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A Multiple Response Prediction Model for Dissimilar AA-5083 and AA-6061 Friction Stir Welding Using a Combination of AMIS and Machine Learning

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Abstract: This study presents a methodology that combines artificial multiple intelligence systems (AMISs) and machine learning to forecast the ultimate tensile strength (UTS), maximum hardness (MH), and heat input (HI) of AA-5083 and AA-6061 friction stir welding. The machine learning model integrates two machine learning methods, Gaussian process regression (GPR) and a support vector machine (SVM), into a single model, and then uses the AMIS as the decision fusion strategy to merge SVM and GPR. The generated model was utilized to anticipate three objectives based on seven controlled/input parameters. These parameters were: tool tilt angle, rotating speed, travel speed, shoulder diameter, pin geometry, type of reinforcing particles, and tool pin movement mechanism. The effectiveness of the model was evaluated using a two-experiment framework. In the first experiment, we used two newly produced datasets, (1) the 7PI-V1 dataset and (2) the 7PI-V2 dataset, and compared the results with state-of-the-art approaches. The second experiment used existing datasets from the literature with varying base materials and parameters. The computational results revealed that the proposed method produced more accurate prediction results than the previous methods. For all datasets, the proposed strategy outperformed existing methods and state-of-the-art processes by an average of 1.35% to 6.78%.

Keywords: artificial multiple intelligence system; friction stir welding; heat input; ultimate tensile strength; maximum hardness; machine learning combination model



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1. Introduction

Aluminum alloys are primary materials used for parts of products in many industries, such as the aviation, automotive, railroad, and marine industries, because of their resistance to chemical reaction corrosion, robustness to force, and formability [1–3]. In particular, AA5XXX and AA6XXX alloys are utilized in various advanced commercial applications because of their strength and good weldability [4,5]. These materials are not avoided for welding complex dissimilar joints. However, in the fusion welding process for complex joints, dissimilar aluminum alloys have low weldability because of differences in chemical composition, mechanical properties, thermal expansion coefficient, and melting point which manifest as metallurgical problems such as distortion, shrinkage, and porosity resulting from the melting and solidification in the weld line [6–8]. Solid-state welding is a method used for welding dissimilar materials which has effective weldability and reduces problems in the weld seam because of the low melting point temperature [9–11]. The friction stir

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welding (FSW) process results in good weld quality, and the weld seam of the two materials has good mechanical properties. However, it is difficult to generate the parameters for dissimilar welding because of the variety of process parameter relationships and their impact on the specification of the weld seam quality [12,13].

There has been much research carried out into FSW of dissimilar aluminum alloys, including relative studies of process parameters and their effect on mechanical properties and metallurgical structure, and these are essential considerations in the configuration of the weld line [14]. The process parameters that influence weld seam quality are: tool rotational speed (TRS), tool travel speed (TTS), shoulder diameter (SD), pin diameter (PD), pin length (PL), penetration depth (PeD), tool tilt angle (TA), pin type (PT), tool traveling method (TM), type of reinforcement particles (TP), and filled additives techniques (TAD) [15–20]. Unsuitable process parameters result in insufficient heat generation and mixing of material, which lead to metallurgical changes involving the grain size, microstructure, defects, and intermetallic compound phases, as well as precipitation in the nugget (NZ), thermomechanically affected (TMAZ), and heat-affected zones (HAZ) [21–24]. As a result, the mechanical properties are not as anticipated. For FSW, the related parameters need to be controlled to achieve good metallurgical structure and mechanical strength.

Luesak et al. [25] reported optimal welding parameters using a modified differential evolution approach in the dissimilar welding of AA5083–AA6061, and particles reinforced the weld seam in the multiresponse process. The welding parameters that influence the metallurgical structure and strength of the weld seam are: rotational speed, tool travel speed, shoulder diameter, tilt angle, pin geometry, type of particles, and tool pin movement. The significant desired responses defining the quality and strength of an FSW weld line are: ultimate tensile strength (UTS), maximum hardness (MH), and heat input (HI). Controlling the welding parameters is essential for the generation of sound mechanical properties [26]. In [27], the author stated that multiobjective optimization of UTS and MH could be predicted using the controllable parameter values as inputs in a prediction model. Examples of multiobjective function prediction methods from the literature include response surface methodology (RSM) [28,29] and grey relation analysis (GRA) [30,31]. Furthermore, the authors of [32] applied an experimental design to develop an artificial multiple intelligence system (AMIS) to solve both single and multiple objectives in FSW and identify an optimal solution.

In recent years, friction stir welding processes have applied artificial intelligence (AI) methods extensively, including in industrial development research [33,34]. To predict mechanical properties, Senapati et al. [35] used an artificial neural network (ANN) simulation involving tensile and yield strength, elongation, bending stress, and grain size, and taking tool rotational speed (TRS), tool travel speed (TTS), and penetration depth (PeD) into consideration. In addition, [36] used a Mamdani-type fuzzy logic model in FSW to predict tensile strength and weld seam hardness, and [37] applied the support vector machine (SVM) method and ANN modeling. Furthermore, [38] simulated FSW parameters and responses using an ANN approach with regard to the hardness in the heat-affected zone (HAZ) and the peak temperature in the stir zone and the HAZ. The result was a solution identical to that in the literature. In the past, machine learning (ML) was often used to sciences and engineering [39] including noisy and sparse data [40]. Therefore, machine learning was used to forecast the multiobjectives of weld seam properties and remains important when combined with AI for high performance. In [41,42], the authors demonstrated the application of AI using the "unlike entirety model" to categorize types of drug resistance in tuberculosis patients and to identify and classify unsavory images. Application of the unlike entirety AI model for forecasting mechanical properties should provide higher-quality solutions. Furthermore, ensemble machine learning (EML) has been developed for use in many forecasting models together with other approaches such as ML to successfully optimize parameters [43]. In [44], the author set out an approach for the categorization of types of drug resistance in tuberculosis patients, and [31] applied the EDL approach to classify irregularities in medical images which were unnoticed when

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checked by radiologists. Our literature review found that the EDL and EML methods provided effective prediction results when compared to the early deep learning (DL) and ML versions of the models.

Therefore, our research used EML and AI for estimation of the UTS, MH, and HI for high weld seam quality in the FSW process. The gaps in the research (see Table 1) are as follows: (1) a gap concerning the methodology for the prediction of UTS, HM, and HI; the EML approach was based on forecasting the multiobjective in the FSW process using the predefined set of parameters; and (2) a gap regarding the types of joining material that the unlike entirety machine learning architecture uses to predict the optimal values of UTS, HM, and HI in the FSW process. In addition, this research makes the following contributions: (1) the combination of AMIS and machine learning methods was used for the first time to predict the multiple responses of dissimilar friction stir welding; and (2) two novel datasets based on the seven controlled parameters were proposed. These were utilized to construct successful algorithms for predicting multiple response friction stir welding using the test data.

Table 1. Literature review of materials, parameters, responses, and methods used in earlier literature and this study.

