated thermal variables, dipole moments and polarizability of both estimated U-shaped structures of SMHBCs I/II and I/III were illustrated in terms of the experimental data of the investigated mesophase, type and stability. The findings could be clarified in terms of the Π - Π aromatic stacking and the association of the flexible alkoxy chains. In general, the effective staking of the aromatic rings could be stabilizing the structure more than the aggregation of the terminals. The pronounced terminal interaction could be a good clarification for the observed nematic mesophase rather than the lateral interaction that enhances the smectic phase (Figure 3).

The predicted data of the DFT theoretical calculations for thermal variables, the polarizability and dipole moment of the individual compounds **Ia**, **Ib**, **II**, **III** and their supramolecular complexes **I/II** and **I/III** are tabulated in Table 3. As shown from Table 3, the stability of the base was dependent on the orientation of the N-atom with respect to the direction of the N=N bond, where the conformer **Ia** showed more stability than **Ib**. Moreover, the H-bonded formation of the complex enhanced the calculated thermal energy. The number of aromatic rings of the carboxylic acid affected the stability of the H-bonding complexes, where, as the number of aromatic rings increased the packing of the molecules by stacking of the aromatic rings increased, and this resulted in an increment in the thermodynamic stability of the molecules [63,66,67,76–79]. It is noteworthy that there was no effect of the H-bond formation on the dipole moment. However, the polarizability of the investigated

compound was highly affected by the H-bond formation 318, 182 and 318 for the individual base I and acids II and III, respectively, and increased to 565, 706 Bohr³ for the H-bonded complexes I/II and I/III. The high polarizability of the complex could be predicted to have the best characteristics in nonlinear optics (NLO) applications.



Figure 3. Optimized geometrical structures of the base I ((a) Ia and (b) Ib), acids (c) II and (d) III and their supramolecular complex (e) I/II and (f) I/III; (•) C-atom; (•) O-atom; (•) N-atom.

Parameter	Ia	Ib	II	III	I/II	I/III
E _{corr}	0.74	0.73	0.35	0.44	1.08	1.17
ZPVE	-1711.82	-1711.82	-810.17	-1150.57	-2522.02	-2862.42
Etot	-1711.78	-1711.78	-810.15	-1150.54	-2521.96	-2862.35
Н	-1711.78	-1711.78	-810.15	-1150.54	-2521.96	-2862.35
G	-1711.91	-1711.91	-810.22	-1150.63	-2522.14	-2862.55
Total Dipole Moment	5.2	7.7	4.3	5.3	4.6	4.2
Polarizability α	474.0	473.3	182.5	318.2	676.8	820.2

Table 3. Thermal parameters (Hartree/Particle) and dipole moment (Debye) of the base **Ia** and **Ib**, acids **II** and **III** and their supramolecular complex **I/II** and **I/III**.

ZPVE: sum of electronic and zero-point energies; Etot: sum of electronic and thermal energies; H: sum of electronic and thermal enthalpies; G: sums of electronic and thermal free energies.

3.4. Frontier Molecular Orbitals and Molecular Electrostatic Potential

The projected ground state isodensity surface projection for the FMOs, HOMO and LUMO, as well as their energies difference (ΔE) of I, II and III and their supramolecular complexes I/II and I/III are shown in Figure 4. Many parameters such as chemical hardness (η) and the global softness (S) might be calculated from the energy gap between HOMO and LUMO of I, II, III, I/II and I/III. These values were calculated as follow:

The hardness:

$$(\eta) = (\mathbf{I} - \mathbf{A})/2 \tag{1}$$

The global softness:

$$(\mathbf{S}) = \mathbf{1}/\Delta \mathbf{E} \tag{2}$$

where I is the ionization energy and A is the electron affinity, $(I - A) = (E_{LUMO} - E_{HOMO})$.

The predicted softness estimated the aptitude of the π electron cloud of more the polarizable compound to be distorted by any interruption during by any chemical reaction associated with an electronic transportation. However, hard less polarizable compounds are rigid enough to resist transfer of electrons. As shown from Table 4, the FMO energy difference and the global softness (S) chemical hardness (η) were significantly affected by the H-bond formation of the complexes I/II and I/III. The H-bond formation between the acid and the base decreased the energy difference

between FMOs (HOMO and LUMO), $\Delta E = 85.97$, 117.34 and 79.07 kcal/mol for the base and acids, respectively; however, it decreased to 73.42 and 67.77 kcal/mol under complex formation for I/II and I/III, respectively. Moreover, the formation of the complex increased the global softness to 0.014 and 0.015 for I/II and I/III instead of 0.012, 0.009 and 0.013 for the base I and acids II and III, respectively. Moreover, the presence of the extra-conjugation of the azo group N=N of the acid III increased the global softness of the H-bonded complex.



Figure 4. The calculated ground state isodensity surface plots for frontier molecular orbitals of (**a**) base **I**, acids (**b**) **II** and (**c**) **III** and their supramolecular complexes (**d**) **I/II** and (**e**) **I/III**; (•) C-atom; (•) O-atom; (•) N-atom.

Compound	E _{HOMO} (Kcal/mol)	E _{LUMO} (Kcal/mol)	ΔE(E _{LUMO} – E _{HOMO}) (Kcal/mol)	$η = \Delta E(E_{LUMO} - E_{HOMO})/2$	$S = 1/\Delta E$
Ι	-149.97	-64.00	85.97	42.98	0.012
II	-151.86	-34.51	117.34	58.67	0.009
III	-143.70	-64.63	79.07	39.53	0.013
I/II	-142.44	-69.03	73.42	36.71	0.014
I/III	-137.42	-69.65	67.77	33.89	0.015

Table 4. Molecular orbital energies, hardness (η) and global softness (S) of base I, acids II and III and their supramolecular complex I/II and I/III.

