



# Communication Operating Characteristic Analysis and Verification of Short-Stroke Linear Oscillating Actuators Considering Mechanical Load

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**Abstract:** Linear oscillating machines are electric devices that reciprocate at a specific frequency and at a specific stroke. Because of their linear motion, they are used in special applications, such as refrigerators for home appliances and medical devices. In this paper, the structure and electromagnetic characteristics of these linear oscillating machines are investigated, and the stroke is calculated according to voltage and motion equations. In addition, static and transient behavior analysis is performed, considering mechanical systems such as springs, damping systems, and mover mass. Furthermore, in this study, the magnetic force is analyzed, experiments are conducted according to the input power, and the current magnitude and stroke characteristics are analyzed according to the input frequency. Finally, the study confirmed that the most efficient operation is possible when the electrical resonance frequency matches the resonance frequency of the linear oscillating machines.

**Keywords:** electromagnetic loss analysis; linear oscillating actuator; linear oscillating motor; longitudinal flux machine

# 1. Introduction

Linear oscillating machines (LOMs) are electric devices that reciprocate at a specific frequency and at a specific stroke. Because of their linear motion, they are used in special applications, such as refrigerators for home appliances, and medical devices. LOMs can be classified according to the movement type as the moving-core-type, moving-coil-type, and moving-magnet-type LOMs. The moving-core-type LOM has the advantage of being able to easily increase the permanent magnet usage and the output; however, the price of such LOMs increases with the increase in magnet usage. The moving-coil-type LOM has the highest output density compared to the other two types, but it is difficult to manufacture. Most LOMs used in practical applications are of the moving-magnet type, in which the mover is light and suitable for high-speed operation; this is the most efficient method of increasing LOM output [1-5]. A novel design of a single-phase short-stroke LOM has been developed for application in refrigeration compressors and other similar equipment because of its advantages such as high transmission efficiency and simple structure [6–9]. However, the evaluation of the LOM performance is difficult because of its reciprocating linear motion. Additionally, unlike rotating machines, measuring the magnetic force of LOMs can be complicated. Therefore, LOM analysis and performance evaluation are essential not only in terms of finite-element method (FEM) analysis but also experimental verification. Various researchers have conducted experimental studies on the electromagnetic force and output of LOMs [10-12]. In the current study, the structural and electromagnetic characteristics of a moving-magnet-type LOM were determined and



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). verified through the analysis and experimental study of magnetic force based on the operating frequency and applied voltage. Because the operation of the LOM is the most efficient at the resonance frequency, the consideration of the operating frequency in the electromagnetic design is essential.

The software used for this study is ANSYS Maxwell 2021 R2. An implicit approach has been utilized, and quadratic type elements were used. All analysis results have a resolution of 100 per electrical cycle.

# 2. Analysis of LOAs

# 2.1. Topology and Features

Figure 1a illustrates the structure of the LOM, comprising an outer core, a coil, and an inner core, and possesses a structure in which the permanent magnet produces a linear reciprocating motion in the z-axis direction. Figure 1b shows the 3D shape of the LOM. The outer and inner cores are laminated in the radial direction to reduce the eddy current loss, and the outer core is made of several divided cores to increase the space utilization. Figure 1c shows the manufactured components of the LOM.



**Figure 1.** (a) Two-dimensional analysis model of LOM, (b) 3D analysis model of LOM, (c) manufactured components of linear oscillating machine.

## 2.2. Electromagnetic Characteristic of LOM

Figure 2 depicts the flux path and flux density of our LOM. The permanent magnet makes a reciprocating motion in the z-axis direction and changes the direction of the main magnetic flux flowing in the outer core, thus generating a back electromotive force (back EMF), which can be calculated as follows:

$$E = -N_{turn} \frac{d\phi}{dt} = -N_{turn} v_s \frac{d\phi}{dz} \tag{1}$$

where  $N_{turn}$  and  $v_s$  are the coil turns and mover speed, respectively. The LOM should be designed to produce a constant stroke. The maximum magnetic stroke is determined by the length of the permanent magnet. The stroke can be identified from the magnetic force and back EMF as the mover moves at a unit speed (1 m/s). Figure 3 shows that the back EMF and magnetic force vary according to the mover's position. In addition, the maximum stroke range can be deduced from the maximum and minimum values of the magnetic force, and the value of the back EMF in this region is confirmed to be constant. As the inductance varies with respect to the position of the mover and the magnitude of the current, the instantaneous inductance can be analyzed, as shown in Figure 4.



Figure 2. Magnetic flux density and flow of the LOM.



Figure 3. Back EMF and magnetic force according to mover position.



Figure 4. Inductance of LOM according to mover position and input current.