Materials	terials Parameter												Res	ponse			Method	l	Ref.	
	TRS (rpm)	TTS (mm/min)	SD (mm)	PD (mm)	PL (mm)	PeD (mm)	TA (Degrees)	TM -	PT -	TP -	TAD -	Other	UTS (MPa)	MH (HV)	HI (°C)	Other	ML	EML	Other	
AA6262	✓	✓	-	-	-	✓	-	-	-	-	-	-	-	✓	-	-	✓	-	-	[45]
A319	✓	✓	-	-	-	-	-	-	-	-	-	No. of Passes	-	✓	-	wear rates	✓	-	-	[46]
AA6061- T6	✓	✓	✓	✓		-	-	-	-	-	-	-	✓	-	-	-	✓	-	-	[47]
AA6061	✓	✓	-	-	-	-	-	-	-	-	-	axial forces	✓	-	-	-	-	✓	-	[48]
AA 2050-T8	✓	✓	✓	-	-	-	✓	-	-	-	-	-	✓	-	-	-	-	✓	-	[49]
AA6061- T6	✓	✓	✓	✓	-	-	✓	-	-	-	-	tool hard- ness	✓	-	-	yield strength	✓	-	-	[50]
AA6082	✓	✓	-	-	-	-	-	-	-	-	-	-	✓	-	-	-	✓	✓		[51]
AA6061	✓	✓	-	-	-	-	-	-	-	-	-	-	✓	-	-	-	✓	-	-	[52]
AA7039	✓	✓	-	-	-	-	✓	-	-	-	-	-	✓	-	-	-	✓	-	-	[53]
ENAW- 6082-T6	✓	✓	-	-	-	-	-	-	-	-	-	-	✓	-	-	-	✓	-	-	[54]
AA6061- T6	✓	✓	-	-	-	-	-	-	-	-	-	-	✓	-	-	-	✓	✓	-	[55]
IS:65032	✓	✓	✓	-	-	-	✓	-	-	-	-	-	✓	-	-	-	-	✓	-	[56]
AA6061	✓	✓	-	-	-	-	-	-	-	-	-	axial forces	✓	-	-	-	-	✓	-	[57]
AA5754/ C11000	✓	✓	✓	-	-	-	-	-	-	-	-	-	✓	-	-	-	✓	-	-	[58]
AA5083- AA6061	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	-	✓	-	-	-	-	✓	-	[59]
AA5083- AA6061	✓	✓	✓	✓	✓	✓	✓	-	-	-	-	-	✓	✓	✓	-	-	✓	-	our

2. Research Methodology

This section presents the research method applied to the artificial multiple intelligence system (AMIS)–machine learning combination model for the prediction of UTS, MH, and HI for AA5083 and AA6061 from the determined parameters. The research outline is shown in Figure 1.

2.1. Dataset Arrangement

The study dataset used in our experiment consisted of a training dataset (80%) and a testing dataset (20%), divided into two groups: 7PI-V1 and 7PI-V2. For example, 7PI-V1 had 57 datasets, divided into 45 training datasets and 12 testing datasets, and this was used to test the performance of the proposed model, as shown in Table 2. The dataset was obtained via an initial demonstration using AA-5083 and AA-6061 materials. The UTS and MH properties of the two materials were as shown in Table 3. The FSW experiment used worksheet plates that were 75 mm wide, 200 mm long, and 6 mm thick.

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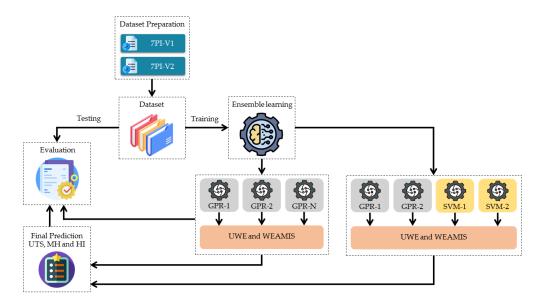


Figure 1. Framework of the AMIS-ML combination model for the forecasting of UTS, MH, and HI.

Table 2. Dataset details.

Dataset Type	7PI-V1	7PI-V2
Training dataset	45	43
Testing dataset	12	11
Total	57	54

Table 3. Mechanical properties of base materials.

Aluminum Alloys	Ultimate Tensile Strength (MPa)	Maximum Hardness (HV)
AA5083	300	91
AA6061	310	107

2.1.1. Dataset 7PI-V1

The parameters used for FSW were as proposed by Luesak et al. [25]: four continuous parameters (rotational speed, tool travel speed, tool shoulder diameter, and tool tilt angle) and three categorical variables (pin geometry, particle types, and tool pin movement). The four continuous variables were set at the variable levels shown in Table 4.

Table 4. Input parameters for friction stir welding.

Continuous Variable									
Parameters	Levels								
Tutuniceis	-1	1							
Tool tilt angle (degrees)	0	0 3							
Tool rotational speed (rpm)	150	150	0						
Tool travel speed (mm/min)	15	135	5						
Shoulder diameter (mm)	18	25							
	Categorical V	ariable							
Parameters		Levels							
Pin geometry Reinforcement particles type Tool pin moving	Straight cylinder Silicon carbide Straight	Hexagonal cylinder Aluminum oxide Zigzag	Threaded cylinder - Circles						

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2.1.2. Dataset 7PI-V2

This dataset was experimentally designed using the Taguchi method [30]. Commercial AA-5083 and AA-6061 alloy cut from work piece plates to dimensions of 75 mm wide, 200 mm long, and 6 mm thick were used in the FSW experiment, and the parameters for the welding experiment are given in Table 5. A CNC milling machine (HAAS, Model TM2) was utilized in the FSW process. The moving direction of the tool was the rolling direction of the specimen, and the tool geometry for the experiment was as shown in Figure 2. During FSW, the heat input was measured using a thermal infrared imaging camera (FLUKE, Model Ti480 Pro). After FSW, a waterjet machine (MAXIEM, Model 1530) was used to cut all the specimens in a transverse direction following the ASTM E8M-04 standard for testing tensile strength and maximum hardness, as shown in Figure 3. The tensile testing was carried out at room temperature using a universal testing machine (LLOYD, Model LS100-Plus) at a crosshead speed of 0.5 mm/min. Microhardness testing was conducted using a Vickers hardness testing machine (Mitutoyo, Model MVK-H1) with a test load of 100 g and a 15 s holding time. The experimental and test procedures are shown in Figure 4. The results of the 7PI-V1 experiment were compared with correlated work to test and confirm the earlier predictions.

Table 5. Input parameters for friction stir welding.

Continuous Variable									
Parameters	Levels								
Turumeters	-1	1							
Tilt angle (degrees)	0	3							
Tool rotational speed (rpm)	800	1500							
Tool travel speed (mm/min)	15								
Shoulder diameter (mm)	18 24								
	Categorical Va	riable							
Parameters		Levels							
Pin geometry	Straight cylinder	Threaded cylinder	Hexagonal cylinder						
Reinforcement particles type	Silicon carbide	Aluminum oxide	-						
Tool pin moving	Straight	Zigzag	Circles						

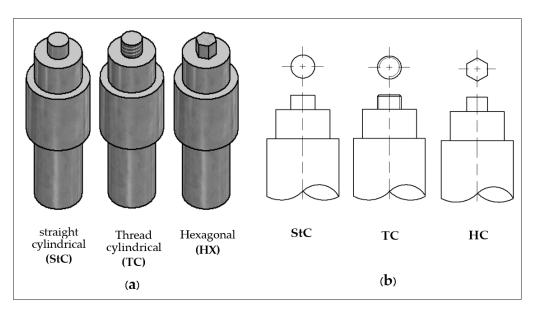


Figure 2. Tool geometry for the experiment: (a) 3D and (b) 2D views.