The charge distribution map for I, II and III and their supramolecular complex I/II and I/III was predicted according to the molecular electrostatic potential (MEP) under the same basis sets (Figure 5). For the negatively charged atomic sites, the red region was located over the aromatic rings and its maximum localized on the carbonyl oxygen of the H-bonded COOH, while alkoxy chains were the blue regions, the least negatively charged atomic sites. Figure 5 shows that there was a considerable impact of H-bond formation on the mapped charge distribution. Recently, our group showed the

relation between the extent and orientation of the mapped charges and the degree of the lateral and terminal interactions [39,41–50]. Such interactions could be used to explain the reason for the variation of the type of the enhanced mesophase in terms of the competitive attractions between end-to-end and side-to-side.



Figure 5. Molecular electrostatic potentials (MEP) of (**a**) base **I**, acids (**b**) **II** and (**c**) **III** and their supramolecular complexes (**d**) **I/II** and (**e**) **I/III**; High negatively charged atomic sites (**the red region**); low negatively charged atomic sites (**the blue region**).

3.5. Refractive Index Measurements

An Abbe refractometer, from Bellingham, England, with a thermostat heating control unit within ± 0.1 °C, was used to determine the refractive index at certain degrees of temperature. The compounds used were exposed to a He-Ne laser source of linearly polarized light (543 nm). The prisms of the Abbe refractometer were modulated for obtaining the planar and homeotropic alignment for measuring n_o and n_e of the LC sample, respectively. The refractive indices n_o and n_e for the compounds (I, II, I/II and I/III) were measured during the cooling process with an accuracy of ± 0.0005 , as in Figures 6–9. It is obvious that as the temperature increased, the values of n_o increased with decrement in n_e values. The sample III needs a high temperature to turn into the liquid crystalline phase, so that the Abbe refractometer cannot measure its refractive indices.



Figure 6. Dependence temperature of refractive indices (\blacksquare) n_0 and (\blacklozenge) n_e for compound I at 543 nm.



Figure 7. Dependence temperature of refractive indices (\blacksquare) n_o and (\blacklozenge) n_e for compound II at 543 nm.



Figure 8. Dependence temperature of refractive indices (■) n_o and (♦) n_e for the complex I/II at 543 nm.



Figure 9. Dependence temperature of refractive indices (\blacksquare) n_0 and (\blacklozenge) n_e for the complex I/III at 543 nm.

The effective geometry α_{eg} parameter represents the spreading of light in the liquid crystals which can be obtained by the following equation [80]:

$$\alpha_{eg} = \frac{n_o}{n_e} \tag{3}$$

Figure 10 shows that the values of α_{eg} for compound I, II, I/II and I/III increased with increment in the temperature in the LC mesophase. At the isotropic phase, the α_{eg} reached unity because of the lower molecular orientation ordering of the material.



Figure 10. Effective geometry parameter α_{eg} for materials (I, II, I/II and I/III) varies with temperatures.

3.6. Birefringence Measurements

3.6.1. Measuring Birefringence by Using Abbe Refractometer

Birefringence Δn of the LC is one of the essential parameters for LCs, which affects the operation of the electro-optic devices [81–83]. Figure 11 shows the values of $\Delta n = n_e - n_o$ for the compounds I, II, I/II and I/III, which were obtained by measuring n_o and n_e at a variable temperature by using a laser light source of wavelength (543 nm). It was noticed that as the temperature increased, the Δn values decreased gradually [81–86].



Figure 11. Temperature dependence of birefringence for materials **I**, **II**, **I/II** and **I/III** at 543 nm. The dots are the measurements of n_0 and n_e , and the solid line corresponds to the fitting by using Cauchy dispersion relation.

The values of birefringence for the individual compounds I and II were greater than that of the supramolecular complex I/II and I/III. The linear geometries of samples I and II caused an enhanced orientational director order, thus increasing the birefringence, while the nonlinear (U-shape) geometries of supramolecular complexes I/II and I/III (as shown in Figure 3) caused a decrement in the director order and birefringence. Additionally, the degree of packing of I/III was higher than that of I/II due to the long aromatic moiety of azo acid III with respect to the alkoxy acid II which caused a higher increase in the value of Δn for I/III than that of I/II, as shown in Figure 11. The values of Δn were plotted with the best fit in Figure 11, where the dots are the values calculated from the measured n_0 and n_e , and the solid line corresponds to the fitting of the curve using the relationship of dispersion of Cauchy.

3.6.2. Measuring Birefringence by Using Modified Spectrophotometer

Birefringence and the transition temperature for LC can be detected from the transmittance spectra during the processes of heating and cooling by using the modified spectrophotometer (MS) technique, as shown in Figure 12 [19,20]. The optical setup consists of diffraction grating (D), rotating disc (Sample, blank, shutter) (R), the mirror (M), the beam splitter (B), the polarizer and analyzer (P_1 and P_2), respectively, and the sample (S) was put into the electric oven with the unit of heating control rate 1 °C/min. Each sample was placed between two slices of the glass separated by four joints of 30 µm thickness in a uniform planar orientation with a parallel director to the cell walls. The edges of the LC cell were sealed with a heat resistant adhesive to avoid the leakage of the material during heating process. The sample cell in the electric oven was placed between two polarizers. The reference

cell was also put between two polarizers, as shown in Figure 12. The intensity of the transmitted light was measured by the (MS) technique as a function of wavelength (200–800 nm) at certain temperatures for compounds I, II, I/II and I/III during heating and cooling temperatures.