## 2.3. Electromagnetic Loss Characteristic of LOM

Electromagnetic loss of LOM consists of copper loss, permanent rotor magnet eddy current loss, and core loss. Since it is difficult to consider the mechanical loss in the design stage, it was ignored in this study.

#### 2.3.1. Copper Loss

The copper loss of LOM consists of DC loss and AC loss. When the operating frequency is high, AC loss must be considered in order to consider the skin effect, but only DC loss is considered because the LOM of this study has a low operating frequency of 60 Hz. Since it is single-phase, the DC loss of copper loss is calculated as follows:

$$P_{copper} = R_{ph} I_{rms}^2 \tag{2}$$

where  $R_{ph}$  and  $I_{rms}$  represent the single-phase winding resistance and rms values of the single-phase current, respectively. Figure 5 shows the copper loss according to the applied current magnitude.



Figure 5. Copper loss analysis result according to applied current.

#### 2.3.2. Eddy Current Loss

The eddy current loss occurring in the permanent magnet can be calculated as a function of the eddy current density and the permanent magnet volume, as shown in Equation (3) [13]:

$$P_{eddy} = \sum_{n} \left\{ \int_{V_m} \frac{|J_{en}^2|}{\sigma_m} dV \right\}$$
(3)

where  $P_{eddy}$ ,  $J_{en}$ ,  $V_m$ , and  $\sigma_m$  represent the total eddy current loss in PM, the *n*th eddy current density harmonic of PM, the PM volume, and the PM conductivity, respectively. In order to reduce the eddy current in the permanent magnet, the LOM in this paper was designed with several magnet segments.

Figure 6a shows the permanent magnet loss distribution obtained by the threedimensional finite element analysis method according to the number of permanent magnet segments. Figure 6b shows the eddy current loss analysis result according to the number of magnet segments. As shown, the eddy current loss decreases as the number of segments of the magnet increases. The LOM of this study has an eight-segment PM in consideration of the eddy current loss reduction.



**Figure 6.** (a) Loss comparison according to the number of permanent magnets; (b) Eddy current loss comparison according to the number of permanent magnet divisions.

## 2.3.3. Core Loss

In this study, core loss analysis was performed using the modified Steinmetz equation presented by Bertotti [14]. In particular, the magnetic flux density and magnetic field behavior of each region were analyzed by dividing the stator into regions [15]. Finally, core loss considering the rotating magnetic field and the alternating magnetic field was calculated. The modified Steinmetz equation considering magnetic behavior is as follows:

$$P_{core} = \sum_{l=1,odd}^{\infty} \alpha_l \left( k_{hl} f_l B_l^{n_{st}} + k_{el} f_l^2 B_l^2 + k_{al} f_l^{1.5} B_l^{1.5} \right), \begin{cases} \alpha = 1, \text{ alternating field} \\ \alpha = 2, \text{ rotationg field} \end{cases}$$
(4)

where  $k_h$ ,  $k_e$ , and  $k_a$  represent the hysteresis loss coefficient, the eddy current loss coefficient, and the excessive loss coefficient, respectively. The rotating magnetic field and the alternating magnetic field are distinguished by  $\alpha$ .

Figure 7a shows the analysis models of the outer stator and the inner stator for core loss analysis. The outer stator is divided into 28 regions, and the inner stator is divided into 7 analysis regions. Figure 8 shows the magnetic flux density in each area of the stator according to the position of the mover. Figure 7b shows the conceptual diagram of the axial ratio. A rotating magnetic field and an alternating magnetic field are distinguished from the ratio of the maximum and minimum values of each component of the normal magnetic flux density and the tangential magnetic flux density. Figure 8a shows the radial magnetic flux density in regions 1, 6, 16, 25, 28, and 32, and Figure 8b shows the axial magnetic flux density. Figure 9 shows the magnetic field behavior analysis for the first harmonic component, third harmonic component, and fifth harmonic component of the magnetic flux density for each region. It can be seen that the magnetic field in most regions of a linear permanent magnet motor consists of an alternating magnetic field. The results of the core loss analysis considering the harmonics of magnetic flux density and magnetic field behavior are shown in Figure 10. It can be seen that the core loss increases as the magnitude of the current and the operating frequency increases. Table 1 shows the loss and efficiency characteristics of the LOM at rated load.



Figure 7. (a) Stator analysis model for core loss analysis; (b) Conceptual diagram of axis ratio.



Figure 8. Flux density in each point of stator according to flux direction: (a) radial and (b) axial.



**Figure 9.** Magnetic field behavior according to stator region: (**a**) region 1, (**b**) region 6, (**c**) region 16, (**d**) region 25, (**e**) region 28, (**f**) region 32.



Figure 10. Core loss analysis result according to driving frequency.

Table 1. LOM losses and efficiency @ rated load.