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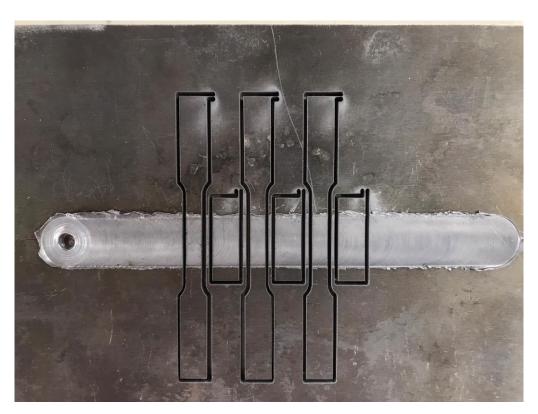


Figure 3. Specimen cutting for tensile and hardness testing.

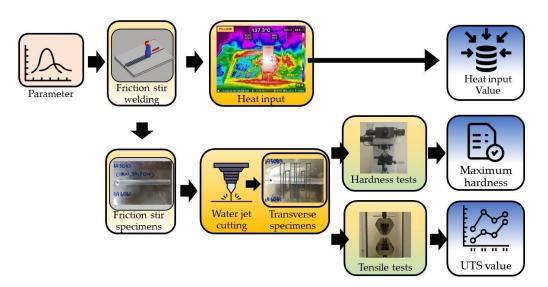


Figure 4. The FSW experimental process.

2.2. AMIS-Machine Learning Combination Model

The AMIS—machine learning combination model was designed to improve the forecasting of the UTS, MH, and HI in FSW of AA-5083 and AA-6061 aluminum alloys. The input variables were all parameters [25] determined according to the method proposed by Matitopanum et al. [59], with the addition of a new method, the AMIS—machine learning combination model, which consists of the following parts.

2.2.1. Gaussian Process Regression

Gaussian process regression (GPR) involves the generation of machine learning combination modeling and was used to improve the presented ensemble machine learning

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model. GPR was used to estimate feasibility, which generates data for the input (X) and output (Y) in the process. These generated models provide a conditional distribution, as shown in Figure 5.

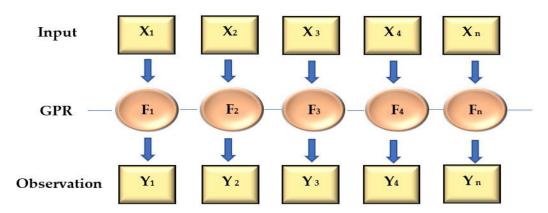


Figure 5. Gaussian process regression [59].

Figure 5 shows GPR using square boxes, circles, and arrow symbols for associated nodes across the monitored values, which require a random variable group.

The general process of GPR is given by the following formula:

$$y = f(x) + N(0, \sigma_n^2) \tag{1}$$

where f(x) is input value; $N(0, \sigma_n^2)$ is noise; and σ_n^2 is noise variance.

One observation is the covariance function (k(x, x')), or radial basis function (RBF) kernel, obtained via the following formula:

$$k(x, x') = \sigma_f^2 \exp\left[\frac{-(x - x')^2}{2l^2}\right]$$
 (2)

$$k(x, x') = \sigma_f^2 \exp\left[\frac{-(x - x')^2}{2l^2}\right] + \sigma_n^2 \delta(x, x')$$
 (3)

where σ_f^2 is determined for the maximum covariance. If $x \approx x'$, then k(x, x') approaches this maximum; f(x) is inseparably related with f(x') in Equation (2).

Where $\delta(x, x')$ is a function of the Kronecker delta in Equation (3). The covariance function is likewise used to support the vector machine of the essence to generate the covariance matrix.

2.2.2. Support Vector Machine

A support vector machine (SVM) is an algorithm-supervised learning method used for regression problems. The purpose of SVM is to find the function that is an exact prediction of the output value from a given input.

Operating in the SVM, which is called the margin, is a regression using the function of distant maximizing to forecast genuine result values. It is expedient to work within the relationship variables of the input and output because the data are complex and cannot easily be modeled via a linear function.

Support vector machine regression is the prediction of the new input to the hyperplane using the identified function for calculation of the result value of prediction. It is defined as a radial basis function (RBF) kernel, using the following equation:

$$k(x, x') = \exp(-\text{gamma} \times ||x - x'||^2)$$
(4)

where gamma is a scaling factor and x, x' are the input vectors.

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2.2.3. Entirety strategy

The homogenous and heterogenous structures use a similar model to proceed with the ensemble strategy. The heterogeneous structure uses the GPR method equal to 50% and the support vector machine equal to 50% as proposed by [59] and shown in Figure 6.

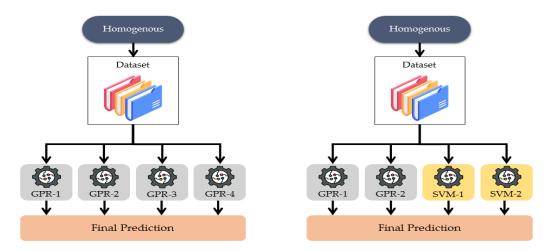


Figure 6. Framework of homogenous and heterogenous structures [59].

2.2.4. Decision Hybridization Strategy

The decision hybridization strategy is the last forecasting stage to report results in the machine learning approach. In addition, it is a way of combining the results of many GPR methods into one, superseding the solution of the presented model.

- Unweighted average ensemble Here, the research presents the learning output via an analysis of the total outdistanced unweighted average to define the merging decision of the model [60].
- Weighted ensemble optimization using artificial multiple intelligence systems (WEAMIS)

The EML method improves the predictive values for the UTS, MH, and HI by developing a cluster of learning techniques, called weighted ensemble optimization, using artificial multiple intelligence systems (WEAMIS) to determine the appropriate fuse weighting approach. Then, WEAMIS is applied to the best weighting, considering the UAE, to improve the quality of the final solution.

An optimal solution model aims to combine the base learner forecast, using an optimized weighting that shows the result in its entirety, with the minimum total predicted root mean square error (RMSE), as shown in Equation (5). The calculation of \hat{y}_i , the ensemble learners, is given by Equation (6):

$$RMSE = \frac{1}{I} \sqrt{\sum_{i=1}^{I} \left(y_i - \hat{y}i \right)^2}$$
 (5)

$$\hat{\mathbf{y}}\hat{\mathbf{i}} = \sum_{j=1}^{J} \omega_{j} \hat{\mathbf{Y}}\hat{\mathbf{j}}$$
 (6)

where $\omega_j \geq 0$ and $\sum_{j=1}^k \omega_j = 1$

The RMSE calculation of a single learner as shown above is obtained using Equation (5), where I represents a determined number of observations, y_i is the actual value of the observation i, \hat{y}_i is the observed prediction i, \hat{Y}_j is the prediction values set when using model j as the learners, and j is the total number of learners to use in the model.

The artificial multiple intelligence systems (AMIS) method uses a system with many artificial multiple intelligences to assist in the identification of optimal solutions [42,51]. The

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system is called an intelligence box (IB), and it has algorithms with unique properties. The AMIS comprises four steps, which are (1) the generation of a set population member known as a work package (WP), (2) performing the WP to select the specified IB, (3) updating track information, and (4) repeating WP steps 2 to 3 until the dissolving condition is met.