Figure 12. Optical set-up of the modified spectrophotometer (MS) technique for measuring the transmittance and phase transition of LC samples, with diffraction grating (D); rotating disk (R); mirror (M); beam splitter (B); two polarizers (P_1 and P_2); and the sample (S) inside electric oven.

Figure 13 indicates the difference in light transmittance at various temperatures with wavelength during the cooling process for the LC sample (I/II) as a representative sample of the data obtained, where the sample was placed between two crossed polarizers. This shape exhibited that the transmittance directly increased from 450 to 550 nm in wavelength and then became almost constant. The increasing transmittance during the LC phase was attributed to the orientational order of the mesogens. The phase transition was measured using the (MS) technique, and the results obtained were consistent with those measured by (DSC) and (POM) methods.



Figure 13. The variable wavelength transmittance for the complex I/II at such temperatures.

Birefringence (Δn) was calculated from the light transmittance of the sample in the LC phase as follows [22,23,34–36]:

$$\Delta n = \frac{\lambda}{\pi t} \sin^{-1} \sqrt{\frac{T_{\perp}(\lambda)}{T_{\parallel}(\lambda)}} \tag{4}$$

where T_{\parallel} and T_{\perp} are the transmission of light produced when the sample was placed between two parallel and crossed polarizers. The values of T_{\perp} and T_{\parallel} at such temperature and wavelength were measured for compounds I, II, I/II and I/III by using the (MS) technique. The sample thickness *t* was measured using a traveling microscope which was 30 µm. The values of Δn of compounds I, II, I/II and I/III in the LC phase under certain temperatures were measured by using a laser source of wavelength 543 nm, as listed in Table 5. These results are equal to the obtained values of Δn by using the Abbe refractometer within the error (±0.005) at the same wavelength and temperature degrees. The (MS) technique enabled us to measure the birefringence directly by knowing the transmission coefficients at different wavelengths.

Table 5. The values of birefringence Δn (by using the MS technique at 543 nm), Δn_0 and β constant for all compounds.

Sample	Δn Temp. (100 °C)	Δn_o	β
Ι	0.18 ± 0.05	0.35	0.12
II	0.23 ± 0.05	0.55	0.32
I/II	0.16 ± 0.05	0.21	0.02
I/III	0.17 ± 0.05	0.38	0.34

3.7. Order Parameters Measurements

The phase transition in the liquid crystal at the transition point T_C (the clearing temperature point) was accompanied with the emergence of some physical quantities such as microscopic and macroscopic order parameters. The microscopic order parameter *S*, which is responsible for the atomic displacement at the phase transition point T_C , was calculated from the measured values of refractive indices (n_e and n_o) of the LC compounds I, II, I/II and I/III by applying the hypothesis of Vuks as follows [87]:

$$S\left(\frac{\Delta\alpha}{\alpha}\right) = \frac{\left(n_e^2 - n_o^2\right)}{\langle n^2 \rangle - 1} \tag{5}$$

where α and $\Delta \alpha$ are the mean molecular polarizability and the anisotropy polarizability, respectively. The scaling factor $\Delta \alpha / \alpha$ was obtained by using Haller's extrapolation method, and by substituting in Equation (5), the order parameter *S* could be calculated for each sample [20,21,83]. Figure 14 shows the correlation between *S* and Δn for the compounds **I**, **II**, **I**/**II** and **I**/**III**, which was directly proportional.

In addition, the macroscopic order parameter can describe some physical properties such as polarization vector and elasticity of the mesogens in the liquid crystal phase. The macroscopic order parameter Q was related to the birefringence Δn and Δn_0 in the LC and crystalline phase, respectively, as follows [28,29]:

$$Q = \frac{\Delta n}{\Delta n_o} \tag{6}$$

where the value of Δn_0 (at T = 0 °C) can be obtained by using the Haller formula as follows [19–26]:

$$\Delta n = \Delta n_o \left(1 - \frac{T}{T_c} \right)^{\beta} \tag{7}$$

 T_C is the transition point (the temperature transition from LC to the isotropic phase) and β is the material constant. From the relation between Δn and $Ln(1-T/T_C)$, the values of Δn_o and β were

obtained for all samples, as shown in Table 5. As shown in Figure 15, the correlation between Q and Δn appeared directly proportional for the compounds I, II, I/II and I/III.



Figure 14. The variable of microscopic parameter (*S*) with birefringence (Δn) for all samples used.



Figure 15. Variable of macroscopic parameter (*Q*) with birefringence (Δn) for all samples used.

It was noted that the values of *S* and *Q* for the samples I/II and I were greater than those for the compounds I/III and II. This behavior may be attributed to the fact that T_C for I/II and I was measured at the transition from the Smectic to isotropic phase, while for I/III and II, T_C was measured at the transition from the nematic to isotropic phase, which changed the results for the different orientational order parameters for each compound.

