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# Values for the Mechanical Properties of Wheat, Maize and Wood Pellets for Use in Silo Load Calculations Involving Numerical Methods

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Abstract: The mechanical properties of the materials stored in agricultural silos determine the loads they generate under static and dynamic conditions. The present work describes the mechanical properties of wheat, maize and wood pellets. Direct shear and triaxial assay devices, and oedometers (all commonly used in geotechnical assays), were used to determine these materials' internal angle of friction, Poisson's ratio, Young's modulus, apparent specific weight, etc. The results for wheat and maize were similar to those previously reported by other authors. For the wood pellets, the results for the internal angle of friction and apparent specific weight were also similar to those found in the literature. However, this is a relatively new type of material, and few results of this type have been reported, certainly not enough for reference values to be available. This work is the first to report this material's dilatancy angle and Poisson's ratio. A table is provided with suggested reference values for the studied mechanical properties of each of the test materials; these can be used in silo load calculations involving numerical methods.

**Keywords:** agricultural silos; numerical methods; mechanical properties; Poisson's ratio; Young's modulus; wood pellets; wheat; maize

# 1. Introduction

Classical silo load calculations, which most commonly involve the use of the Janssen formula [1], allow the loads exerted by stored materials to be determined under static conditions. The values obtained depend on the different mechanical properties of these materials, including the internal angle of friction, the apparent cohesion, the particle–wall coefficient of friction, the apparent specific weight, etc. The literature contains numerous reports on these properties, both for granular materials and for powders, which have been studied for many years [2–13].

In the 1970s, numerical methods began to appear for calculating agricultural silo loads [14]. Since then, they have become ever more important thanks to advances in computing, which have allowed increasingly more complex calculations to be undertaken. These methods have allowed theoretical studies of the loads exerted by materials stored in agricultural silos, both under static and dynamic conditions. Initially, finite element models were used to simulate their behaviour, understanding these materials as a continuous medium [15–18]. More recently, discrete element models have been used since they allow simulations at the particle level [19–25]. Some authors have combined both techniques [19,21,26].

From the point of view of safety, it is under dynamic conditions when the least favourable situations arise, and several studies have examined what happens in such



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). scenarios [27–31]. However, the theoretical results obtained when using classical or numerical techniques require validation in real silos, allowing models to be appropriately adjusted [29,32–34].

It should always be remembered that the reliability of theoretical results obtained via simulations depends on knowing the mechanical properties of the materials analysed. Indeed, both classical theories and numerical simulations require values for the properties they contemplate, such as the Poisson's ratio and the dilatancy angle. These have been determined for some materials [6,35–38], but for others, such as wood pellets, the literature contains no information; laboratory tests are needed to provide the required data.

The aim of the present work was to determine the values of a number of mechanical properties of the following materials commonly stored in silos: wheat (*Triticum*), maize (*Zea mays*) and wood pellets. The results add to those already reported in the literature for the first two and provide some of the first information of their kind for the third.

## 2. Materials and Methods

The assays described in this work were all performed at the Geotechnical Laboratory of the *Centro Universitario de Plasencia* (University of Extremadura). Figure 1 shows the following materials examined:



Figure 1. Samples of wood pellets (left), maize (centre) and wheat (right).

The wood pellets used in this work corresponded to natural wood (100%). Their main characteristics were as follows: diameter =  $6 \pm 1$  mm; length =  $3,15 < L \le 40$  mm; fines  $\le 0.5\%$ ; net calorific value  $\ge 4.6$  kWh/kg; ash  $\le 0.7\%$ ; moisture  $\le 10\%$ ; bulk density =  $600 \le DB \le 750$  kg/m<sup>3</sup>; mechanical durability  $\ge 98\%$ .

The properties determined for these materials were the following: the internal angle of friction ( $\phi$ ), the apparent cohesion (*C*), the particle–wall coefficient of friction ( $\mu$ ), the dilatancy angle ( $\psi$ ), the Poisson's ratio ( $\nu$ ), Young's modulus (E) and the apparent specific weight ( $\gamma$ ).

The assays employed to determine the values for these variables have been described in detail elsewhere [35,38]; information regarding particular conditions is, however, provided here.

## 2.1. Direct Shear Assays

The assays adhered to the procedure established in part 10 of Standard UNE-EN ISO 17892 [39]. Figure 2 shows the semi-automatic direct shear test device as follows:



Figure 2. Semi-automatic direct shear test device.