Step 1. Initial generation of the work package

The step generating the initial work package is random and is set by the NP random vector. The NP is set to the equitable number of SVMs and GPR on 1–100 positions, as recommended by [42,51]. This research used track i=2 random examples, as shown in Table 6.

Table 6. The track i and the position.

Track i\Position	1	2	3	4	5	6	7	8		99	100
1	0.39	0.56	0.24	0.97	0.82	0.33	0.06			0.14	0.29
2	0.67	0.51	0.19	0.72	0.21	0.48	0.80			0.32	0.45

Table 6 shows the initial work package with the value positions 1–100. Then, the initial work package sets the randomized numbers from 0 to 1, and the next work package solution set is selected using a roulette wheel method and entered into the process intelligence box (IB) [61].

The different decisions initial work package selects an IB, individually performing the IB to improve the current solution from each track i. The search probability function process uses the following formula:

$$P_{bt} = \frac{FN_{bt-1} + (1-F)A_{bt-1} + MJ_{bt-1}}{\sum_{bt=1}^{B} FN_{bt-1} + (1-F)A_{bt-1} + MJ_{bt-1}}$$
(7)

where P_{bt} represents the probability of selecting the intelligence box in iteration t; N_{bt-1} is the number of positions that have selected intelligence box b in the previous t iterations; A_{bt-1} is the average objective function of all positions that selected intelligence box b in the previous iteration; and J_{bt-1} is a value which is incremented by 1 if an intelligence box finds the best result in the final iteration. Prasitpuriprecha et al. [42] has recommended that a scaling factor F=2 and improvement factor M=1 are good initial choices.

Step 2. Performing the WP to select the specified IB

In this step, the WP selects the specified IB to improve the quality of the current solution to obtain the optimal solution. Our research designed the following intelligence by utilizing 8 boxes recommended by [32].

$$Y_{ijq} = \rho Y_{rjq} + F1 \left(B_j^{gbest} - Y_{rjq} \right) + F2 \left(Y_{mjq} - Y_{rjq} \right)$$
 (8)

$$Y_{ijq} = Y_{rjq} + F1\left(B_j^{gbest} - Y_{rjq}\right) + F2\left(B_{hj}^{pbest} - Y_{rjq}\right) \tag{9}$$

$$Y_{ijq} = Y_{rjq} + F1(Y_{mjq} - Y_{njq})$$
 (10)

$$Y_{iiq} = S_{ii} (11)$$

$$Y_{ijq} = \begin{cases} Y_{ijq} & \text{if } S_{ij} \le CR^h \\ S_{ijq} & \text{otherwise} \end{cases}$$
 (12)

$$Y_{ijq} = \begin{cases} Y_{ijq} & \text{if } S_{ij} \leq CR^h \\ B_j^{gbest} & \text{otherwise} \end{cases} \tag{13}$$

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$$Y_{ijq} = \begin{cases} Y_{ijq} & \text{if } S_{ij} \le CR^h \\ Y_{njq} & \text{otherwise} \end{cases}$$
 (14)

$$Y_{ijq} = \begin{cases} Y_{ijq} & \text{if } S_{ij} \leq CR^h \\ S_{ij}Y_{ijq} & \text{otherwise} \end{cases} \tag{15}$$

Time the operation in the IB to execute all WPs in iteration t, and each WP will select its preferred IB result to design the method for finding the answer to each problem using Equation (8) to Equation (15), where Y_{ijq+1} is the value of WP track i in iteration t+1, Y_{ijq} is the new value generated in the position using IBs, r,n and m are the specific elements of the WP set (1 to Q) that are not equal to q, S_{ij} is a random number 0–1 of the WP track i element j, and, according to the iteration t, B_j^{gbest} is the value of the global best WP, and B_{hj}^{pbest} is the value of the personal best. A crossover rate (CR^h) value of 0.8 is used, as recommended by [32].

Step 3. Updating track information

Some track information requires updating before it can be used in iterations using the formulae in Equations (16) and (17) as ref [42]:

$$Y_{ijt+1} = \begin{cases} Z_{ijt} & \text{if } f(Z_{ijt}) \leq f(X_{ijt}) \text{ and update } f(X_{ijt}) = f(Z_{ijt}) \\ X_{ijt+1} \text{ otherwise} \end{cases}$$
 (16)

$$W_i = Y_{ijt}$$
 for all i and t. (17)

where Y_{ijt} is the tracked value of i and iteration t+1, $f(Z_{ijt})$ is the value of the objective function of Z_{ijt} and $f(X_{ijt})$ is the objective function value of X_{ijt} . Then, the values of W_i are connected to those of X_{ijt+1} by X_{iit+1} , which is the value of updating.

Step 4. Repeating WP in steps 2 to 3.

Repeat steps 2 to 4 until the termination condition is discovered. The stop criterion is set to 100 iterations [62].

3. Results

The proposed model was simulated in Python using a PC with an Intel Core $^{\text{TM}}$ i3–1.70 GHz CPU and 5 GB of RAM. The framework for the experiments is shown in Figure 7.

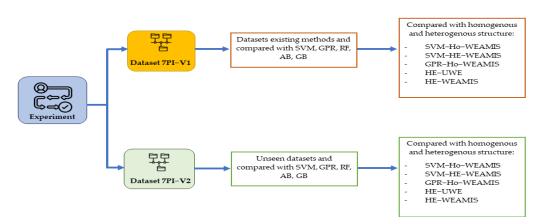


Figure 7. Experimental framework.

The GPR parameters, SVM, random forest (RF), ADA boosting (AB), gradient boosting (GB), and presented models (WEAMIS), taken from [59], are set out in Table 7.

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Table 7. Parameter determination.

Regressors	User-Defined Parameters
GPR [63]	Kernel = 'rbf', gamma = 7, noise = 0.2
RF [51]	Learner = 100 , max leaf = 1
SVM [63]	Kernel = 'rbf', gamma = 7 , $C = 0.2$
AB [57]	Learner = 100 , max leaf = 5
GB [48]	Learner = 100 , max leaf = 5 , learning rate = 0.001
Ho-UWE, HE-UWE, Ho-WEDE, HE-UWE,	
GPR-HO-UWE, GPR-HO-WEDE,	learner = 100
SVM-HO-UWE and SVM-HO-WEDE [57]	
Our presented ensemble learning	
(Ho-WEAMIS, WEAMIS, SVM-HO-WEAMIS	learner = 100
and GPR-HO-WEAMIS)	

3.1. The Offered Model Testing on the Existing Dataset

This experiment was performed using datasets 11P1-V1 and 11PI-V2 as recommended by [59]. In addition to [59], the standard models used in this experiment were modified for use in [51,57,63], and [48], which relate to the GPR, SVM, RF, AB, and GB methods, respectively. The algorithm names GPR-HO-UWE, GPR-HO-WEDE, SVM-HO-UWE, SVM-HO-WEDE, HE-UWE, and HE-WEDE were taken from [59]. The proposed model is named GPR-Ho-WEAMIS, SVM-Ho-WEAMIS, and HE-WEAMIS. The disparate ensemble structure models are attributed to HE-UWE and HE-WEAMIS, as UWE and WEAMIS were used in the decision fusion method. The results from the datasets 11PI-V1 and 11PI-V2 are shown in Table 8.

Table 8. Performance of the various machine learning models on the FSW-11PI-V1 and FSW-11PI-V2 datasets.