It is well known that the mesomorphic and optical activities for certain liquid crystalline compounds depend mainly on mesomeric properties, intermolecular interactions and the stereo conformation of the molecule. In our present study, supramolecular H-bonded complexes, **I/II** and **I/III**, the association of the angular molecules and consequently, their mesophases stabilities depend mainly on several factors, namely: 1. Lateral adhesions of molecules that increase with the alkoxy-chain length. 2. Molecular geometry which varies according the planarity of complexes. 3. The steric effects. 4. End-to-end interaction that varies according to the polarity of the terminals and consequently, the polarizability of

the whole complex. Comparing the thermal stabilities of prepared SMHBCs (I/II and I/III) indicates that all of these parameters (polarity, polarizability, coplanarity), do not have similar effects on the mesomorphic and optical behavior in these investigated complexes.

4. Conclusions

Mesomorphic and optical characterizations were carried out by DSC and polarized optical microscopy (POM) for the compounds I, II and their mixtures (I/II and I/III). The theoretical calculations were performed by the DFT method to predict the geometrical conformation for the present complexes as well as their thermal parameters. Computational calculation results revealed that the H-bonded complexes were of an angular structural shape. Ordinary and extraordinary refractive indices were determined by using the Abbe refractometer technique at different temperatures in the LC phase. Birefringence was also calculated from the difference between the measured data of ne and no and from the transmittance of light at the LC phase of each sample between two crossed and parallel polarizers by using a modified spectrophotometer. The values of birefringence for the individual compounds I and II are greater than that of the supramolecular complex I/II and I/III because of the higher planarity of the individual compounds than that of the coplanar supramolecular complex. Additionally, the values of Δn for I/III were higher than that for I/II due to the long aromatic moiety of azo acid III with respect to the alkoxy acid II, which affects their degree of packing ability. In spite of the higher phase transition temperature decreases for supramolecular complexes than individual compounds, birefringence decreases also. The values of birefringence for the individual compounds I and II are greater than that of the supramolecular complexes I/II and I/III because of the nonlinear (U-shape) geometrical structure of the supramolecular H-bonded complexes. Microscopic and macroscopic order parameters were determined at different temperatures and briefly discussed. Finally, the polarity, polarizability and coplanarity estimated parameters from DFT calculations do not have similar effects on the mesomorphic and optical behavior of the investigated supramolecular complexes.

Supplementary Materials: The following are available online at http://www.mdpi.com/2073-4352/10/8/701/s1, Figure S1: DSC thermograms of 1:1 SMHBCs (a) I/II and (b) I/III at heating rate 10 °C/min upon heating and cooling cycles.

Author Contributions: Data curation, H.A.A., M.H. and A.A.Z.; formal analysis, H.A.A., and O.A.A.; funding acquisition, H.A.A., M.H. and O.A.A.; investigation, H.A.A., M.H. and A.A.Z. and O.A.A.; methodology, H.A.A., A.A.Z.; project administration, M.H. and A.A.Z.; resources, H.A.A., and O.A.A.; software, M.H.; supervision, H.A.A., M.H. and A.Z.; writing—original draft, H.A.A., M.H., A.Z. and O.A.A.; writing—review and editing, H.A.A., M.H. and A.A.Z. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflicts of interest.

References

- 1. De Gennes, P.-G.; Prost, J. The Physics of Liquid Crystals; Oxford University Press: Oxford, UK, 1993; Volume 83.
- 2. Chandrasekhar, S. *Liquid Crystals*; Cambridge University Press: Cambridge, UK; New York, NY, USA, 1994; Volume 49, pp. 587–588.
- 3. Priestly, E. Introduction to Liquid Crystals; Springer: Berlin, Germany, 2012.
- 4. Aleksandriiskii, V.; Novikov, I.; Kuvshinova, S.; Burmistrov, V.; Koifman, O. Dielectric, optical and orientational properties of liquid crystalline 4-alkyloxy-4'-cyanoazoxybenzenes and 4-alkyloxy-4'-cyanoazobenzenes. *J. Mol. Liq.* **2016**, *223*, 1270–1276. [CrossRef]
- 5. Gray, G.W.; Vill, V.; Spiess, H.W.; Demus, D.; Goodby, J.W. *Physical Properties of Liquid Crystals*; John Wiley & Sons: Hoboken, NJ, USA, 2009.
- 6. Wilhelm, E.; Letcher, T. *Heat Capacities: Liquids, Solutions and Vapours*; Royal Society of Chemistry: London, UK, 2010.
- 7. Nalwa, H.S. *Handbook of Low and High Dielectric Constant Materials and Their Applications, Two-Volume Set;* Elsevier: Amsterdam, The Netherlands, 1999.