The semi-automatic shear test device used had a square shear box dimensions 10 cm long and 3 cm deep. It was provided with a load cell of 5 kN with the following technical characteristics: Sensibility: 2.0 (mV/V)  $\pm$  0.1%; Tolerance: 1.5% F.E.; Hysteresis error: 0.023% F.E.; Creep (30 min): 0.019% F.E.; Max. linearity error: 0.021% F.E.; Load limit: 150% F.E.; Min. failure load: 250% F.E.; Protection IP 67. In addition, the device had a linear strain gauge transducer 10 mm travel for measuring the vertical deformation and other one 25 mm travel for measuring horizontal displacement. The technical data of both strain gauge transducers were the following: Linearity < 0.5%; Sensibility = 440 mV/mm ( $\pm$ 10%); Repeatability:  $\pm$ 6 micron; Zero deviation depending on temp < 0.005%/°C; Resistance to crack: 250 g SRS 20 . . . 2000 Hz; Resistance to vibrations: 20 g rms (max 50 g); Protection level IP 66. The speed selector allows developing assays at speeds ranging between 0.00001 and 10 mm/min.

Normal stresses of 20, 30, 100, 200 and 300 kPa were employed. The assay speed was 1 mm/min, with three repetitions for each assay. The vertical deformation of the sample was measured using a deformation sensor. This device was used to determine the internal angle of friction, the apparent cohesion and the dilatancy angle for each material.

The dilatancy angle is determined using the following Equation (1):

$$\Psi = (\Delta \varepsilon_{\rm v} / h_0) / (\Delta \varepsilon_{\rm H} / L) \tag{1}$$

where

 $\Psi$  = Dilatancy angle;

 $\Delta \varepsilon_{v}$  = Increment of the vertical deformation at a time range (mm);  $\Delta \varepsilon_{H}$  = Horizontal displacement variation at a time range (mm);  $h_{0}$  = Initial height of the sample (mm); L = Initial length of the sample (mm).

As well as performing conventional assays, others were performed modifying the shear box to determine the coefficient of friction of the material with the metallic casing (i.e., the particle–wall coefficient of friction). For this, the normal stresses employed were 30, 100, 200 and 300 kPa. The assay speed was again 1 mm/min, with three repetitions at each stress.

As reported in earlier work [36], while Eurocode 1 Part 4 [40] recommends that the ratio between the size of the sample and the size of the grain not be below 40, for the

maize and wood pellets it was clearly distant from this value. However, the interest in the present results outweighs the need to adhere to this criterion, especially bearing in mind the limitations of the apparatus and the lack of any larger devices. Certainly, other researchers [41] have performed direct shear tests limiting the above ratio to 5, similar to that resulting in the present work.

# 2.2. Triaxial Tests

Assays were performed adhering to the procedure described in Part 8 of Standard UNE-EN ISO 17892 [42]. Figure 3 shows the apparatus used, a fully automatic device that requires the use of a multiuse press; in the present work, one with a 50 kN load cell was used.



**Figure 3.** The triaxial test device and multiuse press used. (**a**) Complete apparatus; (**b**) Detail showing the use of the device's 101.6 mm specimen vessel during an assay.

The triaxial test device was provided with two load cells, one of 20 kN and the other of 50 kN, although in this work just the second one was used, as commented. In addition, it has an absolute pressure transducer up to 20 bar ( $20 \text{ kg/cm}^2$ ) and a strain gauge transducer with a measurement range of 0–100 mm. The technical characteristics of both the load cells and the strain gauge transducers were the same provided for the direct shear test device.

The triaxial test device could be used with two sample-holding vessels, one 101.6 mm (4 inches) in diameter and one of 38.1 mm (1.5 inches). In the present work, the 101.6 mm vessel was used with the maize and wood pellets, and the 38.1 mm vessel with the wheat. This device was used in free lateral deformation (FLD) and K<sub>0</sub> assays following methods previously described [35,36,38].

In the FLD assays, the applied confinement pressure was maintained constant and the samples allowed to deform freely until they reached 20% axial deformation (the maximum allowed by Standard UNE-EN ISO 17892), recording the shear stress continuously. The confinement pressures used were 100, 200 and 300 kPa. This allowed the internal angle of friction and apparent cohesion of the test material to be determined following the procedure described for the direct shear tests.