						11PI	-V1						11PI-V2					
Machine Learning and	Training Dataset						Testing Dataset						Testing Dataset					
Ensemble Machine Learning Method	CC			RMSE			СС		RMSE		CC			RMSE				
	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI
GPR [63]	0.983	0.965	0.968	3.73	3.16	6.58	0.990	0.971	0.987	3.73	3.16	6.58	0.995	0.967	0.968	6.69	3.21	7.35
SVM	0.981	0.986	0.971	4.52	2.06	5.69	0.989	0.987	0.991	4.52	2.06	5.69	0.983	0.971	0.976	6.63	3.17	7.09
RF	0.975	0.982	0.979	4.23	2.27	5.75	0.990	0.980	0.990	4.23	2.27	5.75	0.996	0.973	0.985	4.89	2.87	6.21
AB	0.981	0.968	0.978	4.63	2.58	5.77	0.989	0.977	0.990	4.63	2.58	5.77	0.976	0.977	0.983	4.06	2.51	6.11
GB	0.984	0.976	0.981	4.67	2.76	5.83	0.988	0.979	0.991	4.67	2.76	5.83	0.974	0.971	0.976	6.67	3.15	7.12
GPR-HO-UWE	0.989	0.979	0.988	3.62	1.92	4.27	0.993	0.987	0.96	3.62	1.92	4.27	0.989	0.967	0.971	5.72	3.24	7.32
GPR-HO-WEDE	0.990	0.978	0.989	3.67	1.91	4.29	0.992	0.987	0.996	3.67	1.91	4.29	0.994	0.976	0.986	4.09	2.44	6.02
SVM-HO-UWE	0.985	0.973	0.977	4.23	2.27	5.45	0.990	0.980	0.992	4.23	2.27	5.45	0.994	0.980	0.989	4.00	2.31	5.92
SVM-HO-WEDE	0.991	0.982	0.991	4.02	2.11	4.98	0.994	0.982	0.993	4.02	2.11	4.98	0.989	0.979	0.989	3.90	2.34	5.93
HE-UWE	0.992	0.985	0.992	3.53	1.89	4.15	0.993	0.988	0.997	3.53	1.89	4.15	0.994	0.981	0.990	3.78	2.27	5.89
HE-WEDE	0.992	0.990	0.993	3.46	1.88	4.16	0.995	0.989	0.997	3.46	1.88	4.16	0.996	0.987	0.990	3.39	2.07	5.88
HE-WEAMIS	0.994	0.988	0.997	3.32	1.88	4.02	0.996	0.989	0.998	3.32	1.88	4.02	0.998	0.988	0.990	3.22	2.03	5.87
SVM-HO-WEAMIS	0.993	0.987	0.993	3.89	1.89	4.32	0.991	0.988	0.996	3.89	1.89	4.32	0.990	0.982	0.989	3.96	2.21	5.91
GPR-HO-WEAMIS	0.993	0.980	0.996	3.67	1.91	4.28	0.995	0.987	0.996	3.67	1.91	4.28	0.989	0.979	0.989	3.87	2.35	5.92

Table 8 shows the best obtainable method for the evaluation of the UTS, MH, and HI with the 11 enforced parameters for the 11PI-V1 dataset, providing UTS, MH, and HI values of 10.99%, 40.51%, and 38.91%, respectively. The 11PI-V2 dataset produced a solution with UTS, MH, and HI values of 51.87%, 36.76%, and 20.14%, respectively. These solutions display less precision than the best one obtained using the HE-WEAMIS model, in which the RMSE of 11PI-V1 for the UTS reduced from 3.73 to 3.32, the MH reduced from 3.16 to 1.88, and the HI reduced from 6.58 to 4.02. Furthermore, the RMSE of 11PI-V2 for the UTS reduced from 6.69 to 3.22, the MH from 3.21 to 2.03, and the HI from 7.35 to 5.87. This showed that using WEAMIS as the decision approach provided greater accuracy. K-fold cross-validation was executed using 2-cv-, 3-cv-, and 5-cv-fold cross-validation of the model; the results of the experiment are shown in Table 9.

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Madiana					RMSE						
Machine Learning and Ensemble Machine Learning		UTS			МН			HI			
Method	2-cv	3-cv	5-cv	2-cv	3-cv	5-cv	2-cv	3-cv	5-cv		
GPR	6.70 ± 0.12	6.70 ± 0.12	5.33 ± 0.11	7.38 ± 0.41	6.07 ± 0.41	4.93 ± 0.36	11.78 ± 0.56	10.06 ± 0.56	8.51 ± 0.56		
SVM	7.02 ± 0.42	7.02 ± 0.42	5.72 ± 0.37	4.41 ± 0.25	4.13 ± 0.25	3.43 ± 0.22	10.55 ± 0.28	10.08 ± 0.28	7.71 ± 0.28		
RF	7.11 ± 0.21	7.11 ± 0.20	5.69 ± 0.18	5.23 ± 0.38	4.71 ± 0.38	3.92 ± 0.34	11.38 ± 0.75	8.89 ± 0.75	7.56 ± 0.75		
AB [57]	6.18 ± 0.38	6.18 ± 0.38	5.05 ± 0.34	6.63 ± 0.31	5.64 ± 0.31	4.59 ± 0.27	9.47 ± 0.51	10.51 ± 0.51	7.85 ± 0.51		
GB [48]	5.06 ± 0.23	5.06 ± 0.23	4.09 ± 0.20	6.7 ± 0.26	6.07 ± 0.26	5.01 ± 0.23	10.41 ± 0.89	8.98 ± 0.89	7.91 ± 0.89		
GPR-HO-ÚWE	4.66 ± 0.17	4.66 ± 0.17	3.91 ± 0.15	4.08 ± 0.40	4.05 ± 0.40	3.26 ± 0.35	7.55 ± 0.22	7.25 ± 0.22	5.50 ± 0.22		
GPR-HO-WEDE	4.6 ± 0.18	4.6 ± 0.18	3.81 ± 0.16	4.03 ± 0.31	4.11 ± 0.31	3.29 ± 0.28	8.52 ± 0.74	7.21 ± 0.74	5.53 ± 0.74		
SVM-HO-UWE	5.53 ± 0.21	5.53 ± 0.21	4.67 ± 0.18	5.75 ± 0.31	4.70 ± 0.31	3.84 ± 0.28	9.21 ± 0.8	8.48 ± 0.80	7.25 ± 0.80		
SVM-HO-WEDE	5.42 ± 0.34	5.42 ± 0.34	4.21 ± 0.30	5.71 ± 0.33	4.84 ± 0.33	3.79 ± 0.29	8.45 ± 0.41	7.32 ± 0.41	6.33 ± 0.41		
HE-UWE	4.36 ± 0.17	4.36 ± 0.17	3.73 ± 0.15	4.39 ± 0.28	3.86 ± 0.28	3.12 ± 0.25	6.92 ± 0.62	6.39 ± 0.62	5.43 ± 0.62		
HE-WEDE [59]	4.65 ± 0.18	4.65 ± 0.18	3.74 ± 0.16	4.43 ± 0.39	4.01 ± 0.39	3.34 ± 0.35	8.03 ± 0.34	6.29 ± 0.34	5.35 ± 0.34		
HE-WEAMIS	4.56 ± 0.30	4.56 ± 0.31	3.62 ± 0.28	4.84 ± 0.37	3.91 ± 0.37	3.21 ± 0.32	6.19 ± 0.52	5.47 ± 0.52	4.89 ± 0.52		
SVM-HO-WEAMIS	4.57 ± 0.28	4.57 ± 0.28	3.66 ± 0.25	4.25 ± 0.28	4.02 ± 0.28	3.26 ± 0.25	7.84 ± 0.75	7.18 ± 0.75	5.43 ± 0.75		
GPR-HO-WEAMIS	4.63 ± 0.16	4.63 ± 0.16	3.79 ± 0.14	4.78 ± 0.39	3.72 ± 0.39	3.24 ± 0.34	6.71 ± 0.46	7.13 ± 0.46	5.39 ± 0.46		

Table 9. K-fold cross-validation of the models with the training dataset.