- 8. Kumar, S. *Experimental Study of Physical Properties and Phase Transitions*; Cambridge University Press: New York, NY, USA, 2001.
- Gramsbergen, E.F.; de Jeu, W.H. First-and second-order smectic-A to nematic phase transitions in p, p'-dialkylazoxybenzenes studied by birefringence. J. Chem. Soc. Faraday Trans. 2 Mol. Chem. Phys. 1988, 84, 1015–1021. [CrossRef]
- 10. Nesrullajev, A. Texture transformations and thermo-optical properties of nematic mesogen at nematic–isotropic liquid phase transition. *J. Mol. Liq.* **2014**, *196*, 217–222. [CrossRef]
- 11. Zaki, A. Optical measurements of mixture thermotropic liquid crystals. *Opt. Lasers Eng.* **2010**, *48*, 538–542. [CrossRef]
- 12. El-Dessouki, T.A.; Roushdy, M.; Hendawy, N.I.; Naoum, M.M.; Zaki, A.A. Optical measurements of thermotropic liquid crystals. *J. Mod. Phys.* **2013**, *4*, 39. [CrossRef]
- 13. Zaki, A.A. Optical measurements and Speckle Photography for thermotropic liquid crystals Mixtures. *J. Mod. Phys.* **2013**, *4*, 517. [CrossRef]
- 14. Miszczykd, E.; Pieceka, W. Application of modified interference wedge method in measurements of indices of refraction and birefringence of nematic liquid crystals. *Acta Phys. Pol. A* **2013**, *124*, 946–948.
- 15. Okumuş, M.; Özgan, Ş.; Kırık, İ.; Kerli, S. Thermal and optical characterization of liquid crystal 4'-hexyl-4-biphenylcarbonitrile/4-hexylbenzoic acid mixtures. J. Mol. Struct. 2016, 1120, 150–155. [CrossRef]
- Devi, T.; Choudhury, B.; Bhattacharjee, A.; Dabrowski, R. Study of optical parameters of two fluorinated isothiocyanato nematic liquid crystals exhibiting high birefringence. *Opto-Electron. Rev.* 2014, 22, 24–30. [CrossRef]
- 17. Thingujam, K.; Bhattacharjee, A.; Choudhury, B.; Dabrowski, R. Nematic liquid crystals exhibiting high birefringence. *Opt. Rev.* **2016**, *23*, 409–419. [CrossRef]
- 18. Dąbrowski, R.; Kula, P.; Herman, J. High birefringence liquid crystals. Crystals 2013, 3, 443–482. [CrossRef]
- 19. Zaki, A.A.; Ahmed, H.; Hagar, M. Impact of fluorine orientation on the optical properties of difluorophenylazophenyl benzoates liquid crystal. *Mater. Chem. Phys.* **2018**, *216*, 316–324. [CrossRef]
- 20. Zaki, A. Optical measurements of phase transitions in difluorophenylazophenyl benzoate thermotropic liquid crystal with specific orientated fluorine atoms. *Phase Transit.* **2019**, *92*, 135–148. [CrossRef]
- Shen, P.; Zhang, X.; Lu, H.; Su, Z.; Zhou, Y.; Song, B.; Li, X.; Yang, X.; Tu, Y.; Li, C.Y. Effect of Fullerene Volume Fraction on Two-Dimensional Crystal-Constructed Supramolecular Liquid Crystals. *Chem. Asian J.* 2019, 14, 125–129. [CrossRef] [PubMed]
- 22. Lehmann, M.; Dechant, M.; Gerbig, L.; Baumann, M. Supramolecular click procedures in liquid crystals. *Liq. Cryst.* **2019**, *46*, 1985–1994. [CrossRef]
- 23. Saccone, M.; Pfletscher, M.; Kather, S.; Wölper, C.; Daniliuc, C.; Mezger, M.; Giese, M. Improving the mesomorphic behaviour of supramolecular liquid crystals by resonance-assisted hydrogen bonding. *J. Mater. Chem. C* 2019, *7*, 8643–8648. [CrossRef]
- 24. Sharma, V.S.; Shah, A.P.; Sharma, A.S. A new class of supramolecular liquid crystals derived from azo calix [4] arene functionalized 1, 3, 4-thiadiazole derivatives. *New J. Chem.* **2019**, *43*, 3556–3564. [CrossRef]
- 25. Wang, X.; Bai, L.; Kong, S.; Song, Y.; Meng, F. Star-shaped supramolecular ionic liquid crystals based on pyridinium salts. *Liq. Cryst.* **2019**, *46*, 512–522. [CrossRef]
- 26. Alhaddad, O.; Ahmed, H.; Hagar, M. Experimental and theoretical approaches of new nematogenic chair architectures of supramolecular H-bonded liquid crystals. *Molecules* **2020**, *25*, 365. [CrossRef]
- Ahmed, H.; Hagar, M.; Alhaddad, O. New chair shaped supramolecular complexes-based aryl nicotinate derivative; mesomorphic properties and DFT molecular geometry. *RSC Adv.* 2019, 9, 16366–16374. [CrossRef]
- 28. Nafee, S.S.; Ahmed, H.A.; Hagar, M. New architectures of supramolecular H-bonded liquid crystal complexes based on dipyridine derivatives. *Liq. Cryst.* **2020**, 1–14. [CrossRef]
- Alnoman, R.B.; Ahmed, H.A.; Hagar, M.; Abu Al-Ola, K.A.; Alrefay, B.S.; Haddad, B.A.; Albalawi, R.F.; Aljuhani, R.H.; Aloqebi, L.D.; Alsenani, S.F. Induced phases of new H-bonded supramolecular liquid crystal complexes; mesomorphic and geometrical estimation. *Molecules* 2020, 25, 1549. [CrossRef] [PubMed]
- Alnoman, R.B.; Hagar, M.; Ahmed, H.A.; Abu Al-Ola, K.A.; Naoum, M.M.; Al-Elati, F.; Abdullah Zaid, Y.; Alsharif, A.; Al-Juhani, Y.; Abulrhelh, A. Characterization of New H-Bonded Liquid Crystalline Complexes Based on Iminophenyl Nicotinate. *Crystals* 2020, 10, 499. [CrossRef]