For the  $K_0$  assays, the initial confinement pressure exerted was 100 kPa, but at the moment the sample began to deform at the centre it was increased to 200 kPa (all other conditions were maintained). When the sample began to deform again at the centre, the confinement pressure was increased to 300 kPa and the assay continued until an axial deformation of 20% was reached. All assays with the 101.6 mm vessel were performed

at a speed of 1.016 mm/min, while all those with the 38.1 mm vessel were performed at 0.508 mm/min. All assays were performed in triplicate.

The membrane effect was taken into account in both types of assays (as required by Standard UNE-EN ISO 17892) using the following Equation (2):

$$\sigma_{\rm m} = \left[ (4 \times t_{\rm m} \times E_{\rm m}) / D_{\rm m} \right] \times \varepsilon_{\rm vm} \tag{2}$$

where

 $\sigma_m$  = The action of the latex membrane used to surround the sample (kPa);  $t_m$  = The thickness of the membrane when not under stress (mm);  $E_m$  = The Young's modulus of the membrane, measured under stress (kPa);  $D_m$  = The initial internal diameter of the membrane (mm);  $\varepsilon_{vm}$  = The vertical deformation of the membrane (mm).

In the present case, the value for  $\varepsilon_{vm}$  is automatically recorded by the triaxial device's software. The value for  $E_m$  was 1400 kPa, i.e., the value recommended for latex membranes by the above standard. The value of  $t_m$  for the 38.1 mm internal-diameter membrane was 0.2 mm, and for the 101.6 mm internal-diameter membrane it was 1.5 mm.

#### 2.3. Oedometric Assays

These assays were performed following the procedure described in Part 5 of Standard UNE 17892 [43]. Figure 4 shows the apparatus used, a completely automatic device.



Figure 4. Apparatus used in oedometric assays.

The oedometric apparatus is a fully automatic device provided with three oedometers (each cell 75 mm-internal diameter/20 mm high) each equipped with 10 kN load cells. In addition, it has three strain gauge transducers 10 mm travel and PID control for the applied force with a resolution of 1 N. The technical characteristics of both the load cells and the strain gauge transducers are the same provided for the direct shear test device.

Figure 5 shows a sample of wood pellets inside one of the oedometric cells.



Figure 5. A sample of wood pellets inside one of the oedometric cells.

For these assays, normal stresses of 8, 16, 32, 64, 128 and 256 kPa were applied. Using the load and deformation values reached during the unloading process, oedometric modulus was calculated as previously described [35,38], which was then used to derive the elasticity of the test materials. All assays were performed in triplicate.

## 2.4. Determination of the Apparent Specific Weight

These assays were performed following previously described methods [35,38] that adhere to Part 2 of Standard UNE-EN ISO 17892 [44]. The assay speed was 0.382 mm/min; all assays were performed in triplicate. Figure 6 shows the arrangement of the normal Proctor mould in the multiuse press in order to determine the variation in the specific weight of the samples under normal stress.



**Figure 6.** Normal Proctor mould in the multiuse press, used to determine the apparent specific weight of the test materials under normal stress.

#### 2.5. Determination of the Moisture Content

The materials were dried in an oven at 105-110 °C, adhering to Part 1 of Standard UNE-EN ISO 17892 [45] for the maize and wheat samples and to Part 2 of Standard UNE-EN ISO 18134 [46] for the wood pellets. Samples were weighed every 24 h until a constant weight was reached.

# 3. Results

# 3.1. Direct Shear Assays

## 3.1.1. Internal Angle of Friction and Apparent Cohesion

Figure 7 shows the regression line for the Mohr–Coulomb strength envelope obtained for the wheat in the direct shear assays performed at the indicated normal stresses. The slope provides the value for the internal angle of friction and the intersection with the ordinate axis of the apparent cohesion.



**Figure 7.** Regression line for the Mohr–Coulomb strength envelope for wheat obtained from direct shear assays.

The regression line formula for the wheat was y = 0.4458x + 13.115 ( $R^2 = 0.9911$ ), for the maize it was y = 0.5532x + 13.988 ( $R^2 = 0.9817$ ) and for the wood pellets it was y = 0.8592x + 23.017 ( $R^2 = 0.9786$ ).

Figure 8 shows the shape of the stress-deformation curve for the wood pellets under normal stress of 20 kPa (a) and 100 kPa (b). The shear stress is plotted on the ordinate axis, whereas the horizontal deformation is plotted on the abscissa.