Table 9 provides the computational results in which HE-WEAMIS obtains the best solution of all the proposed methods, as evidenced by its lower variance and RMSE.

3.2. Testing of the Proposed Model with the Seven Parameters of the Existing Dataset (7PI-V1)

The values of the seven parameters were obtained randomly, as recommended by [25]. This dataset was tested using the methods set out in Section 3.1. The models used were machine learning and ensemble machine learning, and these provided results for UTS, MH, and HI values. These results were compared with the results from the various methods, as shown in Table 10.

						7F	PI-V1						
Machine Learning and		Т	raining	Dataset			Testing Dataset						
Ensemble Machine Learning Method	CC				RMSE			CC			RMSE		
8	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	
GPR	0.961	0.930	0.971	9.48	7.80	6.22	0.987	0.967	0.978	6.73	7.40	5.10	
SVM	0.959	0.959	0.969	9.62	6.24	6.07	0.982	0.979	0.971	6.22	5.02	5.87	
RF	0.983	0.983	0.997	5.03	3.76	2.79	0.971	0.668	0.962	8.47	7.31	6.31	
AB	0.983	0.967	0.986	6.14	4.73	4.26	0.980	0.985	0.969	7.02	4.55	5.70	
GB	0.984	0.973	0.991	6.08	3.99	3.39	0.966	0.971	0.959	9.66	6.71	6.57	
GPR-HO-UWE	0.993	0.929	0.968	5.04	3.74	3.03	0.993	0.980	0.979	5.03	4.97	5.03	
GPR-HO-WEDE	0.988	0.953	0.971	4.61	3.67	3.01	0.991	0.986	0.980	5.35	4.42	4.97	
SVM-HO-UWE	0.992	0.981	0.991	4.82	3.75	2.81	0.990	0.985	0.975	5.66	4.50	5.51	
SVM-HO-WEDE	0.989	0.965	0.985	4.71	3.63	2.98	0.992	0.987	0.977	5.25	4.18	5.36	
HE-UWE	0.988	0.982	0.995	4.56	3.69	2.79	0.993	0.988	0.977	5.09	4.08	5.20	
HE-WEDE	0.997	0.983	0.992	4.31	3.56	2.73	0.996	0.984	0.982	4.91	4.34	4.85	
HE-WEAMIS	0.999	0.991	0.994	4.12	3.33	2.78	0.996	0.990	0.983	4.89	4.00	4.74	
SVM-HO-WEAMIS	0.998	0.991	0.992	4.23	3.37	2.75	0.996	0.988	0.981	4.90	4.07	4.93	
GPR-HO-WEAMIS	0.997	0.990	0.995	4.17	3.31	2.76	0.997	0.988	0.982	4.87	4.08	4.87	

Table 10. Performance of dissimilar machine learning models on the 7PI-V1 dataset.

Table 10 reveals that HE-WEAMIS is the best prediction method given the seven parameters of 7PI-V1, providing UTS, MH, and HI values of 49.38%, 45.95%, and 24.88%, respectively. The RMSE of 7PI-V1 for UTS reduced from 9.66 to 4.89, MH reduced from 7.40 to 4.00, and HI reduced from 6.31 to 4.74.

Table 11 shows the percentage difference of the results found. HE-WEAMIS was the best method because it provided better solutions than the other methods described in [34]. The HE-WEAMIS results increase the quality of the prediction when compared with the GPR [63], SVM [63], RF [51], AB [57], GB [48], GPR-HO-UWE, GPR-HO-WEDE, SVM-HO-UWE, SVM-HO-WEDE, HE-UWE, HE-WEDE [59], SVM-HO-WEAMIS, and GPR-HO-WEAMIS approaches. The results showed much higher percentages of 27.34%,

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45.95%, and 19.25% for UTS, MH, and HI, respectively, when compared with the approach used by [34]. Furthermore, these results outperform the RF, AB, and GB methods on the UTS, MH, and HI values by 49.38%, 45.28%, and 27.85%, respectively. Then, using the AMIS (HE-WEAMIS) method, the optimum weights can improve the answer quality compared with the UWE (HE-UWE) method for UTS, MH, and HI values by 3.93%, 1.96%, and 8.85%, respectively.

Table 11.	The	different	tratios	(%diff)	of 7PI-V1	dataset

Machine Learning and		%diff	
Ensemble Machine Learning Method	UTS	МН	HI
GPR	27.34	45.95	7.06
SVM	21.38	20.32	19.25
RF	42.27	45.28	24.88
AB	30.34	12.09	16.84
GB	49.38	40.39	27.85
GPR-HO-UWE	2.78	19.52	5.77
GPR-HO-WEDE	8.60	9.50	4.63
SVM-HO-UWE	13.60	11.11	13.97
SVM-HO-WEDE	6.86	4.31	11.57
HE-UWE	3.93	1.96	8.85
HE-WEDE	0.41	7.83	2.27
HE-WEAMIS	0.00	0.00	0.00
SVM-HO-WEAMIS	0.20	1.72	3.85
GPR-HO-WEAMIS	-0.41	1.96	2.67

3.3. The Offered Model Testing with the Unseen Dataset 7 Parameters by Using the Taguchi Method (7PI-V2)

This proposed dataset consisted of seven parameters. The dataset comprises 54 datasets, and the details and results are shown in Table 12. This dataset was analyzed by machine learning methods to compare the models' accuracy; the results are displayed in Table 13.

Table 12. The results of the experiment.

Sets	SD	TA	TRS	TTS	PT	TP	TM	UTS	MH	HI
1	18	0	800	15	TC	SiC	Zigzag	182.66	85.71	412.66
2	21	1.5	800	15	TC	SiC	Zigzag	180.16	85.35	417.50
3	24	3	800	15	TC	SiC	Zigzag	183.40	87.16	409.73
4	18	0	1200	50	StC	SiC	Zigzag	208.71	88.46	442.69
5	21	1.5	1200	50	StC	SiC	Zigzag	209.85	89.71	438.01
6	24	3	1200	50	StC	SiC	Zigzag	207.59	88.64	444.58
7	18	0	1500	75	HC	SiC	Zigzag	239.06	101.87	439.67
8	21	1.5	1500	75	HC	SiC	Zigzag	241.90	100.28	440.63
9	24	3	1500	75	HC	SiC	Zigzag	236.89	102.29	436.69
10	18	0	1200	75	TC	SiC	Straight	240.57	102.71	440.93
11	21	1.5	1200	75	TC	SiC	Straight	241.55	100.47	436.56
12	24	3	1200	75	TC	SiC	Straight	237.73	52.99	434.88
13	18	0	1500	15	StC	SiC	Straight	245.41	101.74	450.34
14	21	1.5	1500	15	StC	SiC	Straight	246.24	101.18	449.26
15	24	3	1500	15	StC	SiC	Straight	242.86	102.18	452.78
16	18	0	800	50	HC	SiC	Straight	157.81	66.98	399.37
17	21	1.5	800	50	HC	SiC	Straight	156.48	65.85	395.32
18	24	3	800	50	HC	SiC	Straight	158.85	64.82	400.29

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 Table 12. Cont.