- Alhaddad, O.A.; Abu Al-Ola, K.A.; Hagar, M.; Ahmed, H.A. Chair-and V-Shaped of H-bonded Supramolecular Complexes of Azophenyl Nicotinate Derivatives; Mesomorphic and DFT Molecular Geometry Aspects. *Molecules* 2020, 25, 1510. [CrossRef] [PubMed]
- 32. Gray, G.W.; Jones, B. The mesomorphic transition points of the para-normal-alkoxybenzoic acids-a correction. *J. Chem. Soc.* **1953**, 4179–4180. [CrossRef]
- 33. Kato, T.; Frechet, J.M. A new approach to mesophase stabilization through hydrogen bonding molecular interactions in binary mixtures. *J. Am. Chem. Soc.* **1989**, *111*, 8533–8534. [CrossRef]
- 34. Kato, T.; Wilson, P.G.; Fujishima, A.; Fréchet, J.M. Hydrogen-bonded liquid crystals. A novel mesogen incorporating nonmesogenic 4, 4'-bipyridine through selective recognition between hydrogen bonding donor and acceptor. *Chem. Lett.* **1990**, *19*, 2003–2006. [CrossRef]
- 35. Kato, T.; Frechet, J.M.; Wilson, P.G.; Saito, T.; Uryu, T.; Fujishima, A.; Jin, C.; Kaneuchi, F. Hydrogen-bonded liquid crystals. Novel mesogens incorporating nonmesogenic bipyridyl compounds through complexation between hydrogen-bond donor and acceptor moieties. *Chem. Mater.* **1993**, *5*, 1094–1100. [CrossRef]
- 36. Kato, T.; Fréchet, J.M.J. Hydrogen bonding and the self-assembly of supramolecular liquid-crystalline materials. *Macromol. Symp.* **1995**, *98*, 311–326. [CrossRef]
- 37. Kihara, H.; Kato, T.; Uryu, T.; Frechet, J.M. Supramolecular liquid-crystalline networks built by self-assembly of multifunctional hydrogen-bonding molecules. *Chem. Mater.* **1996**, *8*, 961–968. [CrossRef]
- 38. Kihara, H.; Kato, T.; Uryu, T.; Frechet, J.M. Induction of a cholesteric phase via self-assembly in supramolecular networks built of non-mesomorphic molecular components. *Liq. Cryst.* **1998**, *24*, 413–418. [CrossRef]
- 39. Chen, K.-Y. Crystal Structure, Hydrogen-Bonding Properties, and DFT Studies of 2-((2-(2-Hydroxyphenyl) benzo [d] thiazol-6-yl) methylene) malononitrile. *Mol. Cryst. Liq. Cryst.* 2015, 623, 285–296. [CrossRef]
- 40. Garcia-Amorós, J.; Reig, M.; Cuadrado, A.; Ortega, M.; Nonell, S.; Velasco, D. A photoswitchable bis-azo derivative with a high temporal resolution. *Chem. Commun.* **2014**, *50*, 11462–11464. [CrossRef] [PubMed]
- 41. Shoji, M.; Tanaka, F. Theoretical study of hydrogen-bonded supramolecular liquid crystals. *Macromolecules* **2002**, *35*, 7460–7472. [CrossRef]
- 42. Sundaram, S.; Jayaprakasam, R.; Dhandapani, M.; Senthil, T.; Vijayakumar, V. Theoretical (DFT) and experimental studies on multiple hydrogen bonded liquid crystals comprising between aliphatic and aromatic acids. *J. Mol. Liq.* **2017**, *243*, 14–21. [CrossRef]
- 43. Hagar, M.; Ahmed, H.; Alhaddadd, O. DFT Calculations and Mesophase Study of Coumarin Esters and Its Azoesters. *Crystals* **2018**, *8*, 359. [CrossRef]
- 44. Hagar, M.; Soliman, S.M.; Ibid, F.; El Sayed, H. Quinazolin-4-yl-sulfanylacetyl-hydrazone derivatives; Synthesis, molecular structure and electronic properties. *J. Mol. Struct.* **2013**, *1049*, 177–188. [CrossRef]
- 45. Soliman, S.M.; Hagar, M.; Ibid, F.; El Sayed, H. Experimental and theoretical spectroscopic studies, HOMO–LUMO, NBO analyses and thione–thiol tautomerism of a new hybrid of 1, 3, 4-oxadiazole-thione with quinazolin-4-one. *Spectrochim. Acta Part A Mol. Biomol. Spectrosc.* **2015**, 145, 270–279. [CrossRef]
- Hagar, M.; Soliman, S.M.; Ibid, F.; El Sayed, H. Synthesis, molecular structure and spectroscopic studies of some new quinazolin-4 (3H)-one derivatives; an account on the N-versus S-Alkylation. *J. Mol. Struct.* 2016, 1108, 667–679. [CrossRef]
- Aboelnaga, A.; Hagar, M.; Soliman, S.M. Ultrasonic Synthesis, Molecular Structure and Mechanistic Study of 1, 3-Dipolar Cycloaddition Reaction of 1-Alkynylpyridinium-3-olate and Acetylene Derivatives. *Molecules* 2016, 21, 848. [CrossRef]
- 48. Ahmed, H.A.; Hagar, M.; El-Sayed, T.H.; Alnoman, R.B. Schiff base/ester liquid crystals with different lateral substituents: Mesophase behaviour and DFT calculations. *Liq. Cryst.* **2019**, *46*, 1–11. [CrossRef]
- Paterson, D.A.; Gao, M.; Kim, Y.-K.; Jamali, A.; Finley, K.L.; Robles-Hernández, B.; Diez-Berart, S.; Salud, J.; de la Fuente, M.R.; Timimi, B.A. Understanding the twist-bend nematic phase: The characterisation of 1-(4-cyanobiphenyl-4'-yloxy)-6-(4-cyanobiphenyl-4'-yl) hexane (CB6OCB) and comparison with CB7CB. *Soft Matter* 2016, *12*, 6827–6840. [CrossRef] [PubMed]
- 50. Martinez-Felipe, A.; Cook, A.G.; Abberley, J.P.; Walker, R.; Storey, J.M.; Imrie, C.T. An FT-IR spectroscopic study of the role of hydrogen bonding in the formation of liquid crystallinity for mixtures containing bipyridines and 4-pentoxybenzoic acid. *RSC Adv.* **2016**, *6*, 108164–108179. [CrossRef]
- Chen, R.; An, Z.; Wang, W.; Chen, X.; Chen, P. Lateral substituent effects on UV stability of high-birefringence liquid crystals with the diaryl-diacetylene core: DFT/TD-DFT study. *Liq. Cryst.* 2017, 44, 1515–1524. [CrossRef]