**Figure 8.** Stress-deformation curve for the wood pellets: (**a**) at a normal stress of 20 kPa; (**b**) at a normal stress of 100 kPa.

The way in which the material breaks is similar under both conditions, with an immediate fall following a peak ratio value. The values in Figure 8b are notably higher than those in Figure 8a. This is due to the increase in the stress state due to the higher normal stress exerted, which hinders the displacement of the particles as the horizontal displacement of the shear box increases. For the particles to leave their initial positions, increasing shear stress is required. Shearing occurs when the shear stress reached equals the shear stress threshold of the material.

Table 1 shows the mean  $\pm$  standard deviation for the internal angle of friction and the apparent cohesion of the tested materials.

**Table 1.** Mean  $\pm$  standard deviation for the internal angle of friction and the apparent cohesion of the tested materials.

Material	Internal Angle of Friction ( $\phi$ )	Apparent Cohesion (C, kPa)
Wheat	$24.0\pm0.~6$	$13.12\pm30.19$
Maize	$29.0\pm0.9$	$13.99\pm26.25$
Wood pellets	$40.7\pm1.2$	$23.02\pm27.89$

The wood pellets (followed by the maize and then the wheat) returned the highest value for the internal angle of friction; therefore, they offered greater resistance to shearing. All three materials returned notable apparent cohesion values, with wheat the highest, followed by maize and wood pellets.

## 3.1.2. Dilatancy Angle

Figure 9 shows the deformation curve (obtained via direct shear assays; abscissa = horizontal deformation, ordinate = vertical deformation) for the wood pellets at 100 kPa (left) and 20 kPa (right). Results for each repetition are shown; it should be noted that while three repetitions were performed at 100 kPa, only the results for two were valid.



Figure 9. Deformation curves for the wood pellets at (a) 100 kPa normal stress and (b) 20 kPa normal stress.

The different repetitions at each normal stress returned similar results. Immediately after beginning the assay, the samples first began to become compressed as the particles adjusted their positions. The resistance they offered to shear then increased significantly until the shearing stress was reached, causing the displacement of the particles and increasing the height of the vessel they occupied inside the shear box. As expected, the vertical deformation values were higher at 20 kPa since the particles are freer to move and become less imbricated, thus achieving a larger dilatancy angle.

Figure 10 shows the differences in the vertical deformation recorded for the wood pellets at the five stress values assayed. Each curve represents the mean values from three repetitions.



Figure 10. Deformation curves for the wood pellets at the different normal stresses assayed.

The difference in the vertical deformation recorded at 300 kPA and 20 kPa is significant because of the reasons explained above.

Table 2 shows the mean  $\pm$  SD for the dilatancy angles obtained for each material under the different normal stresses assayed.

Table 2. Dilatancy angles obtained for each material under the different normal stresses assayed.

Matal	Dilatancy Angle ( $\psi$ )						
Material	20 kPa	30 kPa	100 kPa	200 kPa	300 kPa		
Wheat	$19.7\pm7.2$	$13.7\pm1.0$	$7.4 \pm 1.7$	$6.0\pm2.1$	$4.2\pm1.2$		
Maize	$33.6\pm2.3$	$31.9\pm4.3$	$15.3\pm2.6$	$14.3\pm1.4$	$8.8\pm0.6$		
Wood pellets	$36.4\pm4.8$	$33.2\pm3.2$	$22.8\pm3.4$	$15.7\pm2.5$	$10.4\pm1.2$		

The wood pellets (followed by the maize and wheat) returned the highest dilatancy angles at all the normal stresses exerted, with the maximum value  $(36.4^{\circ})$  recorded at 20 kPa. The maize returned a similarly high value at 20 kPa  $(33.6^{\circ})$ , while that for wheat was much lower  $(19.7^{\circ})$ . In all cases, these values fell as the normal stress exerted increased. For wheat, the dilatancy angle at 300 kPa was  $4.2^{\circ}$ , i.e., 79% smaller than at 20 kPa  $(19.7^{\circ})$ , while for maize, these values were  $8.8^{\circ}$  and  $33.6^{\circ}$ , i.e., 74% smaller at the higher stress. For the pellets, the reduction was 72%  $(33.6^{\circ}$  at 20 kPa and  $10.4^{\circ}$  at 300 kPa) the smallest percentage change registered.

# 3.1.3. Particle–Wall Coefficient of Friction

Figure 11 shows the regression line for the particle–wall coefficient of friction obtained for the maize.