Sets	SD	TA	TRS	TTS	PT	TP	TM	UTS	MH	HI
19	18	0	1500	50	TC	SiC	circles	241.59	102.97	435.56
20	21	1.5	1500	50	TC	SiC	circles	238.71	100.61	433.33
21	24	3	1500	50	TC	SiC	circles	243.06	101.67	437.35
22	18	0	800	75	StC	SiC	circles	165.00	70.13	406.41
23	21	1.5	800	75	StC	SiC	circles	163.27	68.23	403.09
24	24	3	800	75	StC	SiC	circles	166.03	71.19	410.81
25	18	0	1200	15	HC	SiC	circles	234.79	100.85	448.10
26	21	1.5	1200	15	HC	SiC	circles	239.18	101.13	453.24
27	24	3	1200	15	HC	SiC	circles	232.82	98.69	445.69
28	18	0	1200	50	TC	AO	Zigzag	218.72	95.81	428.15
29	21	1.5	1200	50	TC	AO	Zigzag	216.19	96.36	421.99
30	24	3	1200	50	TC	AO	Zigzag	219.79	97.58	432.49
31	18	0	1500	75	StC	AO	Zigzag	241.04	104.83	444.76
32	21	1.5	1500	75	StC	AO	Zigzag	238.78	103.25	434.49
33	24	3	1500	75	StC	AO	Zigzag	242.32	106.27	446.87
34	18	0	800	15	HC	AO	Zigzag	181.35	81.96	418.53
35	21	1.5	800	15	HC	AO	Zigzag	182.14	82.84	421.95
36	24	3	800	15	HC	AO	Zigzag	179.52	79.79	412.45
37	18	0	800	75	TC	AO	Straight	160.05	68.26	406.64
38	21	1.5	800	75	TC	AO	Straight	158.08	67.19	398.61
39	24	3	800	75	TC	AO	Straight	157.68	66.19	399.71
40	18	0	1200	15	StC	AO	Straight	224.48	96.08	435.96
41	21	1.5	1200	15	StC	AO	Straight	221.19	95.27	428.16
42	24	3	1200	15	StC	AO	Straight	226.44	96.99	438.16
43	18	0	1500	50	HC	AO	Straight	240.99	103.9	434.62
44	21	1.5	1500	50	HC	AO	Straight	245.25	104.64	439.87
45	24	3	1500	50	HC	AO	Straight	243.04	104.17	435.95
46	18	0	1500	15	TC	AO	circles	237.02	102.17	438.54
47	21	1.5	1500	15	TC	AO	circles	236.89	102.52	434.77
48	24	3	1500	15	TC	AO	circles	241.69	104.12	440.27
49	18	0	800	50	StC	AO	circles	142.92	61.31	399.77
50	21	1.5	800	50	StC	AO	circles	141.14	60.41	396.66
51	24	3	800	50	StC	AO	circles	141.92	60.71	398.73
52	18	0	1200	75	HC	AO	circles	222.02	90.94	432.71
53	21	1.5	1200	75	HC	AO	circles	223.06	91.63	429.62
54	24	3	1200	75	HC	AO	circles	225.36	93.02	436.71

 Table 13. Compared performance of machine learning methods with the 7PI-V2 dataset.

						7F	PI-V2						
Machine Learning and	Training Dataset							Testing Dataset					
Ensemble Machine Learning Method	CC				RMSE			CC			RMSE		
	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	
GPR	0.922	0.805	0.927	9.22	7.85	6.77	0.891	0.850	0.933	13.15	6.54	8.18	
SVM	0.966	0.781	0.985	6.22	7.06	4.82	0.920	0.898	0.979	11.31	5.39	6.23	
RF	0.995	0.826	0.996	2.74	6.19	3.28	0.968	0.977	0.989	7.19	2.53	4.14	
AB	0.975	0.801	0.989	5.19	6.80	4.25	0.945	0.938	0.982	9.35	4.22	5.69	
GB	0.974	0.806	0.991	4.60	6.45	4.27	0.943	0.946	0.978	9.09	4.05	6.64	
GPR-HO-UWE	0.987	0.808	0.993	3.37	6.36	3.68	0.972	0.957	0.983	6.59	3.45	5.03	
GPR-HO-WEDE	0.994	0.803	0.995	3.12	6.41	3.43	0.978	0.961	0.986	5.84	3.33	4.71	
SVM-HO-UWE	0.989	0.809	0.993	3.26	6.42	3.59	0.981	0.959	0.984	5.45	3.50	4.89	
SVM-HO-WEDE	0.987	0.807	0.993	3.11	6.49	3.69	0.979	0.962	0.986	5.74	3.27	4.71	
HE-UWE	0.992	0.821	0.989	2.83	6.25	3.29	0.977	0.978	0.989	6.02	2.53	4.23	
HE-WEDE	0.993	0.824	0.990	2.51	6.15	3.28	0.977	0.979	0.990	6.07	2.46	4.08	

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						7F	PI-V2						
Machine Learning and	Training Dataset							Testing Dataset					
Ensemble Machine Learning Method	CC			RMSE			CC			RMSE			
	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	UTS	MH	HI	
HE-WEAMIS SVM-HO-WEAMIS GPR-HO-WEAMIS	0.994 0.991 0.991	0.831 0.811 0.824	0.993 0.991 0.995	2.38 3.02 2.66	5.94 6.41 6.29	3.25 3.43 3.25	0.981 0.979 0.978	0.980 0.962 0.979	0.988 0.985 0.987	5.44 5.66 5.86	2.40 2.78 2.45	4.49 4.65 4.56	

Table 13 reveals that HE-WEAMIS is the best method for predicting the UTS, MH, and HI based on the seven parameters of 7PI-V2, providing a better RMSE solution for UTS, MH, and HI than the 7PI-V1 dataset. The predictive solution errors reduced from 13.15 to 5.44, 6.54 to 2.40, and 8.18 to 4.49 for UTS, MH, and HI, respectively.

Table 14 presents the percentage differences in the results, showing that HE-WEAMIS is the best model, similar to the 7PI-V1 dataset in Table 11. The UTS, MH, and HI responses provide high performance values of 58.63%, 63.30%, and 45.11%, respectively, and are higher than those of the RF, AB, and GB methods, which were 41.82%, 43.13%, and 32.38%, respectively. Therefore, using optimum weightings improved the quality of the results with the AMIS (HE-WEAMIS) approach when compared with the values for UTS, MH, and HI from the UWE (HE-UWE) method, with percentage differences in the results of 9.63%, 5.14%, and -6.15%, respectively.

Table 14. The different ratios (percentage difference) for the 7PI-V2 dataset.