- 52. Hagar, M.; Ahmed, H.; Saad, G. New calamitic thermotropic liquid crystals of 2-hydroxypyridine ester mesogenic core: Mesophase behaviour and DFT calculations. *Liq. Cryst.* **2020**, *47*, 114–124. [CrossRef]
- 53. Nafee, S.S.; Ahmed, H.; Hagar, M. Theoretical, experimental and optical study of new thiophene-based liquid crystals and their positional isomers. *Liq. Cryst.* **2020**, 1–12. [CrossRef]
- 54. Nafee, S.S.; Hagar, M.; Ahmed, H.A.; El-Shishtawy, R.M.; Raffah, B.M. The synthesis of new thermal stable schiff base/ester liquid crystals: A computational, mesomorphic, and optical study. *Molecules* **2019**, *24*, 3032. [CrossRef]
- 55. Alnoman, R.; Ahmed, H.A.; Hagar, M. Synthesis, optical, and geometrical approaches of new natural fatty acids' esters/Schiff base liquid crystals. *Molecules* **2019**, *24*, 4293. [CrossRef]
- 56. Ahmed, H.; Hagar, M.; Alhaddad, O. Mesomorphic and geometrical orientation study of the relative position of fluorine atom in some thermotropic liquid crystal systems. *Liq. Cryst.* **2019**, *47*, 404–413. [CrossRef]
- 57. Alhaddad, O.A.; Ahmed, H.A.; Hagar, M.; Saad, G.R.; Abu Al-Ola, K.A.; Naoum, M.M. Thermal and photophysical studies of binary mixtures of liquid crystal with different geometrical mesogens. *Crystals* **2020**, *10*, 223. [CrossRef]
- Alnoman, R.B.; Hagar, M.; Ahmed, H.A.; Naoum, M.M.; Sobaih, H.A.; Almshaly, J.S.; Haddad, M.M.; Alhaisoni, R.A.; Alsobhi, T.A. Binary Liquid Crystal Mixtures Based on Schiff Base Derivatives with Oriented Lateral Substituents. *Crystals* 2020, 10, 319. [CrossRef]
- Hagar, M.; Ahmed, H.A.; Aljohani, G.; Alhaddad, O.A. Investigation of Some Antiviral N-Heterocycles as COVID 19 Drug: Molecular Docking and DFT Calculations. *Int. J. Mol. Sci.* 2020, 21, 3922. [CrossRef] [PubMed]
- Ahmed, H.A.; Mansour, E.; Hagar, M. Mesomorphic study and DFT simulation of calamitic Schiff base liquid crystals with electronically different terminal groups and their binary mixtures. *Liq. Cryst.* 2020, 1–13. [CrossRef]
- 61. Hagar, M.; Ahmed, H.A.; Aouad, M.R. Mesomorphic and DFT diversity of Schiff base derivatives bearing protruded methoxy groups. *Liq. Cryst.* **2020**, 1–12. [CrossRef]
- Naoum, M.M.; Fahmi, A.A.; Mohammady, S.Z.; Abaza, A.H. Effect of lateral substitution on supramolecular liquid crystal associates induced by hydrogen-bonding interactions between 4-(4'-pyridylazo-3-methylphenyl)-4''-alkoxy benzoates and 4-substituted benzoic acids. *Liq. Cryst.* 2010, 37, 475–486. [CrossRef]
- 63. Hagar, M.; Ahmed, H.; Alhaddad, O. Experimental and theoretical approaches of molecular geometry and mesophase behaviour relationship of laterally substituted azopyridines. *Liq. Cryst.* **2019**, *46*, 1440–1451. [CrossRef]
- 64. Naoum, M.M.; Fahmi, A.A.; Refaie, A.A.; Alaasar, M.A. Novel hydrogen-bonded angular supramolecular liquid crystals. *Liq. Cryst.* **2012**, *39*, 47–61. [CrossRef]
- 65. Ahmed, H.; Naoum, M. Mesophase behaviour of azobenzene-based angular supramolecular hydrogen-bonded liquid crystals. *Liq. Cryst.* **2016**, *43*, 222–234. [CrossRef]
- Ahmed, H.; Hagar, M.; Alaasar, M.; Naoum, M. Wide nematic phases induced by hydrogen-bonding. Liq. Cryst. 2018, 46, 550–559. [CrossRef]
- 67. Hagar, M.; Ahmed, H.; Alhaddad, O. New azobenzene-based natural fatty acid liquid crystals with low melting point: Synthesis, DFT calculations and binary mixtures. *Liq. Cryst.* **2019**, *46*, 2223–2234. [CrossRef]
- 68. Ahmed, H.; Hagar, M.; Aljuhani, A. Mesophase behavior of new linear supramolecular hydrogen-bonding complexes. *Rsc. Adv.* **2018**, *8*, 34937–34946. [CrossRef]
- 69. Cleland, W.; Kreevoy, M.M. Low-barrier hydrogen bonds and enzymic catalysis. *Science* **1994**, *264*, 1887–1890. [CrossRef] [PubMed]
- 70. Lizu, M.; Lutfor, M.; Surugau, N.; How, S.; Arshad, S.E. Synthesis and characterization of ethyl cellulose–based liquid crystals containing azobenzene chromophores. *Mol. Cryst. Liq. Cryst.* 2010, 528, 64–73. [CrossRef]
- 71. Martínez-Felipe, A.; Imrie, C.T. The role of hydrogen bonding in the phase behaviour of supramolecular liquid crystal dimers. *J. Mol. Struct.* **2015**, *1100*, 429–437. [CrossRef]
- 72. Ghanem, A.; Noel, C. FTIR investigation of two alkyl-p-terphenyl-4, 4"-dicarboxylates in their crystalline, smectic and isotropic phases. *Mol. Cryst. Liq. Cryst.* **1987**, 150, 447–472. [CrossRef]
- 73. Paterson, D.A.; Martínez-Felipe, A.; Jansze, S.M.; Marcelis, A.T.; Storey, J.M.; Imrie, C.T. New insights into the liquid crystal behaviour of hydrogen-bonded mixtures provided by temperature-dependent FTIR spectroscopy. *Liq. Cryst.* **2015**, *42*, 928–939. [CrossRef]