Figure 11. Particle–wall coefficient of friction obtained for maize in direct shear assays.

The regression line formula was y = 0.3482x + 11.72 ( $R^2 = 0.8324$ ) for the maize, y = 0.5187x + 17.03 ( $R^2 = 0.8103$ ) for the wood pellets and y = 0.2916x + 10.775 ( $R^2 = 0.9847$ ) for the wheat.

Table 3 shows the mean  $\pm$  SD for the particle–wall coefficient of friction for the three materials examined.

Table 3. Particle-wall coefficient of friction for the three materials examined.

Material	Particle–Wall Coefficient of Friction ( $\mu$ )
Wheat	$0.29\pm0.01$
Maize	$0.34\pm0.04$
Wood pellets	$0.52\pm0.06$

The wood pellets returned the highest particle–wall coefficient of friction, a value notably higher than those for the maize and wheat.

#### 3.2. Triaxial Tests

3.2.1. Free Lateral Deformation

Figure 12 shows the FLD regression lines for the wheat (the maize line was very similar) and wood pellets obtained at axial deformations between 10% and 20%.



**Figure 12.** Regression lines for the FLD of the wheat and wood pellets obtained at axial deformations of 10% and 20%: (**a**) wheat, (**b**) wood pellets.

The slopes were steeper when the axial deformation was 20%. The regression line formula for wheat was y = 0.2935x - 1.8833 (R<sup>2</sup> = 0.9807) for an axial deformation of 20% and y = 0.2611x + 3.3353 (R<sup>2</sup> = 0.945) for 10%. For maize, these formulae were y = 1.0946x - 13.287 (R<sup>2</sup> = 0.998) and y = 1.0623x - 10.114 (R<sup>2</sup> = 0.9998), respectively, and for the wood pellets, y = 1.4049x - 28.683 (R<sup>2</sup> = 0.9969) and y = 1.2874x - 22.73 (R<sup>2</sup> = 0.9992), respectively.

Table 4 shows the means  $\pm$  SD for the internal angle of friction and apparent cohesion of the tested materials derived from the above.

For all three materials, the internal angle of friction increased with the axial deformation. The highest value was obtained for the pellets (54.6°), followed by the maize (47.6°) and finally the wheat (16.4°). The value for the wheat fell by 11% at 10% axial deformation compared to 20%, while that of the pellets fell by 7.5%, and the maize by 2%.

With respect to the apparent cohesion values, wood pellets returned the lowest values for this parameter. In fact, these values were negative at between 10 and 20% axial deformations, as well as they were for maize. Wheat was the only material that presented a positive value (3.34 kPa) at 10% axial deformation.

	Internal Angle	of Friction ( $\phi$ )	Apparent Col	nesion (C, kPa)
Material		Axial De	eformation	
	10%	20%	10%	20%
Wheat Maize Wood pellets	$\begin{array}{c} 14.6 \pm 0.5 \\ 46.7 \pm 0.1 \\ 50.5 \pm 2.1 \end{array}$	$\begin{array}{c} 16.4 \pm 0.3 \\ 47.6 \pm 0.3 \\ 54.6 \pm 0.3 \end{array}$	$\begin{array}{c} 3.34 \pm 13.20 \\ -10.11 \pm 9.55 \\ -22.73 \pm 1.66 \end{array}$	$\begin{array}{c} -1.88 \pm 6.54 \\ -13.29 \pm 12.26 \\ -28.68 \pm 20.66 \end{array}$

**Table 4.** Internal angle of friction and apparent cohesion of the tested materials obtained in the triaxial tests at deformations of 10% and 20%.

## 3.2.2. K<sub>0</sub> Assays

Table 5 shows the mean  $\pm$  SD for the Poisson's ratio of all three materials at the different confinement pressures applied.

**Table 5.** Poisson's ratio for the three materials at the three confinement pressures used in the  $K_0$  assays.

		Poisson's Ratio (ν)	
Material	100 kPa	200 kPa	300 kPa
Wheat	$0.39\pm0.01$	$0.38\pm0.00$	$0.37\pm0.01$
Maize	$0.18\pm0.04$	$0.15\pm0.02$	$0.14\pm0.01$
Wood pellets	$0.13\pm0.01$	$0.12\pm0.01$	$0.12\pm0.02$

The wheat returned the highest Poisson's ratios, with the highest (0.39) at a confinement pressure of 100 kPa; the lowest value (0.13) was recorded for the wood pellets at the same confinement pressure. For all three materials, the values tended to decrease with increasing confinement pressure. The maize showed the greatest difference between the maximum and minimum values (22%); for the wood pellets, the difference was 7% and for the wheat, 5%.