Copper Loss	Core Loss	Solid Loss	Power	Efficiency
1.18 W	2.85 W	0.04 W	110 W	96.4%

## 2.4. Dynamic Characteristic of LOM

Figure 11 shows the equivalent electrical circuit, including the mechanical system, which includes load force, spring coefficient, damping coefficient, and mover mass. The analysis of the dynamic characteristic of the LOM, considering the mechanical system, can be calculated from the equations of voltage and motion of the LOM. In the LOM, the back EMF is in series with the stator winding resistance and inductance and is proportional to the speed. The voltage equation of LOM is given by:

$$V_t(t) = R_{ph}i(t) + L_s \frac{di(t)}{dt} + K_e \frac{dx(t)}{dt}$$
(5)

where  $R_{ph}$ ,  $L_s$ ,  $K_e$ , and x are the phase resistance, inductance, back EMF coefficient, and displacement, respectively. Based on Equation (5), the displacement can be derived as:

$$x(t) = \frac{1}{K_e} \int \left( V_t - R_{ph}i - L_s \frac{di}{dt} \right) dt = \frac{1}{K_e} \int E \, dt \tag{6}$$



Figure 11. Analysis model including mechanical system of LOA.

Equation (6) shows that the stroke is calculated by integrating the back EMF. The motion equation of mechanical system is given by:

$$F(t) = K_T i(t) = M \frac{d^2 x(t)}{dt^2} + K x(t) + C_d \frac{dx(t)}{dt}$$
(7)

where  $K_T$  and  $C_d$  are the thrust and damping coefficients, respectively. The mover mass refers to the effective mass that includes the magnet weight and equivalent mass of the piston, and the damping coefficient refers to the viscous resistance between the piston and wall.

In addition, the spring coefficient is calculated as the sum of the mechanical spring coefficient and discharge pressure that changes depending on the load condition. In this study, only mechanical-spring-coefficient values were considered without considering load conditions. The thrust coefficient is assumed to be constant because although its value varies depending on the position of the mover, the effect is small. The mechanical system constants and resonance frequencies of this analysis model are shown in Table 2. Parameters of LOM are shown in Table 3. In Figure 12, it is possible to confirm the phase and magnitude of the current and displacement at the resonance frequency, and it confirms that a difference of 90 degrees occurs. In addition, Figure 13 shows that the resonant frequency changes according to the change of the machine coefficient under no-load and load conditions.

Table 2. Parameters for dynamic analysis of LOM.

Parameter	Value	
Spring Coefficient	34,800 N/m	
Damping Coefficient	0.9 Ns/m	
Mover Mass	0.25 kg	
Resonance Frequency	60 Hz	

Table 3. LOM parameters.

Parameter	Value
Operating frequency	60 Hz
Rated stroke	$\pm 5~\mathrm{mm}$
Outer core radius	59 mm
Stator type	Outer core
Mover type	PM mover
Rated power	100 W
Resistance	1.11 Ω
Inductance	792 mH



Figure 12. Current and displacement analysis results.



Figure 13. Current and displacement analysis results: (a) No load (b) Load.

#### 3. Experiment and Discussion

The LOM experiment confirmed the current and stroke of LOM with the applications of function generator and amplifier, respectively. Figure 14 shows the experimental setup consisting of the LOM, linear coupling, position sensor, and indicator. When AC power was applied to the LOM, the mover reciprocated according to the magnitude and direction of the current. Figure 15 shows the results of the transient-behavior analysis of the LOM according to the applied voltage and frequency. The results of the stroke analysis presented in Figure 15a display the current magnitude, where the smallest current is observed at the resonance frequency. Further, Figure 15b show that the largest stroke is produced at the resonance frequency are the same, the loss of components due to the mover mass and spring disappears so that the most efficient operation is possible. Figure 16 shows the analysis results and experimental results for the applied voltage and current waveform at 40 Hz and 50 Hz.



Figure 14. Experiment set of the LOM.



Figure 15. Transient analysis results of the LOM: (a) current and (b) stroke.



Figure 16. Voltage and current and analysis results and experimental results: (a) 40 Hz (b) 50 Hz.

## 4. Conclusions

This paper introduced the structure and operating principle of the movable-magnettype LOM with the most efficient and simple magnetic circuit. After moving the magnet at a constant speed to determine the magnetic stroke and inductance of the LOM, the driving characteristics were investigated according to the electrical resonance frequency. The LOM was manufactured. In addition, the transient behavior of the LOM was verified by applying an AC voltage. To analyze the transient-behavior characteristics, an analysis was conducted by considering the mechanical-system elements such as spring, damping coefficient, and mover mass. Finally, by using the analysis based on the input voltage and frequency, the authors confirmed that the most efficient operation is possible when the electrical resonance frequency and resonance frequency of the LOM match.

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