- 74. Walker, R.; Pociecha, D.; Abberley, J.; Martinez-Felipe, A.; Paterson, D.; Forsyth, E.; Lawrence, G.; Henderson, P.; Storey, J.; Gorecka, E. Spontaneous chirality through mixing achiral components: A twist-bend nematic phase driven by hydrogen-bonding between unlike components. *Chem. Commun.* 2018, 54, 3383–3386. [CrossRef]
- 75. Ahmed, H.; Naoum, M.; Saad, G. Mesophase behaviour of 1: 1 mixtures of 4-n-alkoxyphenylazo benzoic acids bearing terminal alkoxy groups of different chain lengths. *Liq. Cryst.* **2016**, *43*, 1259–1267. [CrossRef]
- 76. Hagar, M.; Ahmed, H.; Saad, G. Synthesis and mesophase behaviour of Schiff base/ester 4-(arylideneamino) phenyl-4"-alkoxy benzoates and their binary mixtures. *J. Mol. Liq.* **2019**, *273*, 266–273. [CrossRef]
- 77. Liu, Y.; Zhan, G.; Zhong, X.; Yua, Y.; Ganb, W. Effect of pi–pi stacking on the self-assembly of azomethine-type rod–coil liquid crystals. *Liq. Cryst.* **2011**, *38*, 995–1006. [CrossRef]
- Ahmed, H.; Hagar, M.; Saad, G. Impact of the proportionation of dialkoxy chain length on the mesophase behaviour of Schiff base/ester liquid crystals; experimental and theoretical study. *Liq. Cryst.* 2019, 46, 1611–1620. [CrossRef]
- 79. Hagar, M.; Ahmed, H.; El-Sayed, T.; Alnoman, R. Mesophase behavior and DFT conformational analysis of new symmetrical diester chalcone liquid crystals. *J. Mol. Liq.* **2019**, *285*, 96–105. [CrossRef]
- 80. Sreeramakavacham, S.S.; Rao, B.G.S.; Mallika, K.; Kumari, T.V.; Lakshminarayana, S.; Ha, S.T. Novel method for order parameter of ferroelectric liquid crystals by image analysis. *Liq. Cryst.* **2013**, *40*, 384–390. [CrossRef]
- 81. Wu, S.-T.; Hsu, C.-S.; Shyu, K.-F. High birefringence and wide nematic range bis-tolane liquid crystals. *Appl. Phys. Lett.* **1999**, *74*, 344–346. [CrossRef]
- 82. Haller, I. Thermodynamic and static properties of liquid crystals. *Prog. Solid State Chem.* **1975**, *10*, 103–118. [CrossRef]
- 83. Patari, S.; Chakraborty, S.; Nath, A. The optical anisotropy and orientational order parameter of two mesogens having slightly different flexible side chain–a comparative study. *Liq. Cryst.* **2016**, *43*, 1017–1027. [CrossRef]
- 84. Sastry, S.S.; Kumari, T.V.; Mallika, K.; Rao, B.G.S.; Ha, S.-T.; Lakshminarayana, S. Order parameter studies on EPAP alkanoate mesogens. *Liq. Cryst.* **2012**, *39*, 295–301. [CrossRef]
- 85. Kumar, A. Determination of orientational order and effective geometry parameter from refractive indices of some nematics. *Liq. Cryst.* **2013**, *40*, 503–510. [CrossRef]
- 86. Erkan, S.; Cetinkaya, M.; Yildiz, S.; Özbek, H. Critical behavior of a nonpolar smectogen from high-resolution birefringence measurements. *Phys. Rev. E* 2012, *86*, 041705. [CrossRef]
- 87. Li, J.; Wen, C.-H.; Gauza, S.; Lu, R.; Wu, S.-T. Refractive indices of liquid crystals for display applications. *J. Disp. Technol.* **2005**, *1*, 51. [CrossRef]



© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).