# 3.3. Oedometric Assays

Table 6 shows the means  $\pm$  SD for Young's modulus obtained in the oedometric assays.

**Table 6.** Young's modulus for the different materials as obtained in the oedometric assays. Values are expressed in kPa.

	Name al Chuana (L.D.)	Material				
	Normal Stress (KPa)	Wheat	Maize	Wood Pellets		
٩	8	$1405\pm290.6$	$1350\pm148.5$	$1067\pm363.2$		
ycl	16	$977\pm87.9$	$1793\pm172.5$	$1146\pm418.5$		
8	32	$1418 \pm 137.5$	$2331\pm530.5$	$1265\pm185.3$		
lin	64	$2620\pm352.3$	$3476\pm511.8$	$2549 \pm 1480.5$		
oac	128	$4321\pm733.3$	$4714 \pm 511.5$	$3446 \pm 1650.0$		
Ĺ	256	$8693 \pm 1629.2$	$7319\pm355.4$	$4739 \pm 257.4$		
60	128	$51,720 \pm 1011.2$	$44,\!476 \pm 10,\!172.6$	$27,495 \pm 215.7$		
e lin	64	$18,\!883 \pm 997.7$	$22,\!349 \pm 3268.1$	$13,\!404 \pm 38.2$		
ycl	32	$14,\!677 \pm 1793.9$	$20,\!518 \pm 16,\!780.7$	$9674\pm2031.3$		
c	16	$8767\pm208.6$	$6047\pm804.1$	$3868\pm379.7$		
D	8	$3476\pm72.8$	$3660\pm1200.7$	$2363\pm754.5$		

Due to the elastic-plastic behaviour of granulate solids, the elastic modulus can be calculated only during the unloading process, while the loading process allows to determine the so-called compressibility modulus. The reference value for the normal stress in the unloading process was 100 kPa since it can be considered that the maximum pressure reached in most commercial agricultural silos is of that order. Therefore, prorating between 64 and 128 kPa, the wheat would return the highest Young's modulus value (about 37,350 kPa), followed by the maize (about 34,800 kPa) and finally the wood pellets (at a much lower 21,330 kPa). At 128 kPa compared to 64 kPa in the discharge cycle, Young's modulus for the maize and wood pellets fell by 50% and by some 65% for the wheat. However, when comparing those at 64 kPa and 32 kPa, the reduction was 28% for the wood pellets, 22% for the wheat and 8% for the maize.

Figure 13 shows the oedometric curves for the wood pellets (void ratio on the ordinate axis and normal stress on the abscissa). As for the determination of Young's modulus value, the discharge cycle values are those of greatest importance.



Figure 13. Oedometric curves obtained for the wood pellets in the oedometric assays.

3.4. Determination of the Apparent Specific Weight

Table 7 shows change in apparent specific weight of the materials at different normal stresses.

Table 7. Change in apparent specific weight of the materials at different normal stresses.

			Α	pparent Specific	Weight γ (kN/m	1 <sup>3</sup> )		
Material	Normal Stress (kPa)							
	0	25	50	75	100	125	150	200
Wheat	$7.98\pm0.10$	$8.02\pm0.08$	$8.03\pm0.08$	$8.03\pm0.08$	$8.03\pm0.08$	$8.04\pm0.08$	$8.04\pm0.08$	$8.05\pm0.08$
Maize	$7.47\pm0.04$	$7.51\pm0.05$	$7.51\pm0.06$	$7.52\pm0.05$	$7.52\pm0.05$	$7.53\pm0.06$	$7.53\pm0.06$	$7.55\pm0.06$
Wood pellets	$7.08\pm0.04$	$7.10\pm0.04$	$7.11\pm0.03$	$7.12\pm0.04$	$7.12\pm0.04$	$7.13\pm0.03$	$7.13\pm0.04$	

For the wood pellets, a normal stress of 200 kPa could not be reached after taking into account the particle–wall coefficient of friction with the interior of the normal Proctor mould. However, this is of little importance since the normal stress reference value is 100 kPa [36]. The wheat returned the highest apparent specific weight, with values always close to  $8.0 \text{ kN/m}^3$ , followed by the maize (around  $7.50 \text{ kN/m}^3$ ) and finally the wood pellets (around  $7.10 \text{ kN/m}^3$ ). The apparent specific weight for all the materials increased by some 1% at the highest normal stress compared to 0 kPa.