Machine Learning and		%diff	
Ensemble Machine Learning Method	UTS	МН	HI
GPR	58.63	63.30	45.11
SVM	51.90	55.47	27.93
RF	24.34	5.14	-8.45
AB	41.82	43.13	21.09
GB	40.15	40.74	32.38
GPR-HO-UWE	17.45	30.43	10.74
GPR-HO-WEDE	6.85	27.93	4.67
SVM-HO-UWE	0.18	31.43	8.18
SVM-HO-WEDE	5.23	26.61	4.67
HE-UWE	9.63	5.14	-6.15
HE-WEDE	10.38	2.44	-10.05
HE-WEAMIS	0.00	0.00	0.00
SVM-HO-WEAMIS	3.89	13.67	3.44
GPR-HO-WEAMIS	7.17	2.04	1.54

Figure 8a to d shows a comparison of the errors obtained from the dissimilar forecasting models. The GPR-HO-UWE and HE-UWE methods were selected for comparison with the HE-WEAMIS approach. The RMSE values are plotted on the graph with a solid line, an error line, and a plotted error line at a 45° angle. The plotted error line shows the ranges of $\pm 3\%$. All the graphs make it clear that the forecasting solutions obtained using the suggested model are close to the experimentally obtained UTS, MH, and HI values. The graph displays the forecasted and actual values of UTS, MH, and HI. The values are similar to those obtained using the suggested model together with the ensemble learning model.

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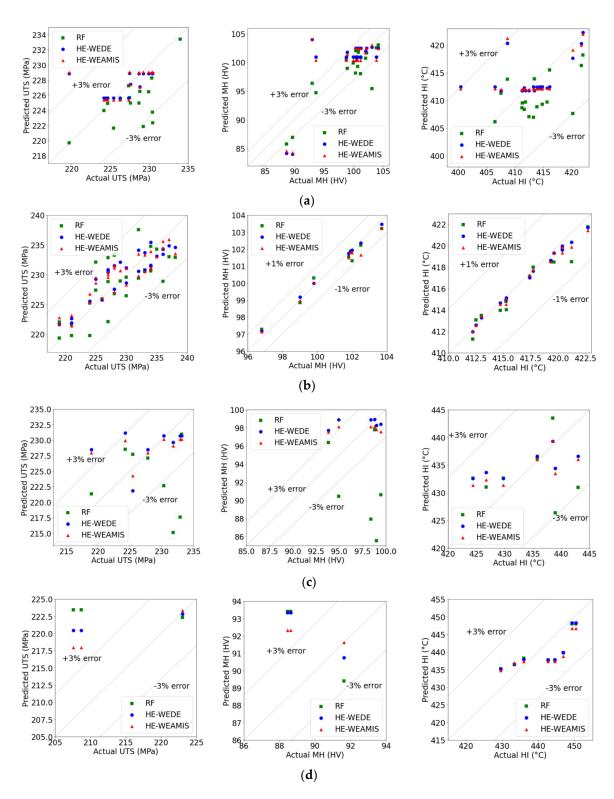


Figure 8. Compared tested value of the actual vs. predicted UTS for (a) 11PI-V1, (b) 11PI-V2, (c) 7PI-V1, and (d) 7PI-V2 datasets.

4. Discussion

We presented an AMIS–machine learning combination model for multiple response prediction of AA-5083/AA-6061 friction stir welding, using the model parameters set out in Table 2, for prediction of the UTS, MH, and HI, including (1) tilt angle, (2) tool travel speed, (3) shoulder diameter, and (4) tool rotation speed. Our research executed and analyzed

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comparisons with the results obtained by [34,64]. The calculation results from testing the proposed approach (HE-WEAMIS) showed that it was superior to the GPR [63], SVM [63], RF [51], AB [57], and GB [48] methods in the literature. These existing methods did not perform as well as the heterogeneous ensemble network model. The resulting findings were consistent with the conclusions of [41,43]. These two studies obtained homogenous and heterogenous ensemble networks and also explained how the practical decision fusion strategy is more effective than UWA methods. The decision fusion strategy is the reason for the significantly higher performance of our proposed model. Our methodology and its results are supported by [43,45,65,66].

In summary, it can clearly be seen from the error percentages for the UTS, MH, and HI that the WEAMIS method outperformed the existing dataset. These error percentages were 15.75%, 16.75%, and 41.35%, respectively, for the 7PI-V1 training and testing datasets, and 56.25%, 59.20%, and 27.62%, respectively, for the 7PI-V2 dataset. However, this method used the difference in the dataset error rate for the training and testing and showed good execution in obtaining a slight difference between the training and testing datasets. The training and testing indicated that our method (WEAMIS) can be tolerant of dataset permutations and outperform them even if the dataset is altered; although the parameter numbers increased for prediction of the UTS, MH, and HI, our model remained effective and outperformed several methods such as SVM, GPR, RF, AB, and GB.

Table 13 shows how the calculated solutions use the controlled parameters at the different levels. Furthermore, Table 2, shows that the proposed model is the most accurate in predicting the UTS, MH, and HI values, according to the results from [62]. Using the ML approach and the cognitive learning method could reduce the RMSE and increase prediction accuracy. Table 13 presents the prediction results using the model for the UTS, MH, and HI of the parameter set, confirming that the results from this method provide the highest accuracy. The respective CC and RMSE results were 0.981 and 5.44 for the UTS, 0.980 and 2.40 for the MH, and 0.988 and 4.49 for the HI. These results are more accurate than those in [34,64].

This article shows how the values of the UTS, MH, and HI can be accurately predicted using a model with an increased number of input parameters. The model presented provides more accurate prediction of the UTS, MH, and HI values with fewer input parameters than the models proposed in [24,34,35,37]. The results of the proposed model are more accurate and can be successfully applied to predict the UTS, MH, and HI for friction stir welding with all input parameters and can identify a solution without sample destruction.

5. Conclusions

Our research studied the characteristics of seven parameters in the FSW process using a machine learning entirety model developed to predict the UTS, MH, and HI. The aluminum alloys AA-5083 and AA-6061 were joined using friction stir welding performed for the experiment. The presented approach gathers the GPR and advocates the use of vector machine models. Two unlike decision fusion methods were applied for this research: the unweighted average model (UAM) and the artificial multiple intelligence system, which was obtained from GPR and SVM. The testing of the proposed model used two datasets to predict the multiple responses of the weld seam. The WEAMIS method provided higher performance than all current methods. The ensemble structures were homogeneous and heterogeneous. When tested using the 7PI-V1 and 7PI-V2 datasets, the averages of the UTS, MH, and HI values were 5.27%, 3.30%, and 4.71%, respectively. Weighting optimization using the AMIS method improved the average solution quality compared with the UWA model. The average values for the UTS, MH, and HI were 6.78%, 3.55%, and 1.35%, respectively. The experimental results from the datasets confirmed that the proposed model outperformed existing methods. Therefore, we conclude that the heterogeneous entirety structure and AMIS improve the fusion weight of the earlier methods.

We conclude that the machine learning combination model should also be able to estimate nonform data by avoiding a full factorial design when conducting the experiment Computation 2023, 11, 100 18 of 20

and generating the research dataset. However, the experiment also shows that the prediction results from the model remain highly accurate when using increased datasets. Future research should progress the research in the following two directions to obtain high-quality results: (1) application-based or online applications using the proposed model for welding, enabling the selection of appropriate parameters to obtain the desired UTS, MH, and HI values; and (2) the exploration of other parameters to obtain new results that could enable the model to be applied to different materials, parameters, and outputs using a progressive function system.

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