Figure 14 shows the change in apparent specific weight for the wood pellets (by way of representation) with changing normal stress.





## 3.5. Determination of the Moisture Content

Table 8 shows the moisture content of the materials as determined by drying them to a constant weight at 105–110  $^{\circ}$ C.

Table 8. Moisture content of the materials.

Material	Moisture Content (%)
Wheat	9.78
Maize	12.77
Wood pellets	6.38

The maize had the highest moisture content, followed by the wheat and the wood pellets.

# 4. Discussion

# 4.1. Direct Shear Assays

4.1.1. Internal Angle of Friction and Apparent Cohesion

For the wheat, the range of values obtained for the internal angle of friction lies over that reported in the literature (with values from 2 to 11% smaller [6,35,47], to around 11% higher [36,38]). For maize, the range is similar to that reported by Horabik et al. [48] and Moya et al. [36], 9% higher than that recorded by Molenda and Horabik [47], and 11% higher than that determined by Lebègue and Boudakian [5]. For the wood pellets, the range reaches 55% higher than that reported by Gallego et al. [49] but is similar to that reported by Wu et al. [50] (who used 6–12 mm-long pellets similar to the present material). Knowing the internal angle of friction for wood pellets is important since it correlates with durability and the resistance to shearing; the greater the resistance to shearing, the greater the possibility that the particles maintain their shape and remain intact during transport and storage [51]. For all three materials, the differences between the present and previously published results might be explained by differences in the moisture content, the bulk density, the consolidation time (there was none in the present work), the shape of the particles, the orientation of the particles within the shear box, the arrangement of the particles and the formation of shear bands [47]. It has also been reported that the mechanical properties of maize, especially the particle thickness, may influence the rupture of the material [52].

For the wheat, the present range of values for the apparent cohesion is notably higher than that reported by other authors [6,35,36,38,47]. Unlike in these latter reports, the apparent cohesion cannot, therefore, be considered negligible. Similarly, the range determined for the maize is higher than that reported by Molenda and Horabik [47] but within that reported by Moya et al. [36]. The range for the pellets could not be compared to any previously published values (when using numerical methods, it is not usually considered

an important variable for this type of material). The moisture content may account for the above discrepancies between reports; the assay speed may also have a little influence [38], as may the shape of the particles and their orientation in the shear box during an assay [35].

# 4.1.2. Dilatancy Angle

For the wheat, the range of dilatancy angle values lies within that reported by some authors [35,36,38,53] but is below that reported by yet others [37]. The range for the maize falls within that reported by Moya et al. [36]. Once again, the range of the pellets cannot be compared with any other; the literature contains no information. The results show that, for all three materials, as the normal stress rises, the dilatancy angle decreases, confirming that reported by Zeng et al. [53]. The latter authors also showed that the void index decreases with rising normal stress.

## 4.1.3. Particle–Wall Coefficient of Friction

For the wheat, the range of values for the particle–wall coefficient of friction is higher (by some 16–21%) than that reported by other authors [11,35,36] but similar to that published by yet others [47]. The values recorded for the maize exceed those reported in the literature [36,47,54]; the same is true for the wood pellets [50]. These discrepancies might be explained in the same manner as described for the internal angle of friction.

#### 4.2. Triaxial Tests

#### 4.2.1. Free Lateral Deformation Assays

For the wheat, the values for the internal angle of friction recorded in the FLD tests were some 5–11% smaller than those reported by other authors [6,35,36,38,53], both at 10% and 20% axial deformation. In contrast, the values for the maize are more than double those reported in the literature [35]. For the wood pellets, they are 10–28% higher than reported by other authors [49,50]. A comparison of the values obtained in the direct shear test with those obtained in the triaxial tests shows those recorded for the wheat in the latter to be 10° (58%) lower, a finding in stark contrast to that reported by other authors when using similar materials [38], and rather more similar to that seen for sand. However, for the maize and wood pellets, the values obtained in the triaxial tests were notably higher than those obtained in the direct shear assays (17° [60%] and 14° [31%], respectively), similar to that previously reported [35] (and therefore quite different to that seen for sand). The factors that might explain the variation between the present and published results are the same as outlined above for the direct shear assays.

For the wheat, the apparent cohesion values are similar to those reported by other authors [6,35,36,38]; since they did not reach 10 kPa, the apparent cohesion for wheat can be considered negligible. For the maize, the values were smaller than those reported by others [36]; since they were close to 10 kPa, the apparent cohesion for maize can also be deemed negligible. For the wood pellets, a maximum value of -22.73 kPa was recorded. There are no results in the literature with which to compare this, but considering the differences observed in the results obtained for this parameter in both direct shear tests and triaxial tests, it would be wise not to regard the apparent cohesion for this material as negligible. The factors that affect these values are the same as those affecting the internal angle of friction, but the moisture content, the orientation of the particles during the assay and the type of particle are likely the most important.

## 4.2.2. K<sub>0</sub> Assays

For the wheat, the Poisson's ratio recorded at the normal stresses exerted (100, 200 and 300 kPa) coincides with values in some reports [36,38,55] but is some 16–18% higher than those recorded in other work [6,35,36,38,47,56]. For the maize, they were similar to values reported by other authors [47] but up to 67% smaller than those reported by yet others [36]. The literature contains no values with which to compare those recorded for the wood pellets.

The possible explanations for these discrepancies are the same as outlined for the FLD tests, although the orientation and arrangement of the particles might be the most important.

#### 4.3. Oedometric Assays

The Young's modulus values recorded for the wheat at a normal stress of 100 kPa are similar to those reported by other authors [35] but 100–150% higher than those reported by yet others [6,36,47]. For the maize, the values at 100 kPa were similar to those reported in other work [36] but 30–80% higher than those reported by other authors [47]. For the wood pellets, the value of 21,330 kPa recorded at 100 kPa is 73% lower than that reported in other work [49], although the latter authors worked with individual pellets. These discrepancies might be explained by differences in the arrangement of the particles in the sample vessel and their moisture content.

## 4.4. Apparent Specific Weight

For the wheat, the apparent specific weight values recorded ranged from 7.98 to  $8.05 \text{ kN/m}^3$ , i.e., within the range reported in numerous studies [3,5,35,36,38,47,48,55–57]. Those for maize ranged from 7.47 to 7.55 kN/m<sup>3</sup>, again similar to those reported by many other authors [5,36,47,48,54,58]. For the wood pellets, values of 7.08–7.13 kN/m<sup>3</sup> were recorded, similar to those reported in certain official documents [58] and slightly higher than those reported in other studies [50,51]. The discrepancy might be explained in terms of the arrangement of the particles in the normal Proctor mould, their moisture content and differences in the materials tested (which may not have been exactly the same).

## 4.5. Moisture Content

The moisture contents of the samples are similar to those reported by other authors [3,5,58]. Limits (<10%) exist for the moisture content of wood pellets in order to guarantee their quality [58] (the pellets in the present work met this criterion).

Table 9 shows the recommended values for the different mechanical properties of the tested materials, as determined from the present results. These values are the means of those recorded in the different assays, except for the dilatancy angle and the Poisson's ratio, for which the maximum values are provided. These values might serve as references for future work.

Material	φ (°)	C (kPa)	¥ (°)	$\mu$ Steel	ν	E (kPa)	$\gamma_{ m ap}$ (kN/m <sup>3</sup> )	H (%)
Wheat	19.3	6.6	19.7	0.29	0.39	37,350	8.03	9.78
Maize	38.8	7.0	33.6	0.34	0.18	34,800	7.52	12.77
Wood pellets	47.7	11.5	36.4	0.52	0.13	21,330	7.12	6.38

Table 9. Recommended values for the different mechanical properties of the tested materials.

#### 5. Conclusions

For all three materials, the values for the internal angle of friction, the particle–wall coefficient of friction and the apparent specific weight were similar to those reported in the literature.

For the maize and wood pellets, the internal angle of friction determined by the direct shear assay was notably smaller than that determined in the triaxial tests. The orientation and arrangement of the particles during the assays might explain this discrepancy.

For all three materials, the particle–wall coefficient of friction was similar to, or higher than that reported in the literature. The type of material actually used in different studies might account for these discrepancies.

This is the first work to report the Young's modulus and dilatancy angle for wood pellets; the results for other properties of this material were similar to those in the literature.

Finally, the present work provides recommended values for the studied properties that can be used in the calculation of silo pressures using numerical methods (either finite or discrete element techniques).

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